

```
{-
These lines declare what principles that are present. The type
checker (not yet implemented) will make sure that all principles
mentioned in types are (at least) well-scoped, and possible also
check some security relationships as well, e.g., does A trust B, and
to what extent.
```

These lines are ignored by the interpreter.

```
In this example, A and B have secret inputs. C and D will receive
shares of A and B's secret inputs in order to compute over them
through an MPC protocol. E and F will then receive output shares from
C and D in order to reconstruct the answer, which is only learned by
E and F (not A, B, C or D).
-}
```

```
-- input parties
principal A
principal B
-- compute parties
principal C
principal D
-- output parties
principal E
principal F
```

```
{-
`cmp` takes a secret input from both `A` and `B` and builds a yao
boolean "secret share" which is (conceptually) immediately sent to
(and shared by) C and D. Specifying yao at this point in the program
(as opposed to when the final results is "revealed") allows for
(e.g.) EMP-style on-the-fly evaluation of a protocol as an
optimization.
```

The input variable `xy` has type $\mathbb{Z}\{\text{isec:A,B}\}$, which reads as "two integers, one for each party `A` and `B`, as independent (i.e., not necessarily equal) secrets." To access A's value, we write `xy.A`, and likewise for B and `xy.B`. `xy.A` is a secret value, and is (yao) "secret-shared" (i.e., encrypted and embeddable inside of a circuit) to C and D by $\text{share}\{\text{yao:C,D}\} \text{xy.A}$. C and D now hold shares of A's secret which will be provided as an input to the next circuit (in this case, a yao garbled circuit with a single comparison) when executed.

The access mode `isec` is distinguished from `ssec`, which reads as "shared secret", in that `ssec` values have the added invariant that all parties have a local copy of the exact same value. E.g., when a result is revealed to some subset of parties with the `reveal` operation. `ssec` values can be used to construct new circuits, whereas `isec` values cannot, or else we would have two parties evaluating different circuits potentially, which would be bad.

The return type $\mathbb{B}\{\text{yao:C,D}\}$ reads as "A boolean value embedded in a yao secret share that is shared among C and D." The type checker will check for valid operations to be used in a mpc computations. In this example, comparison (\leq) is valid because it is supported by the yao protocol. E.g., it may not be possible to execute a circuit that uses comparisons using bgw, so the type checker would reject a program that tried to do so. In this example, we have already committed to

yao but that may not always be the case. Regarding the $\{inp:A,B\}$ part of the function type, this annotation specifies from which parties were secret inputs secret-shared and computed on in some protocol. This enables checking security relationships between principles and flagging violations of the trust model. The interpreter ignores input effect annotations such as this.

The first two steps of `cmp` embed secret inputs from A and B into yao "secret-shares". The last step is a normal comparison operator which is overloaded syntactically to operate over secret share values by executing the protocol over the secret-share. Since we are using yao, we can use the \leq operator unlike in say, bgw, where comparison like this isn't possible. In the future it will be possible to pick whether or not protocol execution operates on-the-fly with small circuits (e.g., in EMP), or as one large circuit in a single protocol. So conceptually $\mathbb{B}\{yao:C,D\}$ is a secret share, and $x \leq y$ executes a circuit of size 1, but in practice $\mathbb{B}\{yao:C,D\}$ could be a circuit constructed by each party, $x \leq y$ builds a larger circuit out of smaller ones, and execution of the protocol is delayed until some later point.

```
-}
```

```
def cmp : Z{isec:A,B} → {inp:A,B} B{yao:C,D}
def cmp = λ xy →
  let x : Z{yao:C,D}
  let x = share{yao:C,D} xy.A
  let y : Z{yao:A,B}
  let y = share{yao:C,D} xy.B
  let r : B{yao:C,D}
  let r = x ≤ y
  in r
```

```
{-
We have moved away from a monadic discipline for tracking effects,
and are now using a more traditional effect system, e.g., an
effectful computation is a function of a dummy argument `•` with an
effect annotation over the arrow. The effect in this function is
 $\{inp:A,B;rev:E,F\}$  which means "inputs are read from parties A and B
and outputs are revealed to E and F." The thinking for now is that it
may be advantageous to track security-critical events in effect
types, at the very least for auditing. If I am using a library
function or some old code, what I really want to know from a security
point of view is whether or not (1) secret inputs are read from disk,
(2) any mpc protocols are executed, and (3) what parties learned the
results of mpc. In particular, if a function has no effect, we know
none of these things happened inside the function, and we may decide
it's not worth out time to audit (from a security perspective). I
realize this isn't the whole story, e.g., we may be crucially
depending on the functionality of some library function to have the
correct ideal functionality, but the idea is here, and we can keep it
around and discuss or drop it.
```

