# Visualization of Thermally-driven Flow over the Alpine Region

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#### **Abstract**

The goal of this thesis was to create a tool for computing and displaying wind trajectories. We would then use it to visualize several test cases from meteorological data. Said data deals with Föhn, a phenomenon that is associated with warm and dry winds in the northern parts of the alps, also bad weather on the south side.

While the focus lay on visualization and analysis of results initially, it later shifted towards reproducing trajectories from a similar tool and improving on that. That worked in the sense that we can obtain trajectories that are practically the same. We can also do it faster and with fewer errors. The visualization part ended up as more of a debugging tool than a user-friendly application.

# Zusammenfassung

Deutsche Version kommt erst, wenn die englische Version fertig ist.

## **Contents**

Lis	st of	Figures	vii
Lis	st of	Tables	ix
1	Intro	oduction	1
2	2.1 2.2 2.3	kground  Data	<b>3</b> 3 4 4
3	3.1 3.2 3.3 3.4	Numeric integration	7 7 8 8 9 9 9
<b>4</b> 5	Res 4.1 4.2 4.3	ults   A look at trajectories   Comparison   Performance    clusion	11 11 14 14
		raphy	18

# **List of Figures**

2.1	points	5
3.1	Interpolation procedure for sampling at the orange point: Order and weights depend on the method used	8
3.2	Structure of the output data: $x_{(i,j)}$ is the value of variable $x$ on trajectory $i$ after the $j$ th timestep	10
4.1	Color according to: Trajectory index(top left), temperature(top right), pressure(bottom left), relative humidity(bottom right)	12
4.2	Colors according to same criteria as in figure 4.1 above. The colors in the upper left case also depend on the trajectory set: Purple/blue forward, orange/black	
	backward	12
4.3	A closer look of the top left part of figure 4.1	13
4.4	Relative humidity is high below and low above	13
4.5	Average distance between LAGRANTO trajectories and ours, timestep is $h =$	
	$1min$ on top, $h = 2min$ in the middle, $h = 5min$ on the bottom $\dots$	15
4.6	Times for tracing a variable number of particles over 60 timesteps and 7 data files	16

## **List of Tables**

2.1	Important variables																							Z
4.1	minportant variables		•			•	•	•	•			•	•	•	•	•	•		•		•	•		_

1

#### Introduction

A common problem in meteorology is to find wind trajectories with certain properties, e.g. passing through a certain region, carrying particularly warm or humid air, etc. LAGRANTO ([SW15]) is an existing Fortran-based program for computing trajectories from wind velocity fields. We aim to create a similar program in C++. While reconstructing LAGRANTO is our base goal, we would like to get better performance and/or results as well.

There are LAGRANTO variants for different types of input data. We work with the COSMO version because all our input data is in the COSMO model.

For the visualization, we use VTK, the Visualization Tool Kit ([SML06].

### **Background**

#### 2.1 Data

We work on a set of NetCDF files containing assorted meteorological data in the COSMO model. Most of the files contain data at a certain point in time and have names like "lfff00000000.nc". The number in the filename corresponds to the time past the reference date using the format DDHHMMSS, so for example "lfff00015000.nc" would contain the data at one hour and fifty minutes. In addition, there is a file "lfff00000000c.nc" (note the c) which holds constant variables like the height of the surface. The reference time for our data is 2016, Nov, 21, 00:00 and the files go from "lfff00000000.nc" (reference date) to "lfff03225000.nc" (3 days 22 hours 50 minutes later) with 10 minutes between files.

Most of the important variables are stored as three-dimensional arrays. The three dimensions are called rlon, rlat and level. rlon and rlat are coordinates in a rotated geographical coordinate system. The levels correspond to the vertical position of a point, but it is not a simple linear transformation. Instead, the constants file holds the necessary information to convert levels to actual height. Further details can be found in section 2.3. Unless noted otherwise, the grid size for our data is always  $1158 \times 774 \times 80$ .

