## Funcons-beta: Giving

## The PLanCompS Project

 ${\tt Funcons-beta/Computations/Normal/Giving/Giving.cbs}^*$ 

## Giving

```
[ Entity given-value
Funcon initialise-giving
Funcon give
Funcon given
Funcon no-given
Funcon left-to-right-map
Funcon interleave-map
Funcon interleave-repeat
Funcon interleave-repeat
Funcon interleave-filter
Funcon fold-left
Funcon fold-right ]

Meta-variables T, T' <: values T? <: values?

Entity given-value(_: values?) ⊢ _ → _
```

The given-value entity allows a computation to refer to a single previously-computed  $V:\mathsf{values}$ . The given value ( ) represents the absence of a current given value.

Funcon initialise-giving(
$$X:() \Rightarrow T'$$
):()  $\Rightarrow T'$   
 $\rightsquigarrow$  no-given( $X$ )

<sup>\*</sup>Suggestions for improvement: plancomps@gmail.com. Issues: https://github.com/plancomps/CBS-beta/issues.

initialise-giving(X) ensures that the entities used by the funcons for giving are properly initialised.

Funcon give(
$$_{-}: T,_{-}: T \Rightarrow T'$$
):  $\Rightarrow T'$ 

give(X, Y) executes X, possibly referring to the current given value, to compute a value V. It then executes Y with V as the given value, to compute the result.

Rule 
$$\frac{\mathsf{given\text{-}value}(V) \vdash Y \longrightarrow Y'}{\mathsf{given\text{-}value}(\_?) \vdash \mathsf{give}(V:T,Y) \longrightarrow \mathsf{give}(V,Y')}$$
Rule  $\mathsf{give}(\_:T,W:T') \leadsto W$ 

Funcon given :  $T \Rightarrow T$ 

given refers to the current given value.

Rule given-value(
$$V$$
: values)  $\vdash$  given  $\longrightarrow V$   
Rule given-value()  $\vdash$  given  $\longrightarrow$  fail

Funcon no-given(
$$_-:() \Rightarrow T'$$
):()  $\Rightarrow T'$ 

no-given(X) computes X without references to the current given value.

$$\begin{aligned} & \text{Rule } \frac{ \text{given-value( )} \vdash X \longrightarrow X' }{ \text{given-value(\_?)} \vdash \text{no-given}(X) \longrightarrow \text{no-given}(X') } \\ & \text{Rule } \text{no-given}(U:T') \leadsto U \end{aligned}$$

**Mapping** Maps on collection values can be expressed directly, e.g., list(left-to-right-map(F, list-elements(L))).

Funcon left-to-right-map(
$$_{-}: T \Rightarrow T',_{-}: (T)^*$$
):  $\Rightarrow (T')^*$ 

left-to-right-map( $F, V^*$ ) computes F for each value in  $V^*$  from left to right, returning the sequence of resulting values.

```
Rule left-to-right-map(F, V : T, V^* : (T)^*) \leadsto left-to-right(give(V, F), left-to-right-map(F, V^*))
Rule left-to-right-map(F, V^*) \leadsto ( )
```

```
Funcon interleave-map(_{-}: T \Rightarrow T',_{-}: (T)^*): \Rightarrow (T')^*
```

interleave-map $(F, V^*)$  computes F for each value in  $V^*$  interleaved, returning the sequence of resulting values.

```
Rule interleave-map(F, V : T, V^* : (T)^*) \leadsto interleave(give(V, F), interleave-map(F, V^*))
Rule interleave-map(F, V : T, V^* : (T)^*) \leadsto ( )
```

```
Funcon left-to-right-repeat(\_: integers \Rightarrow T', \_: integers, \_: integers): \Rightarrow (T')^*
```

