

Funcons-beta: Multisets

The PPlanCompS Project

Funcons-beta/Values/Composite/Multisets/Multisets.cbs*

Multisets (bags)

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[ Type multisets
Funcon multiset
Funcon multiset-elements
Funcon multiset-occurrences
Funcon multiset-insert
Funcon multiset-delete
Funcon is-submultiset ]
```

Meta-variables GT <: ground-values

Built-in Type `multisets`(GT)

`multisets`(GT) is the type of possibly-empty finite multisets of elements of GT .

Built-in Funcon `multiset`($_ : (GT)^*$) : \Rightarrow `multisets`(GT)

Note that `multiset`(\dots) is not a constructor operation. The order of argument values is ignored, but duplicates are significant, e.g., `multiset`(1, 2, 2) is equivalent to `multiset`(2, 1, 2), but not to `multiset`(1, 2) or `multiset`(2, 1).

Built-in Funcon `multiset-elements`($_ : \text{multisets}(GT)$) : $\Rightarrow (GT)^*$

For each multiset MS , the sequence of values V^* returned by `multiset-elements`(MS) contains each element of MS the same number of times as MS does. The order of the values in V^* is unspecified, and may vary between multisets.

*Suggestions for improvement: plancomps@gmail.com.
Issues: <https://github.com/plancomps/CBS-beta/issues>.

Assert `multiset(multiset-elements(S)) == S`

Built-in Funcon `multiset-occurrences($_ : GT, _ : multisets(GT)$) : \Rightarrow natural-numbers`

`multiset-occurrences(GV, MS)` returns the number of occurrences of GV in MS .

Built-in Funcon `multiset-insert($_ : GT, _ : natural-numbers, _ : multisets(GT)$) : $\Rightarrow multisets(GT)$`

`multiset-insert(GV, N, MS)` returns the multiset that differs from MS by containing N more copies of GV .

Built-in Funcon `multiset-delete($_ : multisets(GT), _ : GT, _ : natural-numbers$) : $\Rightarrow multisets(GT)$`

`multiset-delete(MS, GV, N)` removes N copies of V from the multiset MS , or all copies of GV if there are fewer than N in MS .

Built-in Funcon `is-submultiset($_ : multisets(GT), _ : multisets(GT)$) : \Rightarrow booleans`

`is-submultiset(MS_1, MS_2)` tests whether every element of MS_1 has equal or fewer occurrences in MS_1 than in MS_2 .