Table 2.1 gives an overview of the most interesting variables. The three variables UVW define the velocity field: U is the eastward (in the rotated system) component of the wind, V the northward component, and W the upward component. All three have the same units (m/s) and similar but not equal grids. The grids are staggered: All vertices in one grid are translated by half a cell size in one direction. Section 2.2 describes how the staggered grids are handled.

HHL maps the level of a grid point to a physical height. Like W, it is staggered in the vertical direction and needs to be destaggered before it can be used with most other variables. HHL is important because the particle positions have a real height in meters as their third component and there needs to be a way to find grid coordinates from the particle position.

Name	Description	Dimensions	Time-invariant	Staggering	Unit
U	rlon component of velocity	3	no	rlon	m/s
V	rlat component of velocity	3	no	rlat	m/s
W	vertical component of velocity	3	no	level	m/s
HHL	level-to-height map	3	yes	level	m
HSURF	height of surface	2	yes	none	m
P	pressure	3	no	none	Pa
T	temperature	3	no	none	K
RELHUM	relative humidity	3	no	none	%

**Table 2.1:** Important variables

HSURF contains the height of the surface for given (rlon, rlat) coordinates. It is mainly used to prevent particles from leaving the domain through the ground.

The pressure P, temperature T and relative humidity RELHUM are not relevant for the tracing, but they work well as examples of the kind of data one may wish to track along the trajectories.

#### 2.2 Destaggering

U, V, W and HHL are given in staggered grids, recognizable by using srlon, srlat and level1 for certain axes. The staggered grid coordinates lie halfway between the unstaggered grid points. Destaggering is done by averaging the values at two vertices that are adjacent in the staggering direction, then storing the result at the grid position between those vertices. Figure 2.1 shows how staggered (srlon, rlat) and (rlon, srlat) grids are converted to (rlon, rlat). The image also shows that the destaggered version of the grid has one row/column less than the staggered original.

The dimensions of the UVW grid are effectively  $1157 \times 773 \times 80$ . Compared to the default size, this is one element less in rlon and rlat. The number of levels remains at 80 because the staggered axis level1 has size 81.

#### 2.3 Conversion between coordinate systems

The velocities U, V, W, as well as other variables like temperature, are defined on a regular grid with axes corresponding to (rlon, rlat, level).

rlon and rlat can be converted into lon and lat given the (global) coordinates of the rotated north pole ( $\lambda_{pole}$ ,  $\phi_{pole}$ ). In our data,  $\phi_{pole}$  is always  $43^{\circ}$  and  $\lambda_{pole}$  is  $-170^{\circ}$  Converting coordinates

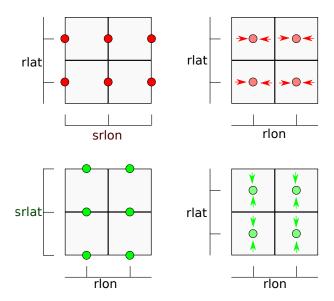


Figure 2.1: Left: Points in staggered grids; Right: Destaggering by averaging two staggered points

nates  $(\lambda_r, \phi_r)$  in the rotated system to the global coordinates  $(\lambda_g, \phi_g)$  is done as follows:

$$\phi_g = \sin^{-1}(\cos\phi_{pole} \cdot \cos\phi_r \cdot \cos\lambda_r + \sin\phi_{pole} \cdot \sin\phi_r); \tag{2.1}$$

$$c_1 = \sin \phi_{pole} \cdot \cos \lambda_r \cdot \cos \phi_r + \cos \phi_{pole} \cdot \sin \phi_r \tag{2.2}$$

$$c_2 = \sin \lambda_r \cdot \cos \phi_r \tag{2.3}$$

$$zarg1 = \sin \lambda_{pole} \cdot c_1 - \cos \lambda_{pole} \cdot c_2 \tag{2.4}$$

$$zarg2 = \cos \lambda_{pole} \cdot c_1 + \cos \lambda_{pole} \cdot c_2 \tag{2.5}$$

$$\lambda_q = atan2(zarg1, zarg2) \tag{2.6}$$

The vertical coordinates z are given in meters above sea level and need to be mapped to grid levels. To that purpose, we have the time-invariant scalar field HHL which maps (staggered) levels at specific grid points to their height.

