

Tutorial Sheet - 1

3.

a) Twin Prime Conjecture:

$$\forall n \in \mathbb{N}, \exists x \in \mathbb{N}, x \geq n : p(x) \wedge p(x+2)$$

Negation of Twin Prime Conjecture:

$$\exists n \in \mathbb{N} : \forall x \in \mathbb{N}, x \geq n \quad p(x) \Rightarrow \neg p(x+2)$$

b) Bertrand's Postulate:

$$\forall n \in \mathbb{N}, \exists x \in \mathbb{N}, n < x \leq 2n : p(x)$$

c)  $\forall n \in \mathbb{N}, \exists x \in \mathbb{N}, x \geq n : p(x) \wedge \forall i \in \{0, 1, \dots, \lfloor \log_{10} x \rfloor\}$

$$\left\lfloor \frac{x}{10^i} \right\rfloor \% 10 \neq 7$$