

Iprs1

# TEORIJA

1 BIT	
0 → 0	
1 → 1	

2 BITA	
00 → 0	
01 → 1	
10 → 2	
11 → 3	

3 BITA	
000 → 0	
001 → 1	
010 → 2	
011 → 3	
100 → 4	
101 → 5	
110 → 6	
111 → 7	

4 BITA	
0000 → 0	
0001 → 1	
0010 → 2	
0011 → 3	
0100 → 4	
0101 → 5	
0110 → 6	
0111 → 7	
1000 → 8	A
1001 → 9	
1010 → 10	B
1011 → 11	C
1100 → 12	
1101 → 13	D
1110 → 14	E
1111 → 15	F

$$\begin{array}{r}
 128 \quad 64 \quad 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \\
 \downarrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \\
 2^7 \quad 2^6 \quad 2^5 \quad 2^4 \quad 2^3 \quad 2^2 \quad 2^1 \quad 2^0
 \end{array}$$

BINARNI → DECIMALNI

PARAN

$$101010 \rightarrow 42$$

$$001100 \rightarrow 12$$

$$010001 \rightarrow 17$$

NEPARAN

DECIMALNI → BINARNI

$$20 \rightarrow \underline{0} \ 10100$$

$$32 \rightarrow \underline{0} \ 01101$$

$$4 \rightarrow 000100$$

HEXADEC → BINARNI

$$A7 \rightarrow \underline{1} \ \underline{0} \ \underline{1} \ \underline{0} \ \underline{0} \ \underline{1} \ \underline{1} \ \underline{1}$$

$$D8 \rightarrow \underline{1} \ \underline{1} \ \underline{0} \ \underline{1} \ \underline{1} \ \underline{0} \ \underline{0} \ \underline{0}$$

$$B6 \rightarrow \underline{1} \ \underline{0} \ \underline{1} \ \underline{1} \ \underline{0} \ \underline{1} \ \underline{1} \ \underline{0}$$

BINARNI → HEXADEC.

$$\underline{1010} \ \underline{0010} \rightarrow 0xA2$$

$$1111 \ 1110 \rightarrow 0xFE$$

$$1100 \ 0110 \rightarrow 0xC6$$

KOMPLEMENT I, II

$$iA \ 10101011$$

$$KOMP1 \ 01010100$$

$$+ \ 1$$

$$KOMP2 \ 01010101$$

$$\underbrace{\hspace{1cm}}_{\text{Kompl. } 2}$$

$$iA \ 10010111$$

$$KOMP1 \ 01101000$$

$$KOMP2 \ 01101001$$

$$iA \ 01010100$$

$$KOMP1 \ 10101011$$

$$+ \ 1$$

\* 1:1 su 0(1)

$$S\_compl1 \leq \text{not}(A);$$

$$S\_compl2 \leq \text{not}(A) + 1;$$

$$\begin{array}{r}
 10010.010 - 13.75 \\
 + 01101.101 \\
 \hline
 01101.110 = 13.75
 \end{array}$$



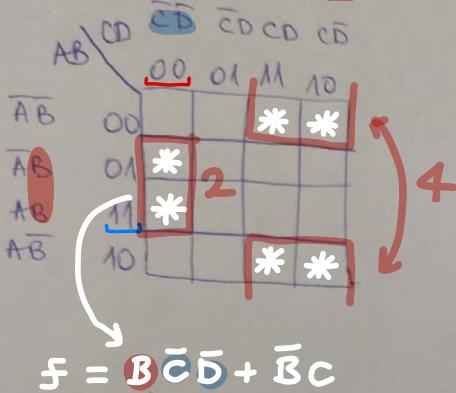
# BULOVA ALGEBRA

## KARNOVÉ MAPY

1°

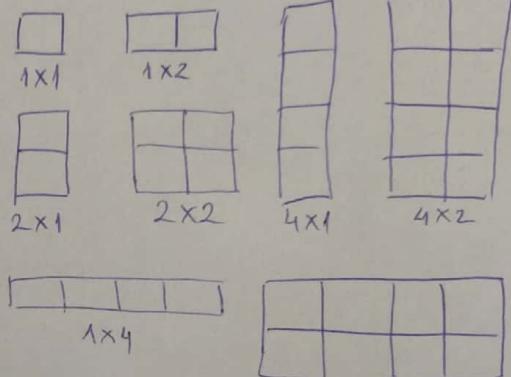
$$f^1(ABCD) = (0000 \downarrow 1110 \downarrow 0000 \downarrow 1110 \downarrow 00 \downarrow \\ 15 \downarrow 14 \downarrow 13 \downarrow 12 \downarrow 11 \downarrow 10 \downarrow 9 \downarrow 8 \downarrow 7 \downarrow 6 \downarrow 5 \downarrow 4 \downarrow 3 \downarrow 2 \downarrow 1 \downarrow 0)$$

$$f^1(ABCD) = (12, 11, 10, 4, 3, 2)$$



$\vec{A} \rightarrow 0$   
 $A \rightarrow 1$

## KARTE:



$$2^{\circ} f^1(ABCD) = (0, 5, 7, 13, 15) = \bar{A}\bar{B}\bar{C}\bar{D} + BD$$

← RADÍ SAM  
POSLÉ

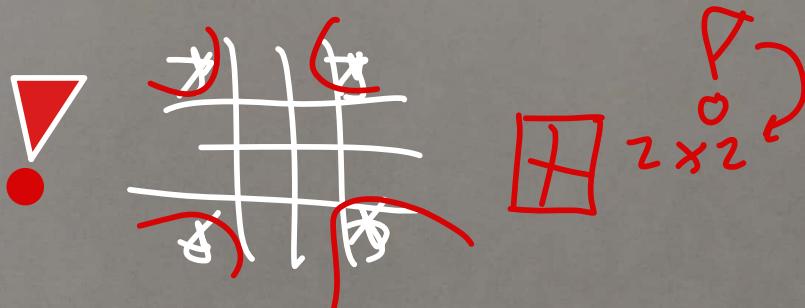
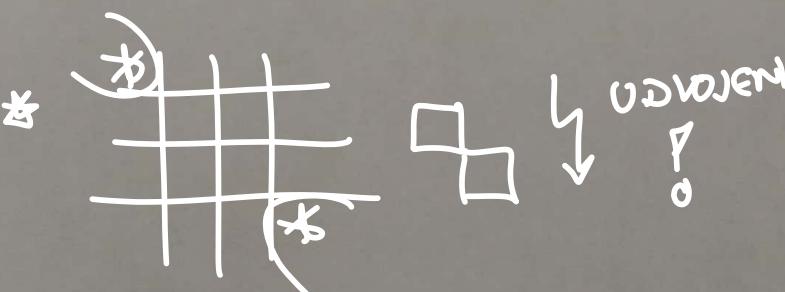
$$3^{\circ} f^1(ABCD) = (8, 9, 10, 12, 13, 14)$$

$$4^{\circ} f^1(ABCD) = (1111101000001010)$$

$$5^{\circ} f^1(ABCD) = (0100011001000110)$$

$$6^{\circ} f^1(ABCD) = (0, 3, 7, 11, 15)$$

$$7^{\circ} f^1(ABCD) = (1010010110100101)$$



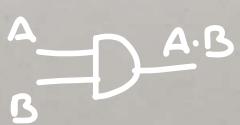
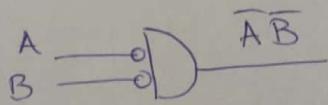
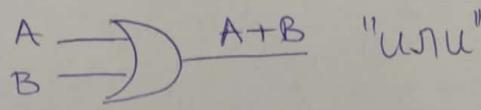
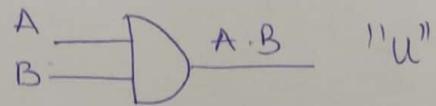
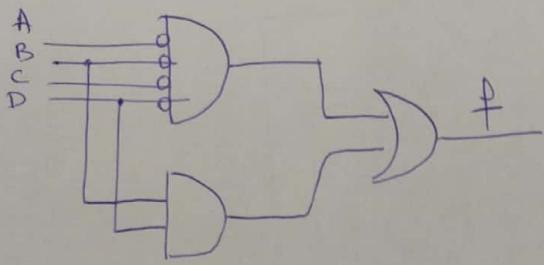


Tabela 1-1. Digitalna logička kola

<b>NOT</b>		$Y = \bar{X}$	<table border="1"> <thead> <tr> <th>X</th> <th>Y</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> </tr> </tbody> </table>	X	Y	0	1	1	0									
X	Y																	
0	1																	
1	0																	
<b>AND</b>		$Y = X_1 X_2$	<table border="1"> <thead> <tr> <th>X<sub>1</sub></th> <th>X<sub>2</sub></th> <th>Y</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td>1</td> <td>1</td> </tr> </tbody> </table>	X <sub>1</sub>	X <sub>2</sub>	Y	0	0	0	0	1	0	1	0	0	1	1	1
X <sub>1</sub>	X <sub>2</sub>	Y																
0	0	0																
0	1	0																
1	0	0																
1	1	1																
<b>OR</b>		$Y = X_1 + X_2$	<table border="1"> <thead> <tr> <th>X<sub>1</sub></th> <th>X<sub>2</sub></th> <th>Y</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>1</td> </tr> </tbody> </table>	X <sub>1</sub>	X <sub>2</sub>	Y	0	0	0	0	1	1	1	0	1	1	1	1
X <sub>1</sub>	X <sub>2</sub>	Y																
0	0	0																
0	1	1																
1	0	1																
1	1	1																
<b>XOR</b>		$Y = X_1 \oplus X_2$	<table border="1"> <thead> <tr> <th>X<sub>1</sub></th> <th>X<sub>2</sub></th> <th>Y</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>0</td> </tr> </tbody> </table>	X <sub>1</sub>	X <sub>2</sub>	Y	0	0	0	0	1	1	1	0	1	1	1	0
X <sub>1</sub>	X <sub>2</sub>	Y																
0	0	0																
0	1	1																
1	0	1																
1	1	0																
<b>NAND</b>		$Y = \overline{X_1 X_2}$	<table border="1"> <thead> <tr> <th>X<sub>1</sub></th> <th>X<sub>2</sub></th> <th>Y</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>0</td> </tr> </tbody> </table>	X <sub>1</sub>	X <sub>2</sub>	Y	0	0	1	0	1	1	1	0	1	1	1	0
X <sub>1</sub>	X <sub>2</sub>	Y																
0	0	1																
0	1	1																
1	0	1																
1	1	0																
<b>NOR</b>		$Y = \overline{X_1 + X_2}$	<table border="1"> <thead> <tr> <th>X<sub>1</sub></th> <th>X<sub>2</sub></th> <th>Y</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td>1</td> <td>0</td> </tr> </tbody> </table>	X <sub>1</sub>	X <sub>2</sub>	Y	0	0	1	0	1	0	1	0	0	1	1	0
X <sub>1</sub>	X <sub>2</sub>	Y																
0	0	1																
0	1	0																
1	0	0																
1	1	0																
<b>XNOR</b>		$Y = \overline{X_1 \oplus X_2}$	<table border="1"> <thead> <tr> <th>X<sub>1</sub></th> <th>X<sub>2</sub></th> <th>Y</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td>1</td> <td>1</td> </tr> </tbody> </table>	X <sub>1</sub>	X <sub>2</sub>	Y	0	0	1	0	1	0	1	0	0	1	1	1
X <sub>1</sub>	X <sub>2</sub>	Y																
0	0	1																
0	1	0																
1	0	0																
1	1	1																

