

# Package ‘aldvmm’

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**Title** Adjusted Limited Dependent Variable Mixture Models

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**Description** The goal of the package 'aldvmm' is to fit adjusted limited dependent variable mixture models of health state utilities. Adjusted limited dependent variable mixture models are finite mixtures of normal distributions with an accumulation of density mass at the limits, and a gap between 100% quality of life and the next smaller utility value. The package 'aldvmm' uses the likelihood and expected value functions proposed by Hernandez Alava and Wailoo (2015) <doi:10.1177/1536867X1501500307> using normal component distributions and a multinomial logit model of probabilities of component membership.

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aldvmm-package

*aldvmm: Adjusted Limited Dependent Variable Mixture Models*


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## Description

The goal of the package 'aldvmm' is to fit adjusted limited dependent variable mixture models of health state utilities. Adjusted limited dependent variable mixture models are finite mixtures of normal distributions with an accumulation of density mass at the limits, and a gap between 100% quality of life and the next smaller utility value. The package 'aldvmm' uses the likelihood and expected value functions proposed by Hernandez Alava and Wailoo (2015) <doi:10.1177/1536867X1501500307> using normal component distributions and a multinomial logit model of probabilities of component membership.

## Examples

```
data(utility)

fit <- aldvmm(eq5d ~ age + female | 1,
  data = utility,
  psi = c(0.883, -0.594),
  ncmp = 2)

summary(fit)

yhat <- predict(fit,
  newdata = utility)
```

## Description

The function `aldvmm()` fits adjusted limited dependent variable mixture models of health state utilities. Adjusted limited dependent variable mixture models are finite mixtures of normal distributions with an accumulation of density mass at the limits, and a gap between 100% quality of life and the next smaller utility value. The package `aldvmm` uses the likelihood and expected value functions proposed by Hernandez Alava and Wailoo (2015) using normal component distributions and a multinomial logit model of probabilities of component membership.

## Usage

```
aldvmm(
  formula,
  data,
  psi,
  ncmp = 2,
  dist = "normal",
  optim.method = NULL,
  optim.control = list(trace = FALSE),
  optim.grad = TRUE,
  init.method = "zero",
  init.est = NULL,
  init.lo = NULL,
  init.hi = NULL,
  se.fit = FALSE,
  level = 0.95
)
```

## Arguments

- |         |   |
|---------|---|
| formula | an object of class "formula" with a symbolic description of the model to be fitted. The model formula takes the form $y \sim x_1 + x_2 \mid x_1 + x_4$ , where the $\mid$ delimiter separates the model for expected values of normal distributions (left) and the multinomial logit model of probabilities of component membership (right).        |
| data    | a data frame, list or environment (or object coercible to a data frame by <code>base::as.data.frame()</code> ) including data on outcomes and explanatory variables in 'formula'.   |
| psi     | a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. <code>c(-0.594, 0.883)</code> ). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in 'psi' does not matter. |
| ncmp    | a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.  |

<code>dist</code>	an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to "normal".
<code>optim.method</code>	an optional character value of one of the following <code>optimr::optimr()</code> methods: "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "nllminb", "Rcgmin", "Rvmmmin" and "hjn". The default method is "Nelder-Mead". The method "L-BFGS-B" is used when lower and/or upper constraints are set using 'init.lo' and 'init.hi'. The method "nllm" cannot be used in the 'aldvmm' package.
<code>optim.control</code>	an optional list of <code>optimr::optimr()</code> control parameters.
<code>optim.grad</code>	an optional logical value indicating if a numerical gradient should be used in <code>optimr::optimr()</code> methods that can use this information. The default value is TRUE. If 'optim.grad' is set to FALSE, a finite difference approximation is used.
<code>init.method</code>	an optional character value indicating the method for obtaining initial values. The following values are available: "zero", "random", "constant" and "sann". The default value is "zero".
<code>init.est</code>	an optional numeric vector of user-defined initial values. User-defined initial values override the 'init.method' argument. Initial values have to follow the same order as parameter estimates in the return value 'par'.
<code>init.lo</code>	an optional numeric vector of user-defined lower limits for constrained optimization. When 'init.lo' is not NULL, the optimization method "L-BFGS-B" is used. Lower limits of parameters have to follow the same order as parameter estimates in the return value 'par'.
<code>init.hi</code>	an optional numeric vector of user-defined upper limits for constrained optimization. When 'init.hi' is not NULL, the optimization method "L-BFGS-B" is used. Upper limits of parameters have to follow the same order as parameter estimates in the return value 'par'.
<code>se.fit</code>	an optional logical value indicating whether standard errors of fitted values are calculated. The default value is FALSE.
<code>level</code>	a numeric value of the significance level for confidence bands of fitted values. The default value is 0.95.

## Details

`aldvmm()` fits an adjusted limited dependent variable mixture model using the likelihood and expected value functions from Hernandez Alava and Wailoo (2015). The model accounts for latent classes, multi-modality, minimum and maximum utility values and potential gaps between 1 and the next smaller utility value. Adjusted limited dependent variable mixture models combine multiple component distributions with a multinomial logit model of the probabilities of component membership. The standard deviations of normal distributions are estimated and reported as log-transformed values which enter the likelihood function as exponentiated values to ensure non-negative values.

