

Enhancement vs Recovery

- **ENHANCEMENT:** The manipulation or transformation of an image, with the aim of increasing its usefulness or visual appearance.
- **RESTORATION/RECOVERY:** The modeling of a degradation the image is subjected to (which resulted in loss of information), and the removal of this degradation (or recovery of the information lost), based on an optimality criterion
- Examples:
 - Modification of intensity values so as to increase contrast **enhancement**
 - Deconvolution **restoration**
 - Inpainting **enhancement or recovery**
 - Smoothing or removal of noise **enhancement or restoration**

Image Enhancement

- No general “theory” behind enhancement
 - Criteria for enhancement are often subjective or too complex to be easily converted to useful objective measures
- The algorithms tend to be qualitative & ad hoc and they are application-dependent
- Application-specific evaluation of its effectiveness

Enhancement Topics

- • Point-wise Intensity Transformations
 - Log, Power-law, Piecewise linear
- • Histogram Processing
- • Spatial Filtering (LSI vs non-linear)
 - Smoothing
 - Sharpening
 - Homomorphic Filtering
- • Pseudo-Coloring
- • Video Enhancement

Point-Wise Intensity Transformations

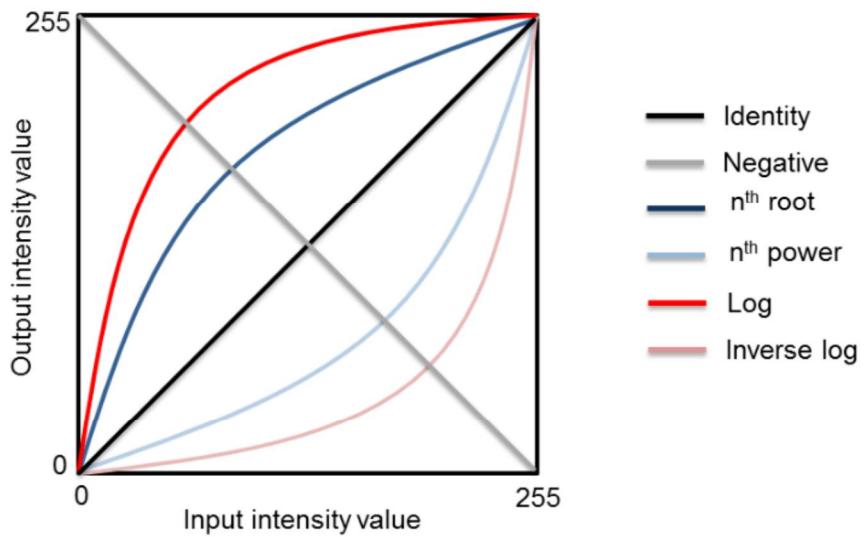
- Expressed by

$$\underline{y(n_1, n_2)} = \mathbf{T}_{\text{point}}[\underline{x(n_1, n_2)}]$$

$$\underline{\mathbf{y}(n_1, n_2)} = \mathbf{T}_{\text{point}}[\underline{\mathbf{x}(n_1, n_2)}]$$

$$\underline{\underline{\mathbf{y}(\mathbf{n})}} = \mathbf{T}_{\text{point}}[\underline{\underline{\mathbf{x}(\mathbf{n})}}]$$

Intensity Transformations



Negative Transformation

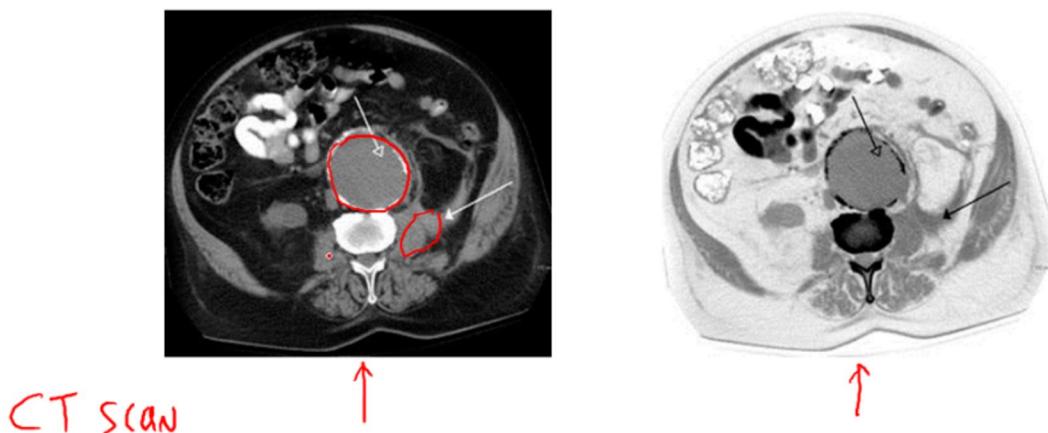


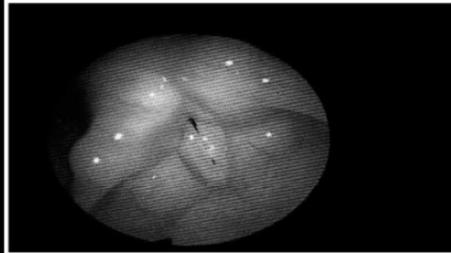
Image source: <http://en.wikipedia.org/wiki/File:RupturedAAA.png>

Log Transformation

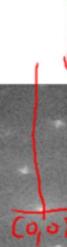
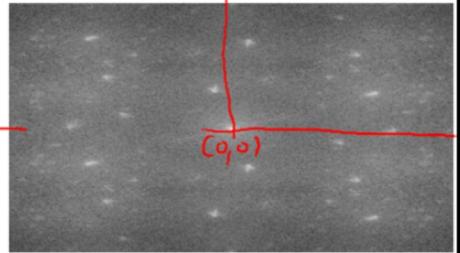
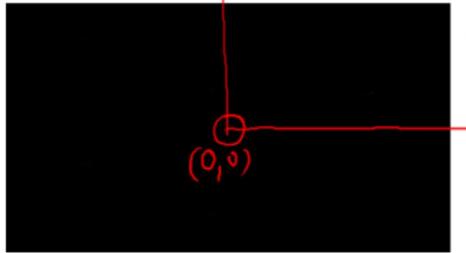
- Log-Transform (expand low – compress high):

$$y(\mathbf{n}) = c \cdot \log(x(\mathbf{n}) + 1)$$

- Used to display Fourier Spectra

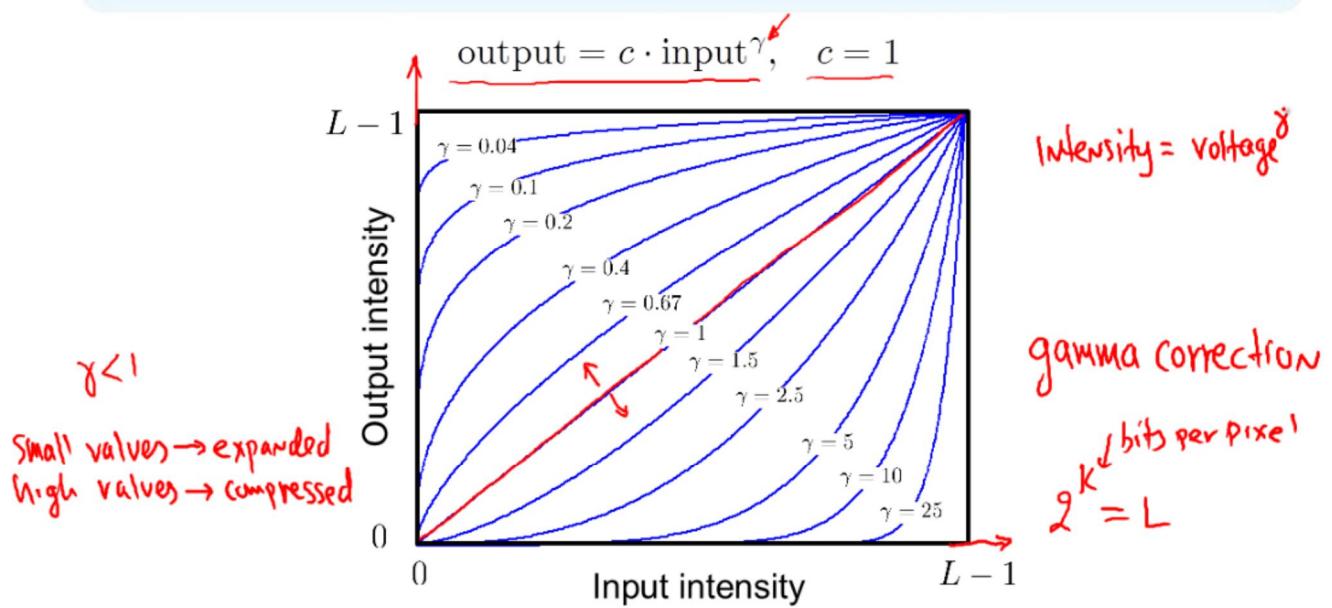


Original



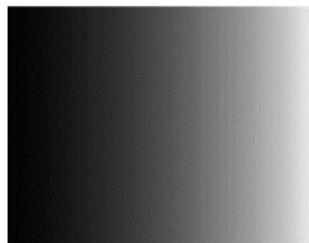
Log-transform of Fourier spectrum magnitude

Power-Law Transformation



Gamma Correction Example

original



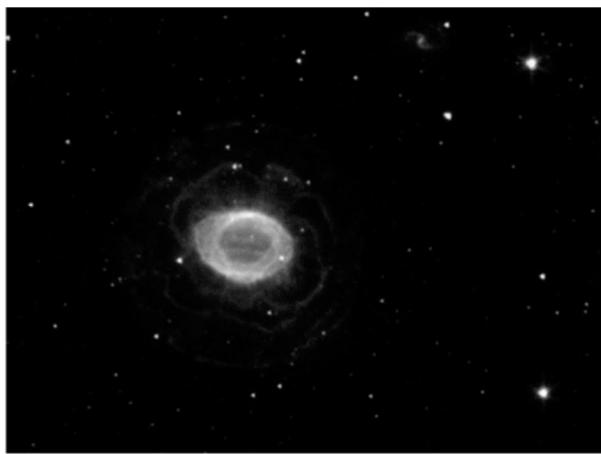
Displayed on
a monitor
with gamma
 $= 2.5$

