

Modelado y Animación por Computador

Tema 2: Modelado

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El Arte de la Animación por Computador

Avances en la tecnología *Visual Milestones*

El Arte de la Animación por Computador

Toy Story (1995)

- ❑ Primer largometraje realizado íntegramente en 3D. **Pixar & Disney Studios.**
- ❑ **Pixar:** creada por *George Lucas* y vendida eventualmente a *Steve Jobs*.
- ❑ Voces protagonistas: Tom Hanks y Tim Allen.
- ❑ Recaudó más de 350 millones de dólares.
- ❑ Solidez de la historia.



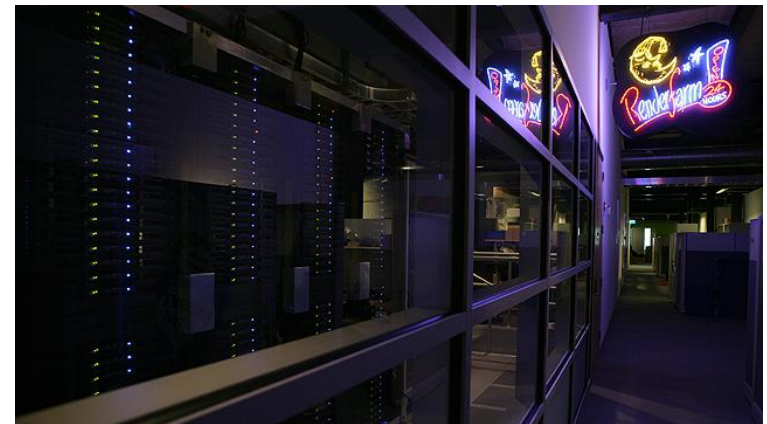
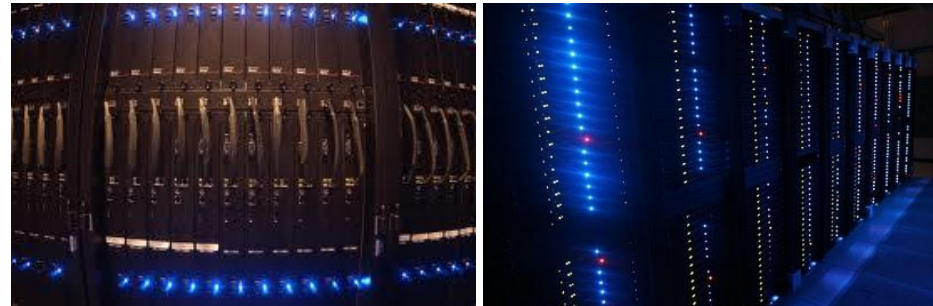
El Arte de la Animación por Computador

3D Computer Animation Studio *(Estudio de animación 3D)*

El Arte de la Animación por Computador

Componentes básicos:

- Visión
- Plan de negocios y funciones
- Lugar de trabajo
- Personal creativo
- Personal producción
- Personal técnico
- Personal administrativo y comercial
- Software genérico
- Software propietario
- **Potencia de procesamiento***
- Almacenamiento periférico
- Red de interconexión
- Equipamiento de entrada/salida



Pixar Render Farm

El Arte de la Animación por Computador

Tipos de software:

- Modelado superficies 3D
- 3D “rigging” y animación
- 2D/3D escáner
- Dibujo 3D
- Captura movimiento
- “Shading” y “rendering”
- Composición
- Edición
- Calibración del color
- Compresión archivos
- **Rotoscoping***
- Web
- Animación 2D
- Dibujo 2D y retoque
- Gestor multimedia
- Backup
- Gestor de red



Rotoscoping: técnica utilizada para generar efectos especiales tales como “aura” sobre objetos (máscaras de contorno). El uso más clásico de “rotoscoping” fue en la trilogía original de *Star Wars*, donde se creó el efecto del sable láser (aura), a partir de un sable de plástico que manejaban los actores. Para conseguir el efecto, los editores trazaron una línea sobre cada fotograma donde aparecía el sable y lo retocaron generando el aura difuminada.

El Arte de la Animación por Computador

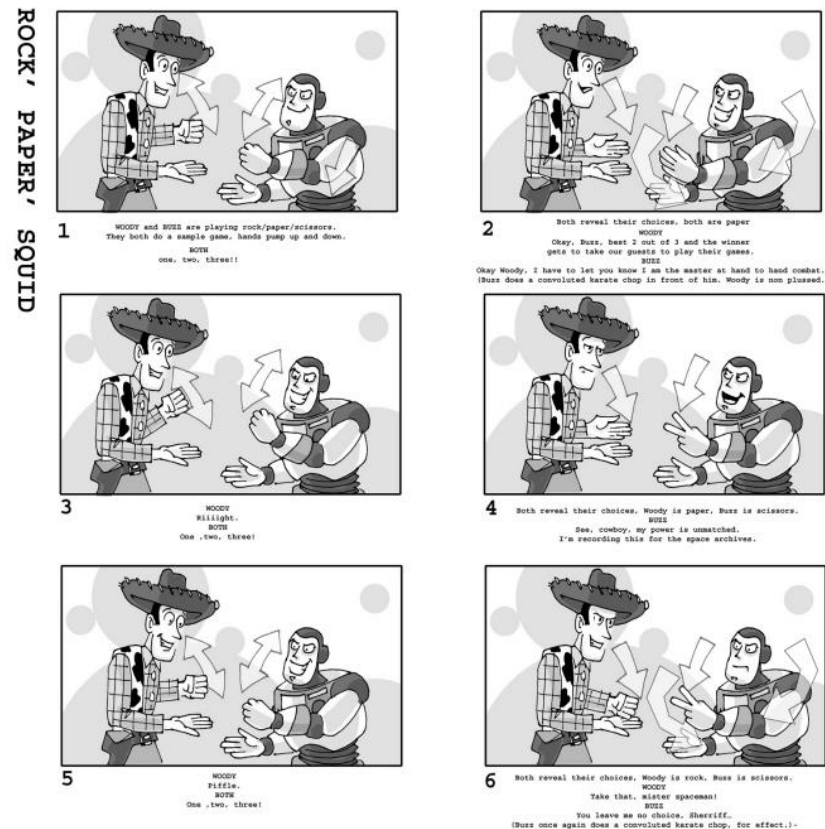
Equipo creativo (movie):

- Director
- Scriptwriter
- Production designer
- Visual effects director
- Art director
- Storyboard artist
- Producer



Equipo administrativo (movie):

- Executive producer
- Production assistant
- Production manager
- Director of postproduction
- Director of finance
- Production accountant



Storyboard Toy Story



El Arte de la Animación por Computador

Equipo de producción (movie):