The minimum utility and the largest utility smaller than or equal to 1 are supplied in the argument 'psi'. The number of distributions/components that are mixed is set by the argument 'ncmp'. When 'ncmp' is set to 1 the procedure estimates a tobit model with a gap between 1 and the maximum utility value in 'psi'. The current version only allows finite mixtures of normal distributions.

The 'formula' object can include a | delimiter to separate formulae for expected values in components (left) and the multinomial logit model of probabilities of group membership (right). If no | delimiter is used, the same formula will be used for expected values in components and the multinomial logit of the probabilities of component membership.

`aldvmm()` uses `optimr::optimr()` for maximum likelihood estimation of model parameters. The argument `'optim.method'` accepts the following methods: "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "nllminb", "Rcgmin", "Rvmmmin" and "hjn". The default method is "Nelder-Mead". The method "nllm" cannot be used in `aldvmm()` because it requires a different implementation of the likelihood function. The argument `'optim.control'` accepts a list of `optimr::optimr()` control parameters. If `'optim.grad'` is set to TRUE the function `optimr::optimr()` uses numerical gradients during the optimization procedure for all methods that allow for this approach. If `'optim.grad'` is set to FALSE or a method cannot use gradients, a finite difference approximation is used. The numerical gradients of the likelihood function are approximated numerically using the function `numDeriv::grad()`. The hessian matrix at maximum likelihood parameters is approximated numerically using `numDeriv::hessian()`.

`'init.method'` accepts four values of methods for generating initial values: "zero", "random", "constant", "sann". The method "zero" sets initial values of all parameters to 0. The method "random" draws random starting values from a standard normal distribution. The method "constant" estimates a constant-only model and uses estimates as initial values of intercepts and standard errors and 0 for all other parameters. The method "sann" estimates the full model using the simulated annealing optimization method in `stats::optim()` and uses parameter estimates as initial values. When user-specified initial values are supplied in `'init.est'`, the argument `'init.method'` is ignored.

By default, `aldvmm()` performs unconstrained optimization with upper and lower limits at  $-\text{Inf}$  and  $\text{Inf}$ . When user-defined lower and upper limits are supplied to `'init.lo'` and/or `'init.hi'`, these default limits are replaced with the user-specified values, and the method "L-BFGS-B" is used for box-constrained optimization instead of the user defined `'optim.method'`. It is possible to only set either maximum or minimum limits.

If `'se.fit'` is set to TRUE, standard errors of fitted values are calculated using the delta method. The standard errors of fitted values in the estimation data set are calculated as  $se_{fit} = \sqrt{G^t \Sigma G}$ , where  $G$  is the gradient of a fitted value with respect to changes of parameter estimates, and  $\Sigma$  is the estimated covariance matrix of parameters (Dowd et al., 2014). The standard errors of predicted values in new data sets are calculated as  $se_{pred} = \sqrt{MSE + G^t \Sigma G}$ , where  $MSE$  is the mean squared error of fitted versus observed outcomes in the original estimation data (Whitmore, 1986).

## Value

`aldvmm()` returns an object of class inheriting from "aldvmm". An object of class "aldvmm" is a list containing the following objects.

<code>coef</code>	a numeric vector of parameter estimates.
<code>se</code>	a numeric vector of standard errors of parameter estimates.
<code>z</code>	a numeric vector of standardized parameter estimates.
<code>p</code>	a numeric vector of p-values of parameter estimates.
<code>lower</code>	a numeric vector of 95% lower confidence limits of parameter estimates.
<code>upper</code>	a numeric vector of 95% upper confidence limits of parameter estimates.
<code>hessian</code>	a numeric matrix object with second partial derivatives of the likelihood function.
<code>cov</code>	a numeric matrix object with covariances of parameters.
<code>n</code>	a scalar representing the number of complete observations with no missing values that were used in the estimation.
<code>k</code>	a scalar representing the number of components that were mixed.
<code>gof</code>	a list including the following elements.

	ll	a numeric value of the negative log-likelihood $-ll$ .
	aic	a numeric value of the Akaike information criterion $AIC = 2n_{par} - 2ll$ .
	bic	a numeric value of the Bayesian information criterion $BIC = n_{par} * \log(n_{obs}) - 2ll$ .
	mse	a numeric value of the mean squared error $\sum (y - \hat{y})^2 / (n_{obs} - n_{par})$ .
	mae	a numeric value of the mean absolute error $\sum  y - \hat{y}  / (n_{obs} - n_{par})$ .
pred		a list including the following elements.
	y	a numeric vector of observed outcomes in 'data'.
	yhat	a numeric vector of fitted values.
	res	a numeric vector of residuals.
	se.fit	a numeric vector of the standard error of fitted values.
	lower.fit	a numeric vector of 95% lower confidence limits of fitted values.
	upper.fit	a numeric vector of 95% upper confidence limits of fitted values.
	prob	a numeric vector expected values of the probabilities of group membership.
init		a list including the following elements.
	est	a numeric vector of initial parameter estimates.
	lo	a numeric vector of lower limits of parameter estimates.
	hi	a numeric vector of upper limits of parameter estimates.
formula		an object of class <code>stats::formula</code> supplied to argument 'formula'.
psi		a numeric vector with the minimum and maximum utility below 1 in 'data'.
dist		a character value indicating the used distribution.
label		a list including the following elements.
	lcoef	a character vector of labels for objects including results on distributions (default "beta") and the probabilities of component membership (default "delta").
	lcp	a character vector of labels for objects including constant distribution parameters (default "sigma" for <code>dist = "normal"</code> ).
	lcmp	a character value of the label for objects including results on different components (default "Comp")
	lvar	a list including 2 character vectors of covariate names for model parameters of distributions ("beta") and the multinomial logit ("delta").
optim.method		a character value of the used <code>optimr::optimr()</code> method.

