

# Solid Mechanics Sessional (MES 451)

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## References

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2. Engineering Mechanics of Solids, E. P. Popov, PHI, 1993.
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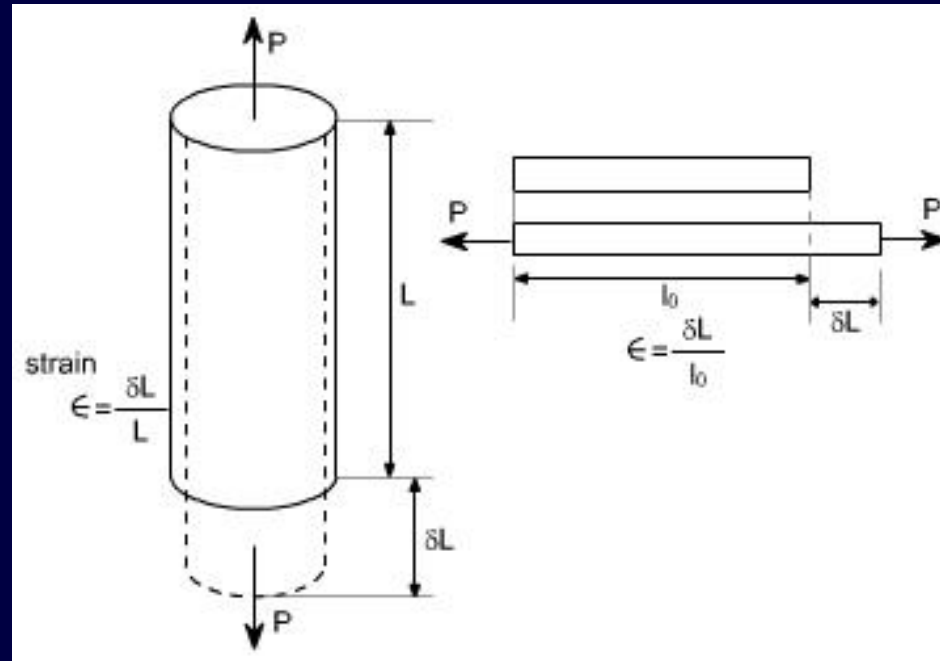
# Syllabus

- ❖ Mohr's Circle on strain Rosette- Graphical Solution.
- ❖ Mohr's Circle on Moment of Inertia - Graphical Solution.
- ❖ Mechanical testing of Engineering Materials.
- ❖ Experiments on the principles of strength of materials.
- ❖ Instrumentation for measurement of deflection under loading.

# Concept of Strains

Linear strain or normal strain or the longitudinal strain:

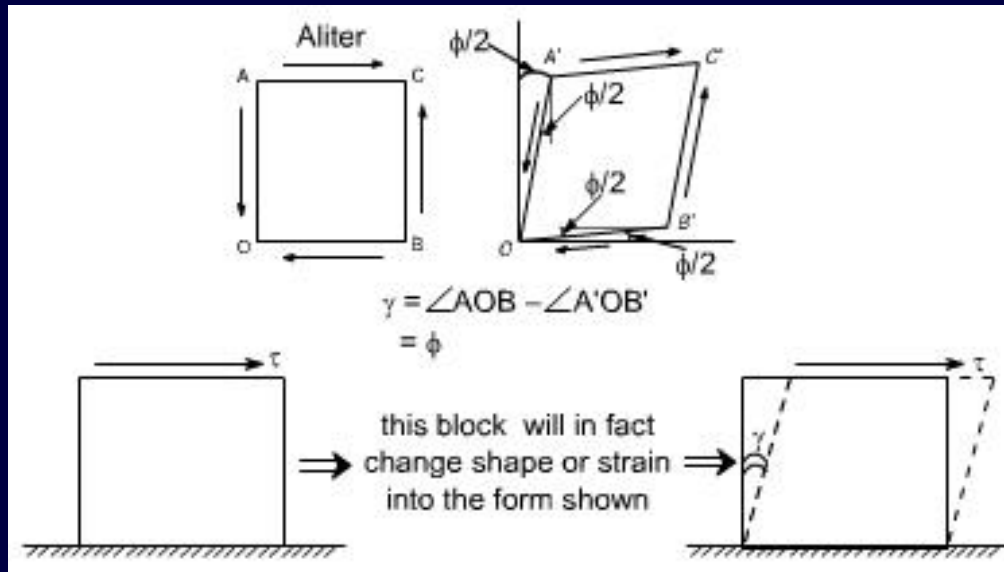
$$\text{strain}(\epsilon) = \frac{\text{change in length}}{\text{original length}} = \frac{\delta L}{L}$$