$$1^{\circ} f = BD + \bar{A}\bar{B}\bar{C}\bar{D}$$

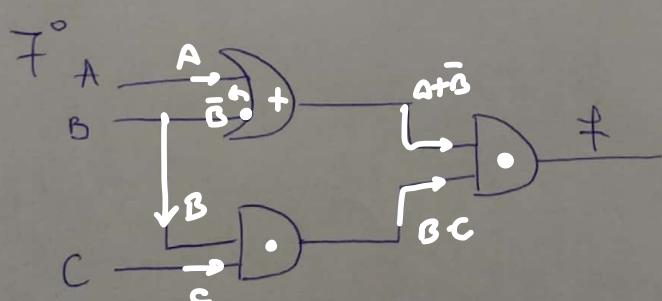
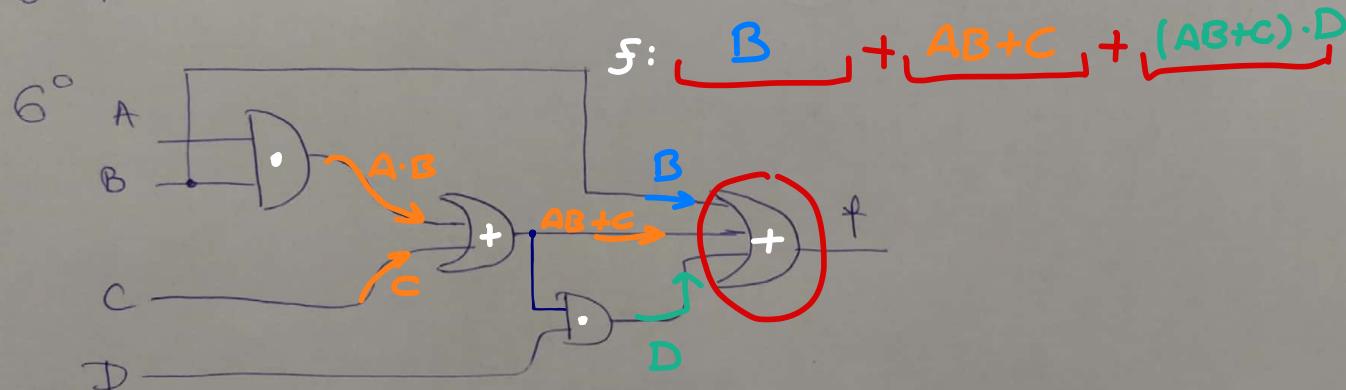


$$2^{\circ} f = \bar{A}\bar{C} + A\bar{C}\bar{D}$$

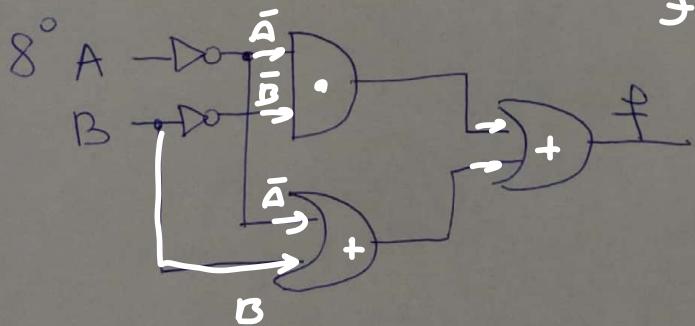
$$3^{\circ} f = \bar{B}\bar{C}\bar{D} + C\bar{D}$$

$$4^{\circ} f = AB + \bar{B}D$$

$$5^{\circ} f = CD + \bar{A}\bar{B}\bar{C}\bar{D}$$

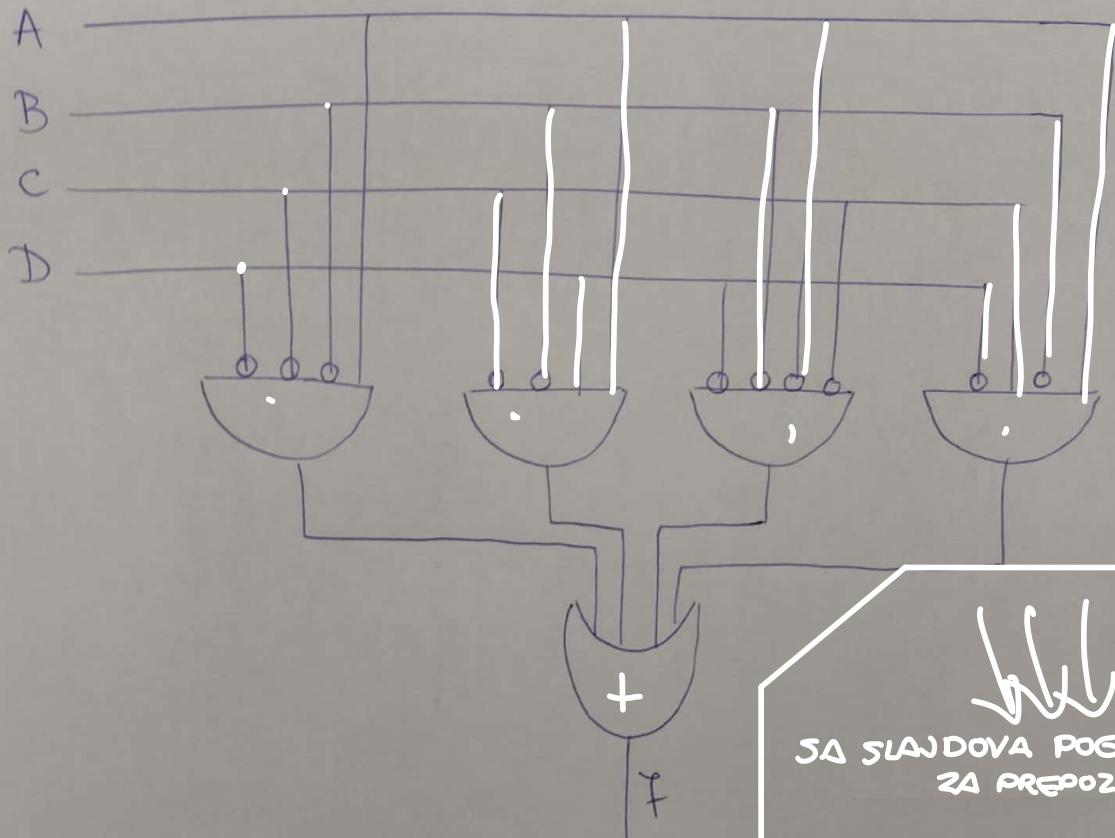


$$f: \boxed{A+\bar{B}} \cdot \boxed{B \cdot C}$$



$$f: \boxed{\bar{A} \cdot \bar{B}} + \boxed{(\bar{A} + B)}$$

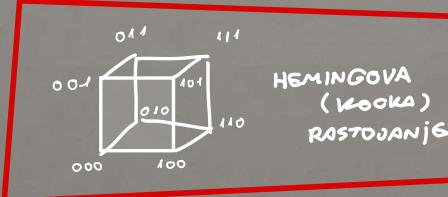
g° SA KLK



$$f = \frac{A\bar{B}\bar{C}\bar{D}}{\text{---}} + \frac{A\bar{B}\bar{C}D}{\text{---}} + \frac{\bar{A}\bar{B}\bar{C}\bar{D}}{\text{---}} + \frac{A\bar{B}C\bar{D}}{\text{---}}$$

$$f = A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D}$$

	$\bar{C}\bar{D}$	$\bar{C}\bar{D}$	$C\bar{D}$	$C\bar{D}$
$\bar{A}\bar{B}$	00	01	11	10
$\bar{A}B$	01			
$A\bar{B}$	11			
$AB$	10	00	01	10



SAM URADIO HAHAH

$$f = A\bar{B}\bar{C} + A\bar{B}\bar{D} + \bar{B}\bar{C}\bar{D}$$

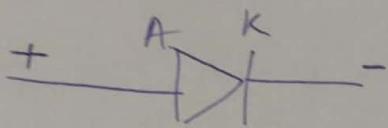
0	→ NULA
1	← JEDINICA
L	← SLABA NULA
H	← SLABA JEDINICA
Z	← VISOKA IMPEDANSA
W	← SLABO NEPOZNATO (KOLIZIJA)
X	← NEPOZNATO (KOLIZIJA)
U	← NEINICIJALIZOVANA
-	← NEDEFINISANO

SPOJNICE  
HAHAHAH

V  
I  
S  
E  
Z  
A  
I  
S  
P  
I  
T

# OSNOVNE PREKIDAČKE KOMPONENTE

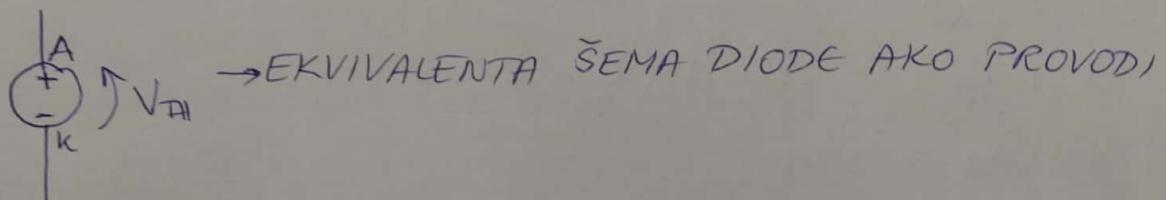
## DIODA



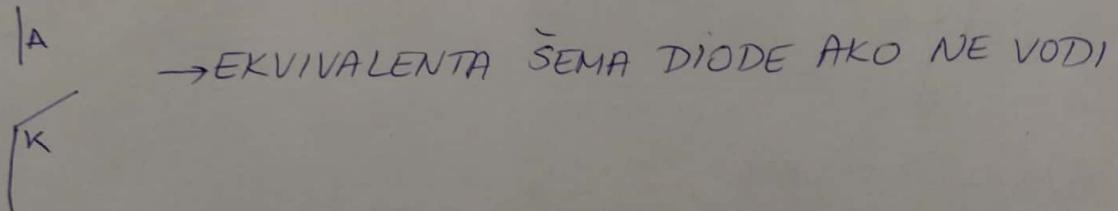
A → ANODA  
K → KATODA

KRITERIJUM UKIĆUĆENJA DIODE:

1)  $U_{AK} \geq V_{TH} \rightarrow$  DIODA PROVODI

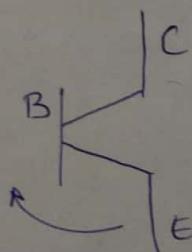


2)  $U_{AK} < V_{TH} \rightarrow$  DIODA NE PROVODI



## TRANZISTOR

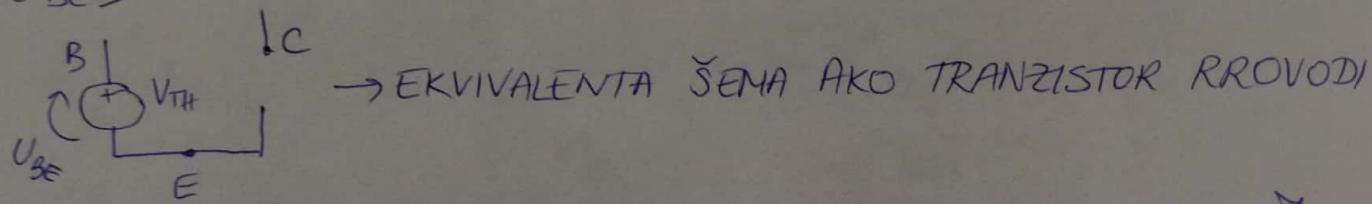
NPN TIP:



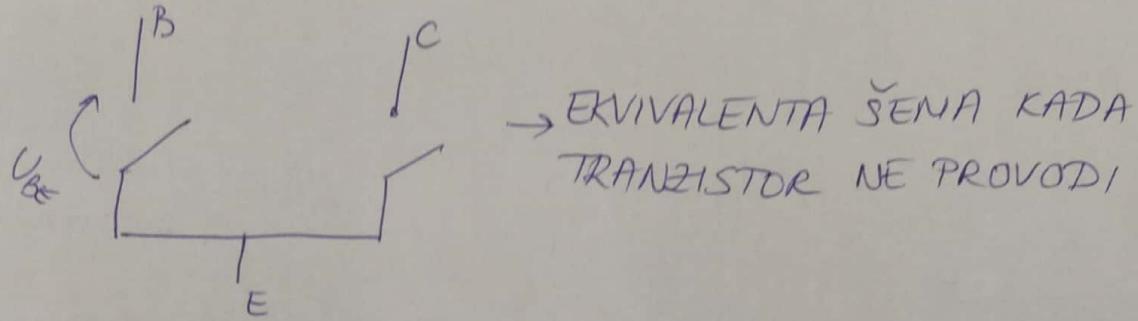
B → BAZA  
E → ENITER  
C → KOLEKTOR

KRITERIJUM PROVODENJA TRANZISTORA

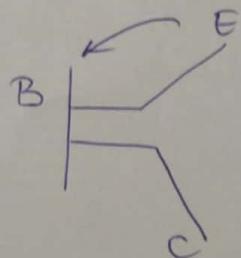
1)  $U_{BE} \geq V_{TH} \rightarrow$  TRANZISTOR PROVODI