The fact that the values are stored in a regular grid that corresponds to an irregular real shape means that one needs to be careful when interpolating values given at coordinates between grid points. Two possible methods are discussed in the following chapter in section ??.

#### **Method**

#### 3.1 Numeric integration

Solving differential equations of all types is a topic for itself. In this section we limit ourselves to describing the methods we use to find the next point of a trajectory given the time-dependent velocity field UVW(p,t), the starting position  $p_{t_0}$  and a timestep of size h.

LAGRANTO uses an iterative variant of Euler's method. The next point  $p_{t_0} + h$  is computed using the average of the velocities at the original point  $p_{t_0}$  and the current guess for  $p_{t_0} + h$ . This method is related to the explicit trapezoidal rule: In the time-invariant case, stopping at  $q_2$  is equivalent to using the explicit trapezoidal rule.

Iterative Euler

$$v_0 = UVW(p_{t_0}, t_0) (3.1)$$

$$v_1 = UVW(p_{t_0}, t_0 + h) (3.2)$$

$$q_1 = p_{t_0} + h \frac{v_0 + v_1}{2} \tag{3.3}$$

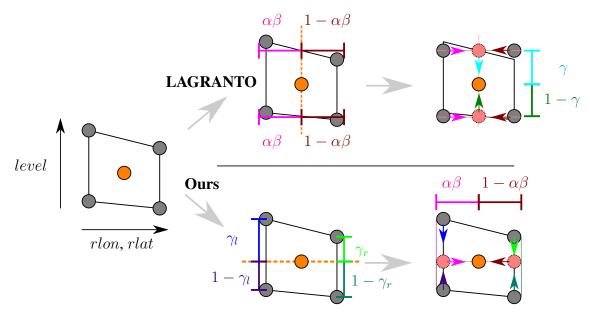
$$v_2 = UVW(q_1, t_0 + h) (3.4)$$

$$q_2 = p_{t_0} + h \frac{v_0 + v_2}{2} \tag{3.5}$$

$$v_3 = UVW(q_2, t_0 + h) (3.6)$$

$$p_{t_0+h} = p_{t_0} + h \frac{v_0 + v_3}{2} \tag{3.7}$$

We preferred to use the classical Runge-Kutta integration scheme. It uses four samples of UVW per iteration like the iterative Euler method, but according to TODO cite that page the iterative



**Figure 3.1:** Interpolation procedure for sampling at the orange point: Order and weights depend on the method used

Euler method has an error  $O(h^3)$  per step whereas the Runge-Kutta method has the lower error  $O(h^5)$  (see for example [?]).

Classical Runge-Kutta

$$k_1 = UVW(p_{t_0}, t_0) (3.8)$$

$$k_2 = UVW(p_{t_0} + k_1 \frac{h}{2}, t_0 + \frac{h}{2})$$
(3.9)

$$k_3 = UVW(p_{t_0} + k_2 \frac{h}{2}, t_0 + \frac{h}{2})$$
(3.10)

$$k_4 = UVW(p_{t_0} + k_3h, t_0 + h) (3.11)$$

$$p_{t_0+h} = p_{t_0} + (k_1 + 2k_2 + 2k_3 + k_4) \frac{h}{6}$$
(3.12)

#### 3.2 Sampling

Sampling the velocity field UVW at a certain position (x,y,z) and time t is a common operation during particle tracing. Because UVW is defined in m/s on a (rlon, rlat, level) grid and the position is given in  $(^{\circ}, ^{\circ}, m)$  some conversions are necessary.

