

Funcons-beta: Binding *

The P_LanCompS Project

Binding.cbs | PLAIN | PRETTY

OUTLINE

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Binding

- [*Type* environments
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- Datatype* identifiers
- Alias* ids
- Funcon* identifier-tagged
- Alias* id-tagged
- Funcon* fresh-identifier
- Entity* environment
- Alias* env
- Funcon* initialise-binding
- Funcon* bind-value
- Alias* bind
- Funcon* unbind
- Funcon* bound-directly
- Funcon* bound-value
- Alias* bound
- Funcon* closed
- Funcon* scope
- Funcon* accumulate
- Funcon* collateral
- Funcon* bind-recursively
- Funcon* recursive]

Meta-variables $T <:$ values

*Suggestions for improvement: plancomps@gmail.com.
Reports of issues: <https://github.com/plancomps/CBS-beta/issues>.

Environments

Type `environments` \rightsquigarrow `maps(identifiers, values?)`

Alias `envs` = `environments`

An environment represents bindings of identifiers to values. Mapping an identifier to () represents that its binding is hidden.

Circularity in environments (due to recursive bindings) is represented using bindings to cut-points called `links`. Funcons are provided for making declarations recursive and for referring to bound values without explicit mention of links, so their existence can generally be ignored.

Datatype `identifiers` ::= { `_ : strings` } | `identifier-tagged(_ : identifiers, _ : values)`

Alias `ids` = `identifiers`

Alias `id-tagged` = `identifier-tagged`

An identifier is either a string of characters, or an identifier tagged with some value (e.g., with the identifier of a namespace).

Funcon `fresh-identifier` : \Rightarrow `identifiers`

`fresh-identifier` computes an identifier distinct from all previously computed identifiers.

Rule `fresh-identifier` \rightsquigarrow `identifier-tagged("generated", fresh-atom)`

Current bindings

Entity `environment(_ : environments)` \vdash `_` \longrightarrow `_`

Alias `env` = `environment`

The environment entity allows a computation to refer to the current bindings of identifiers to values.

Funcon `initialise-binding`(`X` : \Rightarrow `T`) : \Rightarrow `T`
 \rightsquigarrow `initialise-linking(initialise-generating(closed(X)))`

`initialise-binding`(`X`) ensures that `X` does not depend on non-local bindings. It also ensures that the linking entity (used to represent potentially cyclic bindings) and the generating entity (for creating fresh identifiers) are initialised.

Funcon `bind-value`(`I` : `identifiers`, `V` : `values`) : \Rightarrow `environments`
 \rightsquigarrow { `I` \mapsto `V` }

Alias `bind` = `bind-value`

`bind-value`(`I`, `X`) computes the environment that binds only `I` to the value computed by `X`.

Funcon `unbind`(`I` : `identifiers`) : \Rightarrow `environments`
 \rightsquigarrow { `I` \mapsto () }

`unbind`(`I`) computes the environment that hides the binding of `I`.

Funcon `bound-directly`($_ : \text{identifiers}$) : $\Rightarrow \text{values}$

`bound-directly`(I) returns the value to which I is currently bound, if any, and otherwise fails.

`bound-directly`(I) does *not* follow links. It is used only in connection with recursively-bound values when references are not encapsulated in abstractions.

Rule
$$\frac{\text{lookup}(\rho, I) \rightsquigarrow (V : \text{values})}{\text{environment}(\rho) \vdash \text{bound-directly}(I : \text{identifiers}) \longrightarrow V}$$

Rule
$$\frac{\text{lookup}(\rho, I) \rightsquigarrow ()}{\text{environment}(\rho) \vdash \text{bound-directly}(I : \text{identifiers}) \longrightarrow \text{fail}}$$

Funcon `bound-value`($I : \text{identifiers}$) : $\Rightarrow \text{values}$
 $\rightsquigarrow \text{follow-if-link}(\text{bound-directly}(I))$

Alias `bound` = `bound-value`

`bound-value`(I) inspects the value to which I is currently bound, if any, and otherwise fails. If the value is a link, `bound-value`(I) returns the value obtained by following the link, if any, and otherwise fails. If the inspected value is not a link, `bound-value`(I) returns it.

`bound-value`(I) is used for references to non-recursive bindings and to recursively-bound values when references are encapsulated in abstractions.

Scope

Funcon `closed`($X : \Rightarrow T$) : $\Rightarrow T$

`closed`(X) ensures that X does not depend on non-local bindings.

Rule
$$\frac{\text{environment}(\text{map}()) \vdash X \longrightarrow X'}{\text{environment}(_) \vdash \text{closed}(X) \longrightarrow \text{closed}(X')}$$

Rule `closed`($V : T$) $\rightsquigarrow V$

Funcon `scope`($_ : \text{environments}, _ : \Rightarrow T$) : $\Rightarrow T$

`scope`(D, X) executes D with the current bindings, to compute an environment ρ representing local bindings. It then executes X to compute the result, with the current bindings extended by ρ , which may shadow or hide previous bindings.