2)  $U_{BE} < V_{TH} \rightarrow$  TRANZISTOR NE PROVODI

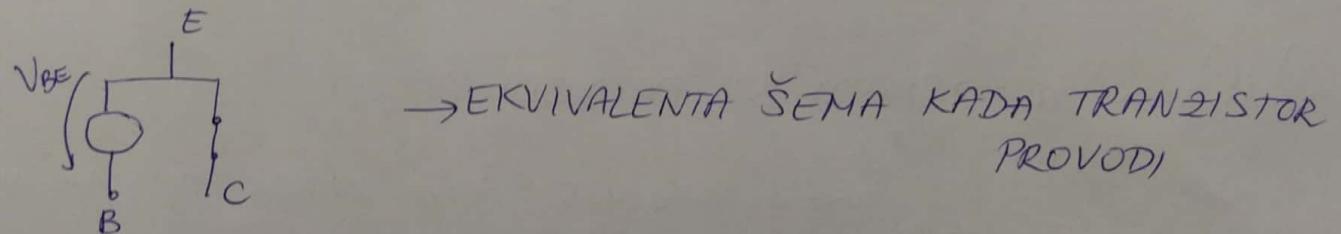


PNP TIP

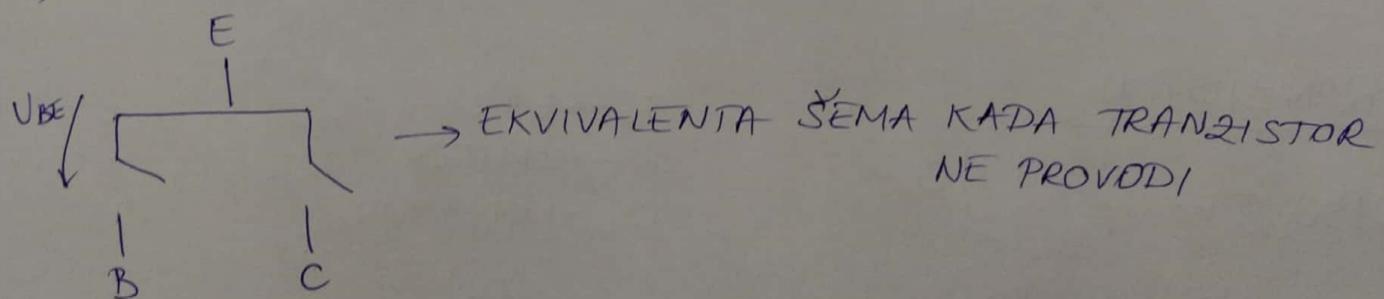


KRITERIJUM UKLJUČENJA

1)  $U_{BE} \leq -|V_{TH}|$

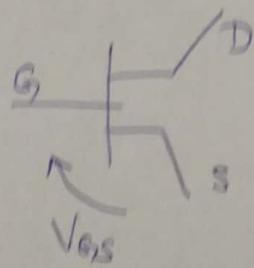


2)  $U_{BE} > -|V_{TH}|$



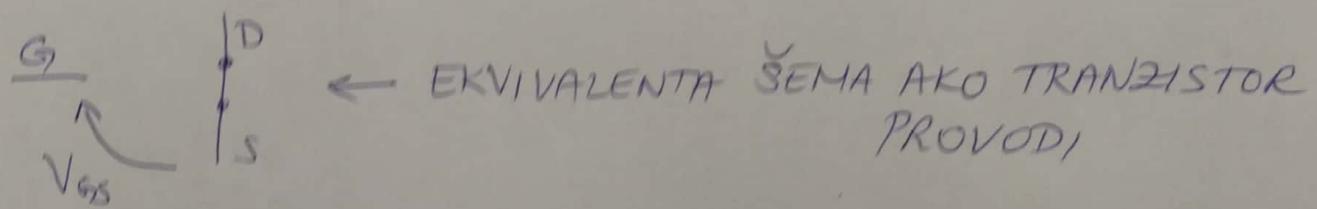
## MOS FET TRANZISTOR

N-MOS

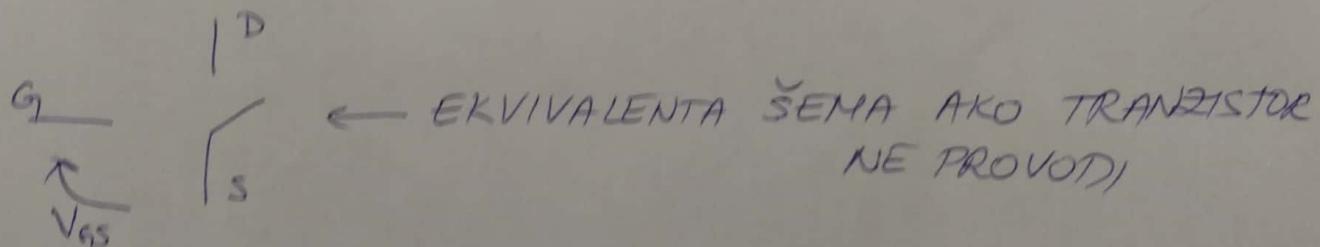


KRITERIJUM UKIĆENJA TRANZISTORA

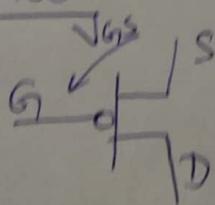
1)  $V_{GS} \geq V_{THNOS}$  → TRANZISTOR PROVODI



2)  $V_{GS} < V_{THNOS}$  → TRANZISTOR NE PROVODI,

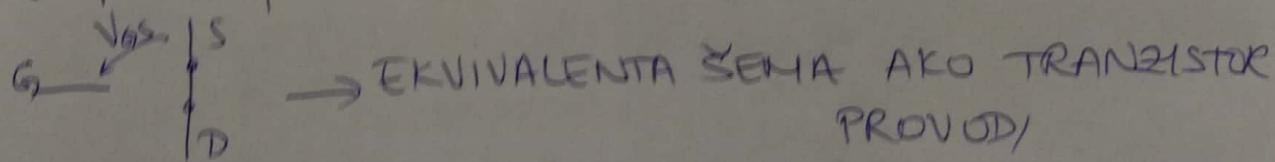


P-MOS

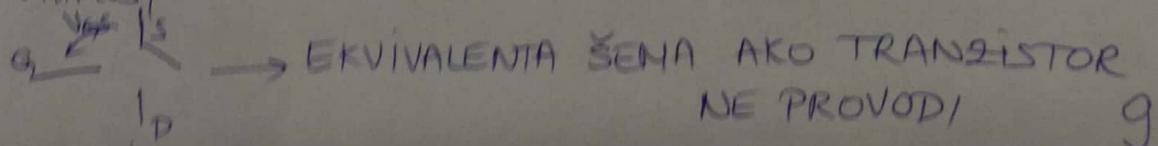


KRITERIJUM UKIĆENJA TRANZISTORA

1)  $V_{GS} \leq -|V_{THNOS}|$  → TRANZISTOR PROVODI



2)  $V_{GS} > |V_{THNOS}|$

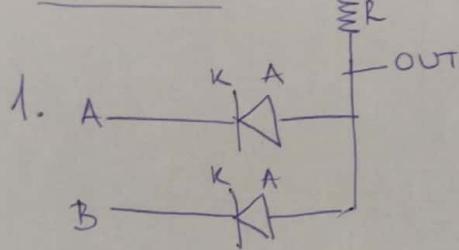


# REALNA LOGIČKA KOLA

$$0 < V_{TH} < V_{CC}$$

↓  
0,6V

## DIODE



A - АНОДА  
K - КАТОДА

ISTINITOSNA TABUICA:

A	B	OUT
0	0	0
0	1	0
1	0	0
1	1	1

"U" KOLO

"00": ПП: ОБЕ ИСКЛЮЧЕНИЕ:  
(УЗЕНИМО УХ)

$$D_1: U_A = V_{CC}$$

$$U_K = 0$$

$$U_{AK} = U_A - U_K = V_{CC} > V_{TH}$$

ПРОВОДИ

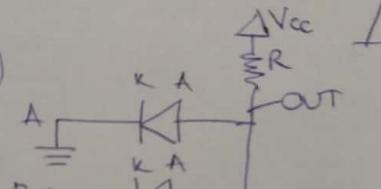
$$D_2: U_A = V_{CC}$$

$$U_K = 0$$

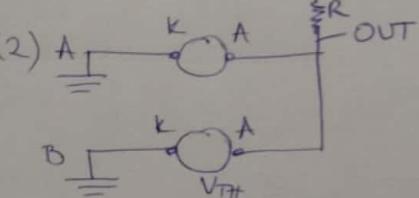
$$U_{AK} = U_A - U_K = V_{CC} > V_{TH}$$

ПРОВОДИ

(1)



(2)



$$OUT = V_{TH} = "0"$$

"01" ПП:  $D_1$  ИСКЛЮЧЕНА,  $D_2$  УКЉУЧЕНА

$$D_1: U_A = V_{CC}$$

$$U_K = 0$$

$$U_{AK} = V_{CC} > V_{TH}$$

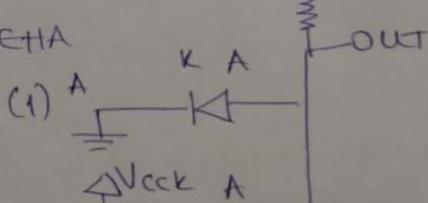
ПРОВОДИ

$$D_2: U_A = V_{CC}$$

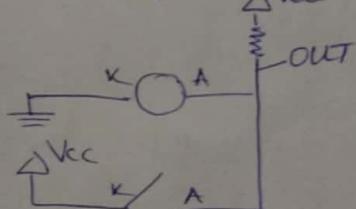
$$U_K = V_{CC}$$

$$U_{AK} = 0 < V_{TH}$$

НЕ ПРОВОДИ



(2)

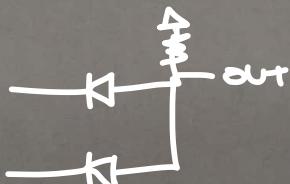


$$OUT = "0"$$

"01 = "10"

NA KLIK

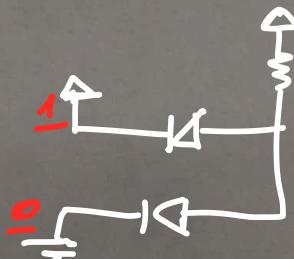
(0) VARIJACIJA



UPAMTIS  
SLIKU ITJT

- 1) 1
- 2) 1L1
- 3) N1
- 4) NIL1

2° TIP KONI DA:



1  
2  
3  
4  
5

- 1) 1
- 2) 0
- 3) 0
- 4) -
- 5) Z

sig nesto  
od ova  
DVA SO/SO

10

"11":

