

# CBU/UU NEUTRINO CRACKER — Module 64 Proof Bundle - Evan Wesley x Vivi The Physics Slayer!

A self-contained mathematical summary of v38–v64

## Executive Summary

Across modules v38–v64 we established, quantified, and cross-stressed a minimal parametric picture that reconciles the observed (toy/profiling-based) *delta-scan* responses with systematic-correlation hypotheses. The key outcomes are:

1. **Correlation-only is mathematically impossible** to reach the observed targets  $d_t$  (v38,v40–v42): even with fully correlated blocks, the ceiling is  $\Delta\chi_{\text{on}}^2 = 15.1748$ , while all targets are  $d_t \ll \Delta\chi_{\text{on}}^2$ .
2. A **Reality Bridge** model—an extra damping factor  $\beta \in (0, 1)$  layered on top of correlated blocks and controlled by a robust-loss fraction  $\alpha_L \in [0, 1]$ —*does* close all targets simultaneously.
3. With a single baseline damping  $\beta_{\text{base}} = 0.829$  (product of mechanism factors) the per-target robust fractions

$$\alpha_L(t) = 1 - \frac{d_t}{\Delta\chi_{\text{on}}^2 \beta_{\text{base}}}$$

reproduce the four targets to within sub-percent rounding.

4. A **single global**  $\alpha_L$  cannot match four distinct  $d_t$  simultaneously if channel totals are preserved; the minimal bounded-drift solution requires an  $\mathcal{O}(0.56)$  fractional capacity band.
5. **Mode asymmetry** (different  $\beta$  for  $\nu$  vs  $\bar{\nu}$ ) is highly degenerate: as long as the *totals* per channel are conserved, a wide range of  $\Delta\beta = \beta_\nu - \beta_{\bar{\nu}}$  is feasible and orthogonal to the core closure.

## 1 Anchors, Notation, and Targets

Let

$$\Delta\chi_{\text{off}}^2 = 29.4931, \quad \Delta\chi_{\text{on}}^2 = 15.1748, \quad \beta_{\text{base}} = 0.829. \quad (1)$$

These “off”/“on” anchors come from the block-correlation stress (v43–v46). The four target combined point-tests (ALL channels at  $\delta \in \{192^\circ, 198^\circ\}$ ) are

$$d_{\text{v38}} = 3.9150, \quad d_{\text{v40}} = 1.2918, \quad d_{\text{v41}} = 1.0980, \quad d_{\text{v42}} = 1.2383. \quad (2)$$

Unless otherwise noted, all  $\Delta\chi^2$  are for the combined four-channel sum.

## 2 Correlation-Only No-Go (v45–v46)

Define a correlation fraction  $f \in [0, 1]$  and correlation-only interpolation

$$\Delta\chi_{\text{corr}}^2(f) = (1 - f) \Delta\chi_{\text{off}}^2 + f \Delta\chi_{\text{on}}^2, \quad f \in [0, 1]. \quad (3)$$

Then  $\Delta\chi_{\text{corr}}^2 \in [\Delta\chi_{\text{on}}^2, \Delta\chi_{\text{off}}^2]$  with *minimum*  $\Delta\chi_{\text{on}}^2$  at  $f = 1$ . For any target  $d$  the correlation-only feasibility requires  $d \geq \Delta\chi_{\text{on}}^2$ . But each observed  $d_t < \Delta\chi_{\text{on}}^2$ , so no  $f$  can satisfy  $\Delta\chi_{\text{corr}}^2(f) = d_t$ .

Therefore, correlation-only is impossible. A convenient diagnostic is the (unphysical)  $f_{\text{corr only}}$  one would need if  $\beta \equiv 1$ :

$$f_{\text{corr only}}(d) = \frac{d - \Delta\chi_{\text{off}}^2}{\Delta\chi_{\text{on}}^2 - \Delta\chi_{\text{off}}^2} \notin [0, 1] \quad \text{for } d < \Delta\chi_{\text{on}}^2. \quad (4)$$

Numerically (v46):  $f_{\text{corr only}} \in \{1.786, 1.970, 1.983, 1.973\}$  for v38,v40,v41,v42 respectively; all are outside  $[0, 1]$ .

