

A shaft is a rotating or stationary member, usually of circular cross-section, having mounted upon it such elements as gears, pulleys, flywheels, cranks, sprockets and other power-transmitting elements. The shafts are relatively long and may be subjected to bending, tension, compression or torsional loads, acting singly or in combination with one another. When they are combined, one may expect to find both static and fatigue strengths to be important design consideration, since a single shaft may be subjected to static stresses, completely reversed stresses and repeated stresses, all acting at the same time.

- a) Transmission shaft It is used to transmit power between the power source and the machines absorbing power. It is generally subjected to torque, bending moment and axial load in combination e.g. line shaft, counter shaft, head shaft and all factory shafts.
- b) Machine shaft It is integral part of a machine. It is used to transfer motion and power within the machine e.g. crank shaft, gear shaft.
- c) Axle It is a stationary or rotating shaft. It does not carry any torsional load. It is subjected to bending moment due to transverse load only. It is used to support rotating parts e.g. axles of automobiles.
- d) Spindle It is a short rotating shafts used to impart motion either to cutting tool or work piece e.g. lathe spindle, drill press spindle.

Materials: Commonly adopted materials are mild steel. In addition, different types of alloy steels are also used for shafts, depending on situation and types of application.

Deflection restraints:  $\delta = L/1200$ , where  $\delta$  and L are maximum transverse deflection of the shaft and length of shaft between bearing supports respectively.

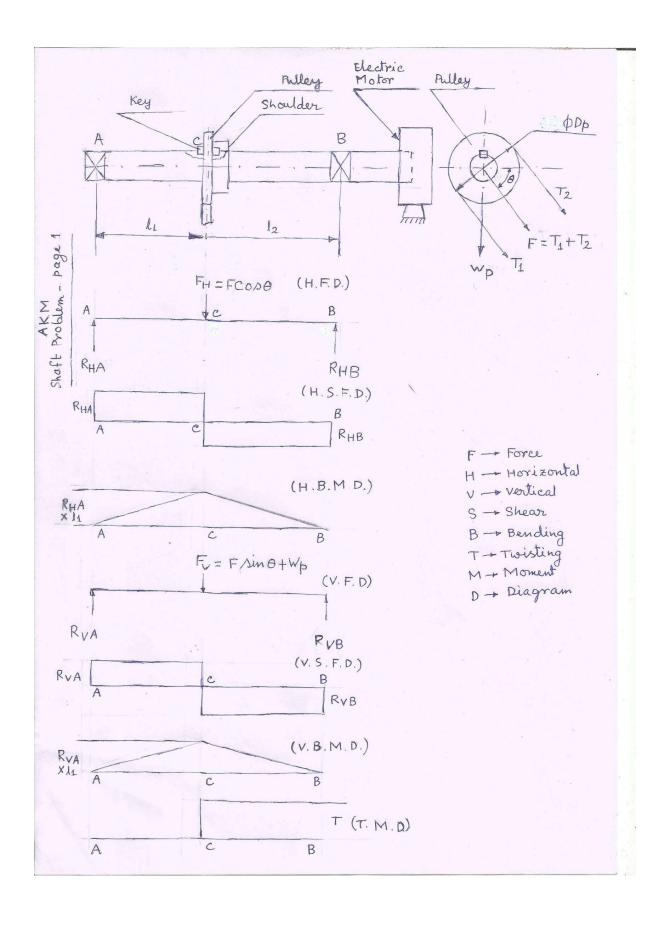
Twist restraint: Maximum twist is 2.5-3.5 degree per meter of shaft length for line shaft. It is with 0.25 degree per meter of machine shaft.

## Problem:

A solid horizontal steel shaft is to run in self-aligning bearings A and B, 2500mm apart. The shaft is driven from the right of right-hand bearing with an electric motor. The power is supplied to a machine from the shaft through a 500mm diameter pulley, mounted on the shaft through a rectangular key at 1200mm from the left-hand bearing. The belt tensions are 1800N and 840N and they are parallel to each other and at 64° to the horizontal. The weight of the pulley is 500N. Determine the diameter of the shaft.