#### 3.2.1 Using local level heights

Mapping x and y to positions in the (rlon, rlat) grid is done using the fact that the grid is rectangular and regular: Assuming  $(\lambda_0, \phi_0)$  are the (rlon, rlat) coordinates of the grid point (0,0) and the distance to the next vertex is  $\Delta_{\lambda}$  (in rlon direction) or  $\Delta_{\phi}$  (in rlat direction), the

grid coordinates are obtained from the real coordinates (x,y) as  $(\frac{x-\lambda_0}{\Delta_\lambda},\frac{y-\phi_0}{\Delta_\phi})$ . By rounding those grid coordinates up or down we get the coordinates of the nearest grid points.

The upper part of Figure 3.1 shows how LAGRANTO interpolates between levels: In a first step, two level heights for the upper and lower level are constructed (shown as split pink and dark red lines). This requires a binary search to locate two levels for the z-coordinate of the sampling point. LAGRANTO essentially performs trilinear interpolation in a box-shaped cell whose exact position and height depends depends on (x,y). Notice how in the third step the corner points have been moved slightly up or down: The differing real heights of the grid points only matter when determining the local level heights. For the final interpolation, all four corner points on one level are considered to be at the same height.

There are three interpolation weights  $(\alpha, \beta, \gamma)$  for the axes (rlon, rlat, level). All of them are computed as  $(\frac{x-x_0}{x_1-x_0}, \frac{y-y_0}{y_1-y_0}, \frac{z-z_0}{z_1-z_0})$ , where  $x_0$  and  $y_0$  are the coordinates of the western and southern grid points and  $z_0$  the (interpolated) height of the lower level.  $(x_1, y_1, z_1)$  is the position of the upper northeastern corner.

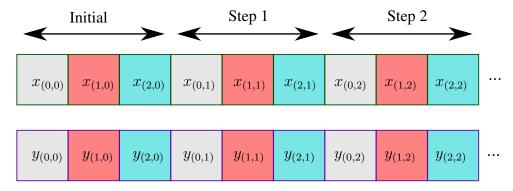
#### 3.2.2 Using adjacent level heights

Finding the grid coordinates of (x,y) and the bilinear interpolation weights  $\alpha$  and  $\beta$  along the rlon and rlat axes is the same as in the previous subsection.

The lower part of figure 3.1 shows how we compute the interpolated value at the orange sample point. On each of the four (two in the picture) columns, we compute interpolation weights  $\gamma_i = \frac{z-z_{0i}}{z_{1i}-z_{0i}}$  after finding lower and upper heights  $z_{0i}$  and  $z_{1i}$  with a binary search on column i in HHL. The last step is bilinearly interpolating between those four values. The weights for the horizontal interpolation (magenta and dark red in the picture) are the same that LAGRANTO uses. For the vertical interpolation, LAGRANTO uses only one set of weights ( $\gamma$  and  $\gamma$ ). Our version has different weights on each column (the pairs for  $\gamma_l$  and  $\gamma_r$  are visible in the picture), making the sampling process slightly more complicated and hopefully accurate.

#### 3.3 Implementation

The tracing process starts by asking the user for initial points, start and end time, size of the timestep, and additional settings like which variables to track, what type of integrator to use, plus a few other options that matter for debugging and comparing to LAGRANTO (mostly concerning how UVW is sampled). After allocating space for the output data, the UVW fields are extracted from the first three appropriate files. As the simulation runs, the oldest field is regularly replaced by new UVW from the next file in line, minimizing the memory needed at runtime. At each step, all trajectories have to be advanced by h. Those that have left the domain are kept at their last positions while the others get positions for the next timestep based on the velocity at their current position.



**Figure 3.2:** Structure of the output data:  $x_{(i,j)}$  is the value of variable x on trajectory i after the jth timestep

#### 3.3.1 Tracing output

The results from the particle tracing are written into a NetCDF file which contains an array for each variable. Time, coordinates in both (lon, lat) and (rlon, rlat), and height are always stored. Other variables like temperature or pressure need to be included in the initial input.

The number of elements per array is  $N_{tra} \cdot (N_{steps} + 1)$ , where the number of trajectories is  $N_{tra}$  and  $N_{steps}$  is the number of integration steps. The arrays are ordered according to timestep first and trajectory second. Figure 3.2 shows an example with 2 arrays, 3 trajectories (gray, red, blue), and 5 timesteps, for a total of 18 elements per array.

