

# Languages-beta: OC-L-07-Expressions \*

The P<sub>L</sub>anCompS Project

OC-L-07-Expressions.cbs | PLAIN | PRETTY

## OUTLINE

### **7 Expressions**

Expression sequences and maps

Matching

Value definitions

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*Language* "OCaml Light"

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\*Suggestions for improvement: [plancomps@gmail.com](mailto:plancomps@gmail.com).  
Reports of issues: <https://github.com/plancomps/CBS-beta/issues>.

## 7 Expressions

*Syntax*  $E : \text{expr} ::=$

- $\text{value-path}$
- $\text{constant}$
- $(' \text{ expr }')$
- $\text{'begin' expr 'end'}$
- $(' \text{ expr } : \text{ typexpr }')$
- $\text{expr comma-expr}^+$
- $\text{expr } : : \text{ expr}$
- $[ \text{ expr } \text{ semic-expr}^* ]$
- $[ \text{ expr } \text{ semic-expr}^* ; ]$
- $[ [ \text{ expr } \text{ semic-expr}^* ] ]$
- $[ [ \text{ expr } \text{ semic-expr}^* ; ] ]$
- $\{ \text{ field } = \text{ expr } \text{ semic-field-expr}^* \}$
- $\{ \text{ field } = \text{ expr } \text{ semic-field-expr}^* ; \}$
- $\{ \text{ expr } \text{'with' field } = \text{ expr } \text{ semic-field-expr}^* \}$
- $\{ \text{ expr } \text{'with' field } = \text{ expr } \text{ semic-field-expr}^* ; \}$
- $\text{expr argument}^+$
- $\text{prefix-symbol expr}$
- $- \text{ expr}$
- $- . \text{ expr}$
- $\text{expr infix-op-1 expr}$
- $\text{expr infix-op-2 expr}$
- $\text{expr infix-op-3 expr}$
- $\text{expr infix-op-4 expr}$
- $\text{expr infix-op-5 expr}$
- $\text{expr infix-op-6 expr}$
- $\text{expr infix-op-7 expr}$
- $\text{expr infix-op-8 expr}$
- $\text{expr } . \text{ field}$
- $\text{expr } . ( \text{ expr } )$
- $\text{expr } . ( \text{ expr } ) <- \text{ expr}$
- $\text{'if' expr 'then' expr ('else' expr)?}$
- $\text{'while' expr 'do' expr 'done'}$
- $\text{'for' value-name } = \text{ expr ('to' | 'downto') expr 'do' expr 'done'}$
- $\text{expr } ; \text{ expr}$
- $\text{'match' expr 'with' pattern-matching}$
- $\text{'function' pattern-matching}$
- $\text{'fun' pattern}^+ \text{'->' expr}$
- $\text{'try' expr 'with' pattern-matching}$
- $\text{let-definition 'in' expr}$
- $\text{'assert' expr}$

$A : \text{argument} ::= \text{expr}$

$PM : \text{pattern-matching} ::=$

- $\text{pattern '->' expr pattern-expr}^*$
- $| \text{'|' pattern '->' expr pattern-expr}^*$

$LD : \text{let-definition} ::= \text{'let' ('rec')? let-binding and-let-binding}^*$

$LB : \text{let-binding} ::=$

- $\text{pattern } = \text{expr}$
- $| \text{value-name pattern}^+ = \text{expr}$
- $| \text{value-name } : \text{ poly-typexpr } = \text{expr}$

