CS-345/M45 Lab Class 2

Release date: 09/02/2021Due date: 11am 23/02/2021

This lab is about utilizing unsupervised learning to cluster data from the Fisher Iris dataset. We will be implementing the k-means and GMM clustering algorithms on some example data by adding our own code to a Jupyter notebook. Packages used in this lab are: numpy, matplotlib, and scikit-learn.

Create a new Jupyter Notebook, titled ClusteringNotebook.ipynb to complete this labtask. Again, use markdown to annotate your notebook as required.

\square Task 2.1 – Fisher Iris Dataset

The first task is to get used to the provided dataset and explore the observed features. Both the data and labels are contained within numpy arrays in the available files on Canvas.

- Download Iris_data.npy and Iris_labels.npy from Canvas, and place them in our working directory.
- Load the data using numpy, storing them in appropriate variables.
- Use Markdown above where you load the data, providing annotation describing the dataset. How many samples? What features? What does Iris_labels.npy contain?
- Visualise Iris_data with a matplotlib scatter plot, using Iris_labels to color the scatter plot (hint: check the API of matplotlib's scatter function). Remember we can only plot two of the features against eachother for the moment. Don't forget to label your axes and give the plot a title.

\square Task 2.2 – k-Means

The second task is to cluster our data with k-means, using unsupervised clustering to attempt to identify groupings within the data in a data-driven way. We will use **all of the feature dimensions** within the Iris dataset in order to cluster the observations we have into k clusters.

- Create a new Markdown cell explaining the code that is to follow.
- Initialize an instance of a scikit-learn KMeans class. To do so, you will need to import KMeans from sklearn.cluster.
- Fit the model to Iris_data (hint: check the API for the fit() function).
- Predict the cluster membership of the samples within Iris_data (hint: check the API for the predict() function).
- Produce a scatter plot from the results of the prediction. Note here that our predicted cluster IDs are unsupervised, so will not necessarily map to the same IDs within Iris_labels.
- Add the k cluster centroids of the model to your plot (hint: check the attributes within a KMeans object and use plt.scatter()).
- Go back and tweak your KMeans model. Consider the API and what arguments you could use to produce a better clustering model. Re-run your cells to see if it improves.

☐ Task 2.3 – Gaussian Mixture Models

The third task is to cluster our Fisher Iris data with a GMM. For this task, we will implement the GMM algorithm in our notebook using the GaussianMixture class of scikit-learn, clustering our data with the posterior probabilities of g Gaussian distributions. We will again use all of the available features.

- Create a new Markdown cell explaining the code that is to follow.
- Create a code cell, in which you initialize an instance of a scikit-learn GaussianMixture class. To do so, you will need to import GaussianMixture from sklearn.mixture.
- Fit the model to Iris_data (hint: check the API for the fit() function).
- Predict the cluster membership of the samples within Iris_data (hint: check the API for the predict() function).
- Produce a scatter plot from the results of the prediction. Note here that our predicted cluster IDs are unsupervised, so will not necessarily map to the labels within Iris_labels.
- Add the g gaussian means of the model to your plot (hint: check the attributes within a GaussianMixture object and use plt.scatter()).
- Predict the posterior probability of each component (Gaussian) given the observed data within Iris_data (hint: check the API for the predict_proba() function).
- Produce a scatter plot **for each component** of the GMM model. Within each scatter plot, plot the component's posterior probabilities as the color intensity for each sample. This should result in g different plots. Provide appropriate labels and titles for your plots. Add a colorbar to each plot.
- Go back and tweak your GaussianMixture model. Consider the API and what arguments you can use to produce a better clustering model. Re-run your cells to see if it improves.

\Box Challenge Task 2.4

K-Means utilises the following equation to iteratively update the cluster membership of the training data, updating the position of the k cluster centroids through a repetition of assignment and update steps. The following describes the function to be minimised:

$$\sum_{j=1}^k \sum_{\mathbf{x} \in C_j} \operatorname{dist}(\mathbf{x}, \mathbf{m}_j)^2$$

GMMs utilise the following equations to achieve their clustering, this time by iteratively repeating Expectation and Maximisation steps. The following describe the update of the GMM parameters for the mixing coefficient, the Gaussian μ s, and the posterior probability covariance matrix:

$$P(j)^{new} = \frac{1}{N} \sum_{n=0}^{N} p^{old}(j|x^n)$$
(1)

$$\mu_j^{new} = \frac{\sum_n^N p^{old}(j|x^n)x^n}{\sum_n^N p^{old}(j|x^n)} \tag{2}$$

$$\sum_{j}^{new} = \frac{\sum_{n}^{N} p^{old}(j|x^{n})(x^{n} - \mu_{j}^{new})(x^{n} - \mu_{j}^{new})^{T}}{\sum_{n}^{N} p^{old}(j|x^{n})}$$
(3)

On Canvas you will find the jupyter notebook ClusteringFromScratch.ipynb. Download this file and have a look inside. Correlate this with your notes from the lectures. Identify where in the code these equations are being implemented.

Consider why it appears the GMM implemented from scratch performs worse than the Gaussian-Mixture model from scikit-learn. Hint: Check out the API and the <code>init_params</code> argument. How could we change our implementation to match the default in scikit-learn's <code>GaussianMixture</code>?