This format matches the output file of LAGRANTO, allowing us to compare the results directly.

#### 3.4 Analysis

Qualitative: We visualize the trajectories using VTK ([SML06]). The trajectories are loaded from an output file and drawn in 3D. The user can move the camera to get a better view. A surface obtained from HHL is also displayed to give a context beyond just the trajectory shape.

rlon and rlat or lon and lat (depending on the settings) correspond to the x and y axes of the renderer. For comparing the results to those from LAGRANTO, the global coordinates (lon, lat) are used because LAGRANTO includes only those in its output. The coordinates on the vertical axis z are rescaled by a factor of  $5 \cdot 10^{-5}$ . While this rescaling does not lead to exact proportions (one unit in horizontal direction does not correspond to the same distance as one unit in vertical direction), it helps make the shapes recognizable. The rescaling is necessary because the x and y values are in degrees and the z values are in meters.

Quantitative: We compare different integrators by giving them the same input and measuring the average distance between their outputs over time. We split the distance into a horizontal and vertical component because the units are different and the total distance would be dominated by the much more chaotic vertical part otherwise.

We use the output from LAGRANTO as a reference and look how the difference to our method evolves over time.

#### Results

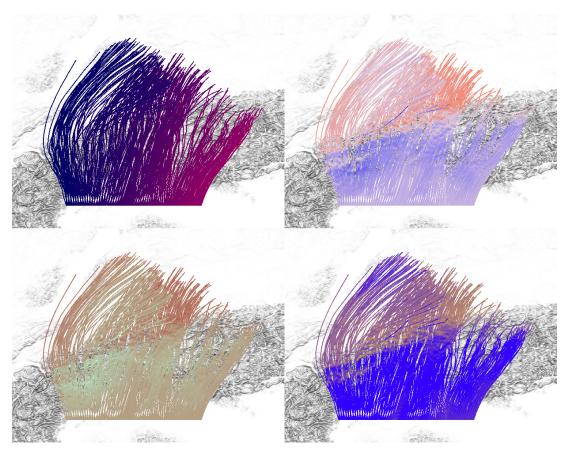
#### 4.1 A look at trajectories

Figures 4.1 and 4.2 show examples of trajectories we computed and visualized. In the top left part, each trajectory has a constant color which depends on its index: Starting at blue for the first trajectory and ending at purple. Figure 4.2 includes another color scheme (black-orange) for the backward trajectories. The upper right part of is colored according to temperature: Blue is cold, white is  $0^{\circ}$ C, red is warm. The lower two sections visualize pressure (red at high values, bright at low ones) and relative humidity (yellow at 0% and blue at 100%).

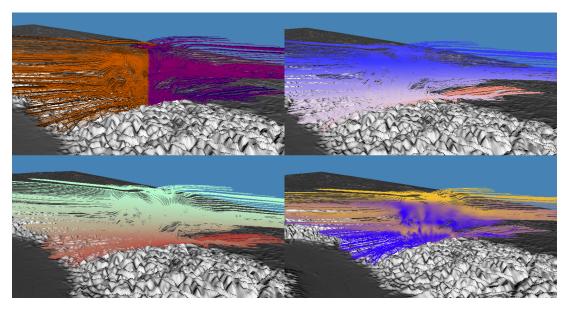
Figure 4.1 shows a set of trajectories starting on the south side of the alps. The particles start at 13:00 of the second day (22.Nov2016) at a latitude of  $45.2^{\circ}N$  and are traced for 5 hours as they move north. The initial points are spread from  $7.5-10.5^{\circ}E$  in lon-direction and 2500-3000m height. The three variables temperature, pressure and humidity appear to be strongly correlated: The colors have similar patterns, starting cold/high/humid and becoming significantly warmer/lower/drier after passing the mountains.