Corrected
with gamma
 $= 0.4$



Display of
the corrected
image

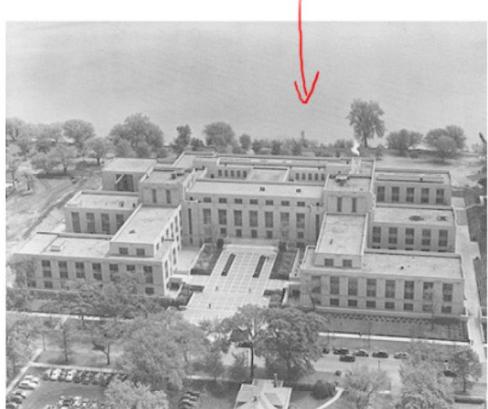
Power-Law Example



http://www.nasa.gov/multimedia/imagegallery/image_feature_679.html

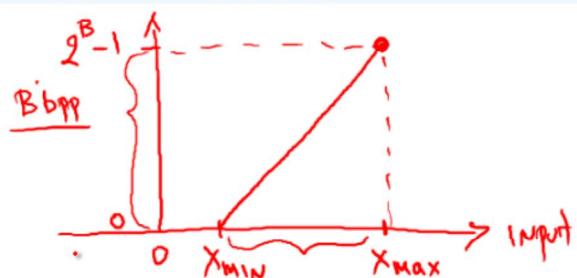
$$\gamma = 0.5$$

Power-Law Example



$$\gamma = 2$$

Contrast Stretching



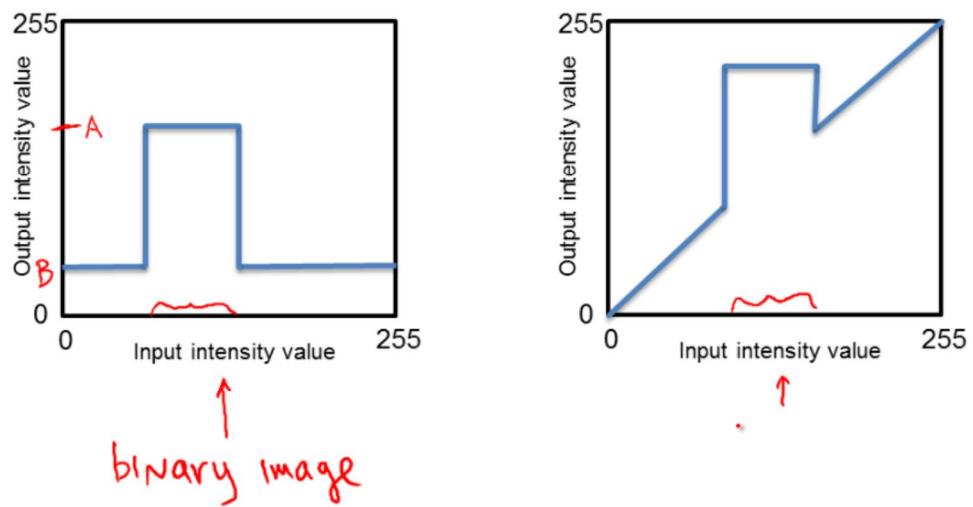
$$y(n) = \frac{2^B - 1}{x_{max} - x_{min}} (x(n) - x_{min})$$

$$x_{max} = \max_n x(n) \quad x_{min} = \min_n x(n)$$

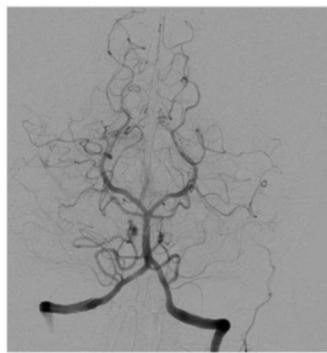
Dynamic Range Expansion



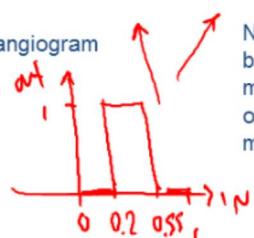
Intensity-Level Slicing



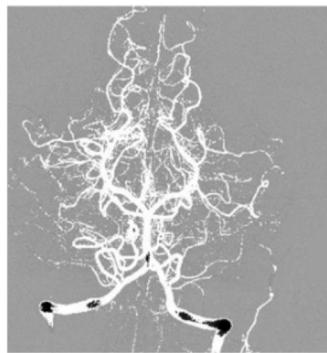
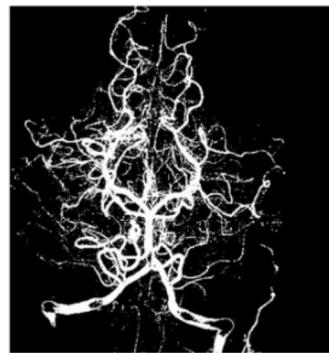
Intensity-Level Slicing



Original angiogram



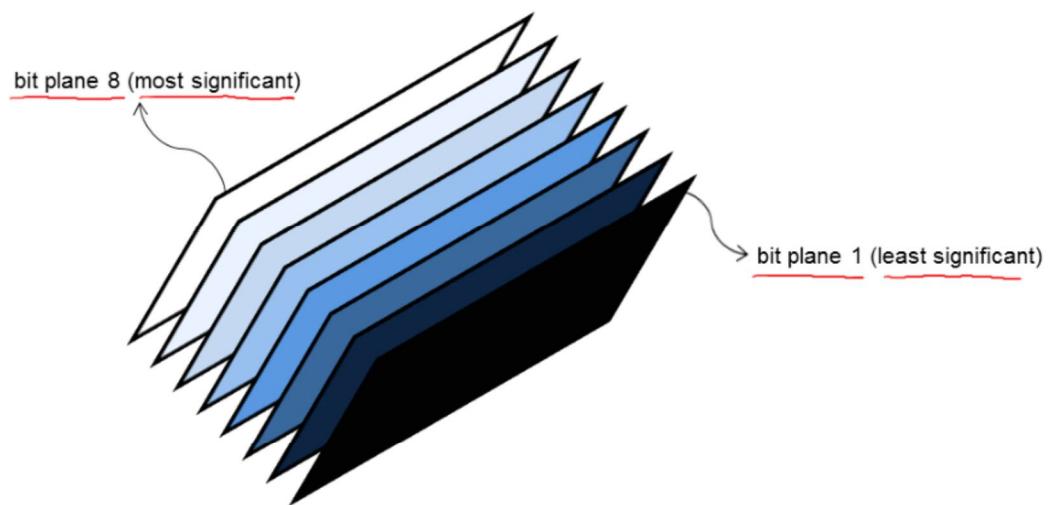
Normalized intensity between 0.2 and 0.55 is mapped to 1, everything outside this range is mapped to 0



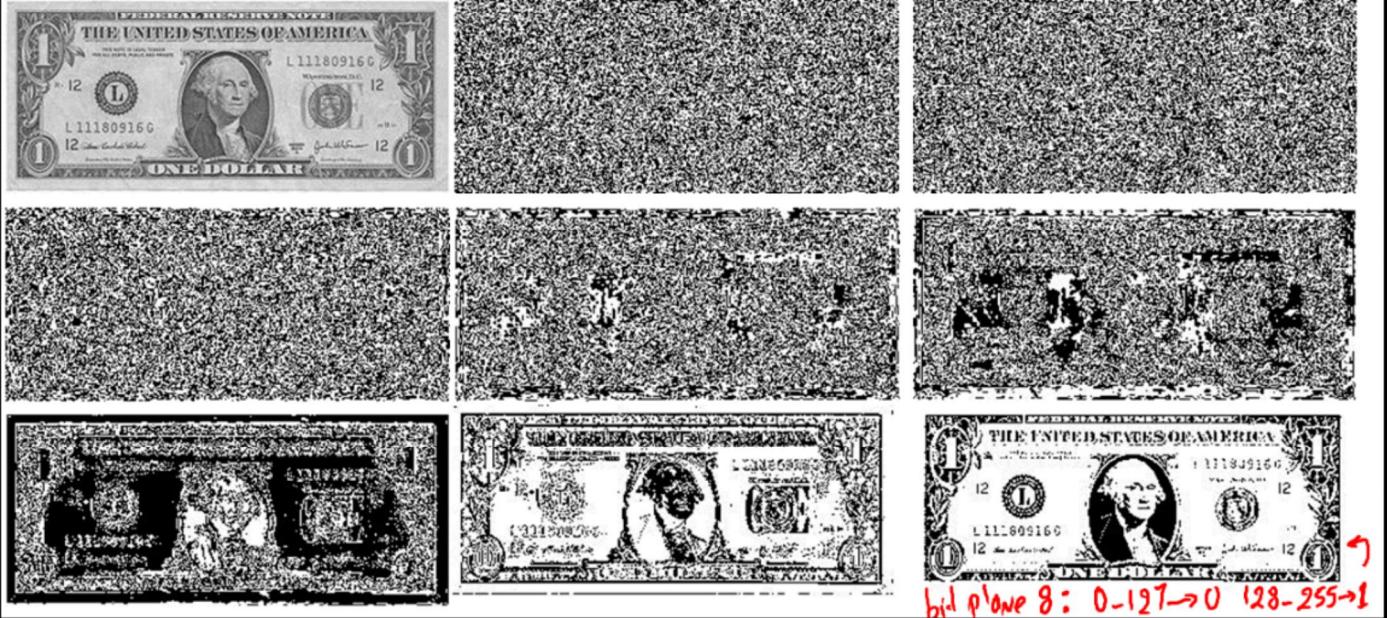
Normalized intensity between 0.2 and 0.55 is mapped to 1, everything outside this range keeps its original value



Bit-Plane Slicing



Bit-Plane Slicing Example



Bit-Plane Slicing Example



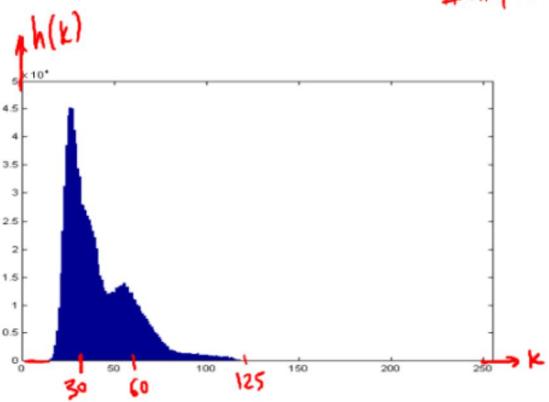
Enhancement Topics

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 - Sharpening
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- Video Enhancement

Image Histogram

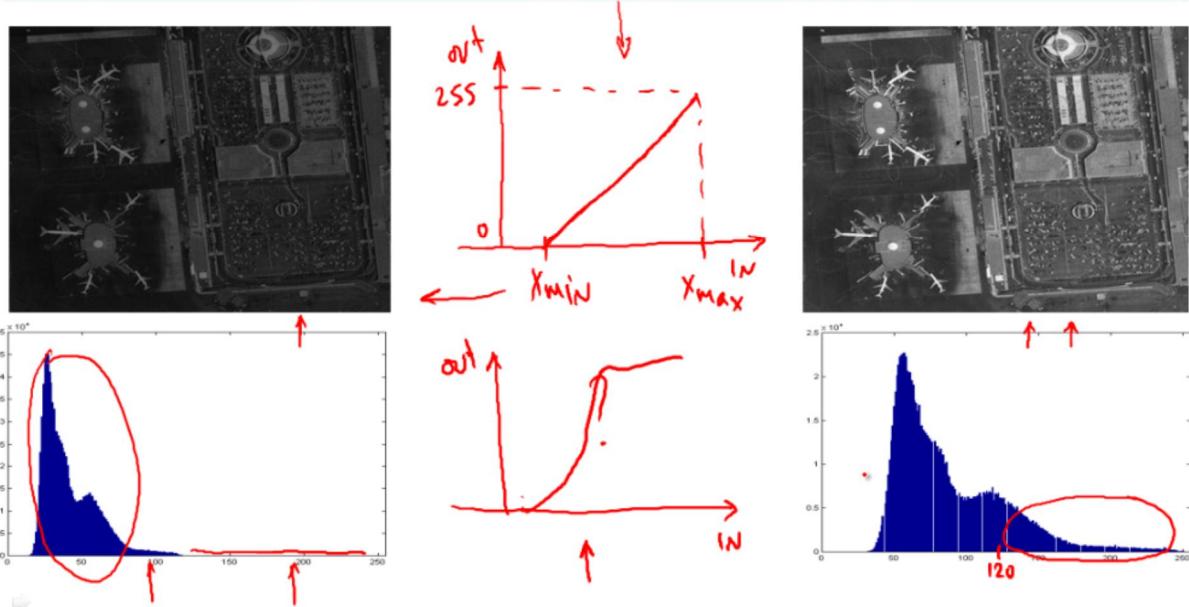
$\underline{h(k)} = \underline{n_k}$, the number of pixels with value \underline{k} , $k = 0, \dots, N - 1$