Use the following data:

Material = FeE 200; Factor of safety = 2.5; Combined shock and fatigue factor for bending = 1.6; Combined shock and fatigue factor for torsion = 1.2; Allowable tensile stress for key material = 120MPa



```
F=T1+T2=1800N+840=2640N
    1= 1200 mm
                              FH = FeoDO = 2640 cos64° = 1157.299828 N
    l2=1300mm
                              F = Frim0+Wp = 2640 sin64°+ 500
    T1 = 1800N
                                  = 2372'816282 +500 = 2872'816282N
Problem - page 2
   T2= 840N
                              R_{HA} = \frac{2640 \times 1300}{1200 + 1300} \cosh 64^{\circ} = \frac{1157 \cdot 299828 \times 1300}{2500}
   Wp = 500N
    Dp = 500 mm
    0 = 64°
                                    = 601 7959103N
                              R_{HB} = \frac{1157.299828 \times 1200}{1200 + 1300} = 555.5039172N
    Material = Fe E 200
     F.S. = 2.5
                              R_{VA} = \frac{2872.816282 \times 1300}{1200 + 1300} = 1493.864466N
    Km = 1.6
     K+=1'2
                              RvB = 2872 816282 X 1206 = 1378 951814N.
  From Design Data Book,
  Tyield = 200 MPa.
                               MHC = RHAX 1 = 601.7959103×1200
  Tyield = 200 = 100 MPa
                                      = 722155 0924 N-mm
  [T] = \frac{100}{2.5} = 40 MPa
                              Mrc = Rvax li = 1493'864466X1200
  Torque calculation:
                                     = 1792637 36 N-mm
  T= (1800-840) x DP
    = 960 × 500 = 240000 N-mm Me= MHe+Mve
                                     = \sqrt{(722155.0924)^2 + (1792637.36)^2}
   c is most critical point
                                     = 1932629.473 N-mm
   M=1932629'473 N-mm.
    Te = \sqrt{(K_m M)^2 + (K_t T)^2} = \sqrt{(1.6 \times 1932629.473)^2 + (1.2 \times 240000)^2}
                            = 3105589'977 N-mm
     d), 3/16Te; d) 3/16×310·5589·977; d), 3/395415·9969
     d> 73'3980877 mm; d> 73'3980877X1'1; d> 80'73789647mm
     We take, d= 82mm For commercial shaft, we take, d= 85mm or 90mm
    N.B.: They keyway is tocated at point & where Te is maximum and is
          critical. So the value of allowable stress is further reduced by 25%
         which equivalent to multiplying with 1:1 i.e. increasing the diameter by 10\%. \sqrt[3]{\frac{1}{0.75}} = 1.100642416 \approx 1.1.
```

Note: From the above discussion, it is understood that the calculated diameter of the shaft depends on the computed values of  $T_e$  and  $[\tau]$ . With the appropriately selected values of  $K_m$  and  $K_t$ , the value of  $T_e$  depends on the values of T and T. It is clear that values of T and T and T values of allowable shear stress also not same along the shaft. The diameter of the shaft is to be calculated at all critical locations and design decision is to be taken based on engineering judgement.

Type of Loading	$C_{m}$	$C_{t}$
Stationary Shaft:		
Load applied gradually	1.0	1.0
Load applied suddenly	1.5-2.0	1.5-2.0
<b>Rotating Shaft:</b>		
Load applied gradually	1.5	1.0
Steady Loads	1.5	1.0
Loads applied gradually with minor	1.5-2.0	1.0-1.5
shocks	2.0-3.0	1.5-3.0
Loads applied suddenly with heavy shocks		

Note: In some books,  $C_m$  and  $C_t$  are denoted as  $K_m$  and  $K_t$  respectively.

Calculation of average torque  $T_{av}$  from rated power [kW] of motor with rpm n:  $(2\pi n \times T_{av})/60 = 1000 \times [kW]$ ;

$$\begin{split} T_{av} &= (60\times 1000) \ / \ (2\pi n) \times [kW] \ N\text{-m} = (9549.296586/n) \ N\text{-m} \approx \ (9550/n) \times [kW] \ N\text{-m} \\ T_{av} &= (9550/n) \times 10^3 \times [kW] \ N\text{-mm}. \end{split}$$

Design Torque  $T_d = T_{av} \times C_s$ .

Note:

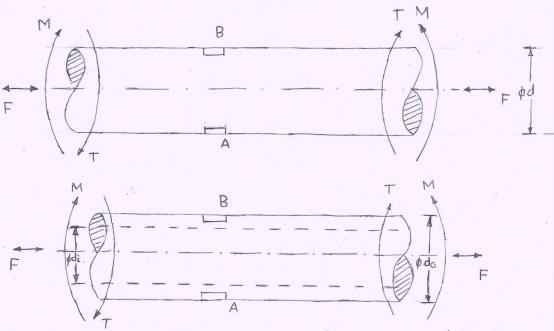
The torque T in the formula  $Te = \int (K_m M)^2 + (K_{\pm} T)^2$  is to be considered as design torque Td. If T be calculated from any data which is an averge based time like rated power ete, it reflects averge value of torque. But the design calculation is to beared on maximum instantane value Tmax of T.

Service factor = Cs = Tmax where Tav = Average value of T

Tmax = Tav X Cs

Ta = Tmax

Cs is selected on the basis of available literature and experience. Cs value for different combination of driving machine and driven machines are different. It also depends on operating condition.