The generic function `base::summary()` can be used to obtain or print a summary of the results. The generic function `stats::predict()` can be used to obtain predicted values and standard errors of predictions in new data.

## References

- Alava, M. H. and Wailoo, A. (2015) Fitting adjusted limited dependent variable mixture models to EQ-5D. *The Stata Journal*, **15**(3), 737–750. doi:[10.1177/1536867X1501500307](https://doi.org/10.1177/1536867X1501500307)
- Dowd, B. E., Greene, W. H., and Norton, E. C. (2014) Computation of standard errors. *Health services research*, **49**(2), 731–750. doi:[10.1111/14756773.12122](https://doi.org/10.1111/14756773.12122)
- Whitmore, G. A. (1986) Prediction limits for a univariate normal observation. *The American Statistician*, **40**(2), 141–143. doi:[10.1080/00031305.1986.10475378](https://doi.org/10.1080/00031305.1986.10475378)

**Examples**

```
data(utility)

fit <- aldvmm(eq5d ~ age + female | 1,
              data = utility,
              psi = c(0.883, -0.594),
              ncmp = 2)

summary(fit)

yhat <- predict(fit,
                 newdata = utility)
```

aldvmm.check

*Checking the Validity of Objects Supplied to aldvmm()***Description**

aldvmm.check() runs validity checks of objects supplied to aldvmm().

**Usage**

```
aldvmm.check(
  formula,
  data,
  psi,
  ncmp,
  dist,
  lcoef,
  lcpair,
  lcmap,
  init.method,
  optim.method,
  optim.grad,
  init.est,
  init.lo,
  init.hi,
  optim.control,
  se.fit,
  level
)
```

**Arguments**

formula	an object of class "formula" with a symbolic description of the model to be fitted. The model formula takes the form $y \sim x_1 + x_2 \mid x_1 + x_4$ , where the $\mid$ delimiter separates the model for expected values of normal distributions (left) and the multinomial logit model of probabilities of component membership (right).
data	a data frame, list or environment (or object coercible to a data frame by <code>base::as.data.frame()</code> ) including data on outcomes and explanatory variables in 'formula'.

psi	a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. <code>c(-0.594, 0.883)</code> ). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in 'psi' does not matter.
ncmp	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.
dist	an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to "normal".
lcoef	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
lcpa	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpa' depends on the distribution supplied to 'dist'.
lcmp	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by <code>summary.aldvmm()</code> .
init.method	an optional character value indicating the method for obtaining initial values. The following values are available: "zero", "random", "constant" and "sann". The default value is "zero".
optim.method	an optional character value of one of the following <code>optimr::optimr()</code> methods: "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "nlminb", "Rcgmin", "Rvmin" and "hjn". The default method is "Nelder-Mead". The method "L-BFGS-B" is used when lower and/or upper constraints are set using 'init.lo' and 'init.hi'. The method "nlm" cannot be used in the 'aldvmm' package.
optim.grad	an optional logical value indicating if a numerical gradient should be used in <code>optimr::optimr()</code> methods that can use this information. The default value is TRUE. If 'optim.grad' is set to FALSE, a finite difference approximation is used.
init.est	an optional numeric vector of user-defined initial values. User-defined initial values override the 'init.method' argument. Initial values have to follow the same order as parameter estimates in the return value 'par'.
init.lo	an optional numeric vector of user-defined lower limits for constrained optimization. When 'init.lo' is not NULL, the optimization method "L-BFGS-B" is used. Lower limits of parameters have to follow the same order as parameter estimates in the return value 'par'.
init.hi	an optional numeric vector of user-defined upper limits for constrained optimization. When 'init.hi' is not NULL, the optimization method "L-BFGS-B" is used. Upper limits of parameters have to follow the same order as parameter estimates in the return value 'par'.
optim.control	an optional list of <code>optimr::optimr()</code> control parameters.
se.fit	an optional logical value indicating whether standard errors of fitted values are calculated. The default value is FALSE.
level	a numeric value of the significance level for confidence bands of fitted values. The default value is 0.95.



**Details**

`aldvmm.check()` checks the validity of arguments of `aldvmm()`.

**Value**

`aldvmm.check` returns warnings or stops the execution of `aldvmm()` if validity checks fail.

aldvmm.cv

*Numerical Approximation of Covariance Matrix***Description**

`aldvmm.cv()` performs a numerical approximation of the covariance matrix of parameter estimates.