**Sign convention for strain:** Tensile strains are positive whereas compressive strains are negative.

- The tangent of the angle through which two adjacent sides rotate relative to their initial position is termed shear strain. In many cases the angle is very small and the angle it self is used, ( in radians ), instead of tangent, so that

$$\gamma = \angle AOB - \angle A'OB' = \phi$$



**Hook's Law:** A material is said to be elastic if it returns to its original, unloaded dimensions when load is removed.

$$\frac{\text{stress}}{\text{strain}} = \text{constant}$$

This constant is given by the symbol E and is termed as the **modulus of elasticity** or **Young's modulus of elasticity**

$$E = \frac{\text{strain}}{\text{stress}} = \frac{\sigma}{\epsilon}$$

$$= P/A / \delta L / L$$

$$E = \frac{PL}{A\delta L}$$

**Poisson's ratio:** If a bar is subjected to a longitudinal stress there will be a strain in this direction equal to  $\sigma/E$  . There will also be a strain in all directions at right angles to  $\sigma$ . The final shape being shown by the dotted lines.

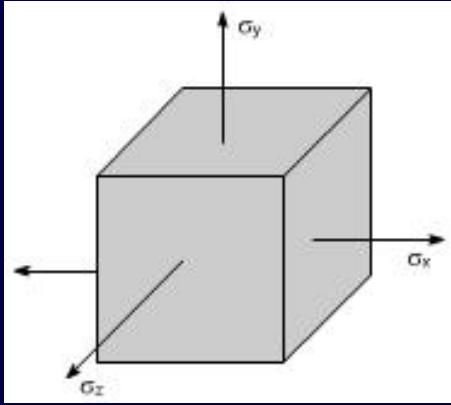
It has been observed that for an elastic materials, the lateral strain is proportional to the longitudinal strain. The ratio of the lateral strain to longitudinal strain is known as the poison's ratio .

**Poisson's ratio ( $\mu$ )** = -lateral strain /longitudinal strain



For most engineering materials the value of m his between 0.25 and 0.33.

**Three dimensional state of strain:** Consider an element subjected to three mutually perpendicular tensile stresses  $\sigma_x$ ,  $\sigma_y$  and  $\sigma_z$  as shown in the figure below.



$$\varepsilon_x = \frac{\sigma_x}{E} - \mu \frac{\sigma_y}{E} - \mu \frac{\sigma_z}{E}$$

$$\varepsilon_y = \frac{\sigma_y}{E} - \mu \frac{\sigma_x}{E} - \mu \frac{\sigma_z}{E}$$

$$\varepsilon_z = \frac{\sigma_z}{E} - \mu \frac{\sigma_x}{E} - \mu \frac{\sigma_y}{E}$$

**Principal strains in terms of stress:** In the absence of shear stresses on the faces of the elements let us say that  $\sigma_x$ ,  $\sigma_y$  and  $\sigma_z$  are in fact the principal stress. The resulting strain in the three directions would be the principal strains.

i.e. We will have the following

$$\varepsilon_1 = \frac{1}{E} [\sigma_1 - \mu \sigma_2 - \mu \sigma_3]$$

$$\varepsilon_2 = \frac{1}{E} [\sigma_2 - \mu \sigma_1 - \mu \sigma_3]$$

$$\varepsilon_3 = \frac{1}{E} [\sigma_3 - \mu \sigma_1 - \mu \sigma_2]$$

The negative sign indicating that if  $\sigma_y$  and  $\sigma_z$  are positive i.e. tensile, these they tend to reduce the strain in x direction.