Пп: ОБЕ ДИОДЕ УКЛЮЧЕНЕ

$$D_1: U_A = V_{CC}$$

$$U_K = V_{CC}$$

$$U_{AK} = 0 < V_{TH}$$

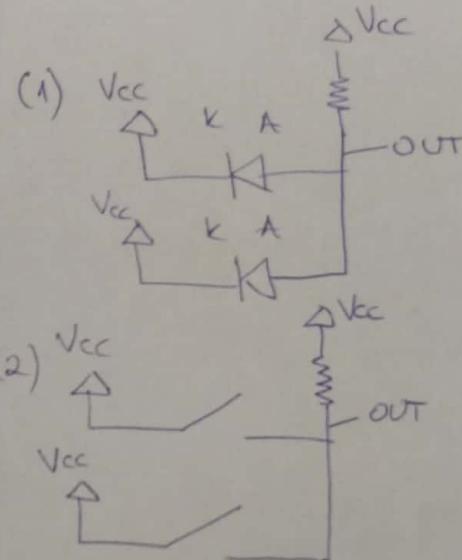
НЕ ПРОВОДИ

$$D_2: U_A = V_{CC}$$

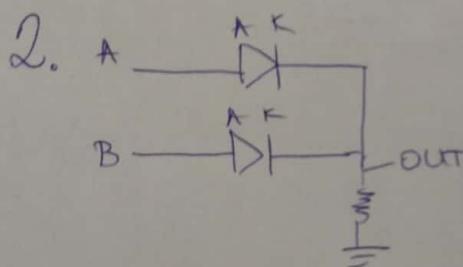
$$U_K = V_{CC}$$

$$U_{AK} = 0V$$

НЕ ПРОВОДИ



$$OUT = V_{CC} = 1$$



ISTINJITOSNA TABLICA:

A	B	OUT
0	0	0
0	1	1
1	0	1
1	1	1

"УЛУ" КОАО

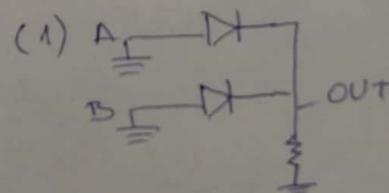
"00": пп. ОБЕ СУ ИСКЛЮЧЕНЕ

$$D_1: U_A = 0$$

$$U_K = 0$$

$$U_{AK} = 0 < V_{TH}$$

НЕ ПРОВОДИ

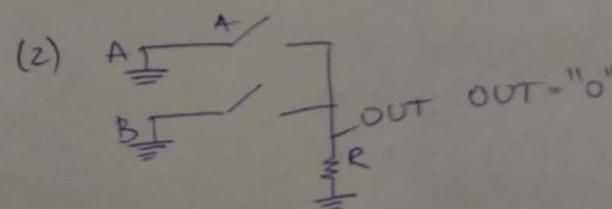


$$D_2: U_A = 0$$

$$U_K = 0$$

$$U_{AK} = 0 < V_{TH}$$

НЕ ПРОВОДИ



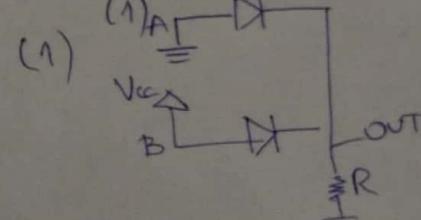
"01": пп. D1 ИСКЛЮЧЕНА, D2 УКЛЮЧЕНА

$$D_1: U_A = 0$$

$$U_K = 0$$

$$U_{AK} = 0 < V_{TH}$$

НЕ ПРОВОДИ

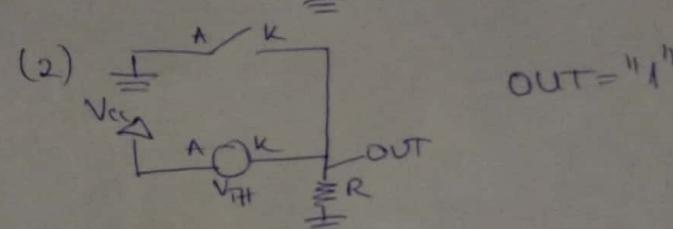


$$D_2: U_A = V_{CC}$$

$$U_K = 0$$

$$U_{AK} = V_{CC} > V_{TH}$$

ПРОВОДИ



"01" = "10"

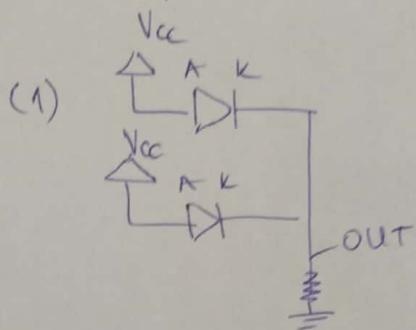
"1": nn: D<sub>1</sub> УКЛЮЧЕНА, D<sub>2</sub> УКЛЮЧЕНА

$$D_1: U_A = V_{cc}$$

$$U_K = 0$$

$$U_{AK} = V_{cc} > V_{TH}$$

ПРОВОДАМ

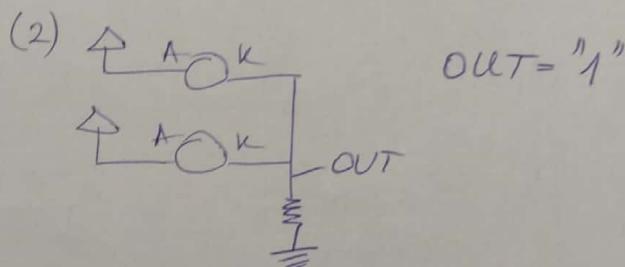


$$D_2: U_A = V_{cc}$$

$$U_K = 0$$

$$U_{AK} = V_{cc} > V_{TH}$$

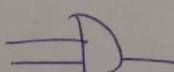
ПРОВОДАМ



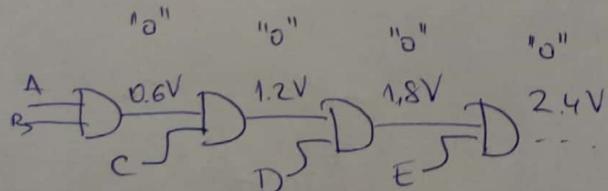
## DRL логика - ПРОБЛЕМИ

- КАСКАДИРАЊЕ!

"0" КОДО



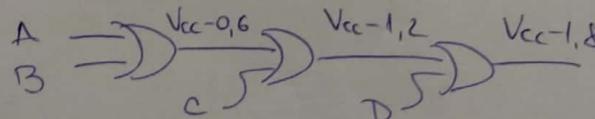
$$OUT = \begin{cases} "0" = 0,6V \\ "1" = V_{cc} \end{cases}$$



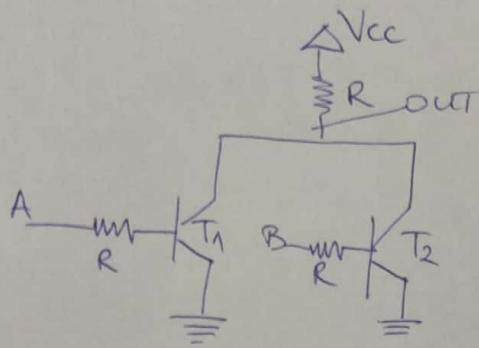
"000" КОДО



$$OUT = \begin{cases} "0" = 0V \\ "1" = V_{cc} - 0,6V \end{cases}$$



# RTL - ОТПОРНИЧКО ТРАНЗИСТОРСКА ЛОГИКА



A	B	OUT
0	0	1
0	1	0
1	0	0
1	1	0

B - БАЗА  
E - ЭМУТЕР

"ЧИЛУ" КОЛО

"00"

$$T_1: U_B = 0$$

$$U_E = 0$$

$$U_{BE} = 0 < V_{TH}$$

$T_1 \rightarrow \text{УКЛб}$

$$T_2: U_B = 0$$

$$U_E = 0$$

$$U_{BE} = 0 < V_{TH}$$

$T_2 \rightarrow \text{УКЛб.}$

"01":  $T_1: U_B = 0$

$$U_E = 0$$

$$U_{BE} = 0 < V_{TH}$$

$T_1 \rightarrow \text{УКЛб.}$

$$T_2: U_B = V_{CC}$$

$$U_E = 0$$

$$U_{BE} = V_{CC} > V_{TH}$$

$T_2 \rightarrow \text{УКЛ.}$

"01" = "10"

"11"

$$T_1: U_B = V_{CC}$$

$$U_E = 0$$

$$U_{BE} = V_{CC} > V_{TH}$$

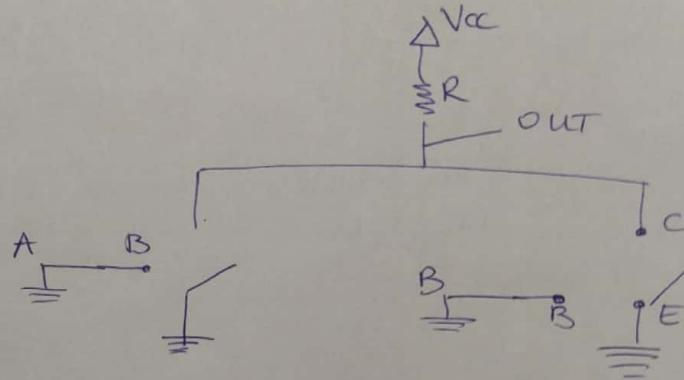
$T_1 \rightarrow \text{УКЛ.}$

$$T_2: U_B = V_{CC}$$

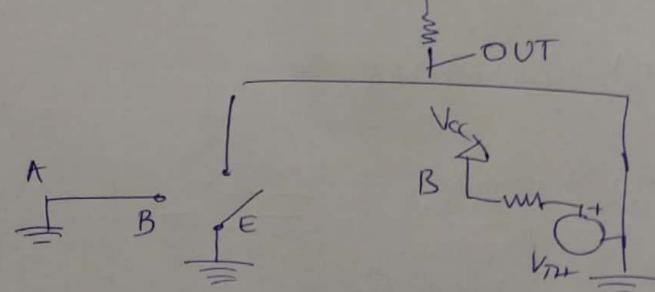
$$U_E = 0$$

$$U_{BE} = V_{CC} > V_{TH}$$

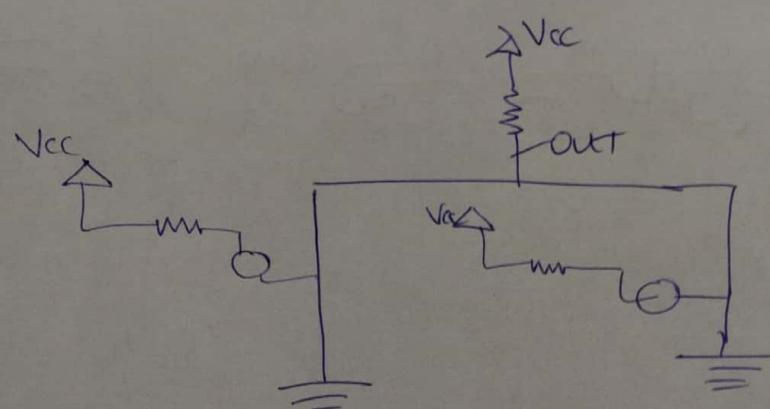
$T_2 \rightarrow \text{УКЛУЧЕН}$



$$\text{OUT} = V_{CC} = 11$$

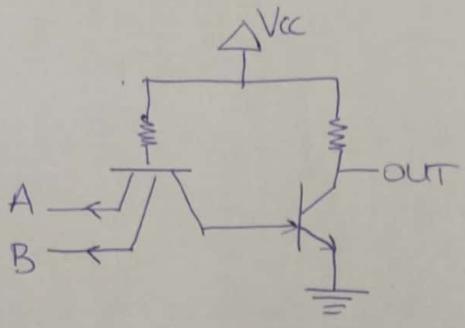


$$\text{OUT} = "0"$$



$$\text{OUT} = "0"$$

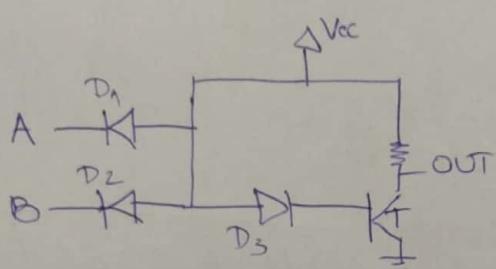
# TTL - TRANZISTORSKO-TRANZISTORSKA LOGIKA