**Usage**

```
aldvmm.cv(ll, par, X, y, dist, psi, ncmp, lcoef, lcpair, lcmp, optim.method)
```

**Arguments**

<code>ll</code>	a function returning the negative log-likelihood of the adjusted limited dependent variable mixture model as a scalar result ( <code>aldvmm.ll()</code> ).
<code>par</code>	a named numeric vector of parameter values.
<code>X</code>	a list of design matrices returned by <code>aldvmm.mm()</code> . 'X' is of length 2 and includes a design matrix for the model of component distributions and a design matrix for the model of probabilities of group membership.
<code>y</code>	a numeric vector of observed outcomes from complete observations in 'data' supplied to <code>aldvmm()</code> .
<code>dist</code>	an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to "normal".
<code>psi</code>	a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. <code>c(-0.594, 0.883)</code> ). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in 'psi' does not matter.
<code>ncmp</code>	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.
<code>lcoef</code>	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
<code>lcpair</code>	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpair' depends on the distribution supplied to 'dist'.
<code>lcmp</code>	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by <code>summary.aldvmm()</code> .

`optim.method` an optional character value of one of the following `optimr::optimr()` methods: "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "nlminb", "Rcgmin", "Rvmin" and "hjn". The default method is "Nelder-Mead". The method "L-BFGS-B" is used when lower and/or upper constraints are set using 'init.lo' and 'init.hi'. The method "nlm" cannot be used in the 'aldvmm' package.

## Details

`aldvmm.cv()` uses `numDeriv::hessian()` to calculate the hessian matrix of the log-likelihood function supplied to 'll' at parameter values supplied to 'par'.

## Value

`aldvmm.cv` returns a list with the following objects.

<code>hessian</code>	a numeric matrix with second-order partial derivatives of the likelihood function 'll'.
<code>cv</code>	a numeric matrix with covariances/variances of parameters in 'par'.
<code>se</code>	a numeric vector of standard errors of parameters in 'par'.
<code>z</code>	a numeric vector of z-values of parameters in 'par'.
<code>p</code>	a numeric vector of p-values of parameter estimates.
<code>upper</code>	a numeric vector of upper 95% confidence limits of parameter estimates in 'par'.
<code>lower</code>	a numeric vector of lower 95% confidence limits of parameter estimates in 'par'.

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<code>aldvmm.getnames</code>	<i>Creating Names of Parameter Vectors</i>
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## Description

`aldvmm.getnames()` creates names of parameter vectors used in `aldvmm()`. The order of the elements in 'lcoef' and 'lcpa' determines the order of parameters and the structure of summary tables returned by `summary.aldvmm()`.

## Usage

```
aldvmm.getnames(X, names, lcoef, lcpa, lcmp, ncmp)
```

## Arguments

<code>X</code>	a list of design matrices returned by <code>aldvmm.mm()</code> . 'X' is of length 2 and includes a design matrix for the model of component distributions and a design matrix for the model of probabilities of group membership.
<code>names</code>	a character vector of names of considered elements (distributions "beta", multinomial logit "delta" or constant distribution parameters, i.e. "lnsigma"). The elements in 'names' are combined with covariate names in 'X' and component labels in 'lcmp' to create a vector of names of parameter vectors.

lcoef	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
lcpair	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpair' depends on the distribution supplied to 'dist'.
lcmp	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by summary.aldvmm().
ncmp	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.

### Value

a character vector of names of parameter vectors used in aldvmm().

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aldvmm.getpar	<i>Extracting Parameters from Parameter Vector into Nested List.</i>
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### Description

aldvmm.getpar() extracts parameters from parameter vectors into nested lists.

### Usage

```
aldvmm.getpar(par, lcoef, lcmp, lcpair, ncmp)
```

### Arguments

par	a named numeric vector of parameter values.
lcoef	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
lcmp	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by summary.aldvmm().
lcpair	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpair' depends on the distribution supplied to 'dist'.
ncmp	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.

### Details

aldvmm.getpar() identifies parameters that belong to coefficients of component distributions (label "beta"), coefficients of the multinomial logit model of probabilities of component membership (label "delta"), constant parameters of component distributions (label "lnsigma" for dist=="normal"), and 1:K components (labels "Comp1" ... "CompK") based on parameter names generated by aldvmm.getnames().

**Value**

a named nested list with parameter vectors for "beta", "delta" and "lnsigma" within all 1:K components. The names of the list correspond to the labels in 'lcoef', 'lcpa' and 'lcmp'.

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aldvmm.gof	<i>Calculating Goodness of Fit Measures</i>
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**Description**

aldvmm.gof() calculates residual- and likelihood-based goodness of fit measures.

**Usage**

```
aldvmm.gof(res, par, ll)
```

**Arguments**

res	a numeric vector of residuals of all observations in the estimation data.
par	a named numeric vector of parameter estimates.
ll	a numeric value of the log-likelihood.

**Details**

aldvmm.gof() calculates mean squared errors as  $MSE = \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n-k}$ , and mean absolute errors as  $MAE = \frac{\sum_{i=1}^n |y_i - \hat{y}_i|}{n-k}$ , where  $y_i$  denotes observed outcomes,  $\hat{y}_i$  denotes fitted values,  $n$  denotes the sample size, and  $k$  denotes the number of parameters. The Akaike information criterion is calculated as  $2k - 2ll$ , and the Bayesian information criterion is calculated as  $k \log(n) - 2ll$ , where  $ll$  denotes the log-likelihood.