**Two dimensional state of strain:** stress in third direction is zero ( $\sigma_z = 0$  or  $\sigma_3 = 0$ ). Although the strains will be there in this direction due to the stresses  $\sigma_1$ ,  $\sigma_2$

$$\varepsilon_1 = \frac{1}{E} [\sigma_1 - \mu \sigma_2]$$

$$\varepsilon_2 = \frac{1}{E} [\sigma_2 - \mu \sigma_1]$$

$$\varepsilon_3 = \frac{1}{E} [-\mu \sigma_1 - \mu \sigma_2]$$

Hence a strain can exist without a stress in that direction

$$\text{i.e if } \sigma_3 = 0; \varepsilon_3 = \frac{1}{E} [-\mu \sigma_1 - \mu \sigma_2]$$

Also

$$\varepsilon_1 \cdot E = \sigma_1 - \mu \sigma_2$$

$$\varepsilon_2 \cdot E = \sigma_2 - \mu \sigma_1$$

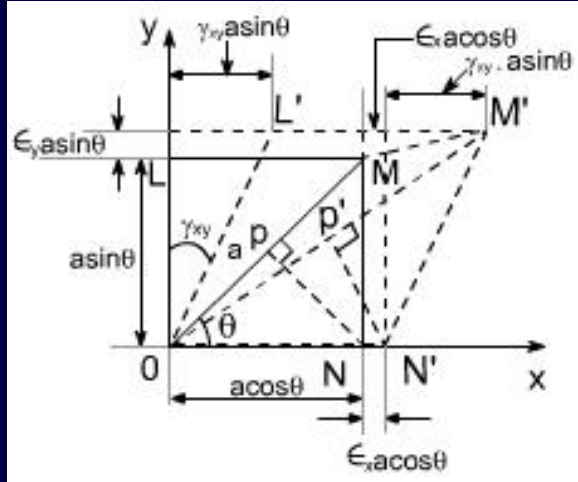
so the solution of above two equations yields

$$\sigma_1 = \frac{E}{(1 - \mu^2)} [\varepsilon_1 + \mu \varepsilon_2]$$

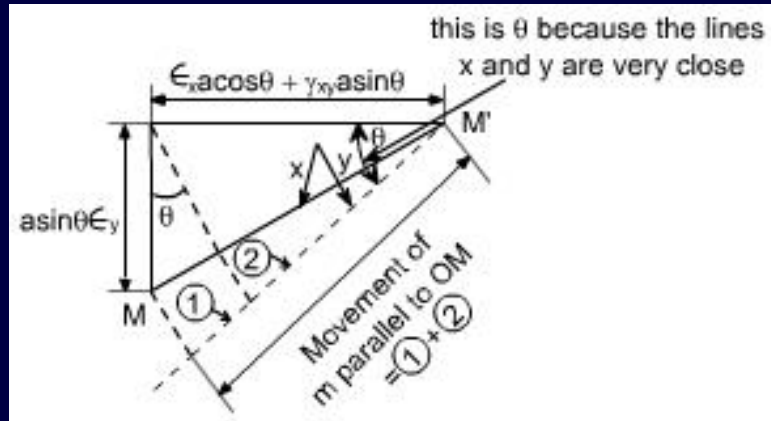
$$\sigma_2 = \frac{E}{(1 - \mu^2)} [\varepsilon_2 + \mu \varepsilon_1]$$

## Strains on an oblique plane ---- (a) Linear strain

Thus the movement of M parallel to OM, which since the strains are small is practically coincident with MM'. and this would be the summation of portions (1) and (2) respectively and is equal to



If M moves to M', then the movement of M parallel to x axis is  $\epsilon_x a \cos \theta + \gamma_{xy} \sin \theta$  and the movement parallel to the y axis is  $\epsilon_y a \sin \theta$



$$= (\epsilon_y a \sin \theta) \sin \theta + (\epsilon_x a \cos \theta + \gamma_{xy} a \sin \theta) \cos \theta$$

$$= a [\epsilon_y \sin \theta \cdot \sin \theta + \epsilon_x \cos \theta \cdot \cos \theta + \gamma_{xy} \sin \theta \cdot \cos \theta]$$

hence the strain along OM

$$= \frac{\text{extension}}{\text{original length}}$$

$$\epsilon_\theta = \epsilon_x \cos^2 \theta + \gamma_{xy} \sin \theta \cdot \cos \theta + \epsilon_y \sin^2 \theta$$

$$\epsilon_\theta = \epsilon_x \cos^2 \theta + \epsilon_y \sin^2 \theta + \gamma_{xy} \sin \theta \cdot \cos \theta$$

$$\text{Recalling } \cos^2 \theta - \sin^2 \theta = \cos 2\theta$$

$$\text{or } 2 \cos^2 \theta - 1 = \cos 2\theta$$

$$\cos^2 \theta = \left[ \frac{1 + \cos 2\theta}{2} \right]$$

$$\sin^2 \theta = \left[ \frac{1 - \cos 2\theta}{2} \right]$$

hence

$$\epsilon_\theta = \epsilon_x \left[ \frac{1 + \cos 2\theta}{2} \right] + \epsilon_y \left[ \frac{1 - \cos 2\theta}{2} \right] + \gamma_{xy} a \sin \theta \cdot \cos \theta$$

