

Name: \_\_\_\_\_

Entry number: \_\_\_\_\_

There are 2 questions for a total of 10 points.

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1. (5 points) Prove or disprove:  $[-1, 1]$  has the same cardinality as  $(1, 3) \cup (4, 6)$ .

2. Let  $A, B, C$  be non-empty sets, and let  $g : A \rightarrow B$  and  $h : A \rightarrow C$  and let  $f : A \rightarrow B \times C$  defined as:

$$f(x) = (g(x), h(x)).$$

Answer the following:

- (a) ( $\frac{1}{2}$  point) State true or false: If  $f$  is onto, then both  $g$  and  $h$  are onto.

(a) \_\_\_\_\_

- (b) ( $\frac{1}{2}$  point) State true or false: If  $g$  and  $h$  are onto, then  $f$  is onto.

(b) \_\_\_\_\_

- (c) ( $\frac{1}{2}$  point) State true or false: If at least one of  $g, h$  is one-to-one, then  $f$  is one-to-one.

(c) \_\_\_\_\_

- (d) ( $\frac{1}{2}$  point) State true or false: If  $g$  and  $h$  are not one-to-one, then  $f$  is not one-to-one.

(d) \_\_\_\_\_

- (e) (3 points) Give reasons for your answer to part (b).