**Value**

aldvmm.gof() returns a list including the following objects.

mse	a numeric value of the mean squared error of observed versus fitted outcomes.
mae	a numeric value of the mean absolute error of observed versus fitted outcomes.
ll	a numeric value of the negative log-likelihood.
aic	a numeric value of the Akaike information criterion.
bic	a numeric value of the Bayesian information criterion.

aldvmm.gr

*Calculating Numeric Gradients of the Negative Log-Likelihood***Description**

`aldvmm.gr()` calculates numerical gradients of the negative log-likelihood returned by `aldvmm.ll()` with respect to parameter values in `'par'`.

**Usage**

```
aldvmm.gr(par, X, y, psi, dist, ncmp, lcoef, lcmp, lcpair, optim.method)
```

**Arguments**

<code>par</code>	a named numeric vector of parameter values.
<code>X</code>	a list of design matrices returned by <code>aldvmm.mm()</code> . <code>'X'</code> is of length 2 and includes a design matrix for the model of component distributions and a design matrix for the model of probabilities of group membership.
<code>y</code>	a numeric vector of observed outcomes from complete observations in <code>'data'</code> supplied to <code>aldvmm()</code> .
<code>psi</code>	a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. <code>c(-0.594, 0.883)</code> ). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in <code>'psi'</code> does not matter.
<code>dist</code>	an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to <code>"normal"</code> .
<code>ncmp</code>	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in <code>'psi'</code> .
<code>lcoef</code>	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default <code>"beta"</code> ) and coefficients of probabilities of component membership (default <code>"delta"</code> ).
<code>lcmp</code>	a character value representing a stub (default <code>"Comp"</code> ) for labeling objects including regression coefficients in different components (e.g. <code>"Comp1"</code> , <code>"Comp2"</code> , ...). This label is also used in summary tables returned by <code>summary.aldvmm()</code> .
<code>lcpair</code>	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of <code>'lcpair'</code> depends on the distribution supplied to <code>'dist'</code> .
<code>optim.method</code>	an optional character value of one of the following <code>optimr::optimr()</code> methods: <code>"Nelder-Mead"</code> , <code>"BFGS"</code> , <code>"CG"</code> , <code>"L-BFGS-B"</code> , <code>"nllminb"</code> , <code>"Rcgmin"</code> , <code>"Rvmin"</code> and <code>"hjn"</code> . The default method is <code>"Nelder-Mead"</code> . The method <code>"L-BFGS-B"</code> is used when lower and/or upper constraints are set using <code>'init.lo'</code> and <code>'init.hi'</code> . The method <code>"nllm"</code> cannot be used in the <code>'aldvmm'</code> package.

**Details**

`aldvmm.gr()` uses `numDeriv::grad()` to perform numerical approximation of gradients of the negative log-likelihood returned by `aldvmm.ll()`.

**Value**

a named numeric vector of first derivatives of the negative log-likelihood of the data with respect to parameters in 'par'.

---

aldvmm.init

*Creating Initial Values*


---

**Description**

aldvmm.init() creates initial values for the minimization of the negative log-likelihood returned by aldvmm.ll() using optimr::optimr().

**Usage**

```
aldvmm.init(
  X,
  y,
  psi,
  ncmp,
  dist,
  init.method,
  init.est,
  init.lo,
  init.hi,
  optim.method,
  optim.control = list(),
  optim.grad = TRUE,
  lcoef,
  lcpa,
  lcma
)
```

**Arguments**

- |      |   |
|------|---|
| X    | a list of design matrices returned by aldvmm.mm(). 'X' is of length 2 and includes a design matrix for the model of component distributions and a design matrix for the model of probabilities of group membership.   |
| y    | a numeric vector of observed outcomes from complete observations in 'data' supplied to aldvmm().  |
| psi  | a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. c(-0.594, 0.883)). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in 'psi' does not matter. |
| ncmp | a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.  |
| dist | an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to "normal".   |

<code>init.method</code>	an optional character value indicating the method for obtaining initial values. The following values are available: "zero", "random", "constant" and "sann". The default value is "zero".
<code>init.est</code>	an optional numeric vector of user-defined initial values. User-defined initial values override the 'init.method' argument. Initial values have to follow the same order as parameter estimates in the return value 'par'.
<code>init.lo</code>	an optional numeric vector of user-defined lower limits for constrained optimization. When 'init.lo' is not NULL, the optimization method "L-BFGS-B" is used. Lower limits of parameters have to follow the same order as parameter estimates in the return value 'par'.
<code>init.hi</code>	an optional numeric vector of user-defined upper limits for constrained optimization. When 'init.hi' is not NULL, the optimization method "L-BFGS-B" is used. Upper limits of parameters have to follow the same order as parameter estimates in the return value 'par'.
<code>optim.method</code>	an optional character value of one of the following <code>optimr::optimr()</code> methods: "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "nllminb", "Rcgmin", "Rvmmmin" and "hjn". The default method is "Nelder-Mead". The method "L-BFGS-B" is used when lower and/or upper constraints are set using 'init.lo' and 'init.hi'. The method "nlm" cannot be used in the 'aldivmm' package.
<code>optim.control</code>	an optional list of <code>optimr::optimr()</code> control parameters.
<code>optim.grad</code>	an optional logical value indicating if a numerical gradient should be used in <code>optimr::optimr()</code> methods that can use this information. The default value is TRUE. If 'optim.grad' is set to FALSE, a finite difference approximation is used.
<code>lcoef</code>	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
<code>lcpa</code>	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpa' depends on the distribution supplied to 'dist'.
<code>lcmp</code>	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by <code>summary.aldivmm()</code> .