$$= \frac{\epsilon_x + \epsilon_y}{2} + \frac{\epsilon_x - \epsilon_y}{2} \cos 2\theta + \frac{1}{2} \gamma_{xy} \sin 2\theta$$

$$\epsilon_\theta = \left\{ \frac{\epsilon_x + \epsilon_y}{2} \right\} + \left\{ \frac{\epsilon_x - \epsilon_y}{2} \right\} \cos 2\theta + \frac{1}{2} \gamma_{xy} \sin 2\theta$$

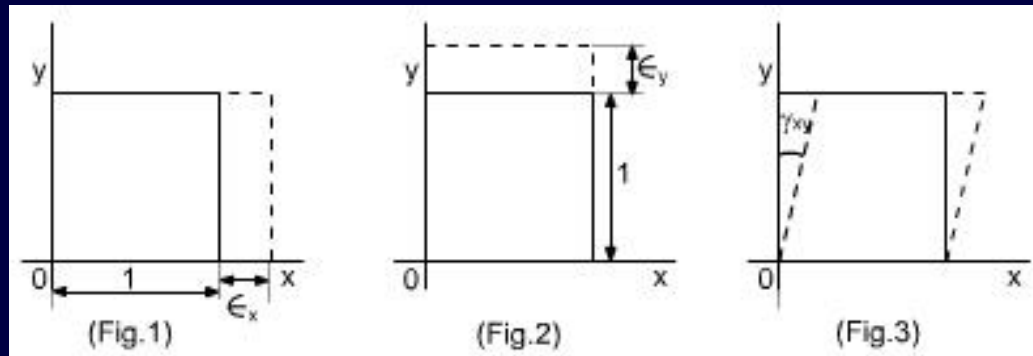
**Shear strain:** shear strain in the direction OM = displacement of point P at the foot of the perpendicular from N to OM; and the following expression can be derived as

$$\frac{1}{2} \gamma_{\theta} = - \left[ \frac{1}{2} (\epsilon_x - \epsilon_y) \sin 2\theta - \frac{1}{2} \gamma_{xy} \cos 2\theta \right]$$

In the above expression  $\frac{1}{2}$  is there so as to keep the consistency with the stress relations. Further -ve sign in the expression occurs so as to keep the consistency of sign convention, because OM' moves clockwise with respect to OM it is considered to be negative strain.

The other relevant expressions are the following :

**Plane Strain:** In xy plane three strain components may exist as can be seen from the following figures:



**Principal planes :**

$$\tan 2\theta_p = \frac{\gamma_{xy}}{\epsilon_x - \epsilon_y}$$

**Principal strains :**

$$\epsilon_{1,2} = \frac{\epsilon_x + \epsilon_y}{2} \pm \sqrt{\left( \frac{\epsilon_x - \epsilon_y}{2} \right)^2 + \left( \frac{\gamma_{xy}}{2} \right)^2}$$

**Maximum shear strains :**

$$\frac{\gamma_{\max}}{2} = \pm \sqrt{\left( \frac{\epsilon_x - \epsilon_y}{2} \right)^2 + \left( \frac{\gamma_{xy}}{2} \right)^2}$$

Plane strain condition is defined only by the components ,  $\epsilon_y$  ,  $\gamma_{xy}$ :  $\epsilon_z = 0$ ;  $\gamma_{xz} = 0$ ;  $\gamma_{yz} = 0$

Plane stress is not the stress system associated with plane strain. The plane strain condition is associated with 3-D stress system and plane stress is associated with 3-D strain system.

## Principal Strain and Mohr's Circle for Strain

$$\epsilon_{\theta} = \left\{ \frac{\epsilon_x + \epsilon_y}{2} \right\} + \left\{ \frac{\epsilon_x - \epsilon_y}{2} \right\} \cos 2\theta + \frac{1}{2} \gamma_{xy} \sin 2\theta \quad (1)$$

$$\frac{1}{2} \gamma_{\theta} = - \left[ \frac{1}{2} (\epsilon_x - \epsilon_y) \sin 2\theta - \frac{1}{2} \gamma_{xy} \cos 2\theta \right] \quad (2)$$

