

Exercises about representation of information

Add a few explanations to demonstrate how to perform each conversion. For example, from decimal to binary we use powers and then explain the corresponding operations.

1. Convert from decimal to binary:

- a. 234 1110 1010
- b. 555 1000101011
- c. 12321 11000000100001
- d. 152 10011000
- e. 32768 1000000000000000

2. Convert from binary to decimal:

- a. 10000000 256
- b. 1011110100 756
- c. 10011101 157
- d. 1111111111 2047

3. Convert from hexadecimal to binary:

- a. 45A0 100010110100000
- b. CF 11001111
- c. AAB2 1010101010110010
- d. 3020 11000000100000

4. Convert from binary to hexadecimal:

- a. 110001000 188
- b. 100010110 116

5. Complete the following conversions related to octal numeral system:

- a. Convert the numbers from exercise 4 to octal.
 - i. 110001000 610
 - ii. 100010110 426
- b. Convert the octal 3020 to binary.
 - i. 3020 11000010000

6. Fill in the gaps, using all the conversions you need. You have to write the steps to transform each number.

BINARY	DECIMAL	HEXADECIMAL	OCTAL
100001	33	21	41
11111111	255	FF	377
11111111	255	FF	377
100001	33	21	41

7. How many bits do you need to represent the following numbers in binary?
 - a. hexadecimal: 4B, 4AA, FF4FA, 345F
 - b. decimal: 100, 256, 255, 32, 31, 3, 4350, 1024, 45, 2^{30} , 63
8. Solve the following parts using ASCII extended (8 bits).
 - a. Write a random text, which contains letters, numbers and other alphanumeric characters.
 - b. Encode to hexadecimal, according ASCII table.
 - c. Convert to binary.

Explanation:

EXERCISE 1:

234 to binary

$$2^7=128$$

128 64 32 16 8 4 2 1

1 1 1 0 0 1 0 1

$$128+0 < 234 == 1$$

$$128+64=192 < 234 == 1$$

$$192+32=224 < 234 == 1$$

$$224+16=240 > 234 == 0$$

$$224+8=232 < 234 == 1$$

$$232+4 > 234 == 0$$

$$232+2 < 234 == 1$$

$$234+1 > 234 == 0$$

555 to binary

$$2^9$$

512 256 128 64 32 16 8 4 2 1

1 0 0 0 1 0 1 0 1 1

$$512+0 < 555 == 1$$

$$512+256 > 555 == 0$$

$$512+128 > 555 == 0$$

$$512+64 > 555 == 0$$

$$512+32=544 < 555 == 1$$

$$544+16 > 555 == 0$$

$$544+8=552 < 555 == 1$$

$$552+4 > 555 == 0$$

$$552+2=554 < 555 == 1$$

$$554+1 < 555 == 1$$

12321 to binary

$$2^{13}=8192$$

8192 4096 2048 1024 512 256 128 64 32 16 8 4 2 1

$8192+0 < 12321 == 1$
 $8192+4096=12288 < 12321 == 1$
 $12288+2048 > 12321 == 0$
 $12288+1024 > 12321 == 0$
 $12288+512 > 12321 == 0$
 $12288+256 > 12321 == 0$
 $12288+128 > 12321 == 0$
 $12288+64 > 12321 == 0$
 $12288+32=12320 < 12321 == 1$
 $12320+16 > 12321 == 0$
 $12320+8 > 12321 == 0$
 $12320+4 > 12321 == 0$
 $12320+2 > 12321 == 0$
 $12320+1 \leq 12321 == 1$

152 to binary
 128 64 32 16 8 4 2 1
 10011000
 $128+0 < 152 == 1$
 $128+64=192 > 152 == 0$
 $128+32=160 > 152 == 0$
 $128+16=144 < 152 == 1$
 $144+8 \leq 152 == 1$
 $152+4$
 $+2$
 $+1$

32768
 $2^{15}=32768$
 32768 16384 8192 4096 2048 1024 512 256 128 64 32 16 8 4 2 1
 1000000000000000

EXERCISE 2:

binary to decimal

100000000

se suma.

$2^8=256$

1011110100 suma = 756

2^9*1

2^8*0

10011101 157

2^7*1

2^6*0

$2^5 \cdot 0$
 $2^4 \cdot 1$
 $2^3 \cdot 1$
 $2^2 \cdot 1$
 $2^1 \cdot 0$
 $2^0 \cdot 1$
 $11111111111 \cdot 2^{11} - 1 == 2047$

EXERCISE 3

45A0
0100 0101 1010 0000
-100010110100000-

CF
-1100 1111-

AAB2
-1010 1010 1011 0010-

3020
0011 0000 0010 0000
-11000000100000-

EXERCISE 4

110001000
1 1000 1000
0001 1000 1000
1 8 8
-188-

100010110
1 0001 0110
0001 0001 0110
1 1 6
-116-

EXERCISE 5

110001000
110 001 000
6 1 0
-610-

100010110
 100 010 110
 4 2 6
 -426-

3020
 011 000 010 000
 -11000010000-

EXERCISE 6

	binary	decimal	hexadecimal	octal
1-		33		
2-			FF	
3-				377
4-	100001			

1. 33 decimal

binary

$2^5=32$

-100001-

Al ser 1 mas q la potencia de 2

tantos 0s como potencia y cambiamos el ultimo por 1

Hexadecimal

100001

10 0001

0010 0001

2 1

-21-

octal

100001

100 001

4 1

-41-

2. FF hexadecimal

binary

FF

-1111 1111-

decimal

2^8-1

-255-

Al ser todo 1s es uno menos q una potencia de 2

la potencia es el numero de digitos. En este caso 8.

octal

11111111
11 111 111
011 111 111
3 7 7
-377-

3.377 octal
The answers have to be the same as the previous exercise.
binary
377
011 111 111
-11111111-

4.100001 binary
The answers are the same as the first one.
decimal
 $2^5 + 2^0 = 33$