- **Visual effects group**
 - Visual effects producer
 - Visual effects supervisor
 - Visual effects editor
 - Visual effects assistant editor
 - Visual effects coordinator
 - Stage technicians
- **Computer animation group**
 - Digital supervisor
 - Computer animation shot supervisors
 - **Computer animators**
 - Production coordinator
- **Modeling and lighting group**
 - Computer modeling supervisor
 - **Modeling TDs**
 - Lighting supervisor
 - **Lighting TDs**
 - **Rendering wranglers**
- **Computer technical support group**
 - CG department manager
 - **CG software developers**
 - CG technical assistants
 - CG systems support
- **Digital compositing and postproduction group**
 - Digital supervisor
 - Digital coordinator
 - **Digital artists**
 - Compositors
 - Digital transfer operator
 - Scanning supervisor
 - **Scanning operators**
 - Rotoscoping supervisor
 - **Rotoscopers**
 - Camera trackers
 - Digital output supervisor
 - Digital color timing supervisor
 - Negative cutter



El Arte de la Animación por Computador

Películas con más influencia:

1. Star Wars 1977
2. Blade Runner 1982
3. 2001: A space odyssey 1968
4. **The Matrix 1999***
5. Jurassic Park 1993
6. Tron 1982
7. King Kong 1933
8. Close Encounters of the Third Kind 1977
9. Alien 1979
10. The Abyss 1989
11. The Empire Strikes Back 1980
12. Metropolis 1927
13. A Trip to the Moon 1902
14. Terminator 2: Judgment Day 1991
15. The Wizard of Oz 1939
16. Who Framed Roger Rabbit 1988
17. Raiders of the Lost Ark 1981
18. Titanic 1997
19. Lord of the Ring: The Fellowship of the Ring 2001
20. Jason and the Argonauts 1963
21. E.T. the Extraterrestrial 1982
22. Toy Story 1995
23. Pirates of the Caribbean: Dead Man's Chest 2006
24. The Ten Commandments 1953
25. The War of the Worlds 1953
26. Forrest Gump 1994
27. Citizen Kane 1941
28. The Seventh Voyage of Sinbad 1958
29. 20.000 Leagues Under the Sea 1954
30. The Terminator 1984
31. Aliens 1986
32. Mary Poppins 1964
33. Lord of the Rings: The Return of the King 2003
34. Forbidden Planet 1956
35. Babe 1995
36. The Day the Earth Stood Still 1951
37. Lord of the Rings: The Two Towers 2002
38. King Kong 2005
39. Avatar 2009

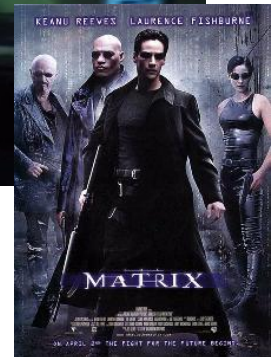


El Arte de la Animación por Computador

Películas con más influencia (The Matrix)



Bullet Time Effect



El Arte de la Animación por Computador

Equipo de producción (Halo3):

Halo 3	
Art.....35	Production.....9
Art Director.....1	Executive Producer.....1
Campaign Environment Leads.....4	Production Leads.....2
Campaign Environment Artists.....7	Producers.....4
Multiplayer Environment Lead.....1	Development Manager.....1
Multiplayer Environment Artists.....3	Studio Manager.....1
3D Art Lead.....1	Test.....4
3D Artists.....5	Test Manager.....1
Animators.....5	Test Leads.....3
Additional Animation.....1	Writing.....4
Concept Art/Skies/Matte Painting.....2	Writing Director.....1
Effects Art Lead.....1	Managing Editor.....1
Effects Artist.....1	Writers.....2
Technical Art Lead.....1	Bungie NET Team.....4
Technical Artists.....3	Bungie Mktg/PR/Comm. Lead.....1
Audio.....3	Web Development Lead.....1
Director/Composer.....1	Web Developer.....1
Audio Lead/Sound Design.....1	Oversight.....1
Sound Design/Additional Music.....1	Bungie Backbone.....7
Cinematics.....3	Senior Business Coordinator.....1
Cinematics Director.....1	Business Administrator.....1
Cinematics Design.....2	IT Lead.....1
Design.....9	Helpdesk Lead.....1
Campaign Design Leads.....2	Security.....3
Campaign Designers.....3	Additional Support.....4
Gameplay Design Play.....1	Graphic Design.....1
Gameplay Designer.....1	Music Composition, Audio Prod.....1
Multiplayer Design Lead.....1	Orchestration.....1
Multiplayer Designer.....1	Story Editor.....1
Engineering.....20	Special Thanks.....21
Engineering Leads.....6	Voice Actors.....50
Campaign Engineers.....5	Cinematics Cast.....10
Graphics Engineers.....4	Artificial Intelligence Cast.....24
Multiplayer Engineers.....5	Brutes.....3
Production Engineering.....9	Brute Chieftain.....1
Production Engineering Lead.....1	Civilians.....2
Production Engineers.....2	Elites.....2
Tools Lead Engineer.....1	Grunts.....4
Tools Engineers.....5	Marines.....9
Graphic Design, User Interface.....4	Sergeants.....2
Graphic Design Lead.....1	Multiplayer Announcer.....1
User Interface.....2	Additional Voices.....15
Graphic Artist.....1	Casting/Voice-Over Prod Svcs.....1
	Cinematic Animation Partners.....36
	Animation Supervisor.....1
	dannfx.....26
	Zoic Studios.....9
	Microsoft Game Studios
	Publishing.....35
	Executive Producer.....1
	Legal/Business Affairs.....3
	Engineering.....4
	Program manager.....1
	Engineering Support.....7
	Finance.....3
	HR/Recruiting.....4
	Research.....4
	User Experience.....5
	User Research Lead.....1
	User Research Engineers.....2
	Microsoft Research Asia.....6
	Researchers.....6
	Microsoft Test.....13
	Test Lead.....1
	SDET.....12
	Microsoft Xbox.....15
	Platform and Xbox Live.....12
	Marketing and PR.....3
	Microsoft.....18
	Localization Teams Europe/Brazil.....5
	Localization Team Japan.....4
	Localization Team Korea.....4
	Localization Team Redmond.....1
	Localization Team Taiwan.....4
	Microsoft Development Partners 12
	FASA.....3
	Rare.....9
	Producers, Engineering and Artistic Contractors.....0
	Filter.....2
	FilmOasis.....7
	Sakson & Taylor.....20
	Excell Data Corporation.....31
	Volt.....63
	Xiversity.....1
	Community.....12
	Biggest Community Supporters.....12