$\frac{h(k)}{\# \text{ of pixels}}$



Probability density function of intensity values

Contrast Stretching



Histogram Equalization

- Objective: Obtain a **flat histogram**
- Normalized histogram

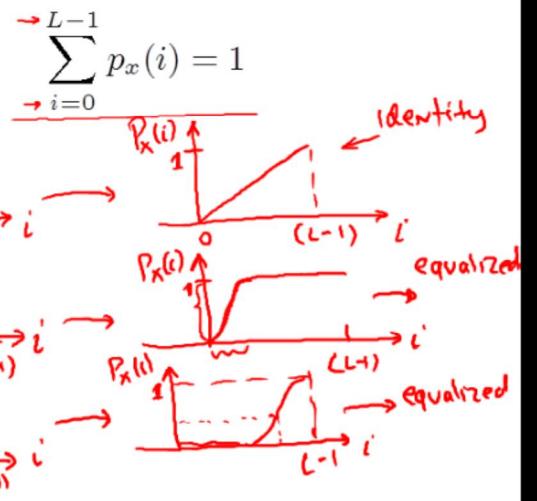
$$pdf \quad p_x(i) = p(x = i) = \frac{n_i}{MN}, \quad 0 \leq i \leq L - 1$$

- Procedure:

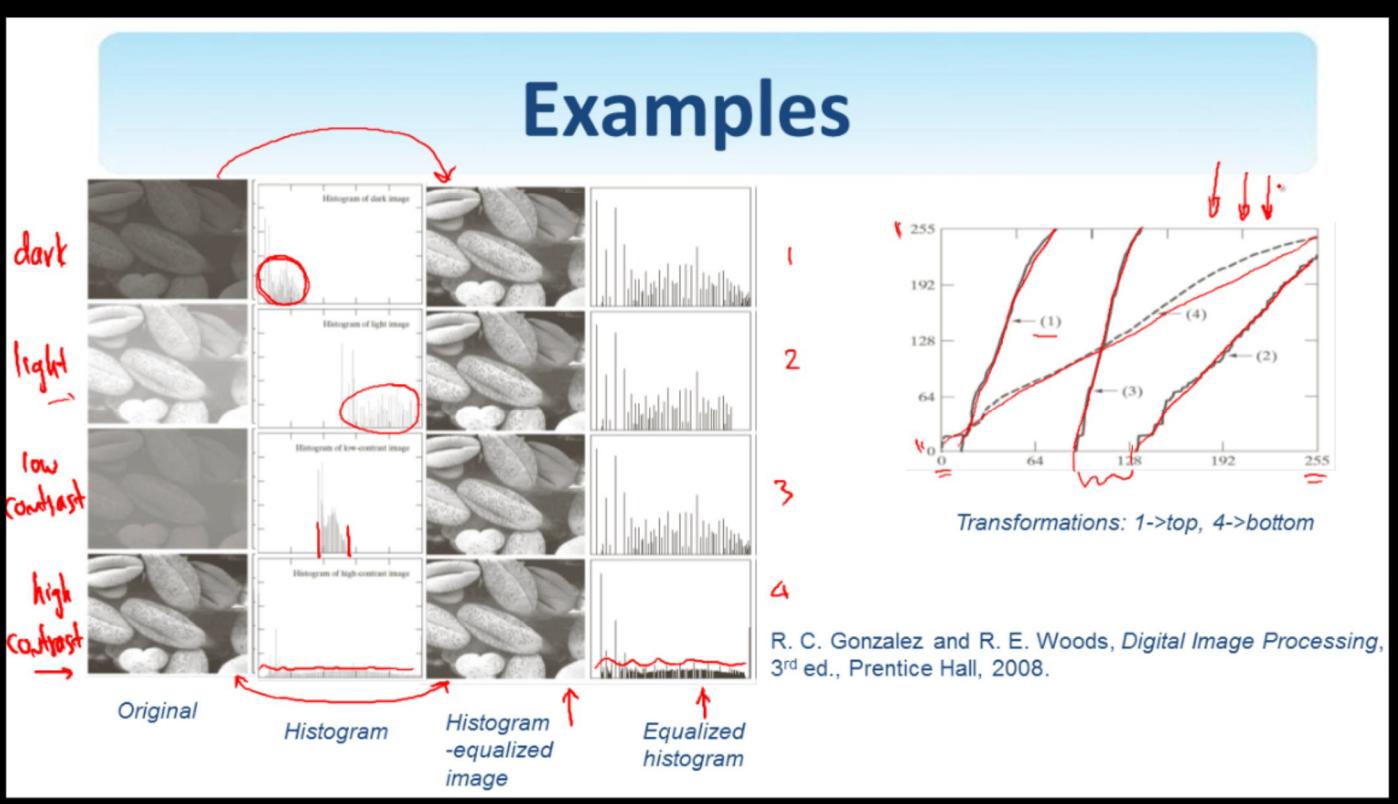
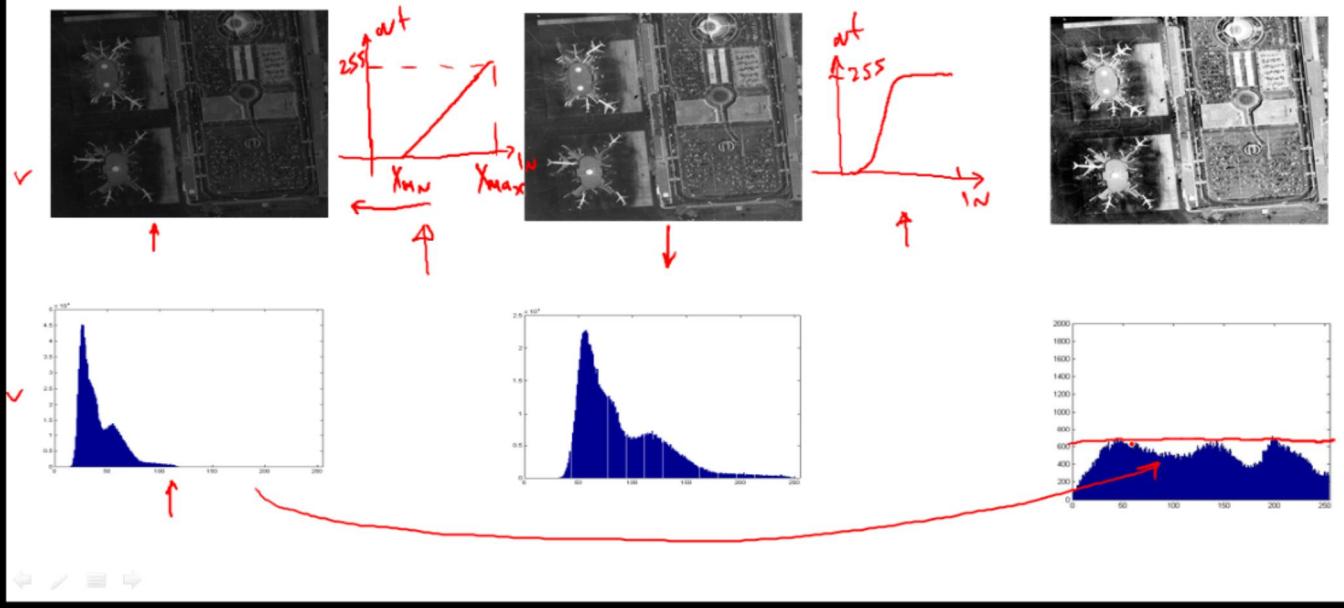
$$\rightarrow P_x(i) = \sum_{j=0}^i p_x(j) \quad cdf$$

$$\tilde{y}(n) = P_x(x(n))$$

$$y(n) = (L - 1) \cdot \tilde{y}(n)$$



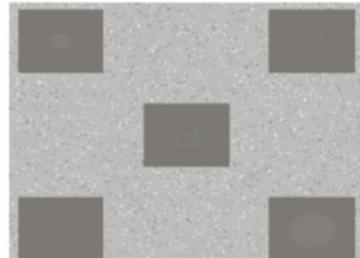
Contrast Stretching vs Histogram Equalization



Local Histogram Equalization



Original image



Global histogram equalization



Local histogram equalization using
a 3×3 neighborhood

R. C. Gonzalez and R. E. Woods, *Digital Image Processing*,
3rd ed., Prentice Hall, 2008.

Enhancement Topics

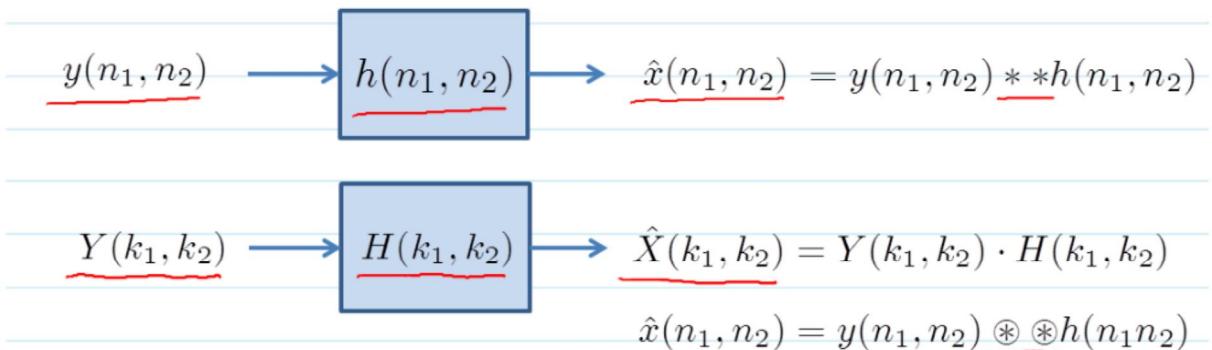
- Point-wise Intensity Transformations
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Smoothing Spatial Filters

