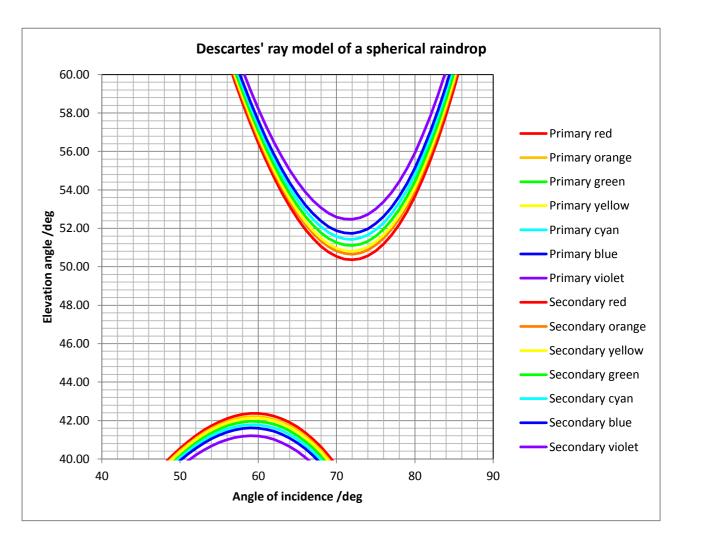
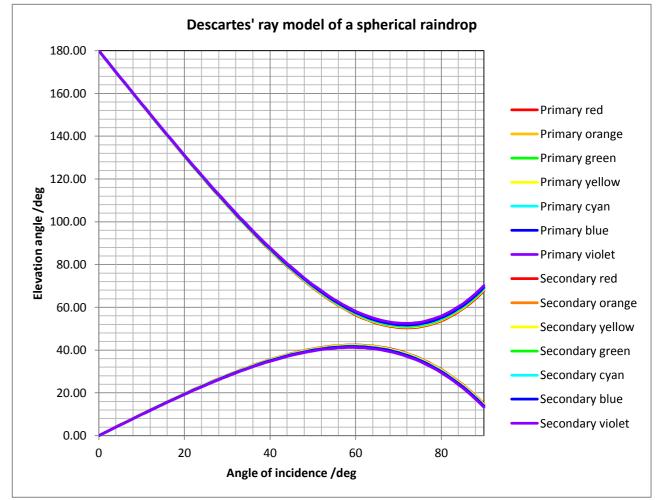
DESCARTES' MODEL OF A RAINBOW

Dr Andrew French. July 2020

SECONDARY BOW **PRIMARY BOW** Orange Yellow Violet Violet Red Green Cyan Blue Red Orange Yellow Green Cyan Blue f/THz f/THz 610 1.3327 1.3350 1.3362 1.3390 1.3321 1.3327 1.3350 1.3362 1.3390 n theta theta epsilon /deg /rad /deg 180.00 0.00 0.02 177.50 177.51 177.51 177.52 0.0 175.00 175.02 175.04 175.01 172.53 172.50 72.51 172.52 172.56 Parallel rays of incident sunlight 0.0 0.0 170.00 70.01 170.03 170.05 170.08 67.52 167.61 167.54 167.56 'Anti solar 0.1 0.1 165.01 65.03 165.06 165.08 165.14 Rain direction' Sun cloud 162.60 162.52 62.55 162.57 0.1 160.13 160.21 160.03 60.06 160.10 157.55 157.63 157.66 157.75 57.59 155.29 55.12 155.20 Rainbow 0.1 0.2 0.2 0.2 0.2 0.3 0.3 0.3 152.61 52.65 152.70 152.74 152.85 50.19 150.24 150.29 ${\cal E}$ 13 147.69 147.74 147.80 147.85 147.97 14 145.41 145.55 145.25 145.30 145.36 142.81 142.87 142.93 142.99 143.13 Horizon Elevation of Sun Observer 140.38 L40.44 140.51 140.57 140.73 above horizon 138.03 138.10 138.17 18 135.62 135.70 135.77 135.94 19 133.39 133.16 133.23 133.31 20 Elevation of deflected beam /deg Primary ε =40.9° to ,42.5°, Secondary ε =50.2° to 53° spherical 22 water droplet 180 23 0.40 24 0.42 160 25 $\varepsilon = \pi - 6\sin^{-1}\left(\frac{\sin\theta}{n}\right) + 2\theta$ 0.44 23.75 23.59 24.44 26 0.45 140 0.47 25.27 0.49 26.10 120 29 0.51 26.91 30 0.52 27.90 27.70 00 100 β 100 80 0.54 28.48 31 32 0.56 29.25 33 0.58 30.00 34 0.59 30.73 60 31.45 35 0.61 31.68 0.63 40 37 0.65 32.83 38 33.49 0.66 20 39 0.68 34.13 $\theta = \sin^2\theta$ $\varepsilon = 4 \sin^2 \theta$ 40 0.70 35.02 34.75 RENE DESCARTES 1596-1650 0.72 20 60 80 40 42 0.73 35.92 θ /deg 43 0.75 37.12 0.77 37.29 37.66 37.42 37.00 79.50 79.87 80.06 0.79 77.64 45 38.24 38.18 37.93 37.80 37.50 77.73 78.11 78.30 0.82 39.13 38.87 38.42 74.20 74.30 74.49 74.70 74.90 0.84 39.64 39.57 39.30 39.16 72.65 72.84 73.05 73.26 0.86 40.04 39.97 39.69 39.56 70.94 71.04 71.24 71.46 71.67 40.42 69.48 0.87 40.35 40.06 39.58 69.68 69.91 70.12 0.89 40.40 40.76 67.86 67.97 68.18 68.40 68.62 40.69 40.25 39.91 69.14 0.91 41.07 41.00 40.70 40.55 40.20 66.40 66.51 66.72 66.95 67.17 0.93 41.34 41.27 41.13 40.97 40.82 40.46 64.98 65.10 65.31 65.55 65.78 0.94 41.58 41.51 41.36 41.20 41.04 63.62 63.74 64.20 64.43 62.44 0.96 41.56 41.39 62.66 62.91 63.14 41.55 61.07 61.19 61.42 62.49 41.95 41.87 41.01 61.67 42.00 59.88 60.24 0.99 42.08 41.67 41.51 41.12 60.01 60.50 60.74 61.33