**left-to-right-repeat**(F, M, N) computes F for each value from M to N sequentially, returning the sequence of resulting values.

```
Rule \begin{tabular}{l} \hline & is-less-or-equal(M,N) == true \\ \hline & left-to-right-repeat(F,M:integers,N:integers) \leadsto left-to-right(give(M,F),left-to-right-repeat(F,int-action of the property of
```

Funcon interleave-repeat( $\_:$  integers  $\Rightarrow T', \_:$  integers,  $\_:$  integers):  $\Rightarrow (T')^*$ 

interleave-repeat (F, M, N) computes F for each value from M to N interleaved, returning the sequence of resulting values.

```
Rule \frac{\text{is-less-or-equal}(M,N) == true}{\text{interleave-repeat}(F,M:\text{integers},N:\text{integers}) \leadsto \text{interleave}(\text{give}(M,F),\text{interleave-repeat}(F,\text{int-add}(M,F)))}{\text{is-less-or-equal}(M,N) == \text{false}}{\text{interleave-repeat}(\_,M:\text{integers},N:\text{integers}) \leadsto (\_)}
```

**Filtering** Filters on collections of values can be expressed directly, e.g., list(left-to-right-filter(P, list-elements(L))) to filter a list <math>L.

```
Funcon left-to-right-filter(\_: T \Rightarrow booleans, \_: (T)^*): \Rightarrow (T)^*
```

left-to-right-filter( $P, V^*$ ) computes P for each value in  $V^*$  from left to right, returning the sequence of argument values for which the result is true.

```
Rule left-to-right-filter(P, V : T, V^* : (T)^*) \leadsto left-to-right(when-true(give(V, P), V), left-to-right-filter(P, V : T, V^* : (T)^*) \leadsto left-to-right(when-true(give(V, P), V), left-to-right-filter(P, V : T, V^* : (T)^*) \leadsto ( )
```

```
Funcon interleave-filter(_{-}: T \Rightarrow booleans, _{-}: (T)^*): \Rightarrow (T)^*
```

interleave-filter  $(P, V^*)$  computes P for each value in  $V^*$  interleaved, returning the sequence of argument values for which the result is true.

```
\textit{Rule} \  \, \mathsf{interleave-filter}(P, V: T, V^*: (T)^*) \leadsto \mathsf{interleave}(\mathsf{when-true}(\mathsf{give}(V, P), V), \mathsf{interleave-filter}(P, V^*)) \\ \textit{Rule} \  \, \mathsf{interleave-filter}(\_) \leadsto (\ )
```

## **Folding**

```
Funcon fold-left(\_: tuples(T, T') \Rightarrow T, \_: T, \_: (T')^*): \Rightarrow T
```

 $\mathsf{fold\text{-}left}(F,A,V^*)$  reduces a sequence  $V^*$  to a single value by folding it from the left, using A as the initial accumulator value, and iteratively updating the accumulator by giving F the pair of the accumulator value and the first of the remaining arguments.

```
 \begin{aligned} &\textit{Rule} \;\; \mathsf{fold\text{-}left}(\_, A: T, (\;)) \leadsto A \\ &\textit{Rule} \;\; \mathsf{fold\text{-}left}(F, A: T, V: T', V^*: (T')^*) \leadsto \mathsf{fold\text{-}left}(F, \mathsf{give}(\mathsf{tuple}(A, V), F), V^*) \end{aligned}
```

```
Funcon fold-right(\_: tuples(T, T') \Rightarrow T', \_: T', \_: (T)^*): \Rightarrow T'
```

 $\mathsf{fold\text{-}right}(F,A,V^*)$  reduces a sequence  $V^*$  to a single value by folding it from the right, using A as the initial accumulator value, and iteratively updating the accumulator by giving F the pair of the the last of the remaining arguments and the accumulator value.

```
Rule fold-right(\_, A: T', ()) \leadsto A
Rule fold-right(F, A: T', V^*: (T)^*, V: T) \leadsto give(tuple(V, fold-right(F, A, V^*)), F)
```