$ALB : \text{and-let-binding} ::= \text{'and' let-binding}$

$CE : \text{comma-expr} ::= , \text{ expr}$

$SE : \text{semic-expr} ::= ; \text{ expr}$

Rule  $\llbracket ' ( E ) ' \rrbracket : \text{expr} = \llbracket E \rrbracket$   
 Rule  $\llbracket \text{'begin' } E \text{ 'end' } \rrbracket : \text{expr} = \llbracket E \rrbracket$   
 Rule  $\llbracket ' ( E : T ) ' \rrbracket : \text{expr} = \llbracket E \rrbracket$   
 Rule  $\llbracket E_1 E_2 A A^* \rrbracket : \text{expr} = \llbracket ( ( E_1 E_2 ) ) A A^* \rrbracket$   
 Rule  $\llbracket PS E \rrbracket : \text{expr} = \llbracket ( ( PS ) ) E \rrbracket$   
 Rule  $\llbracket - E \rrbracket : \text{expr} = \llbracket ( ( \sim - ) ) E \rrbracket$   
 Rule  $\llbracket -. E \rrbracket : \text{expr} = \llbracket ( ( \sim -. ) ) E \rrbracket$   
 Rule  $\llbracket E_1 IO-1 E_2 \rrbracket : \text{expr} = \llbracket ( ( IO-1 ) ) E_1 E_2 \rrbracket$   
 Rule  $\llbracket E_1 IO-2 E_2 \rrbracket : \text{expr} = \llbracket ( ( IO-2 ) ) E_1 E_2 \rrbracket$   
 Rule  $\llbracket E_1 IO-3 E_2 \rrbracket : \text{expr} = \llbracket ( ( IO-3 ) ) E_1 E_2 \rrbracket$   
 Rule  $\llbracket E_1 IO-4 E_2 \rrbracket : \text{expr} = \llbracket ( ( IO-4 ) ) E_1 E_2 \rrbracket$   
 Rule  $\llbracket E_1 IO-5 E_2 \rrbracket : \text{expr} = \llbracket ( ( IO-5 ) ) E_1 E_2 \rrbracket$   
 Rule  $\llbracket E_1 \& E_2 \rrbracket : \text{expr} = \llbracket E_1 \&\& E_2 \rrbracket$   
 Rule  $\llbracket E_1 \text{'or' } E_2 \rrbracket : \text{expr} = \llbracket E_1 || E_2 \rrbracket$   
 Rule  $\llbracket E_1 IO-8 E_2 \rrbracket : \text{expr} = \llbracket ( ( IO-8 ) ) E_1 E_2 \rrbracket$   
 Rule  $\llbracket E_1 . ( E_2 ) \rrbracket : \text{expr} = \llbracket \text{'array\_get' } E_1 E_2 \rrbracket$   
 Rule  $\llbracket E_1 . ( E_2 ) <- E_3 \rrbracket : \text{expr} = \llbracket \text{'array\_set' } E_1 E_2 E_3 \rrbracket$   
 Rule  $\llbracket \text{'if' } E_1 \text{'then' } E_2 \rrbracket : \text{expr} = \llbracket \text{'if' } E_1 \text{'then' } E_2 \text{'else' } ( ( ) ) \rrbracket$   
 Rule  $\llbracket \text{'fun' } P \text{'->' } E \rrbracket : \text{expr} = \llbracket \text{'function' } P \text{'->' } E \rrbracket$   
 Rule  $\llbracket \text{'fun' } P P^+ \text{'->' } E \rrbracket : \text{expr} = \llbracket \text{'fun' } P \text{'->' } ( \text{'fun' } P^+ \text{'->' } E ) \rrbracket$   
 Rule  $\llbracket [ E SE^* ; ' ] \rrbracket : \text{expr} = \llbracket [ E SE^* ] \rrbracket$   
 Rule  $\llbracket [ | E SE^* ; ' | ] \rrbracket : \text{expr} = \llbracket [ | E SE^* | ] \rrbracket$   
 Rule  $\llbracket \{ F = E SFE^* ; ' \} \rrbracket : \text{expr} = \llbracket \{ F = E SFE^* \} \rrbracket$   
 Rule  $\llbracket \{ E_1 \text{'with' } F = E_2 SFE^* ; ' \} \rrbracket : \text{expr} =$   
 $\llbracket \{ E_1 \text{'with' } F = E_2 SFE^* \} \rrbracket$   
 Rule  $\llbracket | P \text{'->' } E PE^* \rrbracket : \text{pattern-matching} = \llbracket P \text{'->' } E PE^* \rrbracket$   
 Rule  $\llbracket VN : PT = E \rrbracket : \text{let-binding} = \llbracket VN = E \rrbracket$   
 Rule  $\llbracket VN P^+ = E \rrbracket : \text{let-binding} = \llbracket VN = ( \text{'fun' } P^+ \text{'->' } E ) \rrbracket$

Semantics  $\text{evaluate}[\_ : \text{expr}] : \Rightarrow \text{implemented-values}$