El Arte de la Animación por Computador

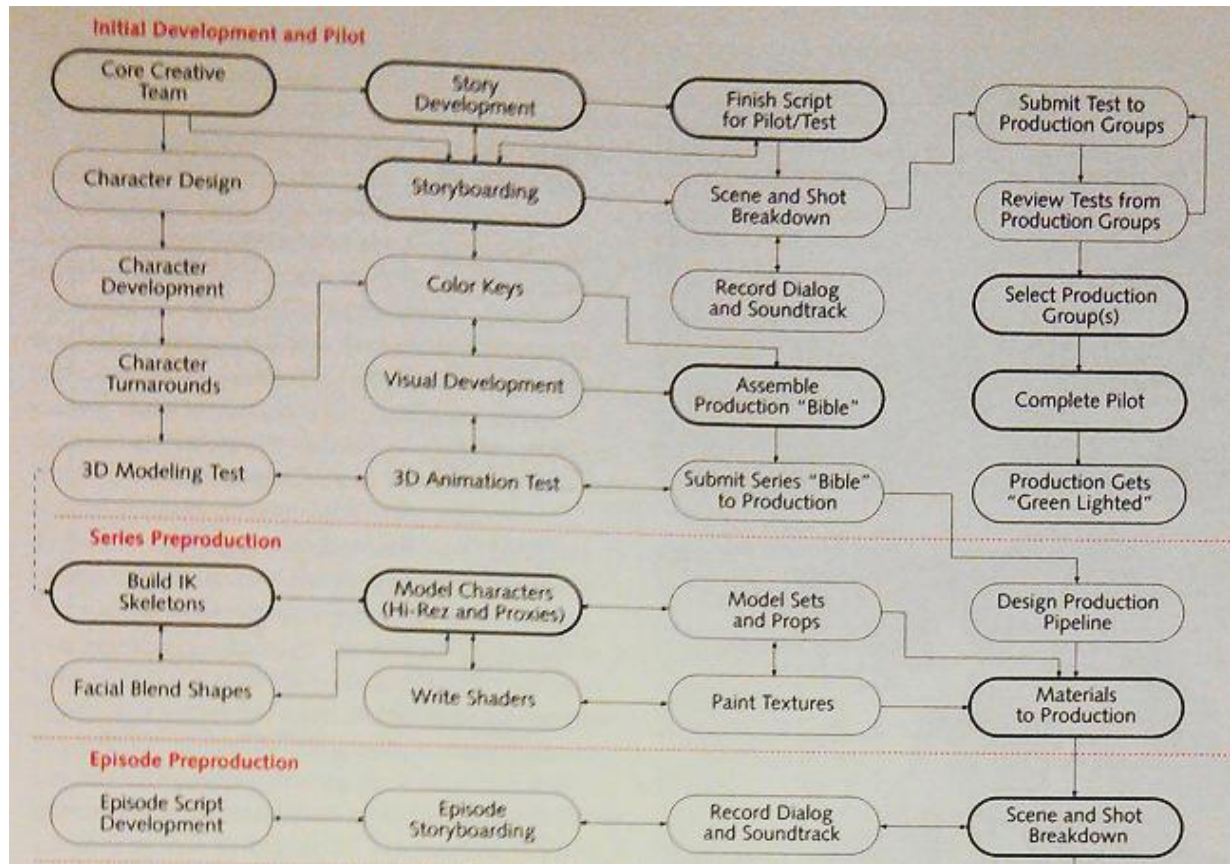
Equipo de producción (Ratatouille):

Ratatouille			
Animation95		Lighting47	Fur and Hair Groom2
Animation Manager.....1		Lighting Managers.....2	Additional Shading.....4
Directing Animators.....2	➔	Technical Lighting Lead.....1	Shading Packet Artists.....2
Animation Preproduction.....7		Lighting Technology Lead.....1	Shade/Paint Coordinators.....2
Animators.....63		Master Lighting Artists.....17	
Fix Animation Lead.....1		Shot Lighting Artists.....21	➔ Production Engineering36
Fix and Additional Animation.....7		Lighting Technology.....3	Team Leads.....5
Crowds Animation Lead.....1		Lighting Coordinator.....1	Software Development.....24
Crowd Animators.....4		Lighting Production Assistant.....1	Infrastructure.....7
Animation Technical Support.....1			
Animation Simulation Artist.....1		Sets and Layout39	Story25
Additional Animation.....3		Set/Layout Manager.....1	Additional Story Supervision.....1
Animation Coordinator.....1		Senior Camera Operator.....1	Story Manager.....1
Animation Technical Coordinator.....1		Layout Lead.....1	Story Artists.....13
Animation Fix Coordinator.....1		Sequence Leads.....3	Additional Storyboarding.....5
Animation Production Assistant.....1		Layout Artists.....9	Animatic Artists.....2
		Previsualization.....2	Script Supervisor.....1
		Layout Coordinators.....2	Story Coordinators.....2
		Set Modeling Lead.....1	
Directing/Supervising47		Sets Technical Lead.....1	Crowds and Simulation24
Director and Screenwriter.....1		Modeling Artists.....7	Postproduction24
Co-Director.....1		Set Dressing Leads.....2	Music22
Producer.....1		Set Dressing Artists.....3	
Executive Producers.....2		Additional Sets Artists.....3	Characters21
Associate Producer.....1		Sets Coordinators.....3	Character Managers.....2
Original Story.....3			Character Leads.....4
Music Composer.....1		Production Office Support39	Modeling and Articulation Artists.....11
Story Supervisor.....1		Art38	Character Scans.....*
Supervising Technical Director.....3		Art Manager.....1	(by Gentle Giant)
Production Designer.....2		Development Art Director.....1	Add. Modeling and Articulation.....1
Supervising Animators.....2		Environment Designer.....1	Character Coordinator.....3
Director of Photography Lighting.....1		Additional Character Design.....3	
Director of Photography Camera.....1		Production Artists.....5	Technical Development20
Character Design.....4		Graphic Designers.....3	
Character Supervisor.....1		Sculptor.....1	Postproduction Sound Services20
Sets Art Director.....1		Matte Painters.....2	(by Skywalker Sound)
Sets Supervisor.....1		Matte Technical Artists.....3	
Shading Art Director.....1		Additional Visual Development.....4	➔ Effects19
Shading Supervisor.....1		Graphics Translations.....2	Effects Manager.....1
Global Technology Supervisor.....1		Molds and Castings.....*	Effects Artists.....17
Effects Supervisor.....1		(by Images in Motion)	Effects Coordinator.....1
Simulation Supervisor.....1		Additional Production Artists.....2	
Groom Supervisor.....1		Art Coordinator.....1	Editorial18
Crowds Supervisor.....1		Art Production Assistants.....2	Cast/Voice Talent.....17
Production Manager.....1		Art Interns.....7	Image Mastering14
Sound Designer.....1			End Titles13
Casting.....2		Shade, Paint and Groom36	Chefs de Pixar10
Additional Story Material.....3	➔	Shade/Paint/Groom Manager.....1	Rendering and Optimization9
Production Accountant.....1		Character Shading Lead.....1	Render Pipeline Group8
Lighting Supervisor.....1		Shading Artists.....17	Additional Voices7
Matte Supervisor.....1		Digital Painters.....6	Moving Pictures Group6
Rendering Supervisor.....1		Lead Groom Artist.....1	Sweatbox2
Additional Prod. Management.....1			



