AP Computer Science — Project 5 - Looping
Dr. Paul Bailey — Tuesday, September 5, 2017

Create one directory called `P5_Looping` to store the `.java` files. Please format the source code using appropriate indentation and all common Java conventions.

The purpose of this project is to practice the material from Savitch sections 4.1 - 4.2.

Create a class `public class Test`, and another class called `public class Program`. Inside the `Program` class, create the `public static void main(String[] args)` method.

You will start by creating various methods, which you should put in the `Test` class. Then write code in the `Program` class to call and test your methods from the `Test` class.

Definition 1. If a and b are integers, we say that a *divides* b, and write $a \mid b$, if there exists an integer k such that $b = ak$.

If $a \mid b$, we say that a is a *factor* of b, and that b is a *multiple* of a.

Program 1. Create a method `public static void mult3or7()` that prints all positive multiples of 3 or 7 which are less than 50, using a while loop.

Program 2. Create a method `public static void mult5or9()` that prints all positive multiples of 5 or 9 which are less than 100, using a for loop.

Program 3. Create a method `public static void squares(int n)` which prints the first n perfect squares, starting with 1.

Program 4. Create a program `public static void primeFactors(int n)` which produces and prints all prime factors of n.

Hint: If you factor out primes as you find them, you do not have to remember or even test if a number is prime. Here is some pseudocode for this:

```
initialize k
while n > 0
    increment k
    while k divides n
        print k
        divide n by k
```

The *Fibonacci sequence* a recursively defined sequence $(F_n)_{n=1}^{\infty}$, given by setting $F_1 = 1$, $F_2 = 1$, and $F_{k+2} = F_k + F_{k+1}$. The numbers F_n are called *Fibonacci numbers*.

The first few Fibonacci numbers are $1, 1, 2, 3, 5, 8, 13, 21, \ldots$. To get the next term in the sequence, add the two previous terms.

Program 5. Create a method `public static void fibonacci(int n)` which prints the first n Fibonacci numbers.

A *Pythagorean triple* is a tuple (a, b, c) of positive integers such that $a^2 + b^2 = c^2$. The Babylonians produced tablets containing tables of Pythagorean triples. It is conjectured that they may have known of the formula to generate such triples: let u and v be any positive integers with $u > v$, and set

- $a = u^2 - v^2$;
- $b = 2uv$;
- $c = u^2 + v^2$.

Then

$$\begin{aligned} a^2 + b^2 &= (u^2 - v^2)^2 + (2uv)^2 \\ &= u^4 - 2u^2v^2 + v^4 + 4u^2v^2 \\ &= u^4 + 2u^2v^2 + v^4 \\ &= (u^2 + v^2)^2 \\ &= c^2. \end{aligned}$$

This proves the first part of the following proposition.

Proposition 1. *Let u, v be positive integers with $u > v$ and set $a = u^2 - v^2$, $b = 2uv$, and $c = u^2 + v^2$. Then (a, b, c) is a Pythagorean triple. Moreover, all Pythagorean triple may be generated in this way.*

These triples are naturally ordered, in increasing order of there u's, then their v's.

Program 6. Create a method `public static void pythagoreanTriples(int n)` which produces and prints the first n Pythagorean triples (that is, starting with the smallest u).

If a and b are positive integers, let $\gcd(a, b)$ denote the greatest common divisor of a and b. A Pythagorean triple (a, b, c) is *primitive* if $\gcd(a, b) = 1$.

Program 7. Add the following method to the `Test` class.

```
public static int gcd(int n, int m)
{
    int r = 0;
    while (r = n % m)
    {
        n = m;
        m = r;
    }
    return m;
}
```

Write code in the `Program` class to test this.

Create a program `public static void primitiveTriples(int n)` which produces and prints the first n primitive Pythagorean triples.