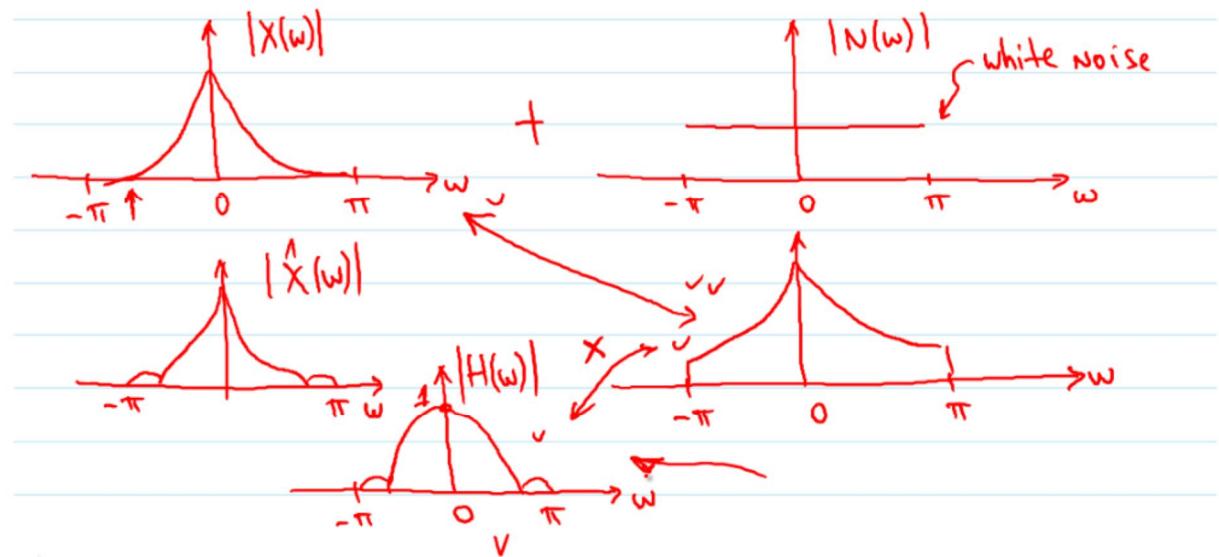
- **Objective:** Enhance image by reducing noise that may be present.
- Will discuss methods that attempt to reduce additive broadband and/or salt and pepper noise, also known as impulsive noise.
- Will discuss additional techniques under recovery

LSI Systems

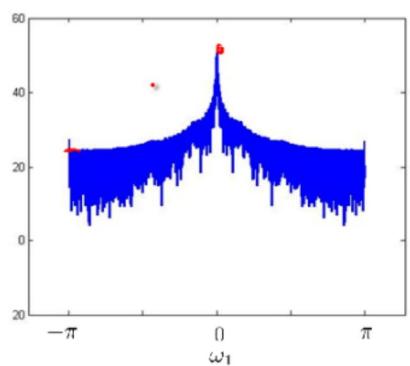
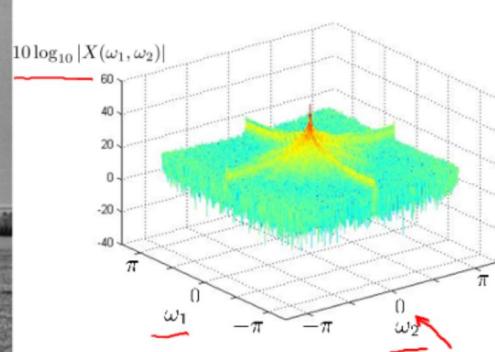
$$\underline{y(n_1, n_2)} = \underline{x(n_1, n_2)} + \underline{w(n_1, n_2)}$$



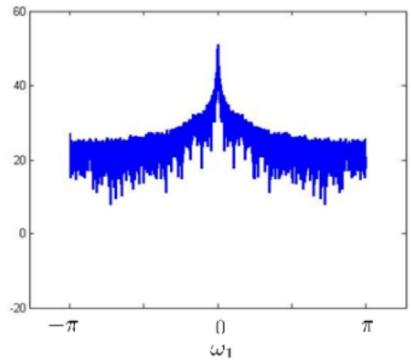
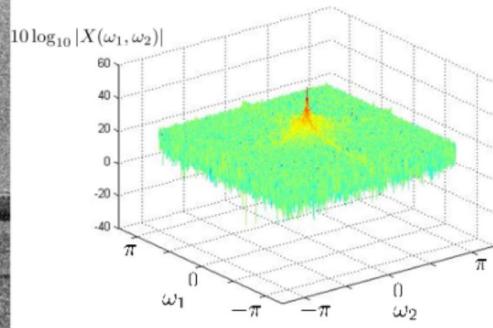
Noise Smoothing in the Frequency Domain



Original Image

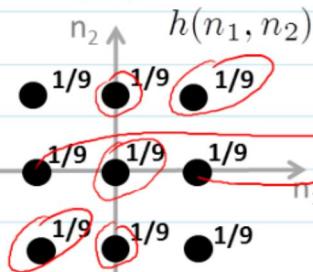


Noisy Image



Frequency Response of Flat Filters

3×3



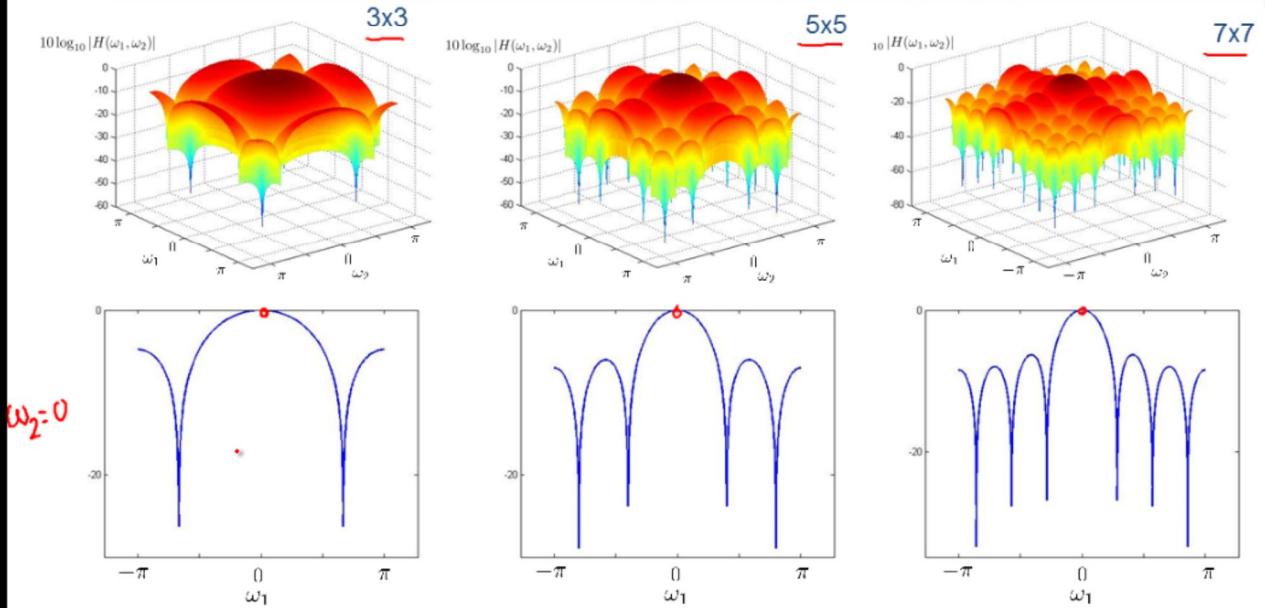
$$H(\omega_1, \omega_2) = \frac{1}{9}$$

$$+ \frac{2}{9} \cos(\omega_1 n_1) + \frac{2}{9} \cos(\omega_2 n_2)$$

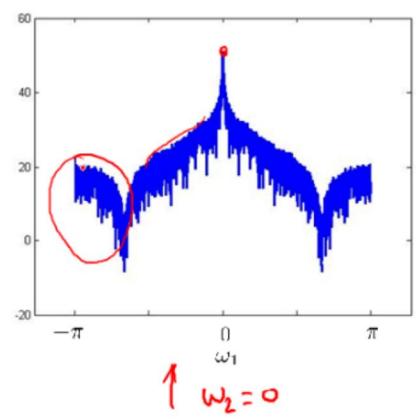
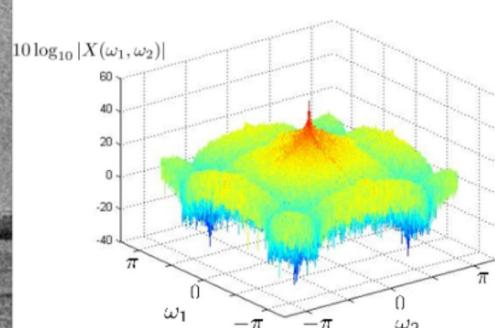
$$+ \frac{2}{9} \cos(\omega_1 n_1 + \omega_2 n_2) + \frac{2}{9} \cos(\omega_1 n_1 - \omega_2 n_2)$$

$$H(0,0) = 1$$

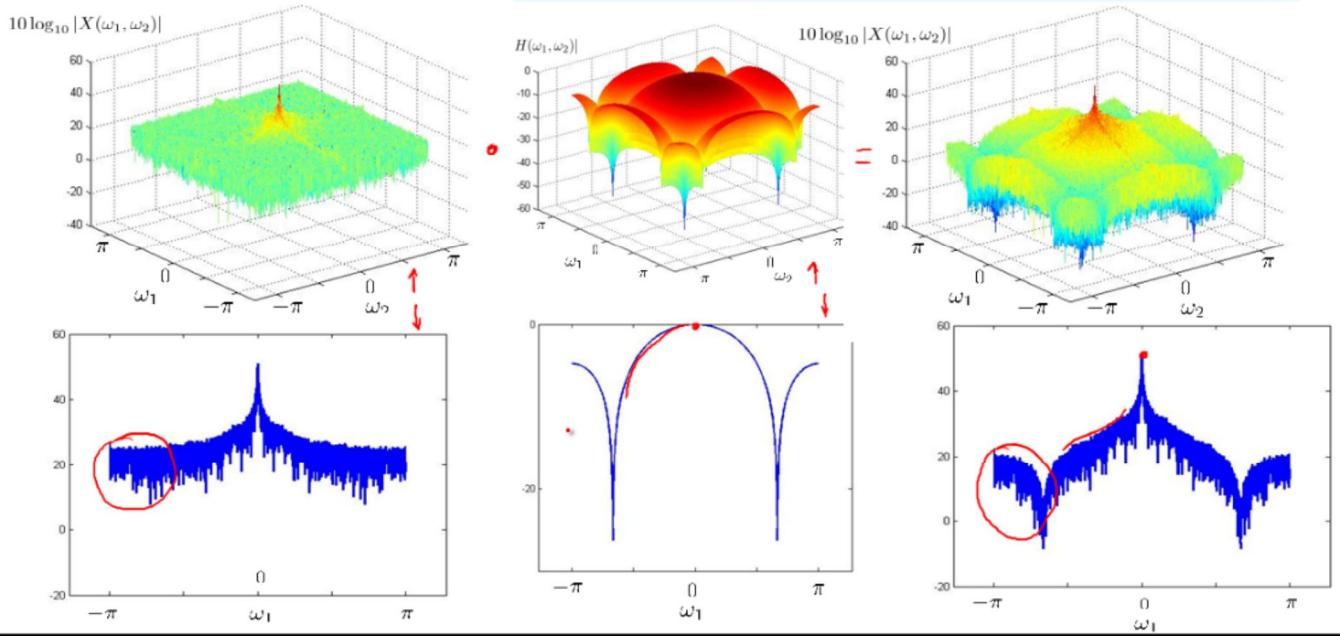
Frequency Response of Flat Filters



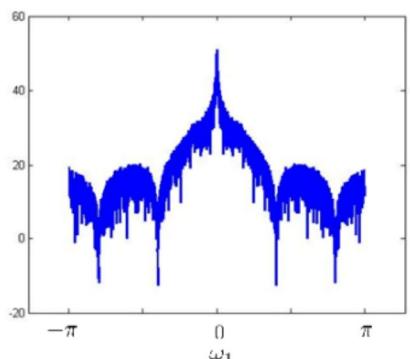
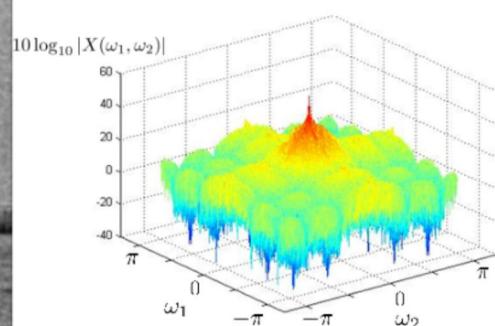
Filtered by 3x3 Filter