`closed`(`scope`(ρ, X)) ensures that X can reference only the bindings provided by ρ .

Rule
$$\frac{\text{environment}(\text{map-override}(\rho_1, \rho_0)) \vdash X \longrightarrow X'}{\text{environment}(\rho_0) \vdash \text{scope}(\rho_1 : \text{environments}, X) \longrightarrow \text{scope}(\rho_1, X')}$$

Rule `scope`($_ : \text{environments}, V : T$) $\rightsquigarrow V$

Funcon `accumulate`($_ : (\Rightarrow \text{environments})^*$) : $\Rightarrow \text{environments}$

`accumulate`(D_1, D_2) executes D_1 with the current bindings, to compute an environment ρ_1 representing some local bindings. It then executes D_2 to compute an environment ρ_2 representing further local bindings, with the current bindings extended by ρ_1 , which may shadow or hide previous current bindings. The result is ρ_1 extended by ρ_2 , which may shadow or hide the bindings of ρ_1 .

`accumulate`($_, _$) is associative, with `map`($_$) as unit, and extends to any number of arguments.

Rule $\frac{D_1 \longrightarrow D'_1}{\text{accumulate}(D_1, D_2) \longrightarrow \text{accumulate}(D'_1, D_2)}$
Rule $\text{accumulate}(\rho_1 : \text{environments}, D_2) \rightsquigarrow \text{scope}(\rho_1, \text{map-override}(D_2, \rho_1))$
Rule $\text{accumulate}(\) \rightsquigarrow \text{map}(\)$
Rule $\text{accumulate}(D_1) \rightsquigarrow D_1$
Rule $\text{accumulate}(D_1, D_2, D^+) \rightsquigarrow \text{accumulate}(D_1, \text{accumulate}(D_2, D^+))$

Funcon $\text{collateral}(\rho^* : \text{environments}^*) : \Rightarrow \text{environments}$
 $\rightsquigarrow \text{checked map-unite}(\rho^*)$

$\text{collateral}(D_1, \dots)$ pre-evaluates its arguments with the current bindings, and unites the resulting maps, which fails if the domains are not pairwise disjoint.

$\text{collateral}(D_1, D_2)$ is associative and commutative with $\text{map}(\)$ as unit, and extends to any number of arguments.

Recurse

Funcon $\text{bind-recursively}(I : \text{identifiers}, E : \Rightarrow \text{values}) : \Rightarrow \text{environments}$
 $\rightsquigarrow \text{recursive}(\{I\}, \text{bind-value}(I, E))$

$\text{bind-recursively}(I, E)$ binds I to a link that refers to the value of E , representing a recursive binding of I to the value of E . Since $\text{bound-value}(I)$ follows links, it should not be executed during the evaluation of E .

Funcon $\text{recursive}(SI : \text{sets}(\text{identifiers}), D : \Rightarrow \text{environments}) : \Rightarrow \text{environments}$
 $\rightsquigarrow \text{re-close}(\text{bind-to-forward-links}(SI), D)$

$\text{recursive}(SI, D)$ executes D with potential recursion on the bindings of the identifiers in the set SI (which need not be the same as the set of identifiers bound by D).

Auxiliary Funcon $\text{re-close}(M : \text{maps}(\text{identifiers}, \text{links}), D : \Rightarrow \text{environments}) : \Rightarrow \text{environments}$
 $\rightsquigarrow \text{accumulate}(\text{scope}(M, D), \text{sequential}(\text{set-forward-links}(M), \text{map}(\)))$

$\text{re-close}(M, D)$ first executes D in the scope M , which maps identifiers to freshly allocated links. This computes an environment ρ where the bound values may contain links, or implicit references to links in abstraction values. It then sets the link for each identifier in the domain of M to refer to its bound value in ρ , and returns ρ as the result.

Auxiliary Funcon $\text{bind-to-forward-links}(SI : \text{sets}(\text{identifiers})) : \Rightarrow \text{maps}(\text{identifiers}, \text{links})$
 $\rightsquigarrow \text{map-unite}(\text{interleave-map}(\text{bind-value}(\text{given}, \text{fresh-link}(\text{values})), \text{set-elements}(SI)))$

$\text{bind-to-forward-links}(SI)$ binds each identifier in the set SI to a freshly allocated link.

Auxiliary Funcon $\text{set-forward-links}(M : \text{maps}(\text{identifiers}, \text{links})) : \Rightarrow \text{null-type}$
 $\rightsquigarrow \text{effect}(\text{interleave-map}(\text{set-link}(\text{map-lookup}(M, \text{given}), \text{bound-value}(\text{given})), \text{set-elements}(\text{map-domain}(M))))$

For each identifier I in the domain of M , $\text{set-forward-links}(M)$ sets the link to which I is mapped by M to the current bound value of I .