ISTINITOSNA TABLICA

A	B	OUT
0	0	1
0	1	1
1	0	1
1	1	0

"HU" KOLO



"00"

$$D_1: U_K = 0V \quad U_A = V_{CC}$$

$$U_{AK} = V_{CC}$$

ПРОВОДИ

$$D_2: U_K = 0V \quad U_A = V_{CC}$$

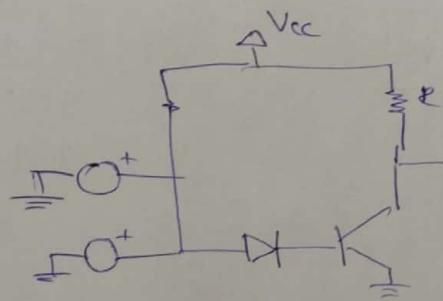
$$U_{AK} = V_{CC}$$

ПРОВОДИ

$$D_3: U_K = 0V \quad U_A = V_{CC}$$

$$U_{AK} = V_{CC}$$

$$\begin{aligned} T: \quad & U_B = V_{CC} \\ & U_E = 0 \\ & U_{BE} > U_{TH} \\ & U_{BE} \text{ ВОДИ} \end{aligned}$$



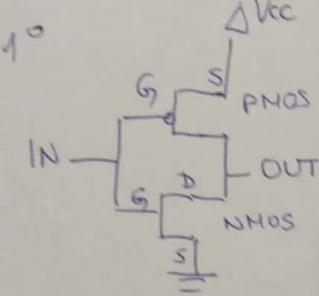
0

0

0

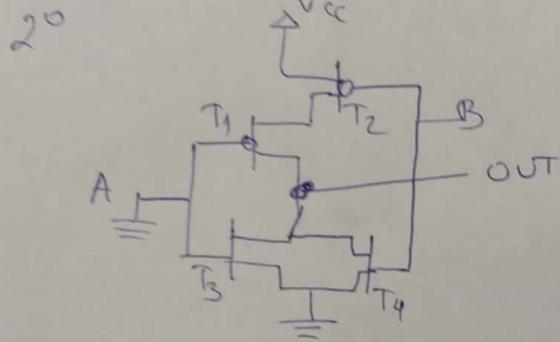
# CMOS KOLA

(NE, NILI, NI)



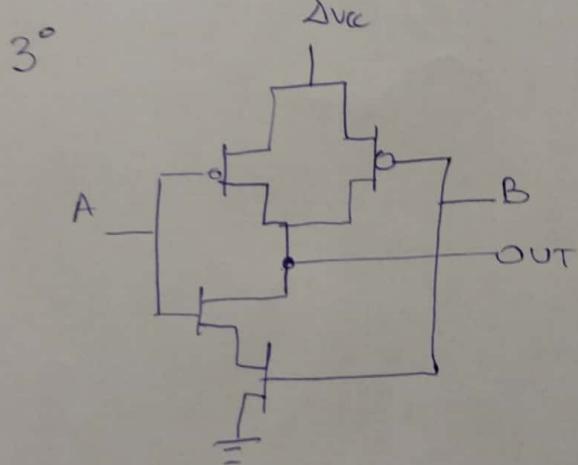
IN	OUT
0	V <sub>CC</sub> = 1
1	0

[NE KOLO]



A	B	OUT
0	0	V <sub>CC</sub> = 1
0	1	0
1	0	0
1	1	0

[NILI KOLO]



A	B	OUT
0	0	V <sub>CC</sub> = 1
0	1	V <sub>CC</sub> = 1
1	0	V <sub>CC</sub> = 1
1	1	0

[NI KOLO]

Julija Jelićanin

Nina Knezevic

Slavisa01

Aleksandar Obr...

Ivona

Tijana Opacic

Julija Jelićanin

Nina Knezevic

Slavisa01

Aleksandar Obradovic

Ivona

Tijana Opacic

Remaining Meeting Time: 01:55

D  
O  
D  
O  
D  
O  
D  
O  
D  
O

2 DIODE 2-1 (2 DIODE) iu  
2TRNN2 R7L 2-2 17:17s NIU  
TTL 2-3 19:20s NI  
3 MOS CMOS 2-4 NG  
NIU  
NI

D  
O  
D  
O  
D  
O  
D  
O  
D  
O

KOJA KOJA TREBA DA SE ZNAJU !

# ZADACI ZA VEŽBU:

S I I I I . F F F

a  $01010.110 = 10.75$  ✓

b  $\begin{array}{r} 10110.011 \\ 01001.100 \\ + \hline 01001.101 \end{array} = 9.625$  ✓

c  $00101.001 = 5.125$  ✓

d  $\begin{array}{r} 11001.100 \\ 00110.011 \\ + \hline 00110.100 \end{array} = 6.5$

e  $00001.111 = 1.875$  ✓

f  $\begin{array}{r} 11110.010 \\ 00001.101 \\ + \hline 00001.110 \end{array} = 1.75$

g  $00111.011 = 7.375$  ✓

h  $\begin{array}{r} 11001.101 \\ 00110.010 \\ + \hline 00110.011 \end{array} = 6.375$

i  $00101.010 = 5.25$  ✓

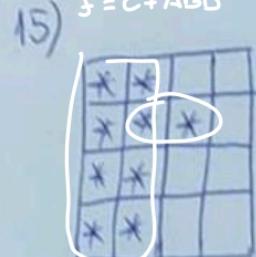
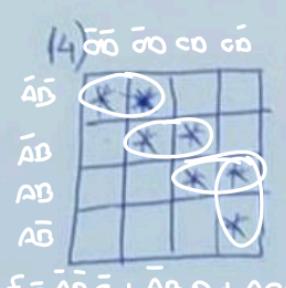
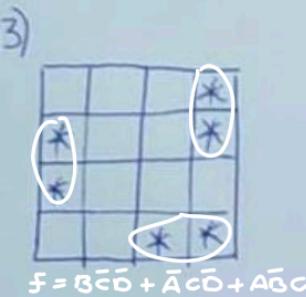
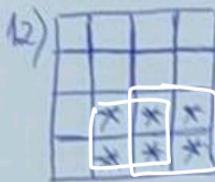
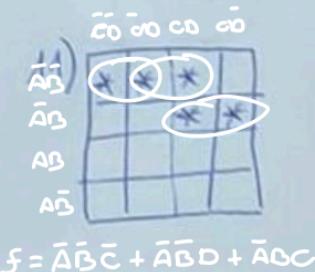
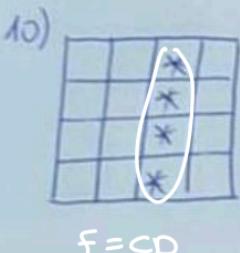
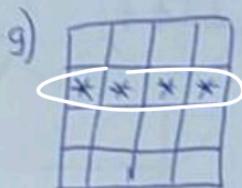
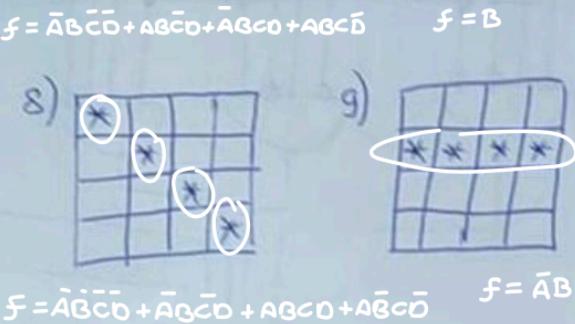
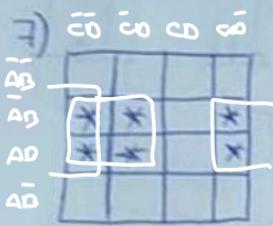
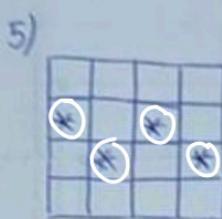
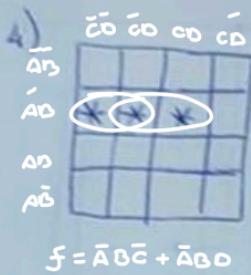
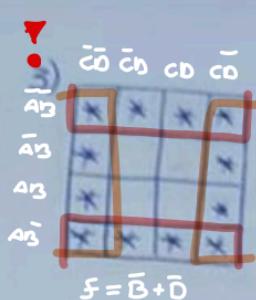
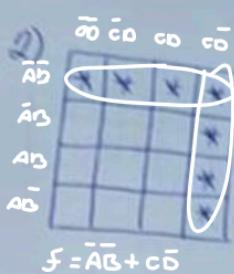
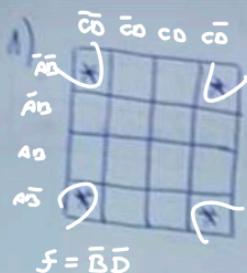
j  $\begin{array}{r} 10110.011 \\ 01001.100 \\ + \hline 01001.101 \end{array} = 9.625$

k  $01111.111 = 15.875$  ✓

	$\bar{c}\bar{d}$	$\bar{c}d$	$cd$	$c\bar{d}$
$\bar{A}\bar{B}$	0	4	3	2
$\bar{A}B$	4	5	7	6
$A\bar{B}$	12	13	15	14
$AB$	8	9	11	10

	$\bar{c}\bar{d}$	$\bar{c}d$	$cd$	$c\bar{d}$
$\bar{A}\bar{B}$	(X)			
$\bar{A}B$	(X)	(X)		
$A\bar{B}$	(X)	(X)	(X)	
$AB$	(X)	(X)	(X)	(X)

$f = BD + \bar{A}\bar{B}\bar{C}\bar{D}$  ✗



16) ?!

$$\bar{A}\bar{B} \quad \bar{A}B \quad AB \quad A\bar{B}$$



$$?!) f = \bar{A}C + \bar{A}B$$

17) ?!

$$\bar{A}\bar{B} \quad \bar{A}B \quad AB \quad A\bar{D}$$



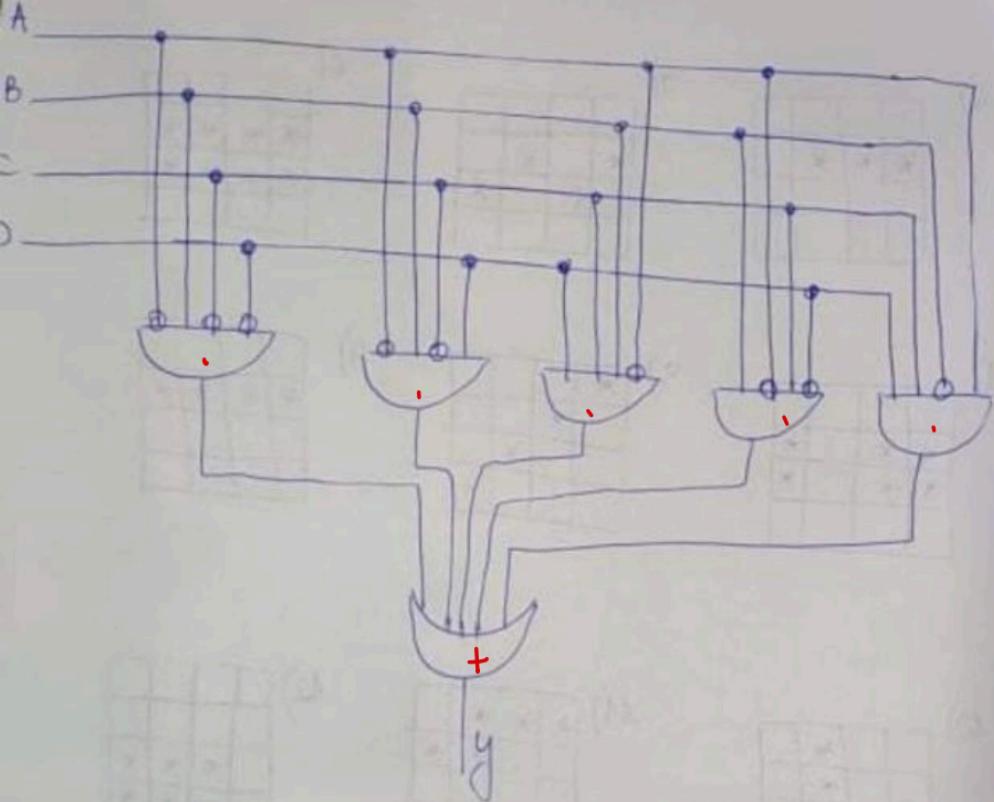
$$?!) f = \bar{A}\bar{C} + B$$

18) ?!

