Create one directory called P7_Looping to store the .java files. Please format the source code using appropriate indentation and all common Java conventions.

The purpose of this project is to practice the material from Savitch sections 4.1 - 4.2.

Create a class public class Utility, and another class called public class Program. Inside the Program class, create the public static void main(String[] args) method.

You will start by creating various methods, which you should put in the Utility class. Then write code in the Program class to call and test your methods from the Utility class.

Definition 1. If a and b are integers, we say that a divides b, and write $a \mid b$, if there exists an integer k such that b = ak.

If $a \mid b$, we say that a is a factor of b, and that b is a multiple of a.

Program 1. Create a method public static void mult3or7() that prints all positive multiples of 3 or 7 which are less than 50, using a while loop.

Program 2. Create a method public static void mult5or9() that prints all positive multiples of 5 or 9 which are less than 100, using a for loop.

Program 3. Create a method public static void squares(int n) which prints the first n perfect squares, starting with 1.

Program 4. Create a program public static void primeFactors(int n) which produces and prints all prime factors of n.

Hint: If you factor out primes as you find them, you do not have to remember or even test if a number is prime. Here is some pseudocode for this:

```
initialize k
while n > 0
    increment k
    while k divides n
        print k
        divide n by k
```

The Fibonacci sequence a recursively defined sequence $(F_n)_{n=1}^{\infty}$, given by setting $F_1 = 1$, $F_2 = 1$, and $F_{k+2} = F_k + F_{k+1}$. The numbers F_n are called Fibonacci numbers.

The first few Fibonacci numbers are $1, 1, 2, 3, 5, 8, 13, 21, \ldots$ To get the next term in the sequence, add the two previous terms.

Program 5. Create a method public static void fibonacci(int n) which prints the first n Fibonacci numbers.

A Pythagorean triple is a tuple (a, b, c) of positive integers such that $a^2 + b^2 = c^2$. The Babylonians produced tablets containing tables of Pythagorean triples. It is conjectured that they may have known of the formula to generate such triples: let u and v be any positive integers with u > v, and set

- $a = u^2 v^2$;
- b = 2uv;
- $c = u^2 + v^2$.

Then

$$a^{2} + b^{2} = (u^{2} - v^{2})^{2} + (2uv)^{2}$$

$$= u^{4} - 2u^{2}v^{2} + v^{4} + 4u^{2}v^{2}$$

$$= u^{4} + 2u^{2}v^{2} + v^{4}$$

$$= (u^{2} + v^{2})^{2}$$

$$= c^{2}.$$

This proves the first part of the following proposition.

Proposition 1. Let u, v be positive integers with u > v and set $a = u^2 - v^2$, b = 2uv, and $c = u^2 + v^2$. Then (a, b, c) is a Pythagorean triple. Moreover, all Pythagorean triple may be generated in this way.

These triples are naturally ordered, in increasing order of there u's, then their v's.

Program 6. Create a method public static void pythagoreanTriples(int n) which produces and prints the first n Pythagorean triples (that is, starting with the smallest u).

If a and b are positive integers, let gcd(a, b) denote the greatest common divisor of a and b. A Pythagorean triple (a, b, c) is primitive if gcd(a, b) = 1.

Program 7. Add the following method to the Utility class.

```
public static int gcd(int n, int m)
{
    int r = 0;
    while (r = n % m)
    {
        n = m;
        m = r;
    }
    return m;
}
```

Write code in the Program class to test this.

Create a program public static void primitive Triples (int n) which produces and prints the first n primitive Pythagorean triples.