## Details

'init.method' accepts four methods for generating initial values: "zero", "random", "constant", "sann". The method "zero" sets initial values of all parameters to 0. The method "random" draws random starting values from a standard normal distribution. The method "constant" estimates a constant-only model and uses estimates as initial values for intercepts and constant distribution parameters and 0 for all other parameters. The method "sann" estimates the full model using the simulated annealing optimization method and uses all parameter estimates as initial values. When user-specified initial values are supplied in 'init.est', the argument 'init.method' is ignored.

By default, `aldivmm()` performs unconstrained optimization with upper and lower limits at  $-\text{Inf}$  and  $\text{Inf}$ . When user-defined lower and upper limits are supplied to 'init.lo' and/or 'init.hi', these default limits are replaced with the user-specified values, and the method "L-BFGS-B" is used for box-constrained optimization instead of the user defined 'optim.method'. It is possible to only set either maximum or minimum limits.

**Value**

aldvmm.init() returns a list with the following objects.

est	a numeric vector of initial values of parameters.
lo	a numeric vector of lower limits of parameters.
hi	a numeric vector of upper limits of parameters.

---

aldvmm.ll	<i>Calculating the Negative Log-Likelihood of the Adjusted Limited Dependent Variable Mixture Model</i>
-----------	---

---

**Description**

aldvmm.ll() calculates the negative log-likelihood of 'data' supplied to aldvmm() at the parameter values in 'par'.

**Usage**

```
aldvmm.ll(par, X, y, psi, ncmp, dist, lcoef, lcpair, lcmp, optim.method)
```

**Arguments**

par	a named numeric vector of parameter values.
X	a list of design matrices returned by aldvmm.mm(). 'X' is of length 2 and includes a design matrix for the model of component distributions and a design matrix for the model of probabilities of group membership.
y	a numeric vector of observed outcomes from complete observations in 'data' supplied to aldvmm().
psi	a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. c(-0.594, 0.883)). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in 'psi' does not matter.
ncmp	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.
dist	an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to "normal".
lcoef	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
lcpair	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpair' depends on the distribution supplied to 'dist'.
lcmp	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by summary.aldvmm().



`optim.method` an optional character value of one of the following `optimr::optimr()` methods: "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "nllminb", "Rcgmin", "Rvmmmin" and "hjn". The default method is "Nelder-Mead". The method "L-BFGS-B" is used when lower and/or upper constraints are set using 'init.lo' and 'init.hi'. The method "nllm" cannot be used in the 'aldvmm' package.

**Details**

`aldvmm.ll()` calculates the negative log-likelihood of the adjusted limited dependent variable mixture model using the likelihood function published in Hernandez Alava and Wailoo (2015). Constant distribution parameters that need to be non-negative (i.e. the standard deviations of normal distributions) enter the likelihood function as log-transformed values.

As the "L-BFGS-B" and "Rcgmin" methods in `optimr::optimr()` fail if they encounter infinite values, the log-likelihood function takes the value -1e+20 if it is infinite during these algorithms.

The names of the parameter vector supplied to 'par' must be generated using `aldvmm.getnames()` because they will be inherited by return values of other functions in the package 'aldvmm'. The names will also be used in the extraction of parameters from parameter vectors into nested lists using `aldvmm.getpar()`.

**Value**

a scalar of the negative log-likelihood of the data at parameter values in 'par'.

**References**

Alava, M. H. and Wailoo, A. (2015) Fitting adjusted limited dependent variable mixture models to EQ-5D. *The Stata Journal*, **15**(3), 737–750. doi:[10.1177/1536867X1501500307](https://doi.org/10.1177/1536867X1501500307)

---

aldvmm.mm	<i>Creating Design Matrices</i>
-----------	---------------------------------

---

**Description**

`aldvmm.mm()` creates two design matrices, one of the model of component distributions ("beta") and one of the model of probabilities of component membership ("delta").

**Usage**

`aldvmm.mm(data, formula, ncmp, lcoef)`

**Arguments**

data	a data frame, list or environment (or object coercible to a data frame by <code>base::as.data.frame()</code> ) including data on outcomes and explanatory variables in 'formula'.
formula	an object of class "formula" with a symbolic description of the model to be fitted. The model formula takes the form $y \sim x_1 + x_2 \mid x_1 + x_4$ , where the <code> </code> delimiter separates the model for expected values of normal distributions (left) and the multinomial logit model of probabilities of component membership (right).

ncmp	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.
lcoef	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").

### Details

aldvmm.mm() uses stats::model.matrix() to create design matrices for models of component distributions ("beta") and probabilities of component membership ("delta") based on 'formula' supplied to aldvmm.ll(). The design matrix for probabilities of group membership is only created if more than one components are specified in 'ncmp'.

