

# Funcons-beta: Functions

The PPlanCompS Project

Funcons-beta/Values/Abstraction/Functions/Functions.cbs\*

## Functions

```
[ Datatype functions
  Funcon function
  Funcon apply
  Funcon supply
  Funcon compose
  Funcon uncurry
  Funcon curry
  Funcon partial-apply ]
```

Meta-variables  $T, T', T_1, T_2 <: \text{values}$

Datatype `functions`( $T, T'$ ) ::= `function`( $A : \text{abstractions}(T \Rightarrow T')$ )

`functions`( $T, T'$ ) consists of abstractions whose bodies may depend on a given value of type  $T$ , and whose executions normally compute values of type  $T'$ . `function`(`abstraction`( $X$ )) evaluates to a function with dynamic bindings, `function`(`closure`( $X$ )) computes a function with static bindings.

Funcon `apply`( $_ : \text{functions}(T, T'), _ : T$ ) :  $\Rightarrow T'$

`apply`( $F, V$ ) applies the function  $F$  to the argument value  $V$ . This corresponds to call by value; using thunks as argument values corresponds to call by name. Moreover, using tuples as argument values corresponds to application to multiple arguments.

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\*Suggestions for improvement: [plancomps@gmail.com](mailto:plancomps@gmail.com).  
Issues: <https://github.com/plancomps/CBS-beta/issues>.

Rule  $\text{apply}(\text{function}(\text{abstraction}(X)), V : T) \rightsquigarrow \text{give}(V, X)$

Funcon  $\text{supply}(- : \text{functions}(T, T'), - : T) : \Rightarrow \text{thunks}(T')$

$\text{supply}(F, V)$  determines the argument value of a function application, but returns a thunk that defers executing the body of the function.

Rule  $\text{supply}(\text{function}(\text{abstraction}(X)), V : T) \rightsquigarrow \text{thunk}(\text{abstraction}(\text{give}(V, X)))$

Funcon  $\text{compose}(- : \text{functions}(T_2, T'), - : \text{functions}(T_1, T_2)) : \Rightarrow \text{functions}(T_1, T')$

$\text{compose}(F_2, F_1)$  returns the function that applies  $F_1$  to its argument, then applies  $F_2$  to the result of  $F_1$ .

Rule  $\text{compose}(\text{function}(\text{abstraction}(Y)), \text{function}(\text{abstraction}(X))) \rightsquigarrow \text{function}(\text{abstraction}(\text{give}(X, Y)))$

Funcon  $\text{uncurry}(F : \text{functions}(T_1, \text{functions}(T_2, T'))) : \Rightarrow \text{functions}(\text{tuples}(T_1, T_2), T')$   
 $\rightsquigarrow \text{function}(\text{abstraction}(\text{apply}(\text{apply}(F,$   
 $\quad \text{checked index}(1,$   
 $\quad \quad \text{tuple-elements given}))),$   
 $\quad \text{checked index}(2,$   
 $\quad \quad \text{tuple-elements given}))))$

$\text{uncurry}(F)$  takes a curried function  $F$  and returns a function that takes a pair of arguments..

Funcon  $\text{curry}(F : \text{functions}(\text{tuples}(T_1, T_2), T')) : \Rightarrow \text{functions}(T_1, \text{functions}(T_2, T'))$   
 $\rightsquigarrow \text{function}(\text{abstraction}(\text{partial-apply}(F,$   
 $\quad \text{given}))))$

$\text{curry}(F)$  takes a function  $F$  that takes a pair of arguments, and returns the corresponding ‘curried’ function.

Funcon  $\text{partial-apply}(F : \text{functions}(\text{tuples}(T_1, T_2), T'), V : T_1) : \Rightarrow \text{functions}(T_2, T')$   
 $\rightsquigarrow \text{function}(\text{abstraction}(\text{apply}(F,$   
 $\quad \text{tuple}(V,$   
 $\quad \quad \text{given}))))$

$\text{partial-apply}(F, V)$  takes a function  $F$  that takes a pair of arguments, and determines the first argument, returning a function of the second argument.