The return type is $\mathbb{B}\{ssec:E,F\}$ which reads as "an unencrypted boolean value known by E and F." Unlike with `isec` values, `ssec` values must be the same among all parties involved.

The first step of `cmp-mpc` enters parallel mode for both A and B by the syntax $\{par:A,B\}$. The read operation will see a local file "el-input.txt" for each party A and B. In our simulator, these live

in ``examples-data/A`` and ``examples-data/B`` respectively. The result is an ``isec:A,B`` which again means "independent secrets for both A and B."

The second step of ``cmp-mpc`` executes the circuit constructed by ``cmp xy`` using ``yao`` between parties C and D. However, this may be a strict or lazy "execution" in that, depending on the protocol, the evaluation might not actually happen until we need a result or force it to happen. Another note: we could have written, e.g., ``yao:A,B`` to have parties A and B be the computation parties as well as the input parties.

The final step of ``cmp-mpc`` reveals the output to parties E and F. This conceptually consists of C and D sending their "shares" of the result value to both E and F, which each combine them to learn the unencrypted value of the result. In the case that the multiparty computation is delayed as a circuit, the execution of protocol takes place as well.

-}

```
def cmp-mpc :  $\mathbb{1} \rightarrow \{\text{inp}:A,B;\text{rev}:E,F\} \mathbb{B}\{\text{ssec}:E,F\}$ 
```

```
def cmp-mpc =  $\lambda \bullet \rightarrow$ 
```

```
  let xy :  $\mathbb{Z}\{\text{isec}:A,B\}$ 
```

```
  let xy = {par:A,B} read  $\mathbb{Z}$  "el-input.txt"
```

```
  let r :  $\mathbb{B}\{\text{yao}:C,D\}$ 
```

```
  let r = cmp xy
```

```
  let o :  $\mathbb{B}\{\text{ssec}:E,F\}$ 
```

```
  let o = reveal{E,F} r
```

```
  in o
```

{-

This one-liner shows how you might do the steps in ``cmp-mpc`` and ``cmp`` in many fewer operations. Notice that the function annotation reads `{inp:A,B;rev:E,F}` meaning that this function send outputs to E and F based on inputs from A and B. We anticipate that the annotations ``share{yao:C,D}`` will not be necessary as we develop sufficiently fancy type inference.

-}

```
def one-liner :  $\mathbb{1} \rightarrow \{\text{inp}:A,B;\text{rev}:E,F\} \mathbb{B}\{\text{ssec}:E,F\}$ 
```

```
def one-liner =  $\lambda \bullet \rightarrow$ 
```

```
  let xy = {par:A,B} read  $\mathbb{Z}$  "el-input.txt"
```

```
  in reveal{E,F} (share{yao:C,D} xy.A)  $\leq$  (share{yao:C,D} xy.B)
```

{-

``main`` just runs both the verbose ``cmp-mpc`` and the shortened ``one-liner`` and returns the two results as a pair. Note the effect annotation in the top-level type, which indicates that execution of `main` has input and reveal effects, in addition to returning a pair of results.

-}

```
def main :  $\{\text{inp}:A,B;\text{rev}:E,F\} \mathbb{B}\{\text{ssec}:A,B\} \times \mathbb{B}\{\text{ssec}:A,B\}$ 
```

```
def main = cmp-mpc  $\bullet$  , one-liner  $\bullet$ 
```