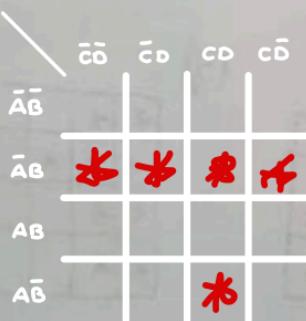
$$\bar{A}\bar{D} \quad \bar{A}B \quad AB \quad A\bar{D}$$



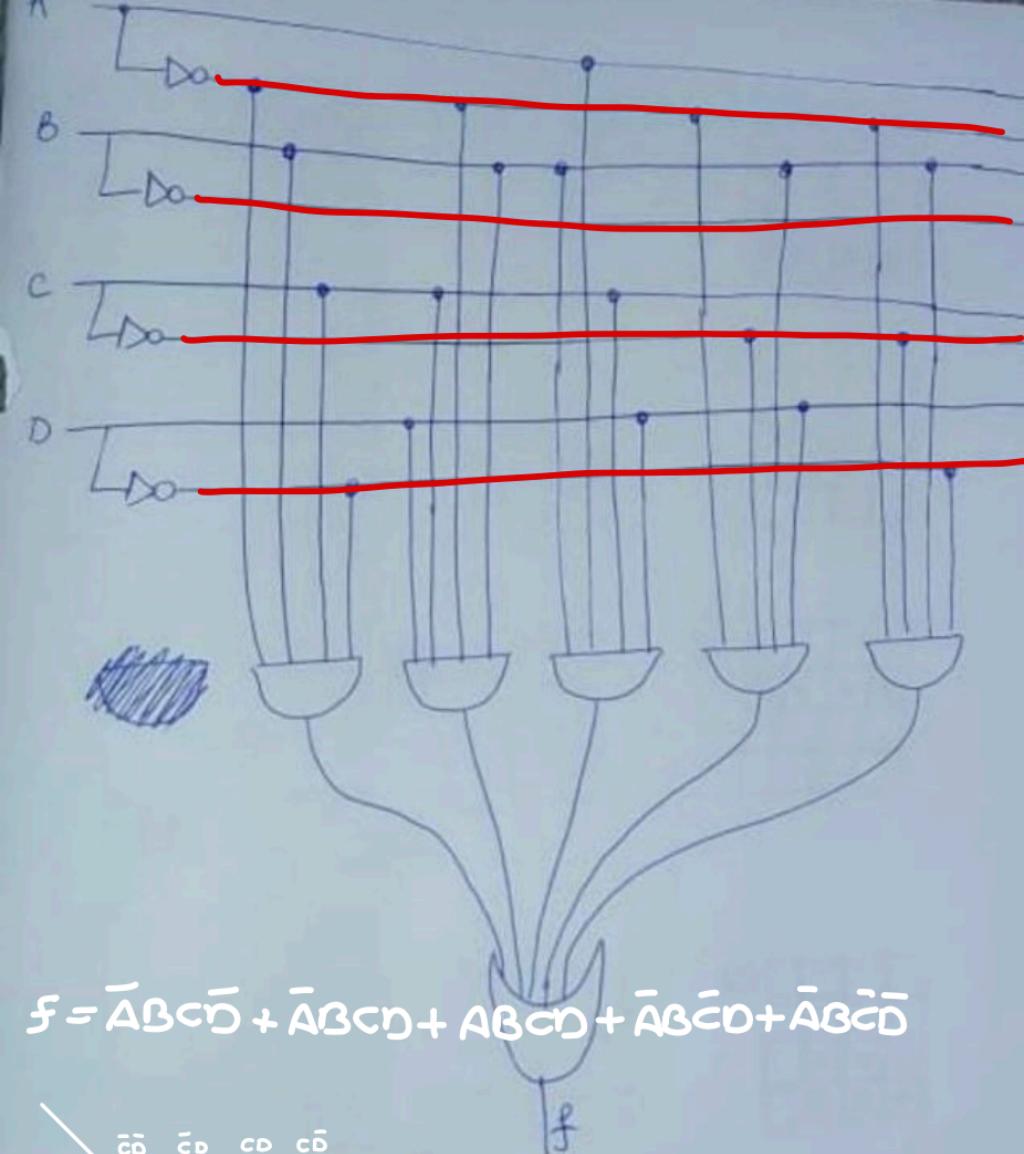
$$?!) f = \bar{B} + C$$



$$f = \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}BcD + \bar{A}Bc\bar{D} + ABcD$$



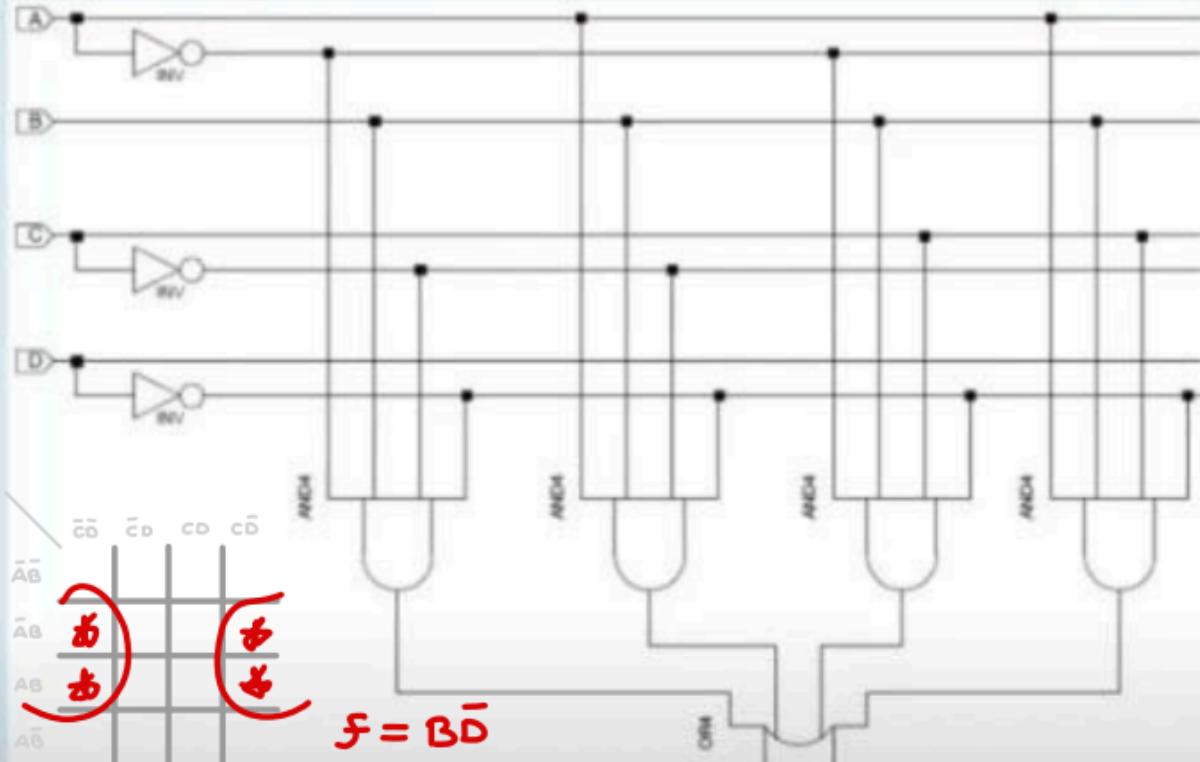
$$f = \bar{A}B + A\bar{B}CD$$



$$f = \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + AB\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D$$

	$\bar{C}\bar{D}$	$\bar{C}D$	$CD$	$C\bar{D}$
$\bar{A}\bar{B}$				
$\bar{A}B$	✓	✓	✓	✓
$AB$			✓	
$A\bar{B}$				

$$f = \bar{A}B + BCD$$



$$f = BD\bar{}$$

$$f = \bar{A}B\bar{C}\bar{D} + AB\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D} + AB\bar{C}\bar{D}$$

## POKAZNA VEŽBA 3

### Priprema za I kolokvijum

#### ZADATAK

KOLOKVIJUM 3

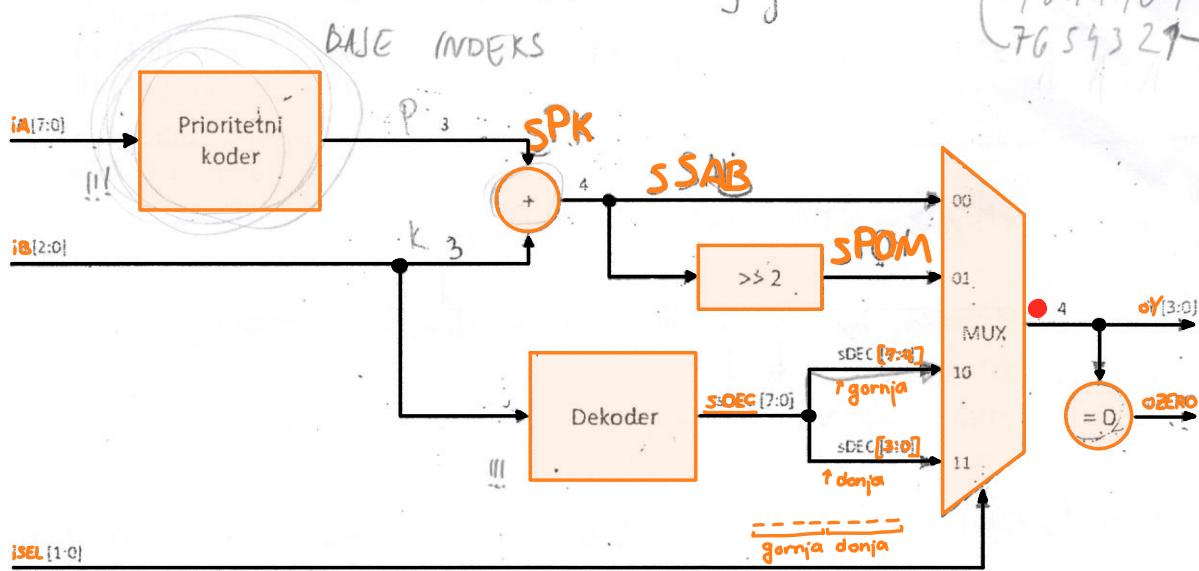
U VHDL jeziku za opis hardvera opisati i simulirati digitalni sistem prikazan na slici koji predstavlja jednostavnu aritmetičko-logičku jedinicu.

Izlazi digitalnog sistema:

- $iA[7:0]$  – prvi ulazni operand koji se preuzima „dekodovan“, tj. kao indeks jednog od 8 bita,
- $iB[2:0]$  – drugi ulazni operand koji se preuzima „kodovan“ u binarnoj predstavi,
- $iSEL[1:0]$  – izbor operacije.

Izlazi digitalnog sistema:

- $oY[3:0]$  – rezultat operacije,
- $oZERO$  – oznaka da li je rezultat operacije jednak nuli.



Slika 1. Aritmetičko-logička jedinica

Operacije koje aritmetičko-logička jedinica podržava su:

- zbir dva ulazna operanda,
- zbir dva ulazna operanda podeljen sa 4, tj. aritmetički pomeren u desno za 2 mesta,
- gornja 4 bita dekodovane vrednosti drugog operanda,
- donja 4 bita dekodovane vrednosti drugog operanda.

