

**Problem 1.** Let  $f(x) = 12 - x^2$ . Consider the region bounded by the graph of  $f$  and the  $x$ -axis. Find the maximum area of a rectangle with one side on the  $x$ -axis which can be contained in the region.

**Problem 2.** Estimate  $\sqrt{78}$  as follows. Let  $f(x) = x^2 - 78$ .

- (a) Find the integer  $a$  such that  $a^2$  is the closest perfect square to 78.
- (b) Find the linear function  $L(X)$  which is tangent to  $f(x)$  at the point  $(a, f(a))$ .
- (c) Find  $r$  such that  $L(r) = 0$ .