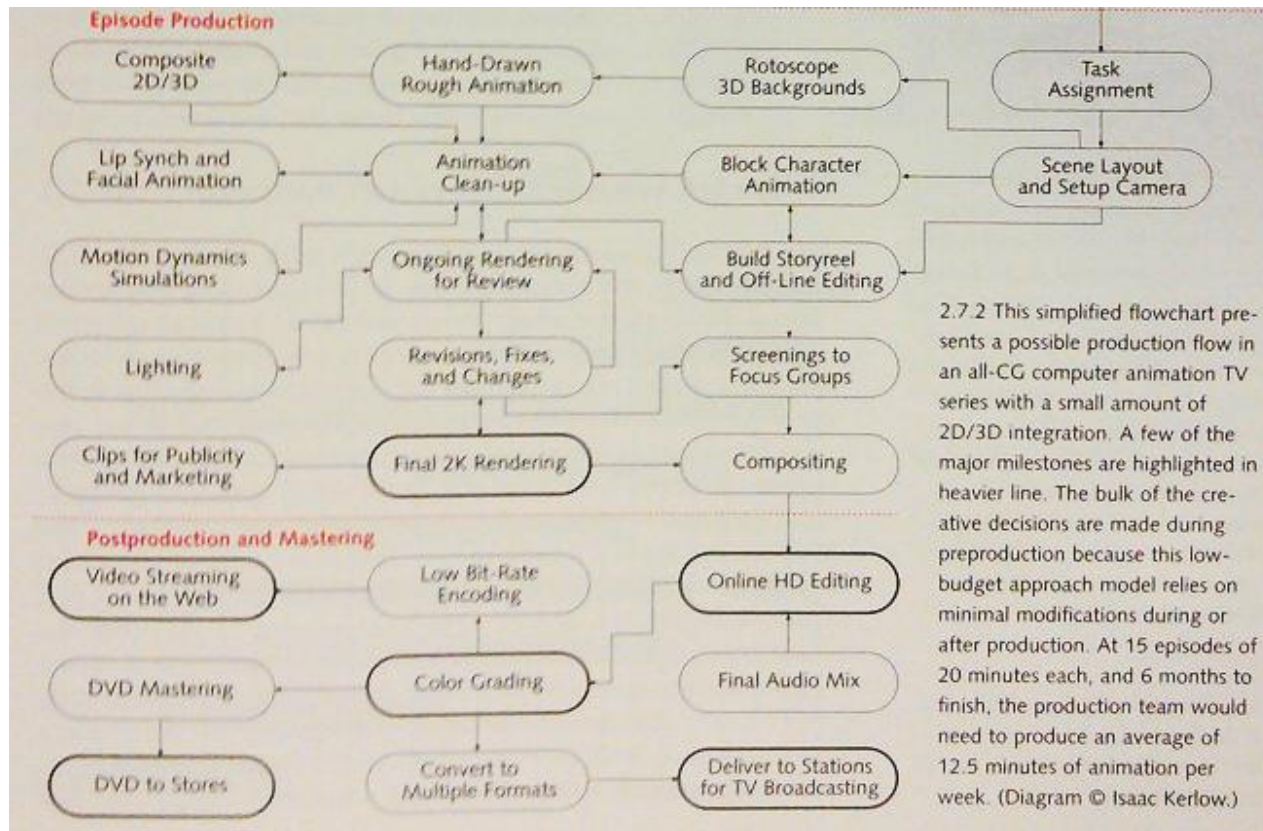
El Arte de la Animación por Computador

3D Production TV flowchart (I):



El Arte de la Animación por Computador

3D Production TV flowchart (II):



El Arte de la Animación por Computador

Proceso de producción en animación por computador:

- **Preproduction tasks:** grabación diálogos (scratch dialog) -> bases para animación caras
- **Storyboards:** unidades de producción, composición escenas, acciones y movimiento de cámara
- **Animatics, story reels, and previsualization:** acciones animadas simplificadas y previsualización
- **Modeling:** escena, personajes y elementos auxiliares...
- **Rough and final scene layout:** composición final de la escena
- **Rigging:** esqueletos internos (IK rigs)
- **Texture painting:** diseño de texturas complejas (material layers)
- **Character animation**
- **Effects animation and technical animation**
- **Review and approval or dailies:** trabajo de supervisión
- **Performance and live action capture on the set:** captura de movimientos de actores reales
- **Lighting and rendering:** iluminación -> posición luces, tipos, efectos... rendering -> shading, proc. textures
- **Rotoscoping and camera tracking**
- **Compositing, postprocesing, and final output**
- **Media asset management and technical support**



El Arte de la Animación por Computador

CGI Workflow example (behind the scenes)

<https://www.youtube.com/watch?v=szJ9Ohi2FNo>

Tema 2: Modelado

- 1.- Introducción
- 2.- Modelos geométricos de representación
- 3.- Técnicas de modelado
- 4.- Transformaciones geométricas**
- 5.- Deformadores
- 6.- Sistemas de partículas
- 7.- Fuerzas
- 8.- Efectos atmosféricos

Transformaciones geométricas

Matrix representation 2D

- Representación de transformaciones 2D con una matriz:

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

- Multiplicación de la matriz por un vector columna \Leftrightarrow aplicación de una transformación a un punto:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$x' = ax + by$$

$$y' = cx + dy$$

Transformaciones geométricas

Matrix representation 2D

- Transformaciones combinadas mediante multiplicación de matrices:

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} e & f \\ g & h \end{bmatrix} \begin{bmatrix} i & j \\ k & l \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Las matrices representan la mejor forma de definir una secuencia de transformaciones geométricas de forma eficiente

Transformaciones geométricas

Matrix representation 2D

- ¿Qué tipos de transformaciones pueden ser representadas con matrices de 2x2?

2D Identity?

$$\begin{aligned}x' &= x \\ y' &= y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Scale around (0,0)?

$$\begin{aligned}x' &= sx * x \\ y' &= sy * y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} sx & 0 \\ 0 & sy \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Transformaciones geométricas

Matrix representation 2D

- ¿Qué tipos de transformaciones pueden ser representadas con matrices de 2x2?