### Value

a named list of numeric matrices.

beta	a numeric design matrix for the model of component distributions.
delta	a numeric design matrix of the multinomial logit model of probabilities of component membership.

---

aldvmm.pred	<i>Predicting Expected Values from Adjusted Limited Dependent Variable Mixture Models</i>
-------------	---

---

### Description

aldvmm.pred() makes predictions of observations in design matrices in 'X' using parameter estimates returned by aldvmm().

### Usage

```
aldvmm.pred(par, X, y = NULL, psi, ncmp, dist, lcoef, lcpair, lcmp)
```

### Arguments

par	a named numeric vector of parameter values.
X	a list of design matrices returned by aldvmm.mm(). 'X' is of length 2 and includes a design matrix for the model of component distributions and a design matrix for the model of probabilities of group membership.
y	a numeric vector of observed outcomes from complete observations in 'data' supplied to aldvmm().
psi	a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. c(-0.594, 0.883)). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in 'psi' does not matter.
ncmp	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.

dist	an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to "normal".
lcoef	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
lcpa	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpa' depends on the distribution supplied to 'dist'.
lcmp	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by summary.aldvmm().

### Details

aldvmm.pred() calculates expected values for observations in 'X' using the expected value function published in Hernandez Alava and Wailoo (2015). Constant distribution parameters that need to be non-negative (i.e. standard deviations of normal distributions) enter the expected value function as log-transformed values.

### Value

a named numeric vector of predicted outcomes. The names of the elements in the vector are identical to the row names of design matrices in 'X'.

---

aldvmm.sefit

*Calculating Standard Errors of Fitted and Predicted Outcomes*


---

### Description

aldvmm.sefit() calculates standard errors of fitted and predicted outcomes using the delta method.

### Usage

```
aldvmm.sefit(
  par,
  yhat,
  X,
  type,
  formula,
  psi,
  cv,
  mse = NA,
  ncmp,
  dist,
  level,
  lcoef,
  lcmp,
  lcpa
)
```

## Arguments

<code>par</code>	a named numeric vector of parameter values.
<code>yhat</code>	a numeric vector of predicted outcomes returned by <code>aldvmm.pred()</code> .
<code>X</code>	a list of design matrices returned by <code>aldvmm.mm()</code> . 'X' is of length 2 and includes a design matrix for the model of component distributions and a design matrix for the model of probabilities of group membership.
<code>type</code>	a character value of either 'fit' or 'pred' indicating whether the standard error of the fit ('fit') or the standard error of predictions in new data ('pred') are calculated.
<code>formula</code>	an object of class "formula" with a symbolic description of the model to be fitted. The model formula takes the form $y \sim x_1 + x_2 \mid x_1 + x_4$ , where the <code> </code> delimiter separates the model for expected values of normal distributions (left) and the multinomial logit model of probabilities of component membership (right).
<code>psi</code>	a numeric vector of minimum and maximum possible utility values smaller than or equal to 1 (e.g. <code>c(-0.594, 0.883)</code> ). The potential gap between the maximum value and 1 represents an area with zero density in the value set from which utilities were obtained. The order of the minimum and maximum limits in 'psi' does not matter.
<code>cv</code>	a numeric matrix with covariances/variances of parameter estimates returned by <code>aldvmm.cv()</code> .
<code>mse</code>	a numeric value of the mean squared error of observed versus predicted outcomes $\sum (y - \hat{y})^2 / (n_{obs} - n_{par})$ for all observations in model matrices 'X' supplied to <code>aldvmm.ll()</code> .
<code>ncmp</code>	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.
<code>dist</code>	an optional character value of the distribution used in the finite mixture. In this release, only the normal distribution is available, and the default value is set to "normal".
<code>level</code>	a numeric value of the significance level for confidence bands of fitted values. The default value is 0.95.
<code>lcoef</code>	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
<code>lcmp</code>	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by <code>summary.aldvmm()</code> .
<code>lcpa</code>	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpa' depends on the distribution supplied to 'dist'.

## Details

`aldvmm.sefit()` calculates standard errors of fitted values using the delta method. Standard errors of fitted values in the estimation data set are calculated as  $se_{fit} = \sqrt{G^t \Sigma G}$ , where  $G$  is the gradient of a fitted value with respect to changes of parameter estimates, and  $\Sigma$  is the estimated covariance matrix of parameters (Dowd et al., 2014). Standard errors of predicted values in new data sets are calculated as  $se_{pred} = \sqrt{MSE + G^t \Sigma G}$ , where  $MSE$  is the mean squared error of fitted versus observed outcomes in the original estimation data (Whitmore, 1986). The gradients of fitted values with respect to parameter estimates are approximated numerically using `numDeriv::jacobian()`.

**Value**

a named numeric vector of standard errors of fitted or predicted outcomes. The names of the elements in the vector are identical to the row names of design matrices in 'X'

**References**

Whitmore, G. A. (1986). Prediction limits for a univariate normal observation. *The American Statistician*, 40(2), 141-143. <https://doi.org/10.1080/00031305.1986.10475378>

Dowd, B. E., Greene, W. H., and Norton, E. C. (2014) Computation of standard errors. *Health services research*, **49**(2), 731–750. [doi:10.1111/14756773.12122](https://doi.org/10.1111/14756773.12122)

aldvmm.sum

*Creating Summary Table***Description**

aldvmm.sum() creates a summary table of regression results.