Sistem simulirati izvršavajući svaku od operacija bar jednom, sa bar 2 različite vrednosti na svakom operandu. Bar jedan od slučajeva treba da rezultuje nulom i bar jedan od slučajeva brojem različitim od nule.

**LOGIČKO PROJEKTOVANJE RAČUNARSKIH SISTEMA 1****Prvi kolokvijum – Grupa 3**

13 Jan 2016

**NAPOMENA**

Za potrebe kolokvijuma koristiti direktorijum C:\materija\LPRS1\_X\_Y\_Z\KOL1, gde je X oznaka studijskog programa (RA, E3), Y broj indeksa i Z godina upisa. Rešenje zadatka treba da se nalazi u tom direktorijumu.

**ZADATAK**

U VHDL jeziku za opis hardvera opisati i simulirati digitalni sistem prikazan na slici koji predstavlja jednostavnu aritmetičko-logičku jedinicu.

Ulazi digitalnog sistema:

- IA [7:0] – prvi ulazni operand,
- IB [7:0] – drugi ulazni operand,
- ISEL [7:0] – izbor operacije.

Izlazi digitalnog sistema:

- oY [7:0] – rezultat operacije.

Operacije koje aritmetičko-logička jedinica podržava su:

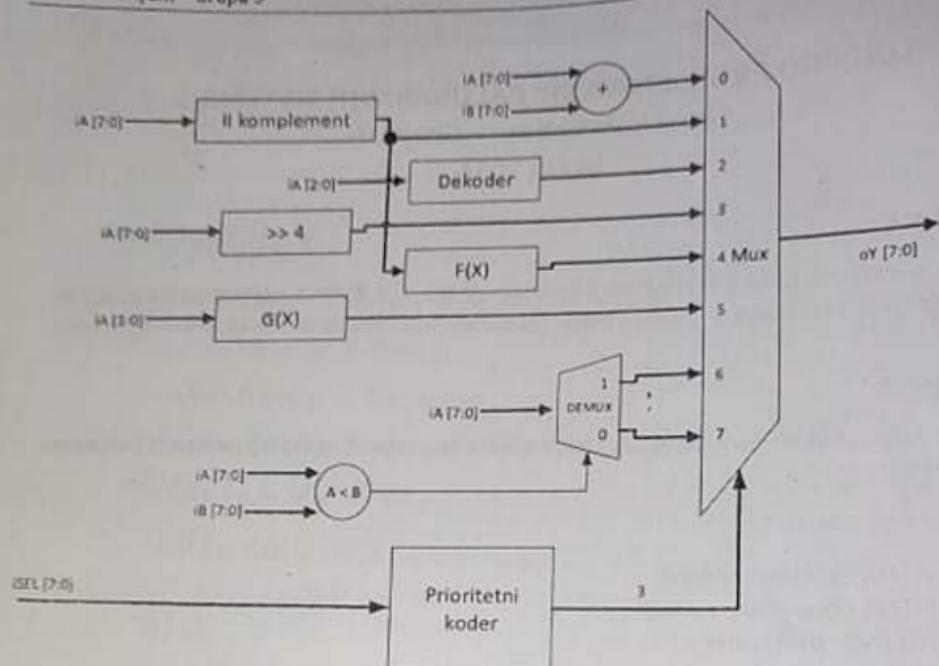
- zbir dva ulazna operanda,
- komplement prvog ulaznog operanda u II predstavi,
- dekodovanje donja 3 bita prvog operanda,
- aritmetičko pomeranje prvog operanda za 4 mesta u desno,
- operacija  $F(X) = 3X$ ,
- nepoznata operacija  $G(X)$  nad donja 4 bita prvog operanda (tabela 1),
- prvi operand, ako je  $A < B$ , u suprotnom 0,
- drugi operand, ako je  $A > B$ , u suprotnom 1.

Izbor operacije se vrši preko prioritetnog kodera kome je prioritetniji bit sa većim indeksom.

Sistem simulirati kroz sledeće testne slučajeve (najmanje 10):

- na izlazu treba da bude 0x07 kao rezultat operacije  $G(X)$ ,
- na izlazu treba da bude 0x08 kao rezultat operacije dekodovanje,
- na izlazu treba da bude 0xCD kao rezultat operacije prvi operand, ako je  $A < B$ ,
- na izlazu treba da bude 0xE8 kao rezultat operacije  $F(X)$ ,
- bar 6 slučajeva ostalih operacija, s tim da se svaka preostala operacija proba bar jednom.

## Prvi kolokvijum - Grupa 3



Slika 1. Aritmetičko-logička jedinica

Tabela 1. Funkcija  $G(X)$ :  $A[3:0] \rightarrow B[7:0]$ 

$A_3$	$A_2$	$A_1$	$A_0$	$B_7-B_4$	$B_3$	$B_2$	$B_1$	$B_0$
0	0	0	0	0000	0	1	0	1
0	0	0	1	0000	0	1	1	0
0	0	1	0	0000	0	1	1	1
0	0	1	1	0000	1	0	0	0
0	1	0	0	0000	1	0	0	1
0	1	0	1	0000	1	0	0	1
0	1	1	0	0000	1	0	1	0
0	1	1	1	0000	1	1	0	0
1	0	0	0	0000	1	1	0	1
1	0	0	1	0000	1	1	1	0
1	0	1	0	0000	1	1	1	1
1	0	1	1	0000	0	0	0	0
1	1	0	0	0000	0	0	0	1
1	1	0	1	0000	0	0	1	0
1	1	1	0	0000	0	0	1	1
1	1	1	1	0000	0	1	0	0

## # TEORIJA ISP

	S1	S2	S3	S4	S5	S6	S7	S8	S9
0	S <sub>6/0</sub>	S <sub>6/0</sub>	S <sub>8/0</sub>	S <sub>8/1</sub>	S <sub>6/0</sub>	S <sub>9/1</sub>	S <sub>2/0</sub>	S <sub>3/1</sub>	S <sub>3/0</sub>
1	S <sub>6/1</sub>	S <sub>8/0</sub>	S <sub>8/1</sub>	S <sub>1/0</sub>	S <sub>8/1</sub>	S <sub>3/0</sub>	S <sub>3/1</sub>	S <sub>9/0</sub>	S <sub>6/1</sub>
	*	+	*	-	*	-	*	-	*
	↑	↑	↑	↑					
					gde nam je 1,0				
					gde nam je 0,0				
					gde sve ima gore 0, dole 1				

S<sub>8/1</sub>  
IDE U 12 LAZ  
STANJE  
(8)

NEMA  
S<sub>1</sub>!!!

S<sub>1</sub> S<sub>2</sub> nisu istog stanja  $\Rightarrow X$

S<sub>1</sub> S<sub>3</sub> jesu istog stanja: S<sub>1</sub> S<sub>3</sub>

S<sub>6/0</sub> S<sub>8/0</sub>

S<sub>6/1</sub> S<sub>8/1</sub>

da imamo 8-8 umesto 6-8,  
onda pisemo u taj red samo "—"

za S<sub>1</sub> S<sub>7</sub> imamo  
6-2, 6-3 ali uvez  
Pifem, pifem, prvo  
MANI BROJ:  
(2-6, 3-6)

	S1	S2	S3	S4	S5	S6	S7	S8	S9
		X							
S2			X						
S3				X					
S4					X	X	X		
S5						X			
S6							X	X	
S7								X	
S8									X
S9									X

NEMA S<sub>9</sub>!!!



Znamo da je samo S<sub>2</sub> znaka +  
znači ni sa čim se neće slagati  
pa možemo odmah X na sve!

1<sup>o</sup> KORAK treba da zapisemo svaku X polje

	O
S <sub>2</sub>	X
S <sub>3</sub>	X
S <sub>4</sub>	X X X
S <sub>5</sub>	X X X
S <sub>6</sub>	X X X X
S <sub>7</sub>	X X X X X
S <sub>8</sub>	X X X X X X
S <sub>9</sub>	X X X X X X X
S <sub>1</sub> S <sub>2</sub> S <sub>3</sub> S <sub>4</sub> S <sub>5</sub> S <sub>6</sub> S <sub>7</sub> S <sub>8</sub>	



- : 1-2, 1-4, 1-6, 1-8
- 2-3, 2-4, 2-5, 2-6, 2-7, 2-8
- 3-4, 3-6, 3-8
- 4-5, 4-7, 4-9
- 5-6, 5-8
- 6-7, 6-9
- 7-8,
- 8-9

2<sup>o</sup> SAO A od tih ↑ porja gledamo da li u zelenim poljima piše neko od tih komb

; onda ih precrtamo (dovoljno je da 1 od 2 broja bude na listi)  
zapisujemo koja su polja precrtaana:



- : 1-7, 3-7, 4-6, 4-8, 5-7, 7-9

+ 3<sup>o</sup> SAO A od tih ↑ porja gledamo da li je u nepreškrabahim ostao neki iz liste ŽUTIH, a ovom slučaju Nije

da ima onda iterativno radimo do kraja

3<sup>o</sup> Zaokružujemo ovo što je ostalo

4<sup>o</sup> ČITAMO AUTOMAT:

- ⇒ 1. svako stanje mora biti bar jednom
- ⇒ 2. svako stanje mora biti samo jednom

recimo  
a)  $(S_1, S_3), (S_1, S_5), (S_1, S_9), (S_3, S_5), (S_3, S_9), (S_5, S_9)$   
 $(S_6, S_8)$  NEMA  $S_2$ ! ponarlijaju se!

b)  $(S_1, S_3, S_5, S_9)(S_6, S_8)(S_2)(S_7)(S_9)$   
TAČAN ODG

znači ugi po ona dva kriterijuma

ELIMINISATI NETAČNE

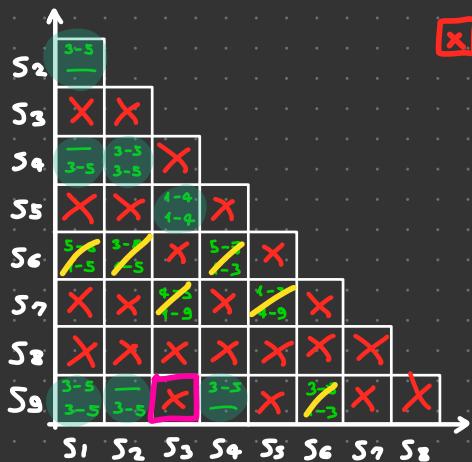
\* bonus: KOLIKO U ZADIMA AUTOMATA?

