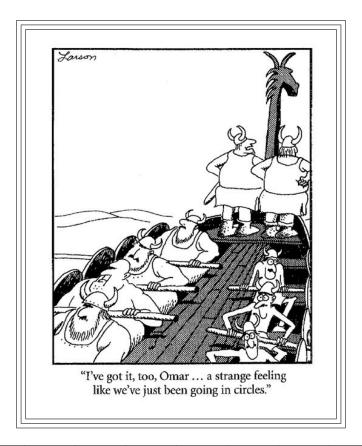
Name:

Algebra II Examination 15 (Test)

Dr. Paul Bailey Thursday, March 31, 2022

The examination contains ten problems which are worth 10 points each, and two bonus problems worth ten points each. All answers must be justified. An appropriate amount of work must be shown of receive credit.



Prob1	Prob2	Prob3	Prob4	Prob5	Prob6	Prob7	Prob8	Prob9	Prob10	Bonus1	Bonus2	Total

Problem 1. (Solving Logarithmic/Rational Equations)

Solve the equation

$$\log_7(x) + \log_7(x - 10) - \log_7(x - 6) = 1.$$

Correctly write the solution set.

Problem 2. Find all $x \in [0, 4\pi]$ such that

$$2\sin(x) = 1.$$

Correctly write the solution set. (Here, x is measured in radians.)

Problem 3. (Finding the Equation of a Line) Let $A = (7, -7)$ and $B = (-3, 13)$. Find slope-intercept form of the equation of the line through A and B .
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Problem 4. (Finding the Equation of a Circle) Let $A = (7, -7)$ and $B = (-3, 13)$. Find the equation of a circle which has \overline{AB} as a diameter.

Problem 5. (Finding Inverses)

Let

$$f(x) = x^2 - 6x - 1.$$

Let g be an inverse function of f. Compute a formula for g(x). State it's domain and range.

Problem 6. (Finding the Domain)

Let

$$f(x) = \frac{\sqrt{x^2 - 8x + 15}}{x^2 - 16}.$$

Find the domain of f. Write your answer as the union of disjoint intervals.

Problem 7. (Factoring Cubics)

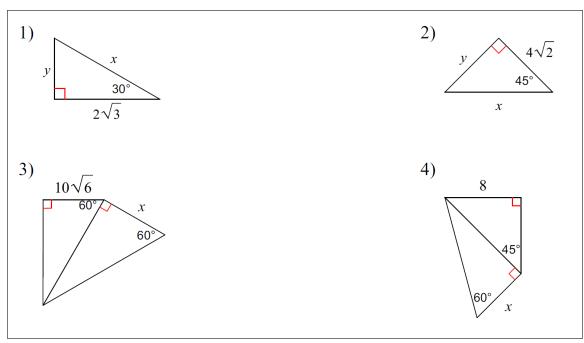
Let

$$f(x) = x^3 - 7x^2 + 11x + 3.$$

Notice that f(3) = 0. Use this to find the other two zeros of f. Write the solution set for the equation f(x) = 0.

Problem 8. (Standard Triangles)

Find x.



Problem 9. (NEW) Thing.

Problem 10. (NEW) Thing.

Problem 11. (Bonus - Lines and Circles)

A line through the origin of slope 2 is tangent to a circle centered at (4,4).

(a) Find the point of tangency.

(b) Write equation of the circle.

Definition 1. Let $f:A\to B$, and let $D\subset B$. The *preimage* of B under f is

$$f^{-1}(D) = \{ a \in A \mid f(a) \in D \}.$$

That is, the preimage of D is the set of all points in the domain which are mapped by f into D.

Problem 12. (Bonus - Preimage)

Let $f: \mathbb{R} \to \mathbb{R}$ be given by $f(x) = 25 - x^2$, where θ is measured in radians. Find the preimage of (9, 16]. Write your answer using correct set notation.