### 3 Reality Bridge Model (v47–v55)

We introduce an extra damping factor  $\beta \in (0, 1]$  beyond block correlation and parameterize the *robust* fraction  $\alpha_L \in [0, 1]$  such that

$$\Delta\chi^2(d | \alpha_L) = \Delta\chi_{\text{on}}^2 \beta_{\text{base}} (1 - \alpha_L). \quad (5)$$

Given a target  $d_t$ , the required robust fraction is

$$\alpha_L(t) = 1 - \frac{d_t}{\Delta\chi_{\text{on}}^2 \beta_{\text{base}}}. \quad (6)$$

With  $\beta_{\text{base}} = 0.829$  and  $\Delta\chi_{\text{on}}^2 = 15.1748$  this yields

Tag	$d_t$	$\frac{d_t}{\Delta\chi_{\text{on}}^2 \beta_{\text{base}}}$	$\alpha_L$	$\beta_{\text{tot}} = \beta_{\text{base}}(1 - \alpha_L)$
v38	3.9150	0.3110	0.6890	0.2580
v40	1.2918	0.1030	0.8970	0.0851
v41	1.0980	0.0870	0.9130	0.0724
v42	1.2383	0.0981	0.9019	0.0816

The closure check  $\Delta\chi^2 = \Delta\chi_{\text{on}}^2 \beta_{\text{tot}}$  reproduces all four targets within rounding (v48–v49).

**Mechanistic Decomposition.** One convenient factorization is  $\beta_{\text{tot}} = \beta_{\text{ms}} \beta_{\text{res}} (1 - \alpha_L)$ , where multi-scale ( $\beta_{\text{ms}}$ ) and resolution ( $\beta_{\text{res}}$ ) pieces combine into  $\beta_{\text{base}} = \beta_{\text{ms}} \beta_{\text{res}} = 0.829$  (v47–v48). The precise split is not unique; what matters is the product.

### 4 Mode Asymmetry (v56–v59)

Let channel totals be preserved but allow different  $\beta$  for  $\nu$  and  $\bar{\nu}$ . Define channel weights  $S_\nu^c$  and  $S_{\bar{\nu}}^c$  with  $S_\nu^c + S_{\bar{\nu}}^c = \Delta\chi_{\text{on}}^{2,c}$  and per-channel constraint

$$S_\nu^c \beta_\nu^c + S_{\bar{\nu}}^c \beta_{\bar{\nu}}^c = \beta_{\text{base}} \Delta\chi_{\text{on}}^{2,c}. \quad (7)$$

Let  $\Delta\beta^c \equiv \beta_\nu^c - \beta_{\bar{\nu}}^c$ . Solving (7) with  $\beta \in [0, 1]$  gives a channel-wise feasible interval for  $\Delta\beta^c$ . Intersecting the four channels (v59) produces a *global* window

$$\Delta\beta \in [-0.2736, +0.2631], \quad (8)$$

within which all channels satisfy (7). Because Eq. (7) conserves each channel's total, the Reality Bridge closure (5) is unaffected by the split:  $\alpha_L(t)$  is unchanged for any common  $\Delta\beta$  in (8).

## 5 Single- $\alpha_L$ Impossibility and Bounded-Drift Feasibility (v60–v62)

If one enforces a *single*  $\alpha_L$  for all tags and also preserves totals, Eq. (5) implies a single common prediction

$$d_{\text{common}} = \Delta\chi_{\text{on}}^2 \beta_{\text{base}} (1 - \alpha_L), \quad (9)$$

which cannot equal four distinct  $d_t$  simultaneously (v60). Minimizing the L2 error gives  $(1 - \alpha_L) = (\sum_t d_t)/(4\Delta\chi_{\text{on}}^2 \beta_{\text{base}})$  and leaves nonzero residuals.

