

\sim mean NOT \wedge means AND \vee means OR

\Rightarrow mean IMPLIES \Leftrightarrow means IF AND ONLY IF \oplus means EXCLUSIVE OR

Problem 1. Prove that $(p \Rightarrow q) \Leftrightarrow (\sim p \vee q)$ by filling out this truth table.

p	q	$p \Rightarrow q$	$\sim p$	$\sim p \vee q$	$(p \Rightarrow q) \Leftrightarrow (\sim p \vee q)$
T	T				
T	F				
F	T				
F	F				

Problem 2. Prove that $((p \vee q) \Rightarrow (p \wedge q)) \Leftrightarrow (p \Leftrightarrow q)$ by filling out this truth table.

p	q	$p \vee q$	$p \wedge q$	$(p \vee q) \Rightarrow (p \wedge q)$	$p \Leftrightarrow q$	$((p \vee q) \Rightarrow (p \wedge q)) \Leftrightarrow (p \Leftrightarrow q)$
T	T				T	
T	F				F	
F	T				F	
F	F				T	

Problem 3. Prove that $((p \vee q) \wedge \sim (p \wedge q)) \Leftrightarrow (p \oplus q)$ by filling out this truth table.

p	q	$p \vee q$	$p \wedge q$	$\sim (p \wedge q)$	$(p \vee q) \wedge \sim (p \wedge q)$	$p \oplus q$	$((p \vee q) \wedge \sim (p \wedge q)) \Leftrightarrow (p \oplus q)$
T	T					F	
T	F					T	
F	T					T	
F	F					F	