Figure 4.2 shows several trajectories passing over Chur (around  $9.53^{\circ}E$   $46.85^{\circ}N$ ). The starting time for the simulation is midnight between the 22. and 23. November. The integration time is 3 hours in both directions (so from 21:00 to 3:00). Temperature and pressure behave as expected, becoming lower at higher altitudes. The relative humidity seems to have two "wet" and "dry" regions each.

Figure 4.3 shows a zoomed-in view where one can see how trajectories make wave shapes over the mountains. In the right part one can also see a few cases where a trajectory suddenly jumps up (TODO actually not very visible, so ... good?). These jumps happen when the trajectory goes trough the ground. LAGRANTO has a similar behaviour and in both cases it can be disabled with an optional flag (in which case trajectories that leave the domain stay in place).



**Figure 4.1:** Color according to: Trajectory index(top left), temperature(top right), pressure(bottom left), relative humidity(bottom right)



**Figure 4.2:** Colors according to same criteria as in figure 4.1 above. The colors in the upper left case also depend on the trajectory set: Purple/blue forward, orange/black backward

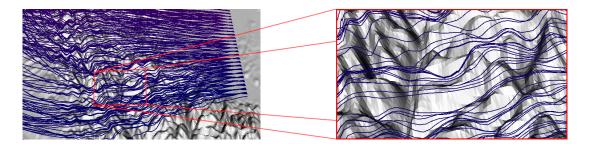


Figure 4.3: A closer look of the top left part of figure 4.1

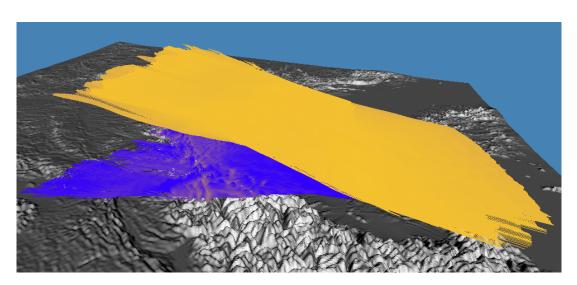


Figure 4.4: Relative humidity is high below and low above

Figure 4.4 shows that the air high above (14 - 16km) has low relative humidity, especially compared to the lower trajectories (which start around height 4km). This is also forward and backward, third day, 3:00 to 9:00. Also visible: The wind speeds are higher above and so the upper trajectories cover more area than the lower ones.

#### 4.2 Comparison

The plots in figure 4.5 plot the difference between trajectories computed by LAGRANTO and five variants of our tracing algorithm. All values are averaged over around 7000 trajectories. The five variants are:

- Copying LAGRANTO: Settings to perform almost the same operations as LAGRANTO
- Sample W correctly: Examining the LAGRANTO code showed that the vertical velocity
  W was being sampled on a staggered grid even after it had been destaggered. This is an
  error.
- Level interpolation on 4 columns: Use the procedure described in section 3.2.2
- Runge-Kutta instead of Iterative Euler: Use a different ODE solver
- All improvements: Combines the three variants above

All trajectories start and end within the boundaries of the domain. Frequent collisions with the ground would distort the results significantly and have been avoided by the choice of starting positions and by not tracing particles for too long.

What can be seen is that the black line is stays at a very low value. There are small variations, but we can reproduce the LAGRANTO results almost exactly.

The right side which measures the average vertical distance looks very chaotic and is not very useful for gathering information. The reason for that is unclear, possibly related to how trajectories make wave shapes over mountains.

The choice of integrator does not matter that much for small timesteps, but in the case of h = 5min the Runge-Kutta curve dominates the left plot. When viewing the actual trajectories, the Runge-Kutta trajectories are usually better at following the shape of the landscape.

It appears that how to sample across levels makes more of a difference than correcting the sampling of W. The fact that both of those affect the z axis may be another factor in the irregular curves on the right side.

#### 4.3 Performance

There are two main performance bottlenecks: Reading the data and doing computations on each particle and timestep. We added a simple OpenMP parallelization for iterating over all trajectories during the simulation phase and hope to at least match the speed of LAGRANTO with that.