- a 2 automata
  - b 5 automata
  - c 3 automata
- } na osnovu rešenja hahahah

#

	S1	S2	S3	S4	S5	S6	S7	S8	S9
0	S <sub>3,10</sub>	S <sub>3,10</sub>	S <sub>4,11</sub>	S <sub>5,10</sub>	S <sub>1,11</sub>	S <sub>8,10</sub>	S <sub>5,11</sub>	S <sub>3,10</sub>	S <sub>3,10</sub>
1	S <sub>3,11</sub>	S <sub>5,11</sub>	S <sub>4,10</sub>	S <sub>3,11</sub>	S <sub>4,10</sub>	S <sub>1,11</sub>	S <sub>9,10</sub>	S <sub>5,10</sub>	S <sub>3,11</sub>
	*	*	-	*	-	*	-	0 X	≠

sveda



- 1-3, 1-5, 1-7, 1-8,  
2-3, 2-5, 2-7, 2-8,  
3-4, 3-6, 3-8, 3-9,  
4-5, 4-7, 4-8,  
5-6, 5-8, 5-9,  
6-7, 6-8,  
7-8, 7-9,  
8-9

1-6, 2-6, 3-7, 4-6, 5-7, 6-9

↑  
da ovde ima tipa 3-5 izbacili bismo  
i S<sub>1</sub>-S<sub>9</sub>, S<sub>1</sub>-S<sub>2</sub>, S<sub>1</sub>-S<sub>4</sub>, itd...

rešenje: (S<sub>1</sub>, S<sub>2</sub>, S<sub>4</sub>, S<sub>9</sub>) (S<sub>3</sub>, S<sub>5</sub>) (S<sub>6</sub>) (S<sub>7</sub>) (S<sub>8</sub>)

da je ovo polje bilo zaokruženo morali bismo u  
prvu zagradu ubaciti S<sub>3</sub> (zbog S<sub>9</sub>) ali bi to  
poruklo i S<sub>5</sub> pa => (S<sub>1</sub>, S<sub>2</sub>, S<sub>3</sub>, S<sub>4</sub>, S<sub>5</sub>, S<sub>9</sub>) (S<sub>6</sub>) (S<sub>7</sub>) (S<sub>8</sub>)

⇒ IMA 5 automata

1.	s1	s2	s3	s4	s5	s6	s7	s8	s9
0	S <sub>10</sub>	S <sub>9</sub>	S <sub>8</sub>	S <sub>7</sub>	S <sub>6</sub>	S <sub>5</sub>	S <sub>4</sub>	S <sub>3</sub>	S <sub>2</sub>
1	S <sub>1</sub>	S <sub>2</sub>	S <sub>3</sub>	S <sub>4</sub>	S <sub>5</sub>	S <sub>6</sub>	S <sub>7</sub>	S <sub>8</sub>	S <sub>9</sub>

РЕЗЕНЬЕ:  $(S_1, S_3, S_5, S_9) \times (S_6, S_8)$   
 $(S_4) \times (S_2) \times (S_4)$

2.	$x \mid s$	$s_1$	$s_2$	$s_3$	$s_4$	$s_5$	$s_6$	$s_7$	$s_8$	$s_9$
0	$S_{5/0}$	$S_{3/0}$	$S_{4/1}$	$S_{5/0}$	$S_{1/1}$	$S_{8/0}$	$S_{5/1}$	$S_{3/0}$	$S_{3/0}$	$S_{3/0}$
1	$S_{5/1}$	$S_{5/1}$	$S_{1/0}$	$S_{3/1}$	$S_{4/0}$	$S_{1/1}$	$S_{3/0}$	$S_{5/0}$	$S_{3/1}$	$S_{3/1}$

repetition:  $(S_1, S_2, S_4, S_3) \times (S_6) (S_7) (S_5)$   
 $\quad\quad\quad\quad\quad (S_3, S_5)$

$$+ - + - + \text{[long expression involving } S_1, S_2, S_3, S_4, S_5, S_6\text{]}$$

	A <sub>1</sub>	A <sub>2</sub>	A <sub>3</sub>	A <sub>4</sub>	A <sub>5</sub>	A <sub>6</sub>	A <sub>7</sub>
0	A <sub>1</sub> /0	A <sub>1</sub> /0	A <sub>6</sub> /1	A <sub>5</sub> /0	A <sub>5</sub> /0	A <sub>5</sub> /0	A <sub>3</sub> /0
1	A <sub>4</sub> /0	A <sub>4</sub> /0	A <sub>4</sub> /0	A <sub>2</sub> /0	A <sub>2</sub> /0	A <sub>4</sub> /0	A <sub>4</sub> /0

RESENJE:  $(S_1, S_5, S_6)(S_2, S_4)(S_3)(S_7)$

+ FRED

5

$\chi^2$	$S_1$	$S_2$	$S_3$	$S_4$	$S_5$	$S_6$	$S_7$	$S_8$	$S_9$	$S_{10}$	$S_{11}$	$S_{12}$
0	$S_{2/0}$	$S_{4/0}$	$S_{6/0}$	$S_{8/0}$	$S_{10/0}$	$S_{12/0}$	$S_{14/0}$	$S_{16/0}$	$S_{18/1}$	$S_{19/0}$	$S_{20/0}$	$S_{21/0}$
+	$S_{3/0}$	$S_{5/0}$	$S_{7/0}$	$S_{9/0}$	$S_{11/0}$	$S_{13/0}$	$S_{15/0}$	$S_{17/0}$	$S_{19/0}$	$S_{21/0}$	$S_{23/0}$	$S_{25/0}$

# Sub  $R_z, R_x, R_y$

1)  $R_z \leftarrow R_x - R_y$  TACAN

2)  $R_x \leftarrow R_y - R_z$

3)  $R_y \leftarrow R_z - R_x$

↑  
OVO BUDE UGL  
I DOLAZI DAL DOBIVANJU  
TABELU

# PONOVITI ONA SLOVA O, I, Z, H, W ...

ČESTA POJAVA U JAN

NE DOLAZI UGL U

JANUARU ALI SVAKAKO TI TREBA  $\frac{0}{=}$



**Tabela 1. Instrukcije procesora**

Operacija	Funkcija	Kod instrukcije
mov Rz, Rx	RZ $\leftarrow$ [RX]	000000
add Rz, Rx, Ry	RZ $\leftarrow$ [RX] + [RY]	000001
sub Rz, Rx, Ry	RZ $\leftarrow$ [RX] - [RY]	000010
and Rz, Rx, Ry	RZ $\leftarrow$ [RX] & [RY]	000011
or Rz, Rx, Ry	RZ $\leftarrow$ [RX]   [RY]	000100
not Rz, Rx	RZ $\leftarrow$ not [RX]	000101
inc Rz, Rx	RZ $\leftarrow$ [RX] + 1	000110
dec Rz, Rx	RZ $\leftarrow$ [RX] - 1	000111
shl Rz, Rx	RZ $\leftarrow$ shl [RX]	001000
shr Rz, Rx	RZ $\leftarrow$ shr [RX]	001001
ashl Rz, Rx	RZ $\leftarrow$ ashl [RX]	001010
ashr Rz, Rx	RZ $\leftarrow$ ashr [RX]	001011
jmp ADDR	PC $\leftarrow$ ADDR	010000
jmpz ADDR	if Z=1 PC $\leftarrow$ ADDR	010001
jmps ADDR	if S=1 PC $\leftarrow$ ADDR	010010
jmpc ADDR	if C=1 PC $\leftarrow$ ADDR	010011
jmpnz ADDR	if Z=0 PC $\leftarrow$ ADDR	010101
jmpns ADDR	if S=0 PC $\leftarrow$ ADDR	010110
jmpnc ADDR	if C=0 PC $\leftarrow$ ADDR	010111
ld Rz, Ry	RZ $\leftarrow$ [[RY]]	100000
st Ry, Rx	[RY] $\leftarrow$ [RX]	110000

KONTROLNI ROM: → PRVO IDE FETCH INSTRUKCIJA D D D  
 dalji redosled nije bitan, bitno da ih  
 sa slike (dodatak) nabrojimo

ima 20 redova  
 pamorabiti 5 bitu!



ADRESA	SADRŽAJ	INSTRUKCIJA
00000	5E3	Fetch
00001	B E3	!
00010	263	!
→ 00011	1B5	LDA
00100	2C3	!
00101	5E7	!
→ 00110	2B3	SUB
00111	2E1	
01000	3CF	
→ 01001	2BR	ADD
01010	2C1	
01011	3CD	
01100	1A3	INC
01101	2EC	
01110	3E3	
01111	3BE	SAL
10000	3CA	
10001	3C7	
10010	1A3	SAR
10011	2C3	
10100	3E3	

# ADRESNI ROM: NEMA FETCH

PA JE PRVA SLEDEĆA SADRŽAJ 1.

sadržaj te instrukcije  
adresa na kojoj počinje  
sadržaj

ADRESA	SADRŽAJ	INSTRUKCIJA
0000	00011	LDA
0001	00110	SUB
0010	01001	ADD
0011	01100	INC
0100	01111	SAL
0101	10010	SAR
0110		
0111		
1000		
1001		
1010		
1011		
1100		
1101		
1110		
1111		

na ispitnom je dat kontrolni rom (tabela 1.)

### Lopčko projektovanje računarskih sistema I

U tabelama nize, dati je sekvenci Fetch (prhvatne faze), kao i posteljne tri faze svake od instrukcija, obzirom da v mikrokontrolerice za svaku od njih upravo Fetch (prhvati).

Fetch (prhvatni) Sif		INC Sif		SAR Sif	
Sekvenca	Kontr. red	Sekvenca	Kontr. red	Sekvenca	Kontr. red
T1	5E3 Hex	T4	2B3 Hex	T4	3B3 Hex
T2	BE3 Hex	T5	2E1 Hex	T5	3EA Hex
T3	263 Hex	T6	3CF Hex	T6	3E7 Hex

LDA Sif		ADD Sif	
Sekvenca	Kontr. red	Sekvenca	Kontr. red
T4	1B5 Hex	T4	2Bk Hex
T5	2C3 Hex	T5	2C1 Hex
T6	5E7 Hex	T6	3CD Hex

Voditi računa o kodovima instrukcija iz Tabele 1, popuniti adresni ROM (Address ROM) i kontrolni ROM (Control ROM) sa Slike 1, tako da realizovana UJ ispravno radi.

Kontrolni ROM (Control ROM)

Adresa	Sadržaj	Instrukcija	Adresa	Sadržaj	Instrukcija
			0000		
			0001		
			0010		
			0011		
			0100		
			0101		
			0110		
			0111		
			1000		
			1001		
			1010		
			1011		
			1100		
			1101		
			1110		
			1111		

Popuniti tabele tako da UJ radi ispravno, voditi računa o poziciji Fetch (prihvatne) mikrooperacije. Ukoliko postoje adrese u adresnom ROM-u čiji sadržaj nije bitan, popuniti ih sa XXXX ili ih ostaviti prazne.

PONOVITI ILARNOOVE MARE !



→ BINARNE KONVERZIJE \* OBAVEZNU

ČIM PITA ŠTA TREBA DO SE  
URADI => DA SE PROŠIRI

  ^  
  KOD SABIRANJA

  ↖ KOMPONENTE:

$$\begin{array}{r} 1101 \\ + 1010 \\ \hline -9 \\ \hline \text{treba} \end{array}$$

1<sup>o</sup> provjerimo koliki su brozevi

$1+4-\underline{8}=-\underline{3} \rightarrow 141 \quad \boxed{-3}$

$2-8=\underline{-6}$

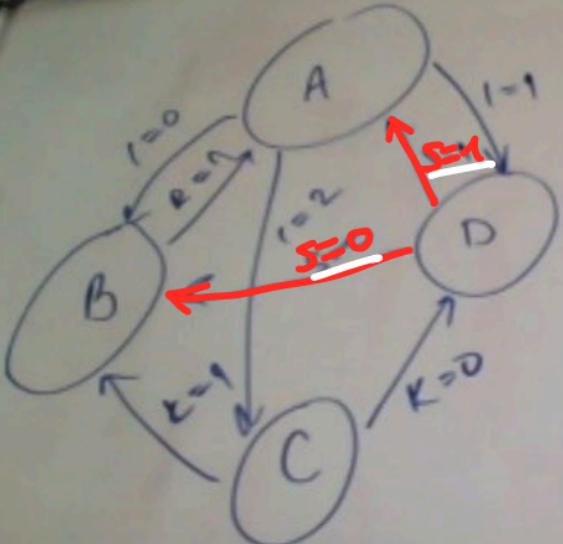
$\begin{array}{r} 1101 \\ -1 \\ \hline 1100 \\ -6 \\ \hline 0011 \\ \hline 3 \end{array}$

nmg da se sabiju zbog prekoračenja

⇒ POTREBNO PROŠIRENJE:

$$10111 = -16 + 4 + 2 + 1 = -9 \quad \cancel{x}$$

= jer je za to prekoračio



when  $X \Rightarrow$

$\text{if } (s=1) \text{ then}$

$\rightarrow \text{sSTATE} = A_i$

$\text{else if } (s=0) \text{ then}$

$\rightarrow \text{sSTATE} = B$

$\text{else}$

$\text{sSTATE} = \text{IDLE}_i$

$\text{end if;}$

State  $i$   $\neq X_i$ :

- 1) A
- 2) B
- 3) C
- 4) D

C carry

S sign

Z zero

3 stvari koje  
su bitne?!

štači ako  
je prenos

jmpnc ~~not~~

jmpns

jmpnz

not

ori

štači ako je znak