2D Rotate around (0,0)?

$$\begin{aligned}x' &= \cos \Theta * x - \sin \Theta * y \\y' &= \sin \Theta * x + \cos \Theta * y\end{aligned}\quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta \\ \sin \Theta & \cos \Theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Shear?

$$\begin{aligned}x' &= x + shx * y \\y' &= shy * x + y\end{aligned}\quad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & shx \\ shy & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Transformaciones geométricas

Matrix representation 2D

- ¿Qué tipos de transformaciones pueden ser representadas con matrices de 2x2?

2D Mirror over Y axis?

$$\begin{aligned}x' &= -x \\ y' &= y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

2D Mirror over (0,0)?

$$\begin{aligned}x' &= -x \\ y' &= -y\end{aligned}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Transformaciones geométricas

Matrix representation 2D

- ¿Qué tipos de transformaciones pueden ser representadas con matrices de 2x2?

2D Translation?

$$\begin{aligned}x' &= x + tx \\ y' &= y + ty\end{aligned}$$

NO!

Solo transformaciones lineales 2D pueden ser representadas con matrices de 2x2

Transformaciones geométricas

Matrix representation 2D

- Las transformaciones lineales son combinaciones de...

- Scale,
- Rotation,
- Shear, and
- Mirror

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$


Transformaciones geométricas

Matrix representation 2D

- Traslación 2D representada con una matriz de 3x3:

- Point represented with *homogeneous coordinates*

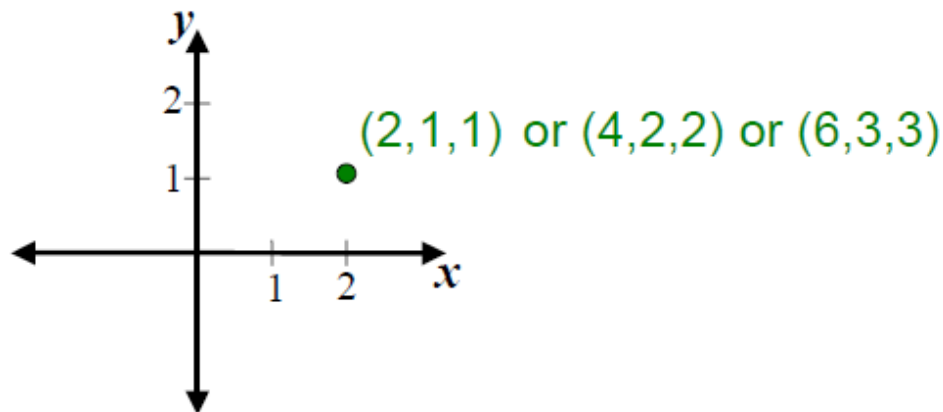
$$\begin{aligned}x' &= x + tx \\ y' &= y + ty\end{aligned}$$


$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & tx \\ 0 & 1 & ty \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Transformaciones geométricas

Matrix representation 2D

- Adición de una tercera coordenada para cada punto 2D:
 - (x, y, w) represents a point at location $(x/w, y/w)$
 - $(x, y, 0)$ represents a point at infinity
 - $(0, 0, 0)$ is not allowed



Sistema de coordenadas idóneo para representar transformaciones

Transformaciones geométricas

Matrix representation 2D

- Transformaciones básicas 2D como matrices 3x3:

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & tx \\ 0 & 1 & ty \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Translate

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} sx & 0 & 0 \\ 0 & sy & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Scale

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta & 0 \\ \sin \Theta & \cos \Theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Rotate

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & shx & 0 \\ shy & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Shear

Transformaciones geométricas

Matrix representation 2D

■ Las transformaciones afines son combinaciones de...

- Linear transformations, and
- Translations

$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Transformaciones geométricas

Matrix representation 2D

- Transformaciones proyectivas...
 - Affine transformations, and
 - Projective warps

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Transformaciones geométricas

Matrix representation 2D

- Las transformaciones pueden ser combinadas mediante multiplicación de matrices:

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \left(\begin{bmatrix} 1 & 0 & tx \\ 0 & 1 & ty \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \Theta & -\sin \Theta & 0 \\ \sin \Theta & \cos \Theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} sx & 0 & 0 \\ 0 & sy & 0 \\ 0 & 0 & 1 \end{bmatrix} \right) \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

$\mathbf{p}' = \mathbf{T}(tx,ty) \mathbf{R}(\Theta) \mathbf{S}(sx,sy) \mathbf{p}$

Transformaciones geométricas

Matrix representation 2D

- La representación matricial es una forma eficiente de representar una secuencia de transformaciones:

- General purpose representation
- Hardware matrix multiply
- Efficiency with premultiplication
 - » Matrix multiplication is associative

$$\mathbf{p}' = (T * (R * (S * \mathbf{p})))$$


$$\mathbf{p}' = (T * R * S) * \mathbf{p}$$

Transformaciones geométricas

Matrix representation 2D

- Precaución: el orden de las transformaciones influye

» Matrix multiplication is not commutative

$$\mathbf{p}' = \mathbf{T} * \mathbf{R} * \mathbf{S} * \mathbf{p}$$


“Global” “Local”

Transformaciones geométricas

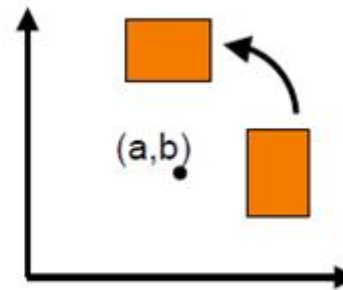
Matrix representation 2D

- Rotación Θ entorno a un punto arbitrario (a,b)

- $M = T(a,b) * R(\Theta) * T(-a,-b)$

The trick:

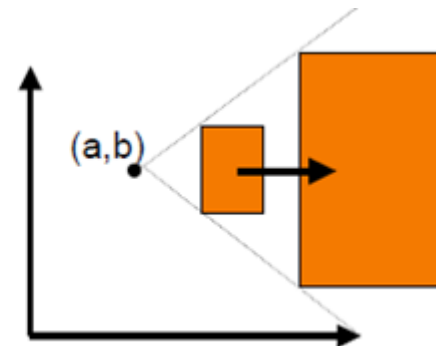
First, translate (a,b) to the origin.
Next, do the rotation about origin.
Finally, translate back.



- Escalado de s_x, s_y entorno a un punto arbitrario (a,b)

- $M = T(a,b) * S(s_x, s_y) * T(-a, -b)$

(Use the same trick.)