**Usage**

```
aldvmm.sum(
  est,
  se,
  z,
  p,
  lower,
  upper,
  n,
  value,
  aic,
  bic,
  ncnp,
  lcoef,
  lcp,
  lcpar,
  lcnp,
  lvar,
  digits = 3
)
```

**Arguments**

est	a named numeric vector of point estimates.
se	a named numeric vector of standard errors of parameters returned by aldvmm.cv().
z	a named numeric vector of standardized coefficients of parameters returned by aldvmm.cv().
p	a named numeric vector of p-values of parameters returned by aldvmm.cv().
lower	a named numeric vector of 95% lower limits of parameters returned by aldvmm.cv().
upper	a named numeric vector of 95% upper limits of parameters returned by aldvmm.cv().

n	a numeric value of the number of complete observations in 'data' supplied to aldvmm().
value	a numeric value of the negative log-likelihood returned by aldvmm.ll().
aic	a numeric value of the Akaike information criterion (AIC) returned by aldvmm.gof().
bic	a numeric value of the Bayesian information criterion (BIC) returned by aldvmm.gof().
ncmp	a numeric value of the number of components that are mixed. The default value is 2. A value of 1 represents a tobit model with a gap between 1 and the maximum value in 'psi'.
lcoef	a character vector of length 2 with labels of objects including regression coefficients of component distributions (default "beta") and coefficients of probabilities of component membership (default "delta").
lcpa	a character vector with the labels of objects including constant parameters of component distributions (e.g. the standard deviation of the normal distribution). The length of 'lcpa' depends on the distribution supplied to 'dist'.
lcmp	a character value representing a stub (default "Comp") for labeling objects including regression coefficients in different components (e.g. "Comp1", "Comp2", ...). This label is also used in summary tables returned by summary.aldvmm().
lvar	a named list of character vectors with column names of design matrices returned by aldvmm.mm().
digits	a numeric value of the number of digits in the reporting table.

### Value

a data.frame object with a summary table of regression results.

---

predict.aldvmm	<i>Predict Method for Adjusted Limited Dependent Variable Mixture Model Fits</i>
----------------	--

---

### Description

The generic function `stats::predict()` calls `aldvmm.pred()` to predict outcomes and their standard errors in new data using `aldvmm.pred()` and `aldvmm.sefit()`.

### Usage

```
## S3 method for class 'aldvmm'
predict(object, newdata, se.fit = FALSE, type = "pred", level = 0.95, ...)
```

### Arguments

object	an object inheriting from class 'aldvmm'.
newdata	a data frame, list or environment (or object coercible to a data frame by <code>base::as.data.frame()</code> ) including explanatory variables for prediction.
se.fit	an optional logical value indicating whether standard errors of fitted values are calculated. The default value is FALSE.
type	a character value of either 'fit' or 'pred' indicating whether the standard error of the fit ('fit') or the standard error of predictions in new data ('pred') are calculated.

level	a numeric value of the significance level for confidence bands of fitted values. The default value is 0.95.
...	further arguments passed to or from other methods.

**Value**

a named list of numeric vectors of predicted outcomes, standard errors and confidence or prediction intervals.

---

summary.aldvm	<i>Summarizing Adjusted Limited Dependent Variable Mixture Model Fits</i>
---------------	---

---

**Description**

The generic function base::summary() calls aldvm.sum() to print the summary table data frame returned by aldvm.sum().

**Usage**

```
## S3 method for class 'aldvm'
summary(object, ...)
```

**Arguments**

object	an object inheriting from class 'aldvm'.
...	further arguments passed to or from other methods.

---

utility	<i>Simulated Example Data of Health State Utilities.</i>
---------	--

---

**Description**

utility is a simulated data frame including health state utilities and patients' age and sex.

**Usage**

```
utility
```

**Format**

A data frame with 200 rows and 3 variables:

utility	a utility value $\{[-0.594, 0.883], 1\}$ .
age	Age in years.
female	Indicator of female sex.

**Examples**

```

set.seed(101010101)
utility <- data.frame(female = rbinom(size = 1,
                                     n = 200,
                                     p = 0.6))
utility[, 'age'] <- stats::rnorm(n = 200,
                               mean = 50 + utility$female*10,
                               sd = 15)
utility[1:50, 'eq5d'] <- stats::rnorm(n = 50,
                                     mean = 0 - 0.1 *
                                     utility[1:50, 'female'] +
                                     0.0005 * utility[1:50, 'age'],
                                     sd = 0.1)
utility[51:200, 'eq5d'] <- stats::rnorm(n = 150,
                                     mean = 0.5 +
                                     0.1 * utility[51:200, 'female'] +
                                     0.0001*utility[51:200, 'age'],
                                     sd = 0.2)
utility[utility$eq5d<(-0.594), 'eq5d'] <- -0.594
utility[utility$eq5d>0.883, 'eq5d'] <- 1
hist(utility$eq5d, breaks = 50)

```



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