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On February 5th, we talked about 4 situations in the simulation:

- L matrix (binary-valued) + Network Guided Thresholding (already done)
- C matrix (continuous) + NG Banding (already done)
- L matrix + NG Banding
- C matrix + NG Thresholding

## Q1

I think the 3rd situation "L + NG Banding" is unfeasible, because we cannot know any ordering from a binary-valued information matrix.

## Q2

The 4th situation "C + NG Thresholding". We must convert  $\hat{C}(\eta)$  into  $\hat{L}(l,p,q)$  , where  $\eta$  is

**Assumption 4.** Represent the proxy correlation matrix as columns.  $C = (c_1, \ldots, c_N)$  and  $\hat{C} = (\hat{c}_1, \ldots, \hat{c}_N)$ . Then

$$\exists \eta \in (0,1], \forall i, \forall k, \lim_{T \to \infty} \Pr\{S_{\eta k}^{c_i} \subseteq S_k^{\hat{c}_i}\} = 1.$$

and l, p, q are

Parameter	Description
ρ	Determines how strong the correlation is and the sparsity of the covariance matrix $\Sigma$
1	Observation level, determines how we classify a pair $(i, j)$ as important, i.e., $L_{ij} = 1$ .
p	Conditional on $L_{ij} = 1$ , the probability of actually observing $G_{ij} = 1$ .
q	Conditional on $L_{ij} = 0$ , the probability of observing $G_{ij} = 1$
au	The Threshold level when we apply generalized thresholding operator
	on $\sigma_{ij}$ where $G_{ij} = 0$ .

Table 1: Description of varying parameters.

(G matrix in the old version notation is  $\hat{L}$  in the new version notation.)

## Q2.1

But there isn't an one-to-one match between  $\hat{C}$  and  $\hat{L}$ .

## Q2.2

You may think we can just pretend  $\hat{L}_{fake}:=I(i\in S_k^{\hat{c}_j}\wedge j\in S_k^{\hat{c}_i})$  , where  $\hat{c}_i$  is the i-th column of  $\hat{C}$  and k is determined by the CV of NG Banding, then apply NG Thresholding.

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But then, the only difference between the two methods is whether we apply thresholding on  $\hat{\sigma}_{ij}$  where  $\hat{L}_{fake}=0$  .