

~min sheet~

Static vs. Dynamics

We are going to split the life of a computer program into two phases

- static = anything that happens before running the program (compile time)

e.g. parsing, static analysis, type checking, lexing, macros, optimisation, compilation

staging

- dynamic = everything that happens when a program is running (runtime)

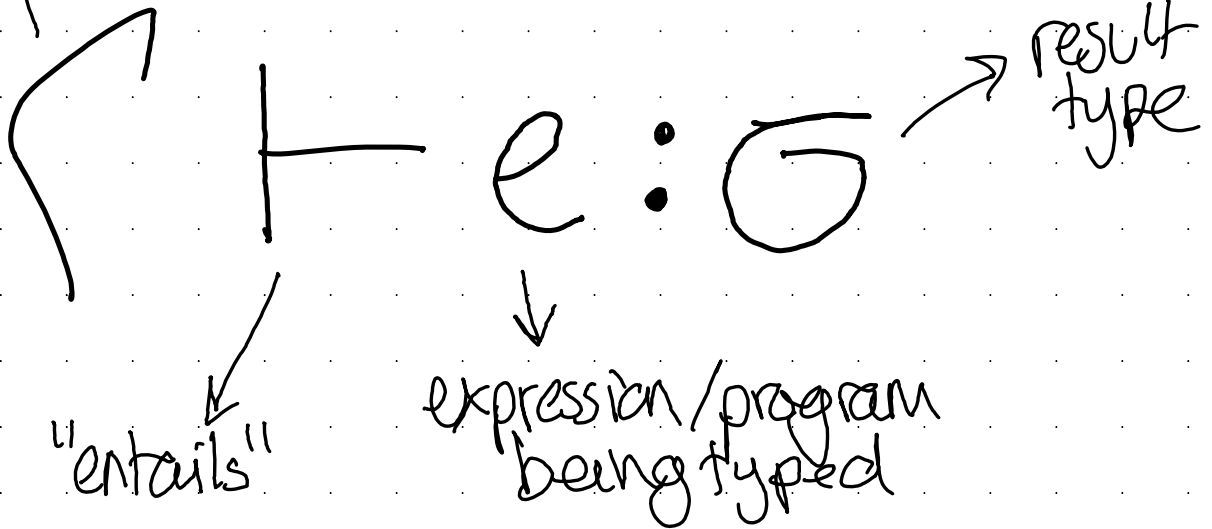
e.g. calculating the result, side-effects (IO, exceptions)

hurts planet.

mems

Typing Judgements

Context (environment):
Set of variables with type assignments
eg $\Gamma = \{x : T, y : G\}$



Terms = well-typed

preterm = unproven to be well typed

Terms = well-typed preterms

Binders

Binder = a language construct that closes over or binds variables

e.g. \forall or \exists

$\forall x.$

let

let $x = \dots$ in

λ

\Rightarrow

sometimes pattern matching

$\lim_{n \rightarrow \infty}$

$\sum \prod \dots$

Bound variables = variables bound by binder

Free variables = variables not bound by a binder

$\lambda x. xy$
binder λ bound x free y

Closed expr = one with no free vars
Open expr = one with free vars

open : $\lambda x. xy$
 $\lambda x. z$

closed : $\lambda t. t$
 $\lambda y. yy$

α -equivalence / convertibility states that the name of a bound variable doesn't matter

i.e. $\lambda x. x =_{\alpha} \lambda y. y$

$\lambda a. ab =_{\alpha} \lambda x. xb$

$\lambda xy. y =_{\alpha} \lambda yx. x$

A little language of numbers + strings - Syntax

Backus-Naur form (BNF)

$\tau ::= \text{Num} \mid \text{str}$ — concrete syntax
syntactic category bars allowed!

Abstract syntax = the syntax of the form as it should appear in the abstract syntax tree (AST)

Concrete syntax = user-friendly abbreviation of the abstract syntax

$e ::= x$ — "recursive" calls

$\text{num } [n]$	
$\text{str } [s]$	
$\text{plus}(e_1; e_2)$	$e_1 + e_2$
$\text{times}(e_1; e_2)$	$e_1 * e_2$
$\text{cat}(e_1; e_2)$	$e_1 ++ e_2$
$\text{len}(e)$	$ e $
$\text{let}(e_1; x.e_2)$	$\text{let } x \leftarrow e_1 \text{ in } e_2$

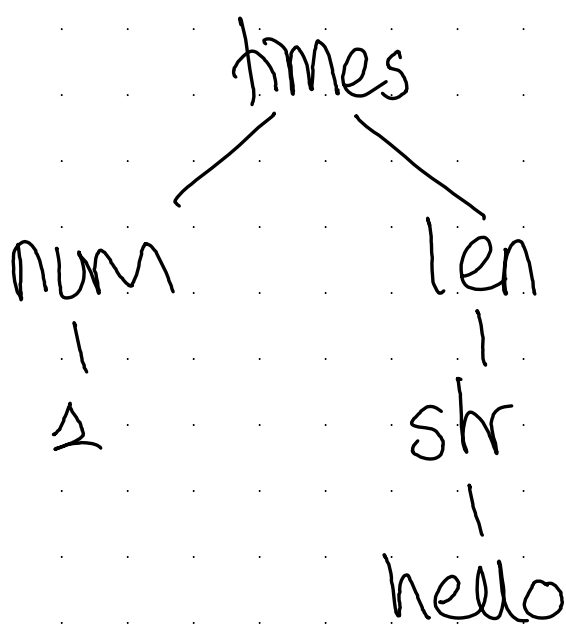
↑ abstract syntax ↑ concrete syntax here

$n \in \mathbb{N}$
 $s \in \Sigma^*$

eg. $\Sigma = \{a, b, c, \dots\}$

eg. $"" \in \Sigma^*$ "hello" $\in \Sigma^*$

$\text{times}(\text{num}[1]; \text{len}(\text{str}[\text{hello}]))$



A little language of numbers + strings - Typing!

linear:

$$\text{VAR} \frac{}{\Gamma, x:\tau \vdash x:\tau}$$

$$\text{VAR} \frac{}{x:\tau \vdash x:\tau}$$

$$\text{NUM} \frac{n \in \mathbb{N}}{\Gamma \vdash \text{num}[n] : \text{Num}}$$

$$\text{Str} \frac{s \in \Sigma^*}{\Gamma \vdash \text{str}[s] : \text{Str}}$$

$$\text{PLUS} \frac{\Gamma \vdash e_1 : \text{Num} \quad \Gamma \vdash e_2 : \text{Num}}{\Gamma \vdash \text{plus}(e_1, e_2) : \text{Num}}$$

$$\text{TIMES} \frac{\Gamma \vdash e_1 : \text{Num} \quad \Gamma \vdash e_2 : \text{Num}}{\Gamma \vdash \text{times}(e_1, e_2) : \text{Num}}$$

$$\text{CAT} \frac{\Gamma \vdash e_1 : \text{Str} \quad \Gamma \vdash e_2 : \text{Str}}{\Gamma \vdash \text{cat}(e_1, e_2) : \text{Str}}$$

$$\text{LEN} \frac{\Gamma \vdash e : \text{Str}}{\Gamma \vdash \text{len}(e) : \text{Num}}$$