Deep Learning for Natural Language Processing

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1 Question

Using the orthogonality and the properties of the trace, prove that, for X and Y two matrices:

$$W^* = \arg\min_{W \in O(\mathbb{R})} \|WX - Y\|_F = UV^T,$$

with $U\Sigma V^T = SVD(YX^T)$.

Answer: we see first that:

$$W^* = \arg\min_{W \in O(\mathbb{R})} \|WX - Y\|_F^2$$

Developing the Frobenius norm's definition and using orthogonality of W:

$$W^* = \arg\min_{W \in O(\mathbb{R})} ||X||_F^2 + ||Y||_F^2 - 2\operatorname{Tr} X^T W Y$$

Consequently:

$$W^* = \arg\max_{W \in O(\mathbb{R})} \operatorname{Tr} X^T W Y = \arg\max_{W \in O(\mathbb{R})} \operatorname{Tr} X^T W Y^2$$

Using trace properties and SVD:

$$W^* = \arg\max_{W \in O(\mathbb{R})} \operatorname{Tr} Y X^T W = \arg\max_{W \in O(\mathbb{R})} \operatorname{Tr} U \Sigma V^T W^2 = \arg\max_{W \in O(\mathbb{R})} \operatorname{Tr} \Sigma V^T W U^2$$

Using Cauchy-Schwarz inequality:

$$\operatorname{Tr} \Sigma \boldsymbol{V}^T \boldsymbol{W} \boldsymbol{U}^2 \leq \operatorname{Tr} \boldsymbol{\Sigma}^T \boldsymbol{\Sigma} \operatorname{Tr} (\boldsymbol{V}^T \boldsymbol{W} \boldsymbol{U})^T \boldsymbol{V}^T \boldsymbol{W} \boldsymbol{U} = \operatorname{Tr} \boldsymbol{\Sigma}^T \boldsymbol{\Sigma}$$

The cost function is strictly convex and the minimal is reached for $W = UV^T$.

Therefore, $W^* = UV^T$.

2 Question

What is your training and dev errors using either the average of word vectors or the weighted-average?

IDF	Dev	Train	Penalty
Without With	0.42 0.41	$0.47 \\ 0.46$	0.25

3 Question

Which loss did you use? Write the mathematical expression of the loss you used for the 5-class classification.

Answer I used the categorical cross entropy. Its mathematical expression for N observations and C=5 classes is:

$$-\frac{1}{N} \sum_{i=1}^{N} \sum_{c=1}^{C} 1_{y_i \in C_c} \log p(y_i \in C_c)$$

where p is the probability output by the network.

4 Question

Plot the evolution of train/dev results w.r.t the number of epochs.

Answer We can that even for a relatively low number of parameters, the network over-fits with a few epochs. [Plot history][plot_history.png]

5 Question

Be creative: use another encoder. Make it work! What are your motivations for using this other model?

Answer The previous network shows a relative poor ability to tackle this challenge because it was over-fitting even with a simple structure. Instead, I think it is a better idea to use a pre-trained network to learn the embeddings. Once the embeddings is achieved, a logistic regression as in Part 3 makes sense.