Relaxing with a symmetric multiplicative drift  $s_t \in [1 - \varepsilon, 1 + \varepsilon]$  per target, the feasibility condition for a given  $\varepsilon$  is the overlap of intervals

$$X \equiv (1 - \alpha_L) \in \bigcap_t \left[ \frac{d_t}{\mathcal{C}(1 + \varepsilon)}, \frac{d_t}{\mathcal{C}(1 - \varepsilon)} \right], \quad \mathcal{C} \equiv \Delta\chi_{\text{on}}^2 \beta_{\text{base}}. \quad (10)$$

The minimal feasible half-width is  $\varepsilon^* \approx 0.562$  with a consistent choice  $X^* = 0.199256$  ( $\alpha_L^* = 0.800744$ ), yielding drifts  $s_t$  that exactly reconstruct each  $d_t$  (v61–v62). Numerically,

$$s_{\text{v38}} = 1.561861, \quad s_{\text{v40}} = 0.515354, \quad s_{\text{v41}} = 0.438039, \quad s_{\text{v42}} = 0.494011. \quad (11)$$

## 6 Per-Channel and Per-Bin Extensions (v51–v53)

Decomposing into channels  $c$  and bins  $b$  with on-anchors  $\Delta\chi_{\text{on}}^{2,c,b}$ ,

$$d = \sum_{c,b} \Delta\chi_{\text{on}}^{2,c,b} \beta_{\text{base}} (1 - \alpha_L) s_{c,b}. \quad (12)$$

Stress-tests with independent  $\pm 20\%$  jitters on  $\Delta\chi_{\text{on}}^{2,c,b}$  show 100% feasibility for recovering the same  $\alpha_L$  per tag, with small ( $\mathcal{O}(10^{-3})$ ) scatter in the required  $\alpha_L$  (v51–v53).

## 7 Robust Priors and Curvature (v41–v42, v54)

We modeled robust profiling by a convex blend of Gaussian and Laplace penalties. For a generic pull  $x$ ,

$$\rho(x; \alpha) = (1 - \alpha) \frac{x^2}{\sigma^2} + \alpha \frac{|x|}{b}, \quad \alpha \in [0, 1]. \quad (13)$$

Increasing  $\alpha$  (more Laplace) modestly increases the point-test  $\Delta\chi^2$  and improves outlier resilience (v42). The  $\delta$ -curvature per channel is well approximated by

$$\Delta\chi_c^2(\delta) = k_c (\delta - 195^\circ)^2, \quad (14)$$

with  $(k_{\text{CRUST\_NO}}, k_{\text{MANTLE\_NO}}, k_{\text{CRUST\_IO}}, k_{\text{MANTLE\_IO}}) \approx (0.029311, 0.039344, 0.033222, 0.041300)$ , reproducing v40 checkpoints at  $\delta = 192^\circ, 195^\circ, 198^\circ$ .

## 8 Leverage and ROI (v39, v55)

Toy leverage studies indicate that (for modest changes)  $\Delta\chi^2$  grows roughly linearly with exposure  $r$  and approximately inversely with per-bin shape systematics. The most effective single levers were reducing shape systematics (e.g., 5%  $\rightarrow$  1%) followed by exposure gains, consistent across channels.

## Conclusions

- The *No-Go* proof eliminates correlation-only explanations for the observed depths  $d_t$ .
- The *Reality Bridge* with a common  $\beta_{\text{base}}$  and per-target  $\alpha_L(t)$  closes all targets and remains robust under outlier stress and mode asymmetry that conserves channel totals.
- A single  $\alpha_L$  can be made compatible only with substantial ( $\sim 56\%$ ) symmetric capacity drift, tightly quantified by the bounded-drift construction.
- Per-bin/channel decompositions and robust blends do not upset these statements; they clarify how budgets redistribute without altering the required global damping picture.

## Numerical Appendix

### Anchors and Targets

Quantity	Symbol	Value
Off-corr anchor	$\Delta\chi_{\text{off}}^2$	29.4931
On-corr anchor	$\Delta\chi_{\text{on}}^2$	15.1748
Baseline damping	$\beta_{\text{base}}$	0.829
Capacity	$\mathcal{C} = \Delta\chi_{\text{on}}^2 \beta_{\text{base}}$	12.5799
Targets	$d_t$	{3.9150, 1.2918, 1.0980, 1.2383}

### Derived Quantities

Tag	$\alpha_L$	$1 - \alpha_L$	$\beta_{\text{tot}}$	$d_{\text{pred}}$
v38	0.689	0.311	0.2580	3.915
v40	0.897	0.103	0.0851	1.292
v41	0.913	0.087	0.0724	1.098
v42	0.902	0.098	0.0816	1.238

*Note:* All numerical values match the print-first module outputs (v38–v64) up to rounding in the last displayed digit.