Shaft under axial load F in addition to axial twisting moment T and & bending moment M

A key is a machine element which is used for connecting two machine parts for preventing relative motion of votation with respect to each other. In many application, the key prevents the lengthwise relative motion also. The connected parts act as a single unit. The key joint consists of shaft, hub and key.

Primary function of the key is to transmit the torque from the shaft to huband vice versa.

A groove called a Keyseat or Keyway is usually cut into the shoft and the hub of the part to be connected.

The commonly adopted forms of Pkeys may be divided into four classes. Keys

Saddle Key Flat Key

Tangent Keys Kennedy Key

Sunk Key i) Rectangular or square Keys

Round Keys Taper pins

ii) gib head Keys

iii) Feather Keys and splined Shafts

iv) woodruff Keys

Taper key is uniform in width but tappered in height. The standardtaper is 1 in 100. The bollow surface is the Key is straight and the top surface is given a taper. The laper is provided for the following reasons.

i) when the Key is inserted in the Keyways of the shaft and hub and pressed by means of hammer, it becomes tight due to wedge action. This ensures the tightness of joint in operating conditions and prevents loosening of the parts.

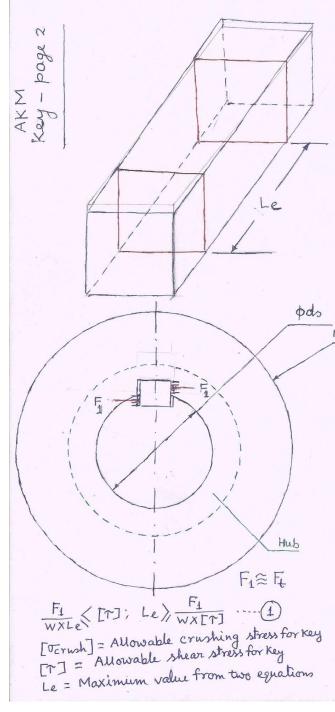
ii) Due to taper, it is easy to remove the key and dismantle

the joint.

Tangential force for Key = F<sub>t</sub>; F<sub>t</sub> × d<sub>s</sub> = T<sub>d</sub>; F<sub>t</sub> = 2T<sub>d</sub>

T<sub>d</sub> = T<sub>av</sub> × e<sub>s</sub>; e<sub>s</sub> = Service factor = T<sub>max</sub>; T<sub>d</sub> = T<sub>av</sub> × e<sub>s</sub>

T<sub>d</sub> = Design torque; d<sub>s</sub> = Diameter of shaft



F1

F2

F1

F1

F2

F1

F2

F1

F2

F1

F2

F3

F4

F1

Le = Effective Length of Key crushing area are FG KJ and ADHE From shearing Let area EFGH = AShear stress =  $\frac{F_1}{A}$ 

Shear stress = F1 wxLe

Bearing stress is also called crushing, erushing stress = F1

Bearing stress = hxLe

F1 ( Terush); Le ), F1 / hx (Terush)

Key Problem - page 1

Torque = 240000 N-mm. Dia of shaft = 82mm.  $F_t = \frac{2T}{ds} = \frac{2\times240000}{82} = 5853.658537$ Dia of shaft = 85 mm,  $\overline{\xi} = \frac{2T}{85} = \frac{2\times240000}{85} = \frac{5647.058824N}{\xi = 5648N}$ Dia of shaft = 90 mm.  $F_t = \frac{2T}{ds} = \frac{2x240000}{90} = 5333'33333N$ [T] = 120 = 60 MPa [Jerush] = 150 MPa For ds = 82mm or 85mm, W= 22mm & h= 14mm.  $F_{t} = 5854 \text{ N}$  Le  $\left(\frac{5854}{22 \times 60}\right)$  Le  $\left(\frac{4.4384848485 \text{ mm}}{2.2 \times 60}\right)$ Le) 5854; Le), 5854; Le), 5.575238 095 For ds = 85mm; W = 22mm 4 h = 14mm  $F_{t} = 5648 \,\text{N}$  Le  $\frac{5648}{22 \times 60}$ ; Le  $\frac{7}{4}$ , 278787879 mm. (Fordy=85mm) Le>, 5648 ; Le>, 5648 ; Le>, 5:3790476 19mm. Le = 5 379047619mm For ds = 90mm; w= 25mm & h= 140mmm

For ds = 90 mm; W = 25 mm & h = 140 mm  $F_t = 5334 \text{ N}$   $Le > \frac{5334}{25 \times 60}$ ; Le > 3.556 mm.  $Le > \frac{5334}{14 \times 150}$ ;  $Le > \frac{5334}{7 \times 150}$ ;  $Le > \frac{508 \text{ mm}}{14 \times 150}$