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Project 1



Pseudocode

Lawnmower

```
function lawnmower(diskArr) {
       numSwap = 0
       newDiskArr = diskArr
       n = total number of disks
      for(i = 0 to n/4 - 1) do
             for(j = 0 \text{ to } n-2) \text{ do}
                    if(newDiskArr[j] is dark AND newDiskArr[j+1] is light)
                           swap newDiskArr[j] and newDiskArr[j+1]
                           numSwap++
                           endif
                    endfor
             for(j = n-1 to 1) step down, do
                    if(newDiskArr[j] is light AND newDiskArr[j-1] is dark)
                           swap newDiskArr[j] and newDiskArr[j-1]
                           numSwap++
                           endif
                    endfor
             endfor
       return (newDiskArr, numSwap)
}
```

<u>Alternate</u>

```
function alternate(diskArr) {
      numSwap = 0
      newDiskArr = diskArr
      n = total number of disks
      for(i = 0 to n/2 - 1)
             start = 0
             if((i+1)\%2==0)
                   start = 0
                   endif
             else
                   start = 1
                   endelse
             for(j = start to n-2) step 2
                   if(newDiskArr[j] is dark AND newDiskArr[j+1] is light
                          swap newDiskArr[j] and newDiskArr[j+1]
                          numSwap++
                          endif
                   endfor
             endfor
      return (newDiskArr, numSwap)
}
```

Step Count

Lawnmower

```
function lawnmower(diskArr) {
       numSwap = 0
                                                                           1
       newDiskArr = diskArr
                                                                           1
       n = total number of disks
                                                                           1
       for(i = 0 to n/4 - 1) do
             for(j = 0 \text{ to } n-2) \text{ do}
                    if(newDiskArr[j] is dark AND newDiskArr[j+1] is light)
                           swap newDiskArr[j] and newDiskArr[j+1]
                           numSwap++
                                                                           1
                           endif
                    endfor
             for(j = n-1 to 1) step down, do
                    if(newDiskArr[j] is light AND newDiskArr[j-1] is dark)
                           swap newDiskArr[j] and newDiskArr[j-1]
                           numSwap++
                                                                           1
                           endif
                    endfor
             endfor
       return (newDiskArr, numSwap)
}
```

for(j = 0 to n-2),

$$sc = \sum_{0}^{n-2} 7 = \sum_{1}^{n-1} 7 = 7n - 7$$

for(j = n-1 to 1) step down

$$sc = \sum_{1}^{n-1} 7 = 7n - 7$$

$$7n - 7 + (7n - 7) = 14n - 14$$

for(i = 0 to n/4 - 1)

$$sc = \sum_{0}^{\frac{n}{4}-1} (14n - 14) = \sum_{1}^{\frac{n}{4}} (14n - 14) = (14n - 14)\frac{n}{4} = \frac{7}{2}n^2 - \frac{7}{2}n$$

$$Total\ sc = \frac{7}{2}n^2 - \frac{7}{2}n + 3$$

<u>Alternate</u>

```
function alternate(diskArr) {
      numSwap = 0
                                                                        1
      newDiskArr = diskArr
                                                                        1
      n = total number of disks
                                                                        1
      for(i = 0 to n/2 - 1)
             start = 0
                                                                 1
             if((i+1)\%2==0)
                                                                  3
                   start = 0
                                                           1
                   endif
             else
                   start = 1
                                                           1
                   endelse
             for(j = start to n-2) step 2
                   if(newDiskArr[j] is dark AND newDiskArr[j+1] is light
                          swap newDiskArr[j] and newDiskArr[j+1]
                          numSwap++
                                                                        1
                          endif
                   endfor
             endfor
      return (newDiskArr, numSwap)
}
```

for(j = start to n-2) step 2

in this case, start can only be 0 OR 1, use 0 because we are taking the upper bound

$$\sum_{0}^{n-2} 7 \, step2 = \sum_{1}^{n-1} 7 \, step2 = \sum_{1}^{\frac{n-1}{2}} 7 \, = \frac{7}{2} n - \frac{7}{2}$$

$$\frac{7}{2}n - \frac{7}{2} + 5 = \frac{7}{2}n + \frac{3}{2}$$

for(i = 0 to n/2 - 1)

$$\sum_{0}^{\frac{n}{2}-1} (\frac{7}{2}n + \frac{3}{2}) = \sum_{1}^{\frac{n}{2}} (\frac{7}{2}n + \frac{3}{2}) = \frac{7}{2}n + \frac{3}{2} (\frac{n}{2}) = \frac{7}{4}n^2 + \frac{3}{4}n$$

$$Total\ sc = \frac{7}{4}n^2 + \frac{3}{4}n + 3$$

Analysis

Lawnmower

$$Total\ sc = \frac{7}{2}n^2 - \frac{7}{2}n + 3 \in O(n^2)$$

Proof by definition:

$$f(n) = \frac{7}{2}n^2 - \frac{7}{2}n + 3$$

$$g(n) = n^2$$

$$f(n) \le c * g(n)$$
 for $n \ge n_0$

$$c = \frac{7}{2} + \frac{7}{2} + 3 = 10$$

$$n_0 = 1$$

$$\frac{7}{2} - \frac{7}{2} + 3 = 3 \le 10$$

Proof by limit theorem:

$$L = \lim_{n \to \infty} \frac{f(n)}{g(n)} = \lim_{n \to \infty} \frac{\frac{7}{2}n^2 - \frac{7}{2}n + 3}{n^2} = \lim_{n \to \infty} \frac{(\frac{7}{2}n^2 - \frac{7}{2}n + 3)'}{(n^2)'} = \lim_{n \to \infty} \frac{\frac{7}{2}n - \frac{7}{2}}{n} = \lim_{n \to \infty} \frac{\frac{7}{2}}{1} = \frac{7}{2}$$

$$L = \frac{7}{2} \ge 0$$
 and is a constant

Alternate

$$Total\ sc = \frac{7}{4}n^2 + \frac{3}{4}n + 3$$

Proof by definition:

$$f(n) = \frac{7}{4}n^2 + \frac{3}{4}n + 3$$

$$g(n) = n^2$$

$$f(n) \le c * g(n)$$
 for $n \ge n_0$

$$c = \frac{7}{4} + \frac{3}{4} + 3 = \frac{11}{2}$$

$$n_0 = 1$$

$$\frac{7}{4} + \frac{7}{4} + 3 = \frac{11}{2} \le \frac{11}{2}$$

Proof by limit theorem:

$$L = \lim_{n \to \infty} \frac{f(n)}{g(n)} = \lim_{n \to \infty} \frac{\frac{7}{4}n^2 + \frac{3}{4}n + 3}{n^2} = \lim_{n \to \infty} \frac{(\frac{7}{4}n^2 + \frac{3}{4}n + 3)'}{(n^2)'} = \lim_{n \to \infty} \frac{\frac{7}{4}n + \frac{7}{4}}{n} = \lim_{n \to \infty} \frac{\frac{7}{4}}{1} = \frac{7}{4}$$

$$L = \frac{7}{4} \ge 0$$
 and is a constant