Transformaciones geométricas

Matrix representation 3D

- Misma idea que las transformaciones 2D
 - Homogeneous coordinates: (x,y,z,w)
 - 4x4 transformation matrices

$$\begin{bmatrix} x' \\ y' \\ z' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Transformaciones geométricas

Matrix representation 3D

$$\begin{bmatrix} x' \\ y' \\ z' \\ w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Identity

$$\begin{bmatrix} x' \\ y' \\ z' \\ w \end{bmatrix} = \begin{bmatrix} sx & 0 & 0 & 0 \\ 0 & sy & 0 & 0 \\ 0 & 0 & sz & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Scale

$$\begin{bmatrix} x' \\ y' \\ z' \\ w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & tx \\ 0 & 1 & 0 & ty \\ 0 & 0 & 1 & tz \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Translation

$$\begin{bmatrix} x' \\ y' \\ z' \\ w \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Mirror over X axis

Transformaciones geométricas

Matrix representation 3D

Rotate around Z axis:

$$\begin{bmatrix} x' \\ y' \\ z' \\ w \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\sin \Theta & 0 & 0 \\ \sin \Theta & \cos \Theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Rotate around Y axis:

$$\begin{bmatrix} x' \\ y' \\ z' \\ w \end{bmatrix} = \begin{bmatrix} \cos \Theta & 0 & -\sin \Theta & 0 \\ 0 & 1 & 0 & 0 \\ \sin \Theta & 0 & \cos \Theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Rotate around X axis:

$$\begin{bmatrix} x' \\ y' \\ z' \\ w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \Theta & -\sin \Theta & 0 \\ 0 & \sin \Theta & \cos \Theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

Transformaciones geométricas

Global deformations

- Alan Barr, SIGGRAPH '84
- A 3x3 transformation matrix affects all vertices
 - $P' = M(P)P$
- $M(P)$ can taper, twist, bend...

¿SIGGRAPH?

Transformaciones geométricas

SIGGRAPH

SIGGRAPH (short for **S**pecial Interest **G**roup on **GRAPH**ics and Interactive Techniques) is the name of the annual conference on computer graphics (CG) convened by the ACM SIGGRAPH organization. The first SIGGRAPH conference was in 1974. The conference is attended by tens of thousands of computer professionals. Past SIGGRAPH conferences have been held in Los Angeles, Dallas, New Orleans, Boston and elsewhere across the United States.

<http://www.siggraph.org/s2014/>

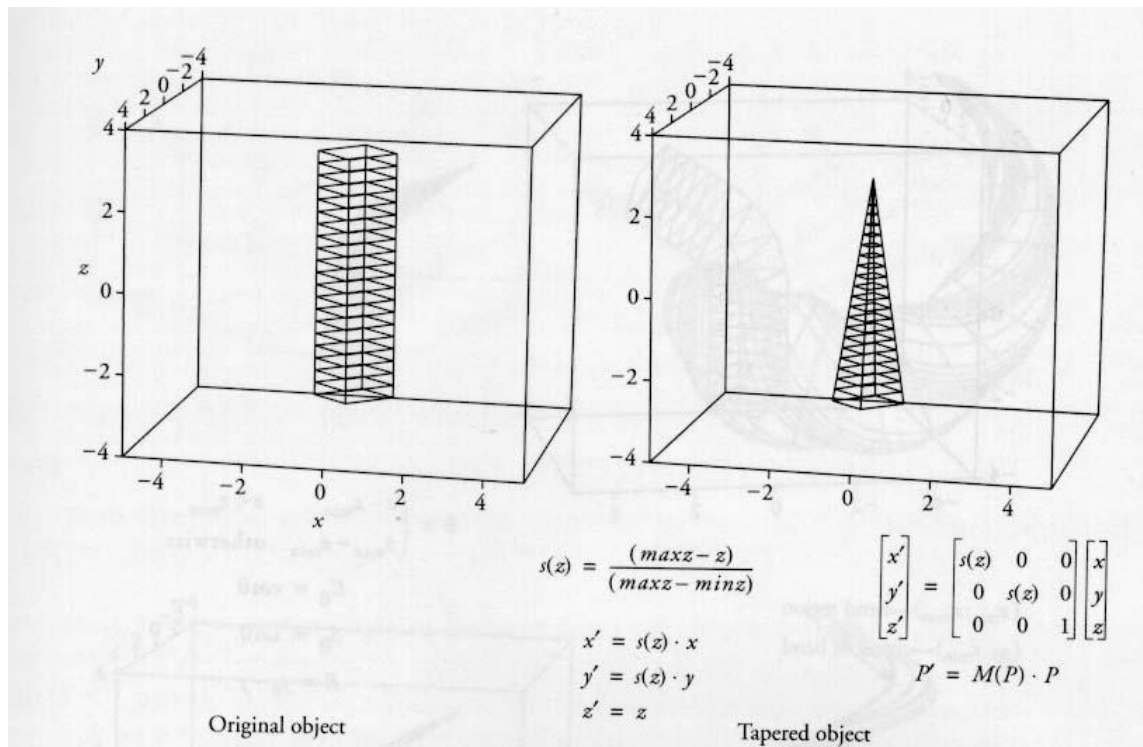
http://www.youtube.com/watch?v=GJ5L0zkTkB4&list=PLUPhVMQuDB_avy_6-qmDg5R-0pwCYvTt4&index=4