Rule  $\text{evaluate}[VP] = \text{bound}(\text{value-name}[VP])$

Rule  $\text{evaluate}[CNST] = \text{value}[CNST]$

Rule  $\text{evaluate}['( E ':' T ')'] = \text{evaluate}[E]$

Rule  $\text{evaluate}[E_1 ', ' E_2 CE^*] =$   
 $\text{tuple}(\text{evaluate-comma-sequence}[E_1 ', ' E_2 CE^*])$

Rule  $\text{evaluate}[E_1 ':' E_2] = \text{cons}(\text{evaluate}[E_1], \text{evaluate}[E_2])$

Rule  $\text{evaluate}['[ E SE^* ']'] = [\text{evaluate-semic-sequence}[E SE^*]]$

Rule  $\text{evaluate}['[| E SE^* |']'] =$   
 $\text{vector}(\text{left-to-right-map}(\text{allocate-initialised-variable}(\text{implemented-values}, \text{given}), \text{evaluate-semic-sequence}[E SE^*]))$

Rule  $\text{evaluate}['[| ' |']'] = \text{vector}()$

Rule  $\text{evaluate}['\{ F '=' E SFE^* \}'] =$   
 $\text{record}(\text{collateral}(\text{evaluate-field-sequence}[F '=' E SFE^*]))$

Rule  $\text{evaluate}['\{ E_1 \text{'with'} F '=' E_2 SFE^* \}'] =$   
 $\text{record}(\text{map-override}(\text{evaluate-field-sequence}[F '=' E_2 SFE^*], \text{checked record-map}(\text{evaluate}[E_1])))$

Rule  $\text{evaluate}[CSTR E] =$   
 $\text{variant}(\text{constr-name}[CSTR], \text{evaluate}[E])$

Otherwise  $\text{evaluate}[E_1 E_2] =$   
 $\text{apply}(\text{evaluate}[E_1], \text{evaluate}[E_2])$

Rule  $\text{evaluate}[E '.' F] =$   
 $\text{record-select}(\text{evaluate}[E], \text{field-name}[F])$

Rule  $\text{evaluate}[E_1 '\&\&' E_2] =$   
 $\text{if-true-else}(\text{evaluate}[E_1], \text{evaluate}[E_2], \text{false})$

Rule  $\text{evaluate}[E_1 '||' E_2] =$   
 $\text{if-true-else}(\text{evaluate}[E_1], \text{true}, \text{evaluate}[E_2])$

Rule  $\text{evaluate}['\text{if } E_1 \text{'then'} E_2 \text{'else'} E_3] =$   
 $\text{if-true-else}(\text{evaluate}[E_1], \text{evaluate}[E_2], \text{evaluate}[E_3])$

Rule  $\text{evaluate}['\text{while } E_1 \text{'do'} E_2 \text{'done'}] =$   
 $\text{while}(\text{evaluate}[E_1], \text{effect}(\text{evaluate}[E_2]))$

Rule  $\text{evaluate}['\text{for } VN '=' E_1 \text{'to'} E_2 \text{'do'} E_3 \text{'done'}] =$   
 $\text{effect}(\text{left-to-right-map}(\text{case-match}(\text{pattern-bind}(\text{value-name}[VN]), \text{evaluate}[E_3]), \text{integer-sequence}(\text{evaluate}[E_1], \text{evaluate}[E_2])))$

Rule  $\text{evaluate}['\text{for } VN '=' E_1 \text{'downto'} E_2 \text{'do'} E_3 \text{'done'}] =$   
 $\text{effect}(\text{left-to-right-map}(\text{case-match}(\text{pattern-bind}(\text{value-name}[VN]), \text{evaluate}[E_3]), \text{reverse integer-sequence}(\text{evaluate}[E_2], \text{evaluate}[E_1])))$

Rule  $\text{evaluate}[E_1 ';' E_2] =$   
 $\text{sequential}(\text{effect}(\text{evaluate}[E_1]), \text{evaluate}[E_2])$

Rule  $\text{evaluate}['\text{match } E \text{'with'} PM] =$   
 $\text{give}(\text{evaluate}[E], \text{else}(\text{match}[PM], \text{throw}(\text{qcaml-light-match-failure})))$

Rule  $\text{evaluate}['\text{function } PM] =$   
 $\text{function closure}(\text{evaluate}[PM], \text{value-name}[PM])$

## Expression sequences and maps

*Semantics*  $\text{evaluate-comma-sequence}[\_ : (\text{expr comma-expr}^*)] : (\Rightarrow \text{implemented-values})^+$