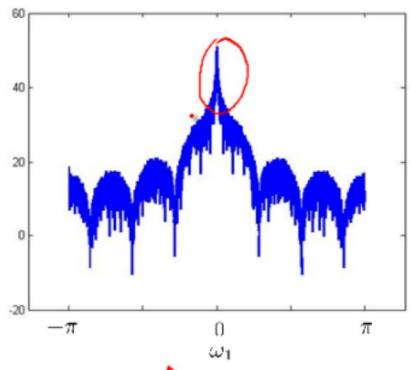
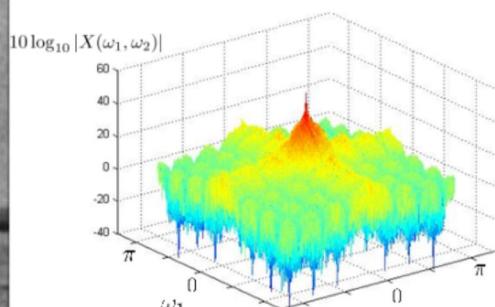
Frequency Domain Filtering



Filtered by 5x5 Filter



Filtered by 7x7 Filter



Noise Smoothing Example



(a) Original image. (b) Original with additive Gaussian noise. (c) Filtered image with a 3x3 average filter. (d) Filtered image with a 5x5 average filter. (e) Filtered image with a 7x7 average filter.

Spatially Adaptive Noise Smoothing

$$y(n_1, n_2) = \left(1 - \frac{\sigma_n^2}{\sigma_{x_l}^2}\right)x(n_1, n_2) + \frac{\sigma_n^2}{\sigma_{x_l}^2}\bar{x}(n_1, n_2)$$

noise variance
mean, average, flat filter
local image variance

$$\sigma_{x_l}^2 = \frac{1}{N} \sum_{(n_1, n_2) \in N} (x(n_1, n_2) - \bar{x}(n_1, n_2))^2$$

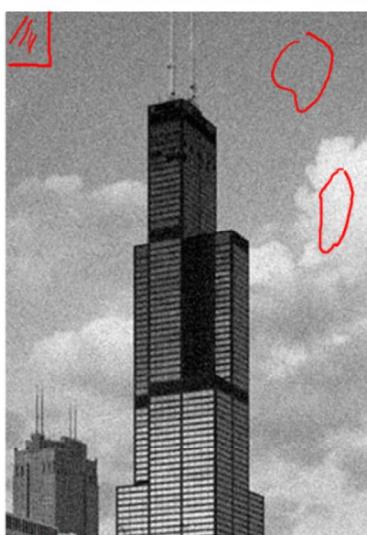
$$\bar{x}(n_1, n_2) = \frac{1}{|N|} \sum_{(n_1, n_2) \in N} x(n_1, n_2)$$

flat
3 \square $|N|=9$

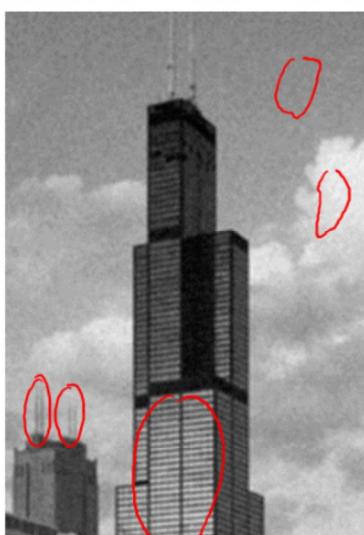
edges: $\sigma_{x_l}^2 > \sigma_n^2 \rightarrow \frac{\sigma_n^2}{\sigma_{x_l}^2} \rightarrow 0 \Rightarrow y(n_1, n_2) = x(n_1, n_2)$

flat area: $\sigma_{x_l}^2 < \sigma_n^2 \rightarrow \frac{\sigma_n^2}{\sigma_{x_l}^2} \approx 1 \Rightarrow y(n_1, n_2) = \bar{x}(n_1, n_2)$

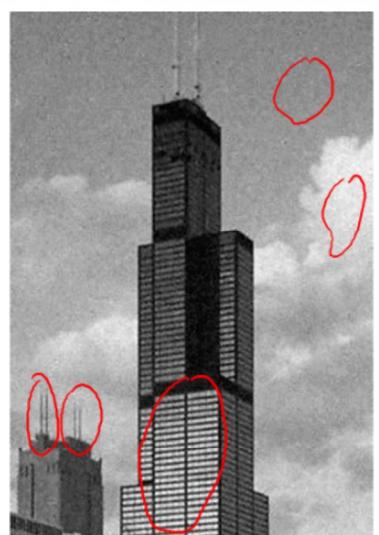
Adaptive Spatial Filtering Example



Noisy image



Filtered image by a 3x3 flat filter



Filtered image by a 3x3 spatially adaptive flat filter

Median Filtering

$$y(n_1, n_2) = \text{median}\{x(n_1 - m_1, n_2 - m_2), (m_1, m_2) \in \mathcal{N}\}$$

Median obtained by sorting all pixels in the analysis window in increasing or decreasing order of amplitudes and picking the middle value if the number of pixels is odd, or the average of the two values in middle if the number of pixels is even.

Properties of median filters

1. Non-linear ~~data drop out / spike~~
2. Good for reducing impulsive (salt and pepper) noise and removing isolated lines and pixels while preserving spatial resolution (reduced blurring) and edges.
3. Poor performance in case of **broadband noise**.
4. 1D median filters have better performance in preserving edges (discontinuities) than 2D median filters.

$x(n_1, n_2) = a$ P_a bipolar \rightarrow salt + pepper

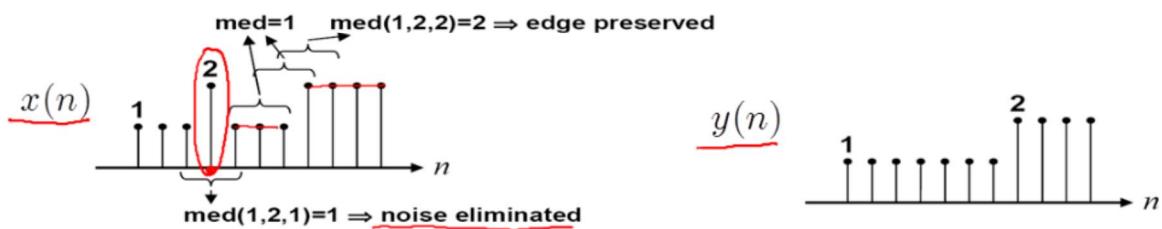
$x(n_1, n_2) = b$ P_b Unipolar \rightarrow salt pepper



1D Median Filtering Example

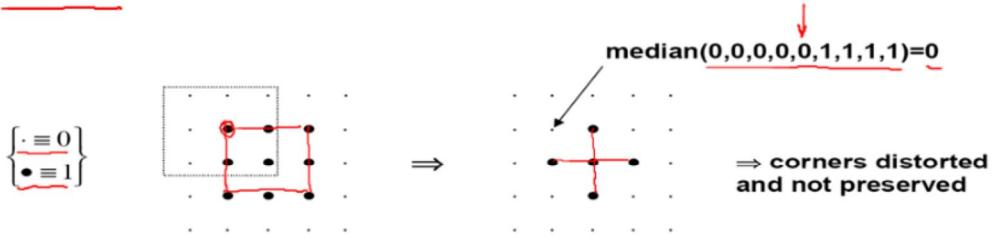
3-point median filter

$$y(n) = \text{median}\{x(n-1), x(n), x(n+1)\}$$



2D Median Filtering Example

- 2D 3x3 median filter



- Since 1D median filter tends to preserve edges of 1D sequences it is preferable to use separable median filtering.
 - Filter image with a vertical 1D median
 - Filter the resulting image with a horizontal 1D median

2D Median Filtering Example



a
b
c
d

(a) Original image. (b) Original with additive salt-and-pepper noise. (c) Filtered image with a 3x3 median filter. (d) Filtered image with a 5x5 median filter.

Noise Reduction Example

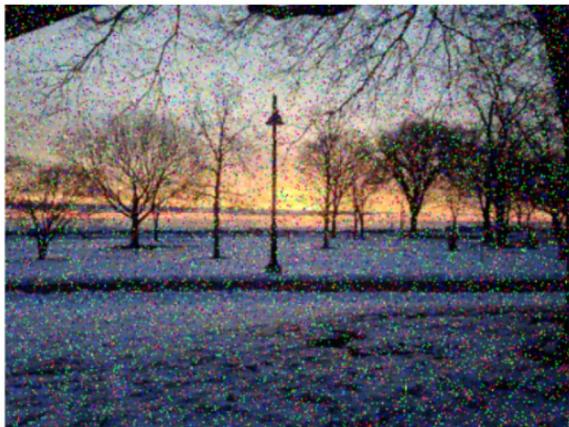


Noisy Image



Gaussian 5x5 Filtering

Noise Reduction Example



Noisy Image



3x3 Median Filtering

Noise Reduction Example



Noisy Image



Gaussian 5x5 Filtering

Noise Reduction Example



Noisy Image



3x3 Median Filtering (pass #1)

Noise Reduction Example



Noisy Image



3x3 Median Filtering (pass #2)

Noise Reduction Example



Noisy Image



3x3 Median Filtering (pass #3)

Order Statistic Filters

Median filter $y(n_1, n_2) = \text{median}_{(m_1, m_2) \in \mathcal{N}} \{x(m_1, m_2)\}$

\mathcal{N} neighborhood centered at (n_1, n_2)

Max filter $y(n_1, n_2) = \max_{(m_1, m_2) \in \mathcal{N}} \{x(m_1, m_2)\}$ **pepper - noise**

Min filter $y(n_1, n_2) = \min_{(m_1, m_2) \in \mathcal{N}} \{x(m_1, m_2)\}$ **salt - noise**

Mid-point filter $y(n_1, n_2) = \frac{1}{2} \left(\max_{(m_1, m_2) \in \mathcal{N}} \{x(m_1, m_2)\} + \min_{(m_1, m_2) \in \mathcal{N}} \{x(m_1, m_2)\} \right)$

Alpha-trimmed mean filter $y(n_1, n_2) = \frac{1}{|\mathcal{N}| - \alpha} \sum_{(m_1, m_2) \in \mathcal{N}} x_r(m_1, m_2)$
 $\alpha = 0$: arithmetic mean
 $\alpha = |\mathcal{N}| - 1$: median

where $x_r(m_1, m_2)$ are the remaining values after we delete the $\frac{\alpha}{2}$ lowest and highest values