Transformaciones geométricas

Global deformations

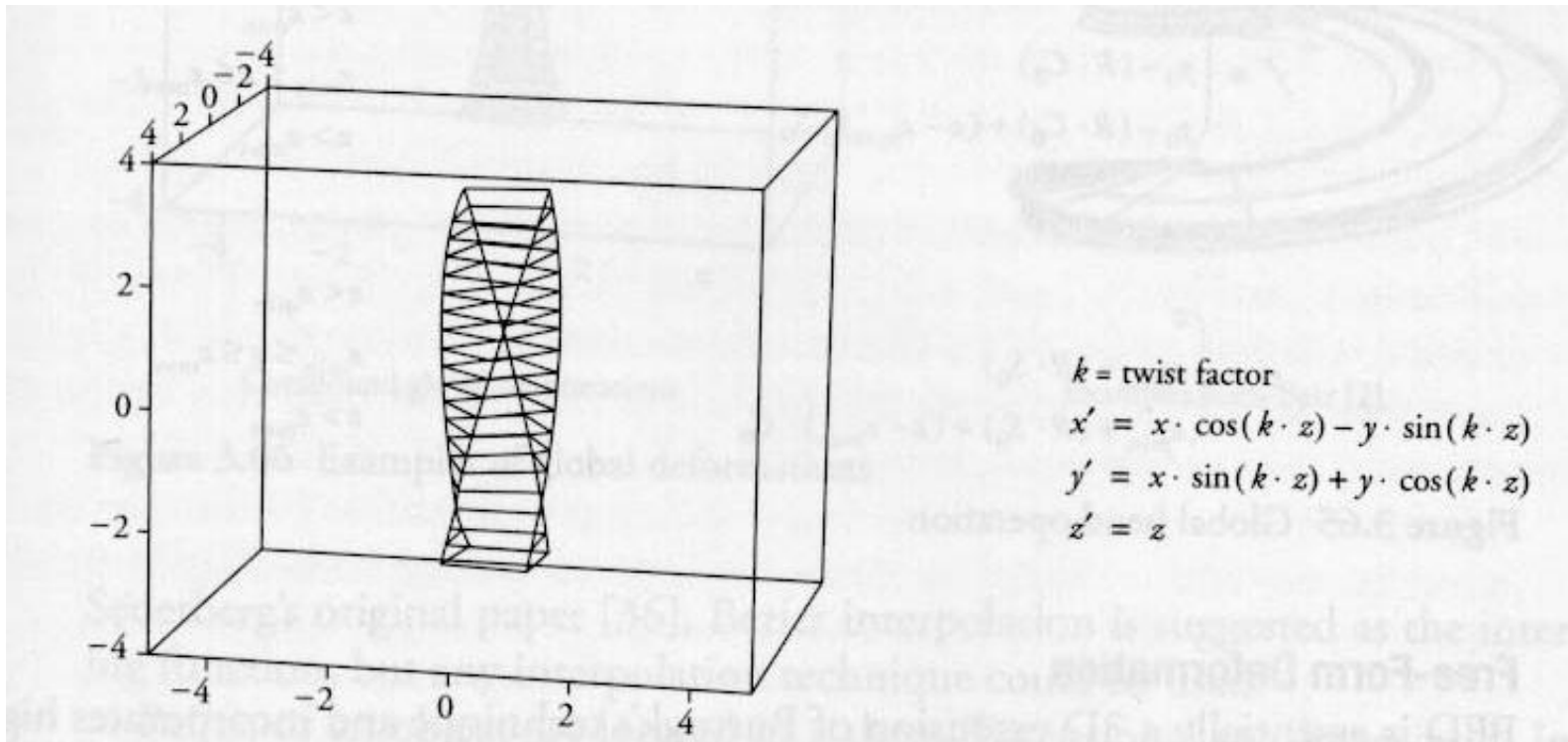
Taper



Transformaciones geométricas

Global deformations

Twist



Transformaciones geométricas

Global deformations

Bend

(z_{\min}, z_{\max}) —bend region

(y_0, z_{\min}) —center of bend

$$x' = x$$

$$y' = \begin{cases} y & z < z_{\min} \\ y_0 - (R \cdot C_\theta) & z_{\min} \leq z \leq z_{\max} \\ y_0 - (R \cdot C_\theta) + (z - z_{\max}) \cdot S_\theta & z > z_{\max} \end{cases}$$

$$z' = \begin{cases} z & z < z_{\min} \\ z_{\min} + (R \cdot S_\theta) & z_{\min} \leq z \leq z_{\max} \\ z_{\min} + (R \cdot S_\theta) + (z - z_{\max}) \cdot C_\theta & z > z_{\max} \end{cases}$$

$$\theta = \begin{cases} z - z_{\min} & z < z_{\max} \\ z_{\max} - z_{\min} & \text{otherwise} \end{cases}$$

$$C_\theta = \cos \theta$$

$$S_\theta = \sin \theta$$

$$R = y_0 - y$$

$$z < z_{\min}$$

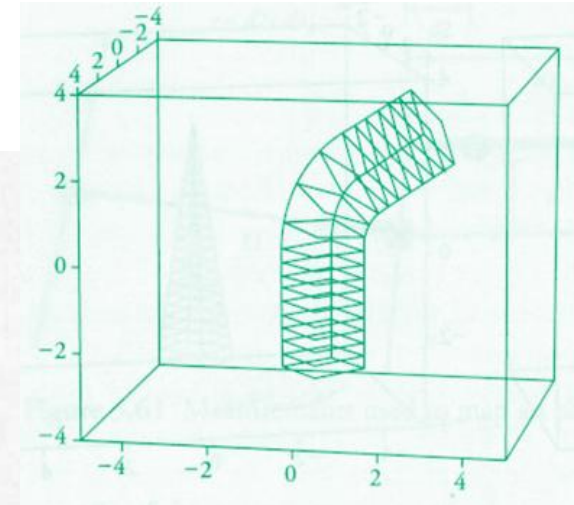
$$z_{\min} \leq z \leq z_{\max}$$

$$z > z_{\max}$$

$$z < z_{\min}$$

$$z_{\min} \leq z \leq z_{\max}$$

$$z > z_{\max}$$



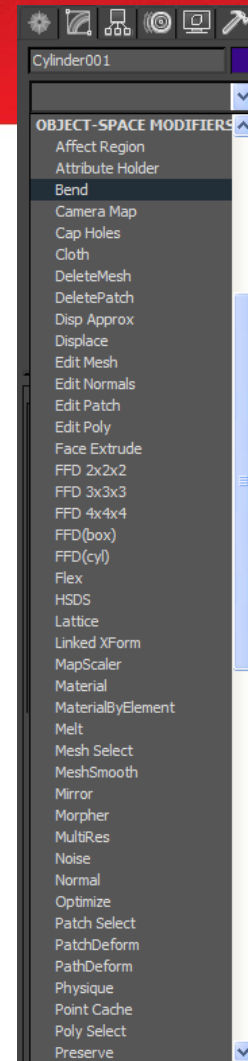
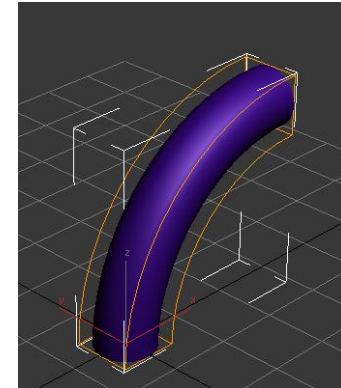
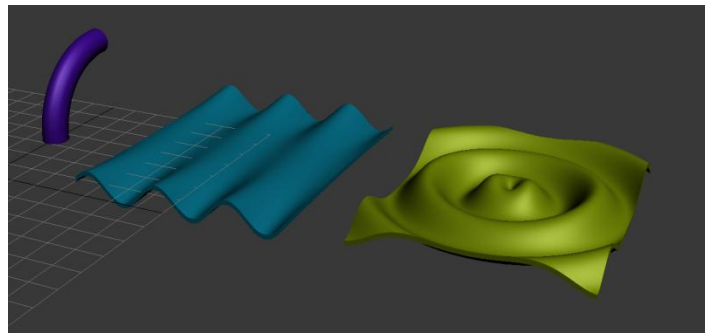
Transformaciones geométricas

Modifiers

3D Studio Max

- Bend
- Taper
- Twist
- Spherify
- Noise
- Ripple
- Skew
- Squeeze
- Stretch
- Wave

