

## 1 Single machine scheduling with sum of completion times

MIP model:

$$\min \sum_{i \in [1, n]} s_i + d_i \quad (1)$$

$$s_i + d_i \leq s_j \quad \forall (i, j) \in P \quad (2)$$

$$s_i + d_i \leq s_j + M.b_{ji} \quad \forall i, j \in [1, n] : i \neq j \quad (3)$$

$$b_{ij} = 1 - b_{ji} \quad \forall i, j \in [1, n] : i < j \quad (4)$$

$$\text{integer } s_i \in \mathbb{Z}^+ \quad \forall i \in [1, n] \quad (5)$$

$$\text{integer } b_{ij} \in \{0, 1\} \quad \forall i, j \in [1, n] : i \neq j \quad (6)$$

CP Optimizer model:

$$\min \sum_{i \in [1, n]} \text{endOf}(o_i) \quad (1)$$

$$\text{endBeforeStart}(o_i, o_j) \quad \forall (i, j) \in P \quad (2)$$

$$\text{noOverlap}([o_i]_{i \in [1, n]}) \quad (3)$$

$$\text{interval } o_i \text{ size } d_i \quad \forall i \in [1, n] \quad (4)$$