Mean Filters

Arithmetic mean filter $y(n_1, n_2) = \frac{1}{|\mathcal{N}|} \sum_{(m_1, m_2) \in \mathcal{N}} x(m_1, m_2)$
 \mathcal{N} neighborhood centered at (n_1, n_2)

Geometric mean filter $y(n_1, n_2) = \left[\prod_{(m_1, m_2) \in \mathcal{N}} x(m_1, m_2) \right]^{\frac{1}{|\mathcal{N}|}}$

Harmonic mean filter $y(n_1, n_2) = |\mathcal{N}| \left[\sum_{(m_1, m_2) \in \mathcal{N}} \frac{1}{x(m_1, m_2)} \right]^{-1}$ Gaussian salt Not pepper

Contra-harmonic mean filter $Q=0$: arithmetic mean $Q > 0$ eliminates pepper salt
 $Q=-1$: harmonic mean $y(n_1, n_2) = \left[\sum_{(m_1, m_2) \in \mathcal{N}} x(m_1, m_2)^{Q+1} \right] \left[\sum_{(m_1, m_2) \in \mathcal{N}} x(m_1, m_2)^Q \right]^{-1}$

Filtering Examples

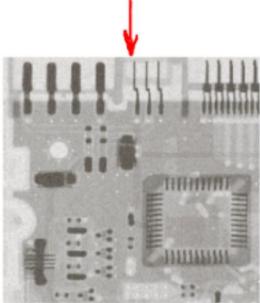


Image corrupted by
additive uniform noise

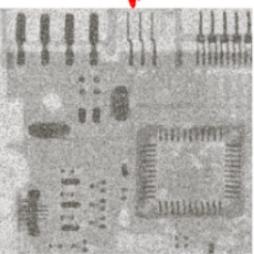
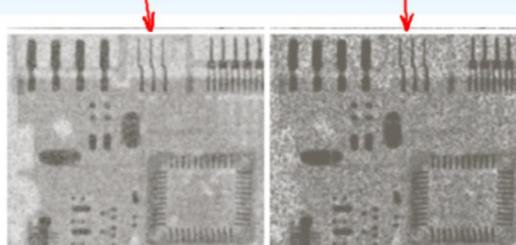
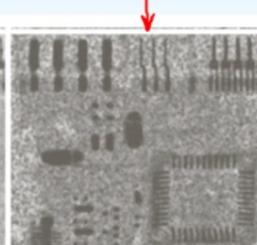


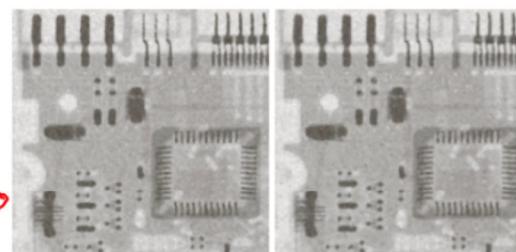
Image corrupted by both
additive uniform noise and
salt-and-pepper noise



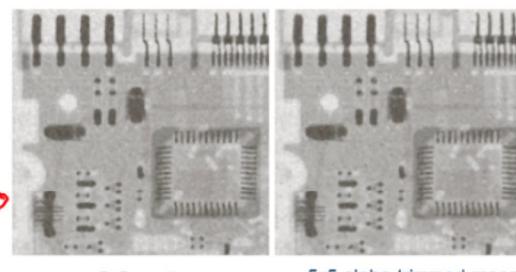
5x5 arithmetic mean



5x5 geometric mean



5x5 median



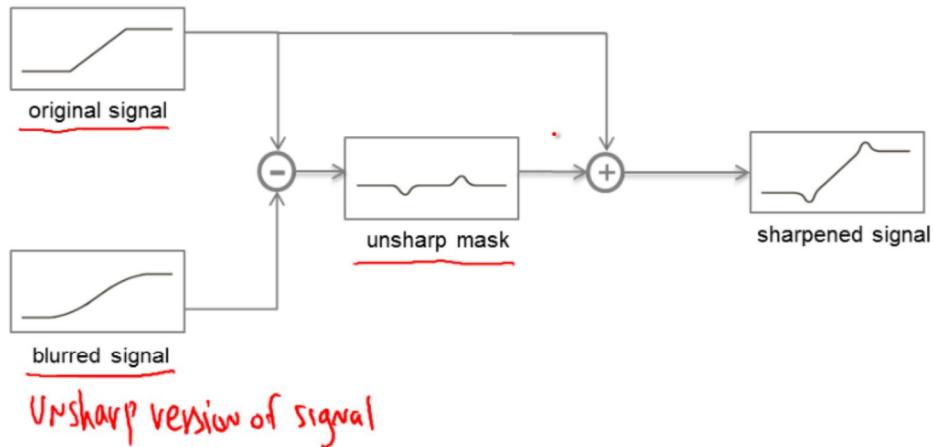
5x5 alpha-trimmed mean
alpha=5

R. C. Gonzalez and R. E. Woods, *Digital Image Processing*, 3rd edition, Pearson Prentice Hall, 2008.

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Unsharp Masking and Highboost Filtering



Unsharp Masking and Highboost Filtering

$$\underline{y_{\text{mask}}(n_1, n_2)} = \underline{x(n_1, n_2)} - \underline{x_L(n_1, n_2)} \quad \text{Unsharp mask}$$

$$\underline{y(n_1, n_2)} = \underline{x(n_1, n_2)} + a\underline{y_{\text{mask}}(n_1, n_2)} = \underline{x_L(n_1, n_2)} + \underbrace{(1+a)x_H(n_1, n_2)}_{\alpha > 1 \text{ highboost filtering}}$$

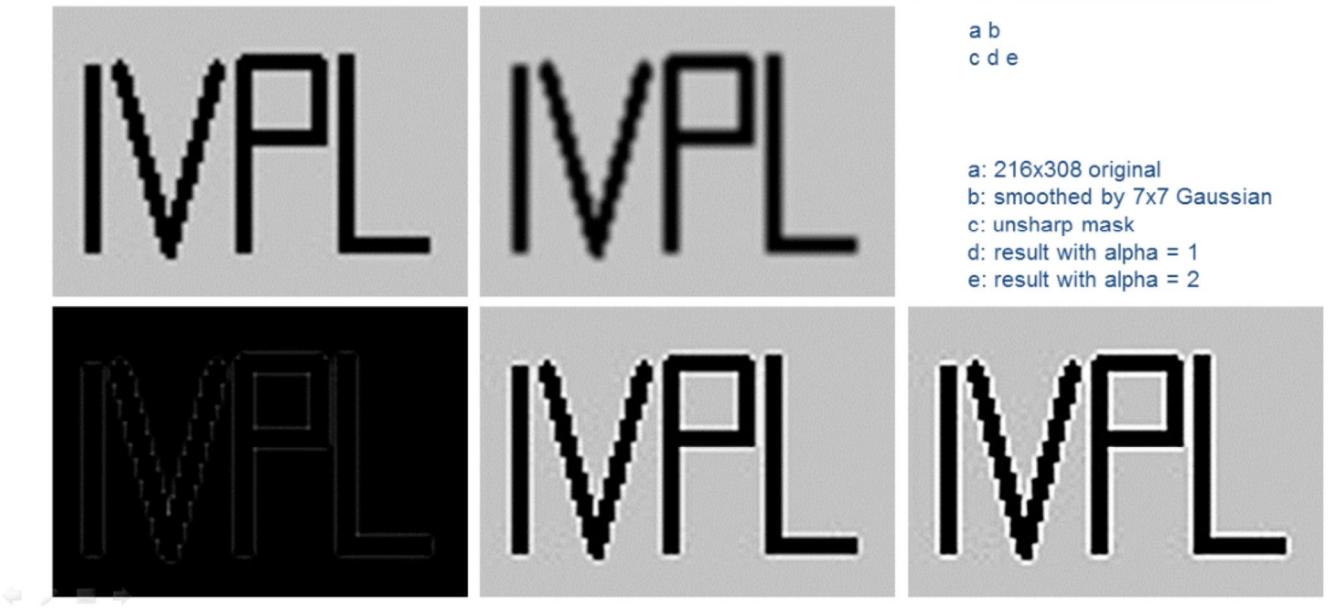
$$x(n_1, n_2) = x_L(n_1, n_2) + x_H(n_1, n_2)$$

$\alpha > 1$ highboost filtering
 $\alpha < 1$ de-emphasizes mask

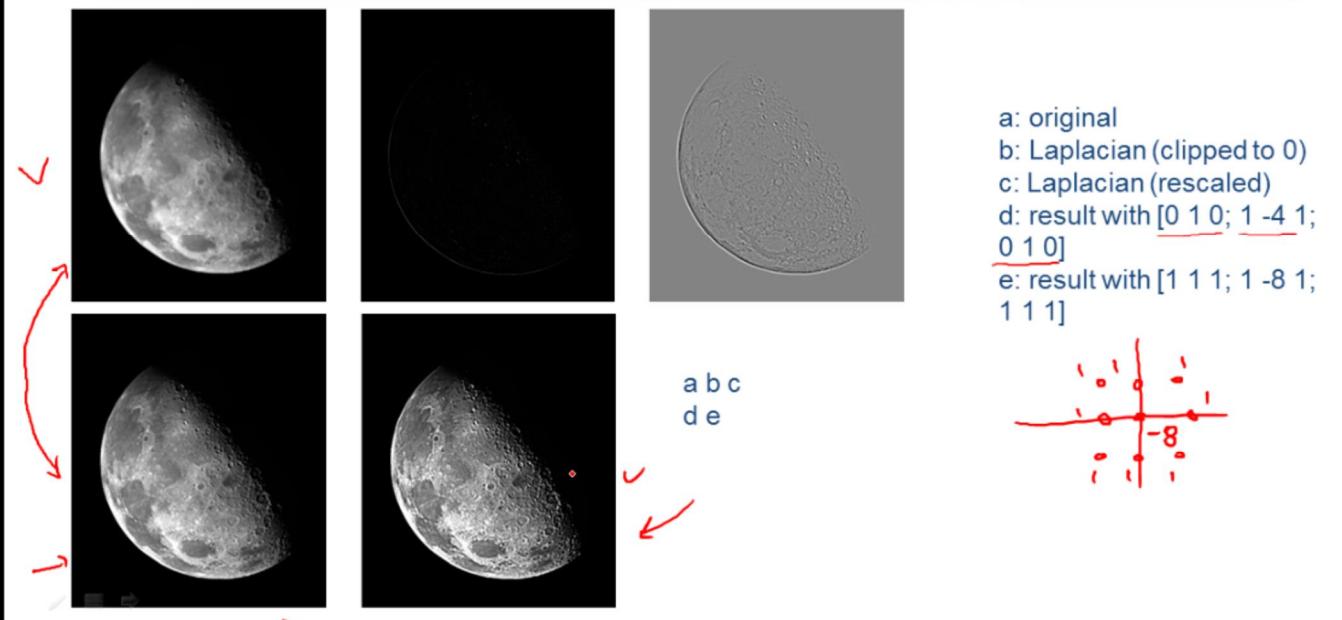


$\alpha = 1$

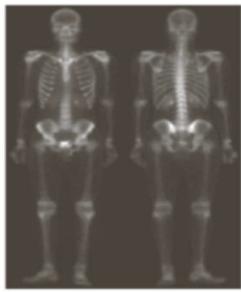
Unsharp Masking



Sharpening Spatial Filters



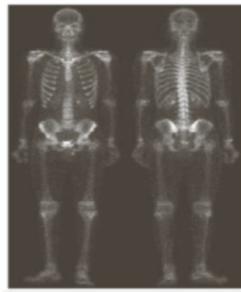
Combining Spatial Enhancement Methods



(a): Whole body bone scan



(b): Laplacian of (a)



