

# Funcons-beta: Booleans

The P<sub>L</sub>anCompS Project

Funcons-beta/Values/Primitive/Booleans/Booleans.cbs\*

## Booleans

```
[ Datatype booleans
  Alias bools
  Funcon true
  Funcon false
  Funcon not
  Funcon implies
  Funcon and
  Funcon or
  Funcon exclusive-or
  Alias xor ]
```

```
Datatype booleans ::= true
                    | false
```

```
Alias bools = booleans
```

```
Funcon not(_ : booleans) : ⇒ booleans
```

`not(B)` is logical negation.

```
Rule not(false) ⇔ true
```

```
Rule not(true) ⇔ false
```

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\*Suggestions for improvement: [plancomps@gmail.com](mailto:plancomps@gmail.com).  
Issues: <https://github.com/plancomps/CBS-beta/issues>.

*Funcon* `implies`(`_ : bool`, `_ : bool`) : `⇒ bool`

`implies`(`B1`, `B2`) is logical implication.

*Rule* `implies`(`false`, `false`)  $\rightsquigarrow$  `true`

*Rule* `implies`(`false`, `true`)  $\rightsquigarrow$  `true`

*Rule* `implies`(`true`, `true`)  $\rightsquigarrow$  `true`

*Rule* `implies`(`true`, `false`)  $\rightsquigarrow$  `false`

*Funcon* `and`(`_ : bool*`) : `⇒ bool`

`and`(`B, ...`) is logical conjunction of any number of Boolean values.

*Rule* `and`( )  $\rightsquigarrow$  `true`

*Rule* `and`(`false`, `_ : bool*`)  $\rightsquigarrow$  `false`

*Rule* `and`(`true`, `B* : bool*`)  $\rightsquigarrow$  `and`(`B*`)

*Funcon* `or`(`_ : bool*`) : `⇒ bool`

`or`(`B, ...`) is logical disjunction of any number of Boolean values.

*Rule* `or`( )  $\rightsquigarrow$  `false`

*Rule* `or`(`true`, `_ : bool*`)  $\rightsquigarrow$  `true`

*Rule* `or`(`false`, `B* : bool*`)  $\rightsquigarrow$  `or`(`B*`)

*Funcon* `exclusive-or`(`_ : bool`, `_ : bool`) : `⇒ bool`

*Alias* `xor` = `exclusive-or`

`exclusive-or`(`B1`, `B2`) is exclusive disjunction.

*Rule* `exclusive-or`(`false`, `false`)  $\rightsquigarrow$  `false`

*Rule* `exclusive-or`(`false`, `true`)  $\rightsquigarrow$  `true`

*Rule* `exclusive-or`(`true`, `false`)  $\rightsquigarrow$  `true`

*Rule* `exclusive-or`(`true`, `true`)  $\rightsquigarrow$  `false`