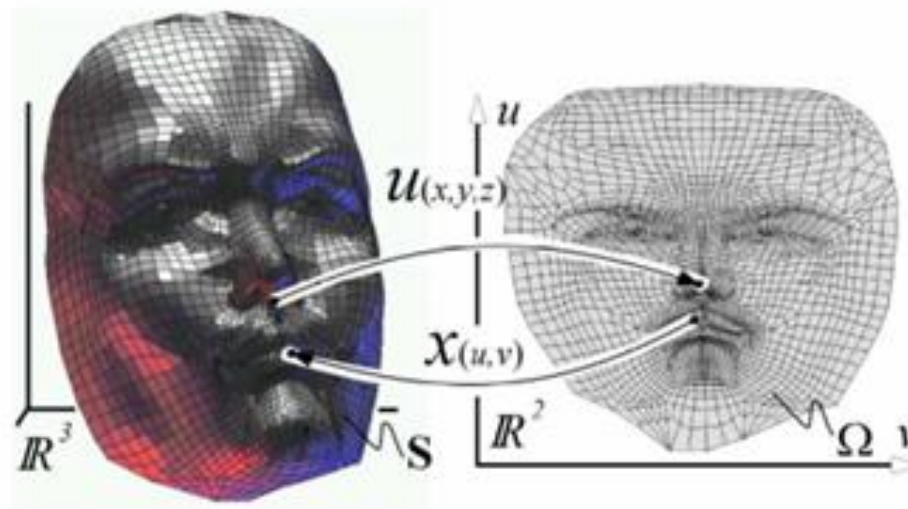
Object-space modifiers



Transformaciones geométricas

Polygonal Mesh Processing. Analysis.

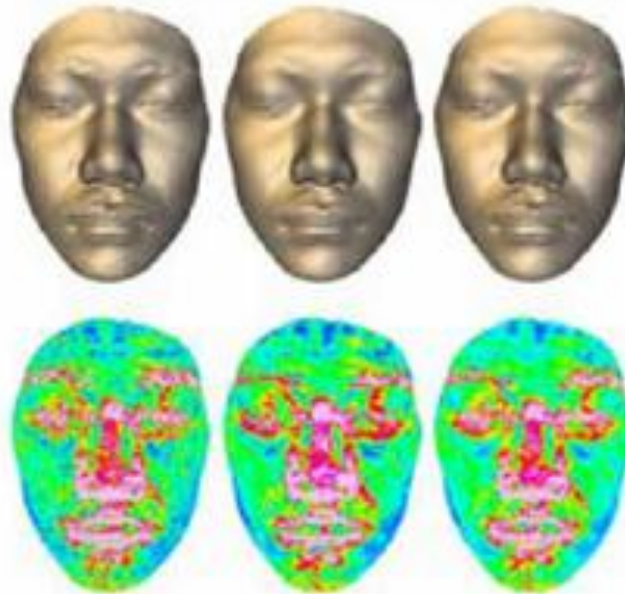
Parametrization



Transformaciones geométricas

Polygonal Mesh Processing. Analysis.

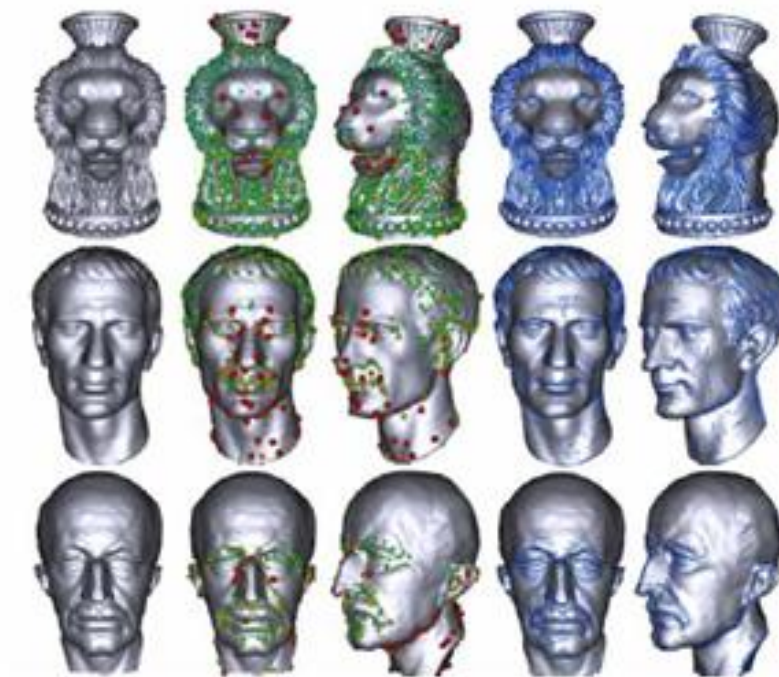
Differential geometry



Transformaciones geométricas

Polygonal Mesh Processing. Analysis.

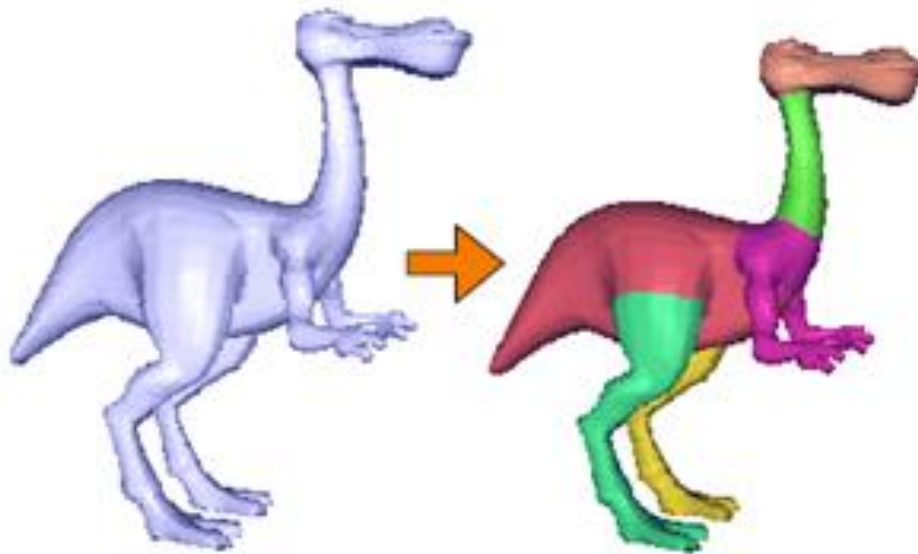
Feature detection



Transformaciones geométricas

Polygonal Mesh Processing. Analysis.

Segmentation



Transformaciones geométricas

Polygonal Mesh Processing. Editing.

Smoothing, sharpening, deformation, etc.



Smoothing



Sharpening

Transformaciones geométricas

Modifiers

3D Studio Max

- Cap holes
- Mesh smooth
- Optimize
- ProOptimizer
- Smooth
- Turbo smooth
- Welder

Object-space modifiers