(c): (a)+(b)



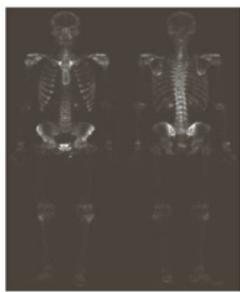
(d) Sobel gradient of (a)

R. C. Gonzalez and R. E. Woods, *Digital Image Processing*, 3rd edition, Pearson Prentice Hall, 2008.

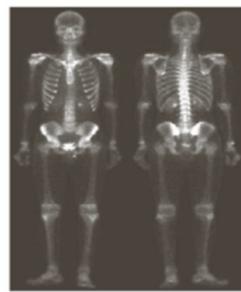
Combining Spatial Enhancement Methods



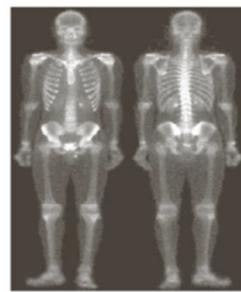
(e) Smoothed Sobel gradient
With a 5x5 average



(f) Product of sharp image (c)
and smoothed Sobel
gradient (e)



(g) Sharp image obtained
By sum of original (a) and (f)



(h) Power law transformation
of (g)

R. C. Gonzalez and R. E. Woods, *Digital Image Processing*, 3rd edition, Pearson Prentice Hall, 2008.

Enhancement Topics

- Point-wise Intensity Transformations
 - Log, Power-law, Piecewise linear
- Histogram Processing
- Spatial Filtering (LSI vs non-linear)
 - Smoothing
 - Sharpening
 - Homomorphic Filtering
- Pseudo-Coloring
- Video Enhancement

Motivation

- **Image with a large dynamic range**, e.g., a natural scene on a bright sunny day, recorded on a **medium with a small dynamic range**, results in image contrast significantly reduced especially in the dark and bright regions
- **Objective: Reduce** dynamic range & increase local contrast **prior** to recording it on medium with a small dynamic range

Image Model

$$x(n_1, n_2) = i(n_1, n_2) \cdot r(n_1, n_2)$$

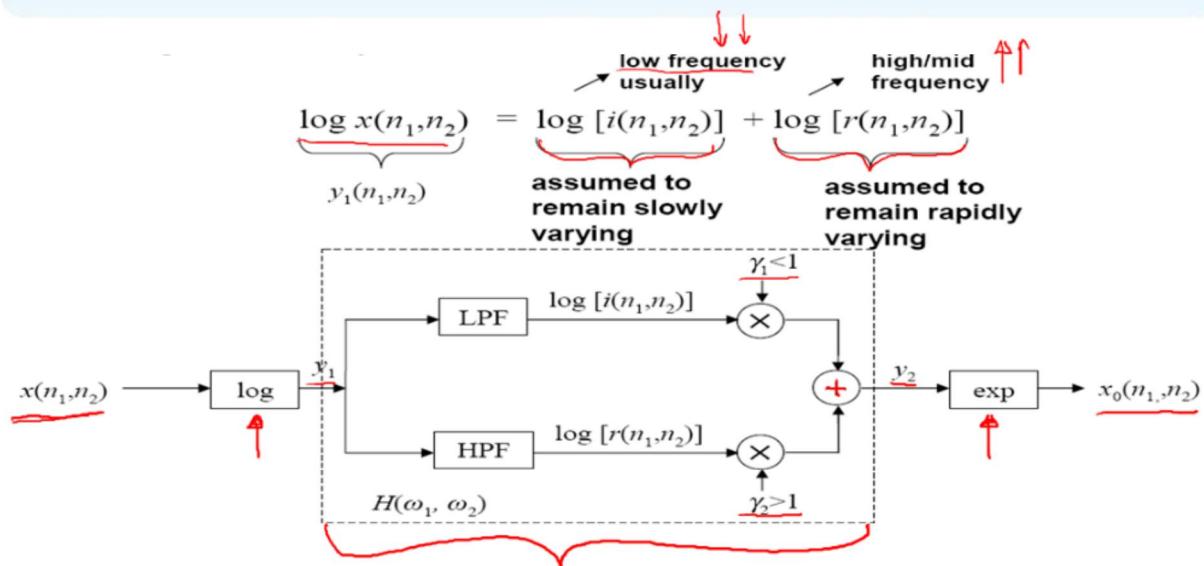
Image formed by recording light reflected from objects which are illuminated by some light source

Illumination: assumed to be slowly varying and main contributor to dynamic range

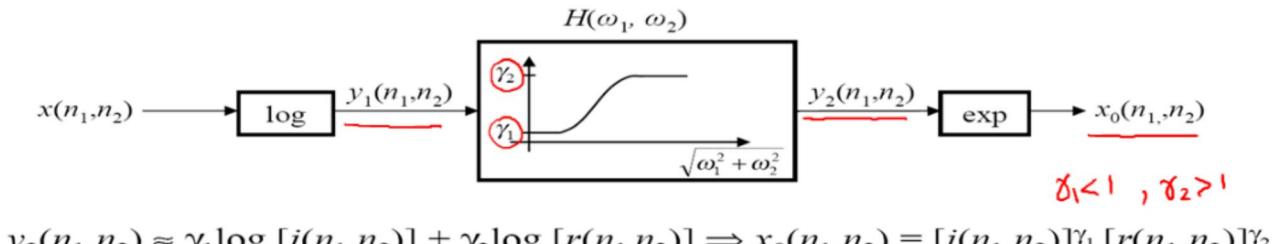
Reflectance: represents details of objects and assumed to vary rapidly and the primary contributor to local contrast

- To decrease dynamic range, decrease $i(n_1, n_2)$
- To increase local contrast, increase $r(n_1, n_2)$

Homomorphic Processing



Homomorphic Processing



$$y_2(n_1, n_2) = \underline{\gamma_1 \log [i(n_1, n_2)]} + \underline{\gamma_2 \log [r(n_1, n_2)]} \Rightarrow x_0(n_1, n_2) = \underline{[i(n_1, n_2)]^{\gamma_1}} \underline{[r(n_1, n_2)]^{\gamma_2}}$$

- Filtering in the log intensity domain
- **Note:** Log intensity domain also considered as a perceptual domain since image intensities appear to be modified at the peripheral level of HVS by some form of nonlinearity such as a logarithmic operation.

Homomorphic Processing Example



Enhancement Topics

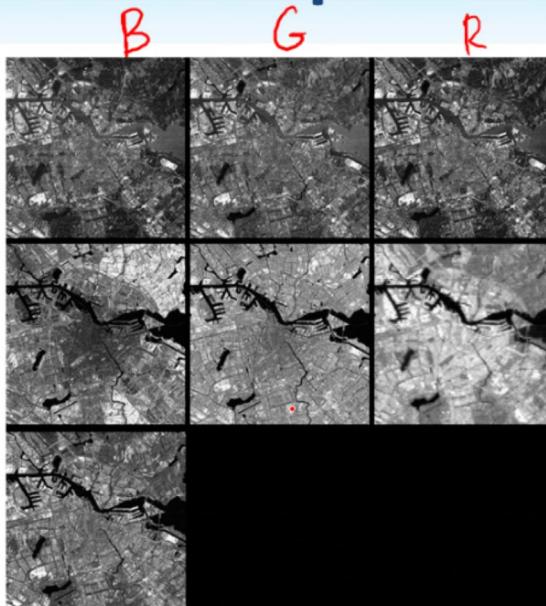
- Point-wise Intensity Transformations
 - Log, Power-law, Piecewise linear
- Histogram Processing
- Spatial Filtering (LSI vs non-linear)
 - Smoothing
 - Sharpening
 - Homomorphic Filtering
- Pseudo-Coloring
- Video Enhancement

Pseudo-Coloring

Reason:

1. Place normal objects in “strange” color for attention
2. Color a normal scene to match the color sensitivity of a human viewer
3. Exploit contrast sensitivity
4. Produce a natural color representation of a set of multi-spectral images of a scene
5. Colorization of black and white images and videos

LANDSAT Multi-Spectral Images



ESA Landsat

LANDSAT Multi-Spectral Images



Bands 1-2-3

Bands 4-3-2

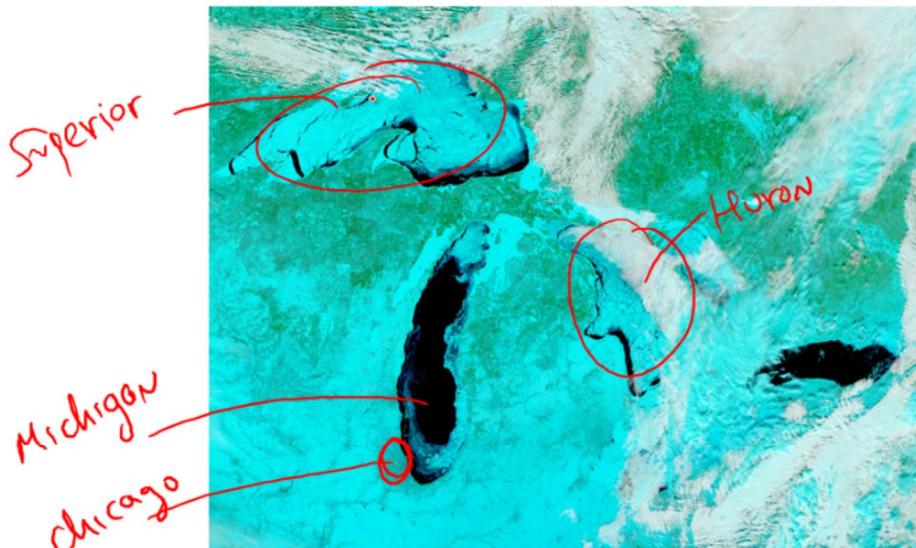


Bands 7-4-2



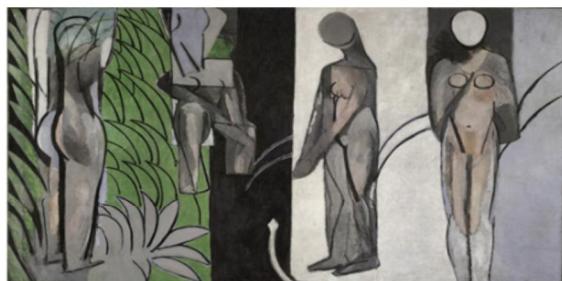
USGS/NASA Landsat

Pseudo-coloring



NASA/Jeff Schmaltz, MODIS Land Rapid Response Team, NASA GSFC

Colorization



Henri Matisse, *Bathers by a River*

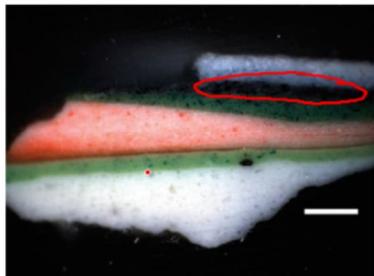
March–May 1909, fall 1909–spring 1910, May–November 1913, early spring–November 1916, January–October (?) 1917.



