

```
{-
These lines declare that `A` and `B` are principles, and the type checker
(not yet implemented) will make sure that all principles mentioned in types
are (at least) well-scoped, and possibly also check some security relationships
as well, e.g., does A trust B, and to what extent.
```

These lines are ignored by the interpreter.

```
-}
principal A
principal B
```

```
{-
`cmp` takes a secret input from both `A` and `B` and builds a circuit which
compares them, returning a boolean.
```

The input variable `xy` has type `Z[64]{isec:A,B}`, which reads as “a 64-bit integer as independent (i.e., not necessarily equal) secrets for each party `A` and `B`.” To access `A`'s value, we write `xy.A`, and likewise for `B` and `xy.B`. `xy.A` is a secret value, and can be embedded inside of a circuit with `~xy.A`. All parties share this circuit, and `A`'s value inside `~xy` will be provided as an input to the circuit when executed using a protocol (e.g. yao).

The access mode `isec` is distinguished from `ssec`, which reads as “shared secret”, in that `ssec` values have the added invariant that all parties have a local copy of the exact same value. E.g., when a result from mpc is revealed to some subset of parties. `ssec` values can be used to construct new circuits, whereas `isec` values cannot, or else we would have two parties evaluating different circuits, which would be bad.

The return type `B{ccir:A,B}` reads as “a circuit comprised of comparison operations on numeric types with embedded secret inputs from `A` and `B`”. The fact that a comparison operator is embedded **in** the circuit computation is tracked coarsely at the **type** level. E.g., it may not be possible to execute a `ccir` using `bgw`, and we want to throw a runtime error (and **type** error) **if** the programmer tries to do it.

The first two steps of the function embed secret inputs from `A` and `B` into single-node circuits—they are degenerate circuits with just the embedded secret value. The **type** of these circuits is `ncir`, which says “no operations”. The last step is a normal comparison operator which is overloaded syntactically to operate over circuit values, giving a circuit result **type** `ccir` which tracks the comparison operation.

```
-}
def cmp : Z[64]{isec:A,B} → B{ccir:A,B}
def cmp = λ xy →
  let x : Z[64]{ncir:A}
  let x = ~xy.A
  let y : Z[64]{ncir:B}
  let y = ~xy.B
  let r : B{ccir:B}
  let r = x ≤ y
  in r
```

```
{-
We have moved away from a monadic discipline for tracking effects, and are now
using a more traditional effect system, e.g., an effectful computation is a
function of a dummy argument `•` with an effect annotation over the arrow. The
effect in this function is {inp:A,B;rev:} which means “inputs are read from
parties `A` and `B`, but nothing is revealed to any part”. The thinking for now
```

is that it may be advantageous to track security-critical events in effect types, at the very least for auditing. If I am using a library function or some old code, what I really want to know from a security point of view is whether or not (1) secret inputs are read from disk, (2) any mpc protocols are executed, and (3) what parties learned the results of mpc. In particular, if a function has no effect, we know none of these things have happened inside the function, and we may decide it's not worth our time to audit (from a security perspective). I realize this isn't the whole story, e.g., we may be crucially depending on the functionality of some library function to have the correct ideal functionality, but the idea is here, and we can keep it around and discuss or drop it.

The return type is `ℬ{yshare:A,B}` which reads as “a boolean which is encrypted and recoverable by `A` and `B` by combining encrypted values (e.g., secret shares), and readily embeddible inside a future circuit which is later executed using yao”. Basically this function has decided to execute the circuit `cmp` using yao, and what comes back is like a secret share, and it can either be revealed, or embedded inside a future yao computation.

Although this doesn't occur in this example file, suppose you took two values `a,b : ℬ{yshare:A,B}` and xor'd them like so `a ⊕ b`. The resulting type would be `ℬ{bcir:yshare:A,B}`, that is, a circuit with boolean operations and embedded yao encrypted values. Maybe we should just call this `ℬ{ycir:A,B}`, because the only protocol it makes sense to run it with is yao.

The first step of `cmp-mpc` enters parallel mode for both `A` and `B` by the syntax `{par:A,B}`. The read operation will see a local file “el-input.txt” for each party `A` and `B`. In our simulator, these live in `examples-data/A` and `examples-data/B`. The result is an `isec:A,B` which again means “independent secrets for both A and B”.

The final step of `cmp-mpc` executes the circuit constructed by `cmp xy` using `yao` between parties `A` and `B`. We could have written, e.g., `mpc{yao:C,D}` which would have resulted in (1) A and B send secret-shares of their inputs to C and D, (2) C and D execute yao protocol, and (3) C and D end up with (secret-share) encrypted results which can later be revealed.

-}

```
def cmp-mpc : 1 → {inp:A,B;rev:} ℬ{yshare:A,B}
```

```
def cmp-mpc = λ • →
```

```
  let xy : Z[64]{isec:A,B}
```

```
  let xy = {par:A,B} read Z[64] "el-input.txt"
```

```
  let r : ℬ{yshare:A,B}
```

```
  let r = mpc{yao:A,B} cmp xy
```

```
  in r
```

{-

`cmp-mpc-rev` run `cmp-mpc` and then reveals the result to each other. Here the `reveal` expression takes as input `ℬ{yshare:A,B}` and returns as output `ℬ{ssec:A,B}`. Just as with `mpc`, you could write `reveal{C,D}` and the meaning of that program is that `A` and `B` send their shares to both `C` and `D`, who then recombine them to learn the result.

-}

```
def cmp-mpc-rev : 1 → {inp:A,B;rev:A,B} ℬ{ssec:A,B}
```

```
def cmp-mpc-rev = λ • →
```

```
  let r : ℬ{yshare:A,B}
```

```
  let r = cmp-mpc •
```

```
  let p : ℬ{ssec:A,B}
```

```
let p = reveal{A,B} r
in p
```

```
{-
`main` just runs `cmp-mpc-rev` to completion. Running this example shows the
result of `main`
-}
def main : B{ssec:A,B}
def main = cmp-mpc-rev •
```