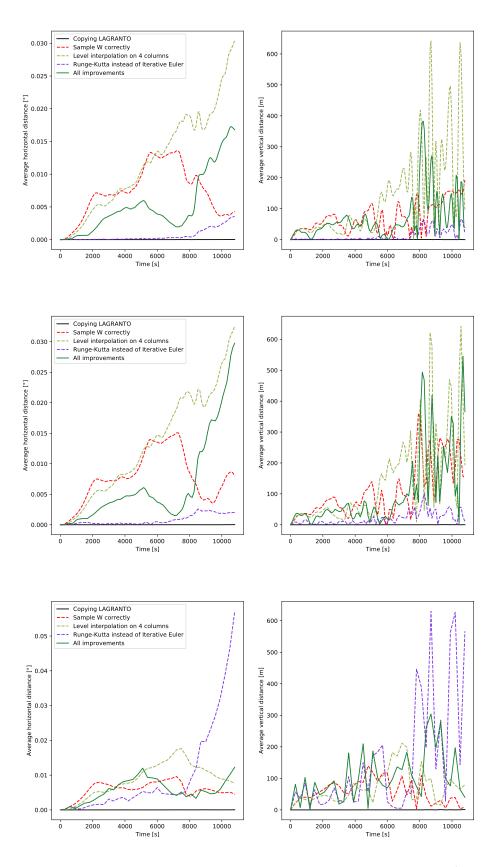


Figure 4.5: Average distance between LAGRANTO trajectories and ours, timestep is h=1min on top, h=2min in the middle, h=5min on the bottom

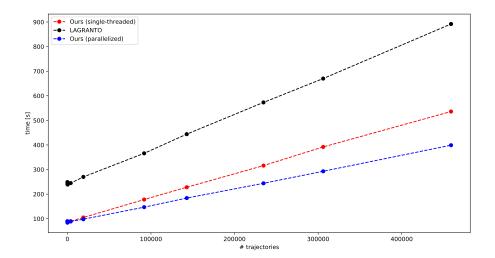


Figure 4.6: Times for tracing a variable number of particles over 60 timesteps and 7 data files

Figure 4.6 plots the measured times for a test case of computing different numbers of trajectories. As expected, the time scales linearly in the number of trajectories. Our method is faster than LAGRANTO in all cases. In the early part, where the reading of the data makes up almost all of the time, our version does in roughly 1.5 minutes what LAGRANTO does in 4. Increasing the number of trajectories, it becomes evident that our version also has a better scaling, even when unparallelized.

All time measurements were taken on the same machine: It has an  $Intel^{\mathbb{R}}$   $Core^{TM}$  i5-3427U CPU with 4 cores running at 1.80 GHz with 7.7 GiB of memory.

#### Conclusion

The basic functionality of computing trajectories according to input data works well. The visualization and analysis parts ended up rather limited due to time constraints.

Comparing to LAGRANTO: Better performance and arguably better results have been achieved. Some features are missing but would be quite simple to add (initial points read from a file, write down only every *n*th iteration). I'm sure I missed some others TODO

While the particle tracer works, it can still be extended. Because the region of interest for this project was relatively small and compact, the solver can not handle trajectories that reach the boundaries of the coordinate system (poles, date line). The borders of the local domain hold issues as well. Particles near the ground and outside the (rlon, rlat) domain are handled differently between LAGRANTO and our code and both methods lead to undesirable results sometimes. The parallelization of the solver is currently very simple and could most likely be improved in several ways.

The visualization with VTK is very limited. While it is possible to read trajectories and show how they pass over the landscape, most settings are hardcoded. Displaying different trajectories or changing the variables requires changing the code. Optimally this would have been done using a GUI. Currently all loaded trajectories are displayed at once and there is no way to, for example, select only those that pass through a certain region or those with a certain average temperature.

Originally there were plans for more postprocessing, visitation maps, finding cool stuff in the visualization...TODO

## **Bibliography**

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- [SW15] M. Sprenger and Heini Wernli. The lagranto lagrangian analysis tool version 2.0. *Geoscientific Model Development*, 8, 08 2015.