Druet, Nov. 1913

The Art Institute of Chicago, Charles H. and Mary F. S. Worcester Collection, 1953.158. ©2010 Succession H. Matisse/ Artists Rights Society (ARS), New York.)

Scribbles



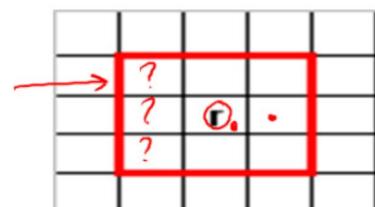
An example of a microscopic cross section at 200x original magnification taken from the white head of the standing figure at farthest right. The dark gray layer that is present between the darker green and light blue relates to the November 1913 campaign documented in Druet's photograph. The thick white layer at the bottom is the ground, or preparation layer, applied on top of the canvas support.

Basic Principle of the Algorithm

- Changes in color correspond in general to changes in intensity
- Create a weighing scheme: assign a pixel **chrominance** based on **chrominance of nearby pixels with similar intensity Y**
- **Minimize (in YUV color space)**

$$J(U) = \sum_{\mathbf{r}} \left(\underline{U(\mathbf{r})} - \sum_{\mathbf{s} \in N(\mathbf{r})} w_{\mathbf{rs}} \underline{U(\mathbf{s})} \right)^2$$

$$w_{\mathbf{rs}} \propto e^{-\underline{(Y(\mathbf{r}) - Y(\mathbf{s}))^2 / 2\sigma_r^2}}$$



$$\underline{\underline{Ax=b}}$$

Druet Colorized



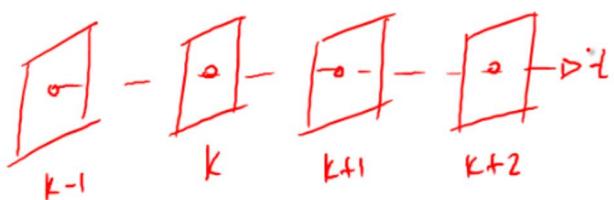
Druet, Nov. 1913



Colorized Druet

Video Enhancement

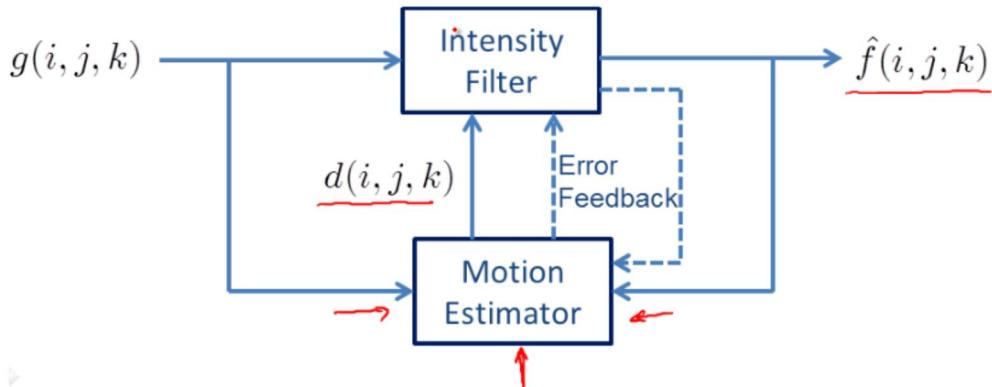
- 2D vs 3D
- Noise Filtering
 - 3D filtering (no ME, motion-dependent, explicit ME)
- Motion Picture/Animation Video Artifact removal



Noise Filtering

- Degradation Model

$$\underline{g(i, j, k)} = \underline{f(i, j, k)} + n(i, j, k)$$



Non-MC Spatio-temporal Filtering

FIR:

$$\hat{f}(\underline{i}, \underline{j}, \underline{k}) = \sum_{(p, q, l) \in S} w(\underline{p}, \underline{q}, \underline{l}) g(\underline{i} - p, \underline{j} - q, \underline{k} - l)$$

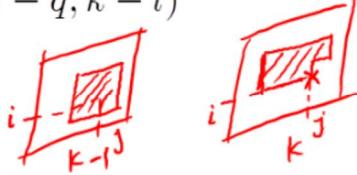
- Average filter
- 3D Wiener
- $w(p, q, l)$ is a function of the spatio-temporal edge

Brailean, J. C., R. P. Kleihorst, S. Efstratiadis, A. K. Katsaggelos, and R. L. Lagendijk, "Noise Reduction Filters for Dynamic Image Sequences: A Review", *IEEE Proceedings*, vol. 83, issue 9, pp. 1272-1292, Sept. 1995.

Non-MC Spatio-temporal Filtering

IIR: $\hat{f}(i, j, k) = [1 - \underline{\alpha}(i, j, k)]\hat{f}_b(i, j, k) + \underline{\alpha}(i, j, k)g(i, j, k)$

$$\hat{f}_b(i, j, k) = \sum_{(p, q, l) \in \underline{\mathcal{S}}} \gamma(p, q, l)\hat{f}(i - p, j - q, k - l)$$



- 3D Kalman Filter
- Order statistics based filters

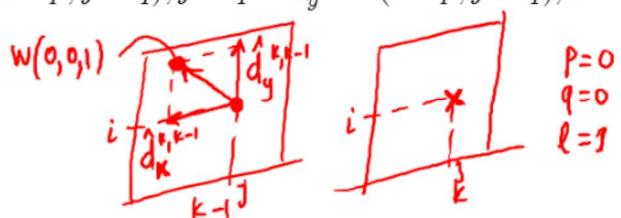
$$\hat{f} = \underline{\text{MEDIAN}}[\underline{\max}(m_1, m_2, m_3, m_4, m_5), g, \underline{\min}(m_1, m_2, m_3, m_4, m_5)]$$



MC Spatio-temporal Filtering

FIR

$$\hat{f}(i, j, k) = \sum_{(p, q, l) \in \underline{\mathcal{S}}} w(p, q, l)g(i - p - \hat{d}_x^{k, k-l}(i - p, j - q), j - q - \hat{d}_y^{k, k-l}(i - p, j - q), k - l)$$



IIR

$$\hat{f}(i, j, k) = [1 - \alpha(i, j, k)]\hat{f}_b(i, j, k) + \alpha(i, j, k)g(i, j, k)$$

with

$$\hat{f}_b(i, j, k) = \sum_{(p, q, l) \in \underline{\mathcal{S}}} \gamma(p, q, l)\hat{f}(i - p - \hat{d}_x^{k, k-l}(i, j), j - q - \hat{d}_y^{k, k-l}(i, j), k - l)$$



Degraded Animation Video



Tom, B., M. G. Kang, M. - C. Hong, and A. K. Katsaggelos, "Detection and Removal of Anomalies in Digitized Animation Film", *Int. Journal of Imaging Systems and Technology*, vol. 9, issue 4, pp. 283-293, 1998.

Enhancement of Motion Pictures

- Blotches (due to dirt, sparkle, film abrasion, scratches and fingerprints on the cellulose surface)
- Intensity flicker (or “boiling effect”)
- Vinegar syndrome

Animation Characteristics

- Large image sizes (Fantasia, 2048x1216 pixels, 36 bits/pixel)
- Large “un-natural” motion
- Scratches, fingerprints, spots
- Duplicated frames and severe illumination changes

Blotch Detection

- They occur only on one frame
- Compute

$$g_k = \frac{1}{2}(f_{k-1} + f_{k+1})$$

$$\underline{\tau_i} = \mu_{d_i} + \eta_i \sigma_{d_i}, \quad i = 1, 2, 3$$

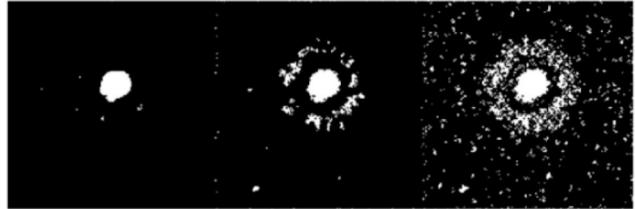
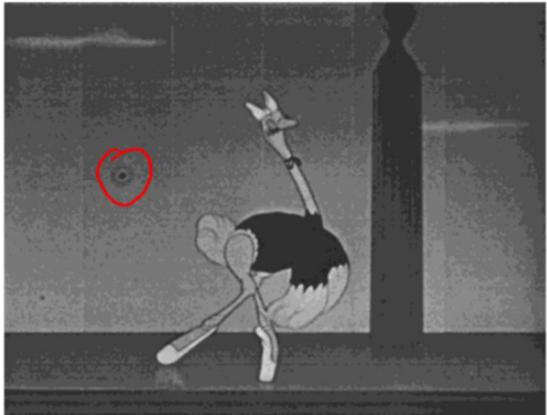
$$d_1 = |g_k - f_k|$$

$$d_2 = |f_{k-1} - f_k|$$

$$d_3 = |f_k - f_{k+1}|$$

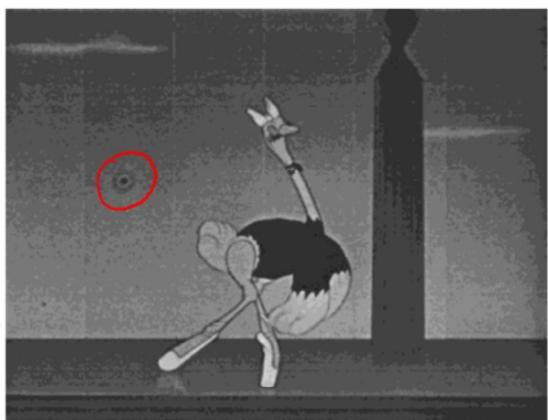
$$b_i(m, n) = \begin{cases} 1, & \text{if } d_i(m, n) \geq \tau_i \\ 0, & \text{if } d_i(m, n) \leq \tau_i \end{cases}$$

Detected Blotches



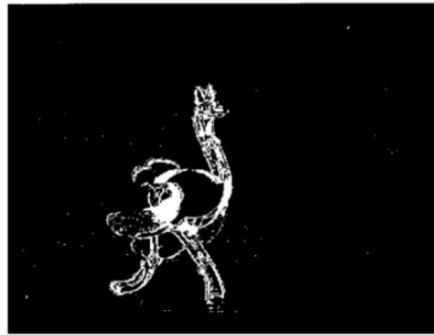
$\eta = 3, 2, 1$

Blotch Removal

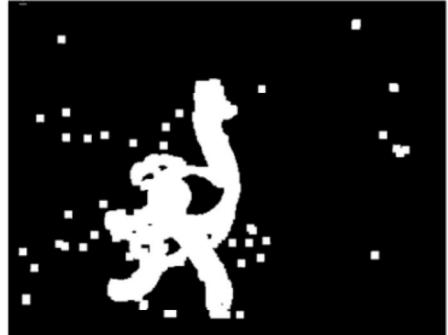


Motion-Dependent Filtering

$$\hat{f}_k(m, n) = \underbrace{(1 - \alpha(\text{mask})) f_k(m, n)}_{\text{original}} + \underbrace{\alpha(\text{mask}) \mu_k(m, n)}_{\text{motion}}$$



mask



expanded mask

NO MOTION $\alpha=1$

MOTION $\alpha=0$

Enhanced Animation Video



Degraded Animation Video