*Rule*  $\text{evaluate-comma-sequence}[E_1 \text{ ',' } E_2 \text{ CE}^*] =$   
 $\text{evaluate}[E_1], \text{evaluate-comma-sequence}[E_2 \text{ CE}^*]$

*Rule*  $\text{evaluate-comma-sequence}[E] = \text{evaluate}[E]$

*Semantics*  $\text{evaluate-semicolon-sequence}[\_ : (\text{expr semic-expr}^*)] : (\Rightarrow \text{implemented-values})^+$

*Rule*  $\text{evaluate-semicolon-sequence}[E_1 \text{ ';' } E_2 \text{ SE}^*] =$   
 $\text{evaluate}[E_1], \text{evaluate-semicolon-sequence}[E_2 \text{ SE}^*]$

*Rule*  $\text{evaluate-semicolon-sequence}[E] = \text{evaluate}[E]$

*Semantics*  $\text{evaluate-field-sequence}[\_ : (\text{field '=' expr semic-field-expr}^*)] : (\Rightarrow \text{envs})^+$

*Rule*  $\text{evaluate-field-sequence}[F_1 \text{ '=' } E_1 \text{ ';' } F_2 \text{ '=' } E_2 \text{ SFE}^*] =$   
 $\{\text{field-name}[F_1] \mapsto \text{evaluate}[E_1]\},$   
 $\text{evaluate-field-sequence}[F_2 \text{ '=' } E_2 \text{ SFE}^*]$

*Rule*  $\text{evaluate-field-sequence}[F \text{ '=' } E] = \{\text{field-name}[F] \mapsto \text{evaluate}[E]\}$

## Matching

*Semantics*  $\text{match}[\_ : \text{pattern-matching}] : (\text{implemented-values} \Rightarrow \text{implemented-values})^+$

*Rule*  $\text{match}[P_1 \text{ '->' } E_1 \text{ ' | ' } P_2 \text{ '->' } E_2 \text{ PE}^*] =$   
 $\text{match}[P_1 \text{ '->' } E_1], \text{match}[P_2 \text{ '->' } E_2 \text{ PE}^*]$

*Rule*  $\text{match}[P \text{ '->' } E] = \text{case-match}(\text{evaluate-pattern}[P], \text{evaluate}[E])$

## Value definitions

*Semantics*  $\text{define-values}[\_ : \text{let-definition}] : \Rightarrow \text{environments}$

*Rule*  $\text{define-values}[\text{'let' } LB \text{ ALB}^*] = \text{define-values-nonrec}[LB \text{ ALB}^*]$

*Rule*  $\text{define-values}[\text{'let rec' } LB \text{ ALB}^*] =$   
 $\text{recursive}(\text{set}(\text{bound-ids-sequence}[LB \text{ ALB}^*]),$   
 $\text{define-values-nonrec}[LB \text{ ALB}^*])$

*Semantics*  $\text{define-values-nonrec}[\_ : (\text{let-binding and-let-binding}^*)] : \Rightarrow \text{environments}$

*Rule*  $\text{define-values-nonrec}[LB_1 \text{ 'and' } LB_2 \text{ ALB}^*] =$   
 $\text{collateral}(\text{define-values-nonrec}[LB_1], \text{define-values-nonrec}[LB_2 \text{ ALB}^*])$

*Rule*  $\text{define-values-nonrec}[P \text{ '=' } E] =$   
 $\text{else}(\text{match}(\text{evaluate}[E], \text{evaluate-pattern}[P]),$   
 $\text{throw}(\text{ocaml-light-match-failure}))$

*Semantics*  $\text{bound-ids-sequence}[\_ : (\text{let-binding and-let-binding}^*)] : \text{ids}^+$

*Rule*  $\text{bound-ids-sequence}[LB] = \text{bound-id}[LB]$

*Rule*  $\text{bound-ids-sequence}[LB_1 \text{ 'and' } LB_2 \text{ ALB}^*] =$   
 $\text{bound-id}[LB_1], \text{bound-ids-sequence}[LB_2 \text{ ALB}^*]$

*Semantics*  $\text{bound-id}[\_ : \text{let-binding}] : \text{ids}$

*Rule*  $\text{bound-id}[VN \text{ '=' } E] = \text{value-name}[VN]$

*Otherwise*  $\text{bound-id}[LB] = \text{fail}$