58	1.01	42.32	42.16	42.08	41.92	41.75	41.58	41.18
59	1.03	42.36	42.20	42.12	41.96	41.78	41.61	41.21
60	1.05	42.37	42.20	42.12	41.95	41.77	41.60	41.19
61	1.06	42.32	42.15	42.07	41.90	41.72	41.54	41.12
62	1.08	42.23	42.06	41.97	41.80	41.62	41.44	41.01
63	1.10	42.09	41.92	41.83	41.66	41.47	41.28	40.85
64	1.12	41.90	41.73	41.64	41.46	41.27	41.08	40.64
65	1.13	41.66	41.49	41.39	41.21	41.02	40.83	40.39
66	1.15	41.37	41.19	41.10	40.92	40.72	40.53	40.07
67	1.17	41.03	40.84	40.75	40.56	40.36	40.17	39.71
68	1.19	40.62	40.44	40.34	40.15	39.95	39.75	39.29
69	1.20	40.16	39.97	39.88	39.69	39.48	39.28	38.81
70	1.22	39.64	39.45	39.35	39.16	38.95	38.75	38.27
71	1.24	39.07	38.87	38.77	38.58	38.37	38.16	37.68
72	1.26	38.42	38.23	38.13	37.93	37.72	37.51	37.02
73	1.27	37.72	37.52	37.42	37.22	37.00	36.79	36.30
74	1.29	36.95	36.75	36.65	36.45	36.23	36.02	35.52
75	1.31	36.11	35.91	35.81	35.60	35.38	35.17	34.66
76	1.33	35.21	35.01	34.90	34.70	34.47	34.26	33.75
77	1.34	34.24	34.03	33.93	33.72	33.49	33.28	32.76
78	1.36	33.20	32.99	32.88	32.67	32.44	32.23	31.71
79	1.38	32.08	31.87	31.76	31.55	31.32	31.10	30.58
80	1.40	30.89	30.68	30.57	30.36	30.13	29.91	29.38
81	1.41	29.63	29.42	29.31	29.10	28.86	28.64	28.11
82	1.43	28.30	28.08	27.97	27.76	27.52	27.30	26.77
83	1.45	26.88	26.67	26.56	26.34	26.11	25.88	25.35
84	1.47	2 5.39	25.18	25.07	24.85	24.62	24.39	23.85
85	1.48	23.83	23.61	23.50	23.28	23.05	22.82	22.28
86	1.50	22.18	21.97	21.86	21.64	21.40	21.17	20.63
87	1.52	20.46	20.24	20.13	19.91	19.67	19.45	18.90
88	1.54	18.66	18.44	18.33	18.11	17.87	17.64	17.10
89	1.55	16.78	16.56	16.45	16.23	15.99	15.76	15.22
90	1.57	14.82	14.60	14.49	14.27	14.03	13.80	13.26

58.52	58.76	58.88	59.12	59.38	59.63	60.23
57.45	57.69	57.82	58.06	58.33	58.58	59.19
56.45	56.70	56.83	57.07	57.34	57.60	58.22
55.52	55.77	55.90	56.15	56.42	56.69	57.32
54.65	54.91	55.04	55.30	55.58	55.84	56.48
53.86	54.12	54.25	54.51	54.80	55.07	55.72
53.14	53.41	53.54	53.81	54.10	54.37	55.03
52.50	52.77	52.91	53.18	53.47	53.75	54.42
51.94	52.21	52.35	52.63	52.92	53.21	53.89
51.46	51.74	51.88	52.16	52.46	52.75	53.44
51.07	51.34	51.49	51.77	52.08	52.37	53.07
50.76	51.04	51.18	51.47	51.78	52.08	52.78
50.53	50.82	50.97	51.26	51.57	51.87	52.59
50.40	50.69	50.84	51.13	51.45	51.76	52.48
50.36	50.66	50.81	51.10	51.43	51.74	52.47
50.42	50.72	50.87	51.17	51.49	51.81	52.55
50.57	50.87	51.03	51.33	51.66	51.98	52.73
50.83	51.13	51.29	51.59	51.93	52.25	53.00
51.18	51.49	51.65	51.96	52.29	52.61	53.38
51.64	51.95	52.11	52.42	52.76	53.09	53.86
52.21	52.52	52.68	52.99	53.33	53.66	54.44
52.88	53.19	53.36	53.67	54.01	54.35	55.13
53.66	53.98	54.14	54.46	54.80	55.14	55.93
54.55	54.87	55.04	55.35	55.70	56.04	56.83
55.56	55.88	56.04	56.36	56.71	57.05	57.85
56.67	57.00	57.16	57.49	57.84	58.18	58.98
57.91	58.23	58.40	58.72	59.08	59.42	60.22
59.26	59.58	59.75	60.08	60.43	60.77	61.58
60.72	61.05	61.22	61.54	61.90	62.24	63.06
62.31	62.63	62.80	63.13	63.49	63.83	64.65
64.01	64.34	64.51	64.83	65.19	65.54	66.35
65.83	66.16	66.33	66.66	67.01	67.36	68.18
67.77	68.10	68.27	68.60	68.96	69.30	70.12