Re writing the equation (1) as below :

$$\left[ \epsilon_{\theta} - \left\{ \frac{\epsilon_x + \epsilon_y}{2} \right\} \right] = \left\{ \frac{\epsilon_x - \epsilon_y}{2} \right\} \cos 2\theta + \frac{1}{2} \gamma_{xy} \sin 2\theta \quad (3)$$

squaring and adding equations (2) and (3)

$$\left[ \epsilon_{\theta} - \left\{ \frac{\epsilon_x + \epsilon_y}{2} \right\} \right]^2 + \left\{ \frac{1}{2} \gamma_{\theta} \right\}^2 = \left[ \left\{ \frac{\epsilon_x - \epsilon_y}{2} \right\} \cos 2\theta + \frac{1}{2} \gamma_{xy} \sin 2\theta \right]^2 + \left[ \frac{1}{2} (\epsilon_x - \epsilon_y) \sin 2\theta - \frac{1}{2} \gamma_{xy} \cos 2\theta \right]^2$$

$$\left[ \epsilon_{\theta} - \left\{ \frac{\epsilon_x + \epsilon_y}{2} \right\} \right]^2 + \left\{ \frac{1}{2} \gamma_{\theta} \right\}^2 = \left\{ \frac{\epsilon_x + \epsilon_y}{2} \right\}^2 + \frac{\gamma_{xy}^2}{4}$$

Now as we know that

$$\epsilon_{1,2} = \frac{\epsilon_x + \epsilon_y}{2} \pm \sqrt{\left\{ \frac{\epsilon_x - \epsilon_y}{2} \right\}^2 + \left\{ \frac{\gamma_{xy}}{2} \right\}^2}$$

$$\epsilon_1 + \epsilon_2 = \epsilon_x + \epsilon_y$$

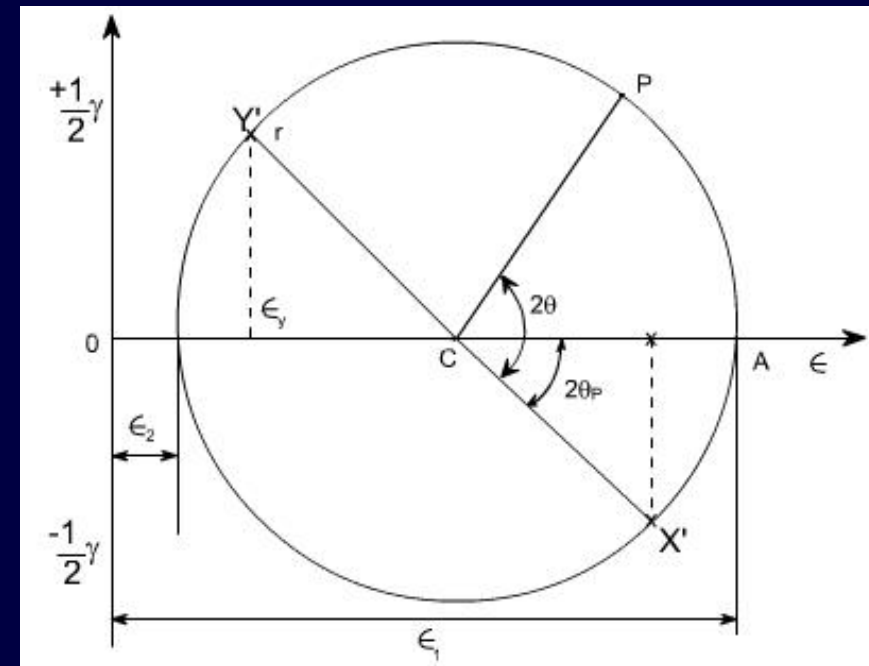
$$\left( \frac{\epsilon_1 - \epsilon_2}{2} \right)^2 = \left( \frac{\epsilon_x - \epsilon_y}{2} \right)^2 + \frac{\gamma_{xy}^2}{4}$$

Therefore the equation get transformed to

$$\left[ \epsilon_{\theta} - \left\{ \frac{\epsilon_1 + \epsilon_2}{2} \right\} \right]^2 + \left[ \frac{\gamma_{\theta}}{2} \right]^2 = \left( \frac{\epsilon_1 - \epsilon_2}{2} \right)^2 \quad (4)$$

If we plot equation (4) we obtain a circle of radius  $\left( \frac{\epsilon_1 - \epsilon_2}{2} \right)$  with center at  $\left( \frac{\epsilon_1 + \epsilon_2}{2}, 0 \right)$

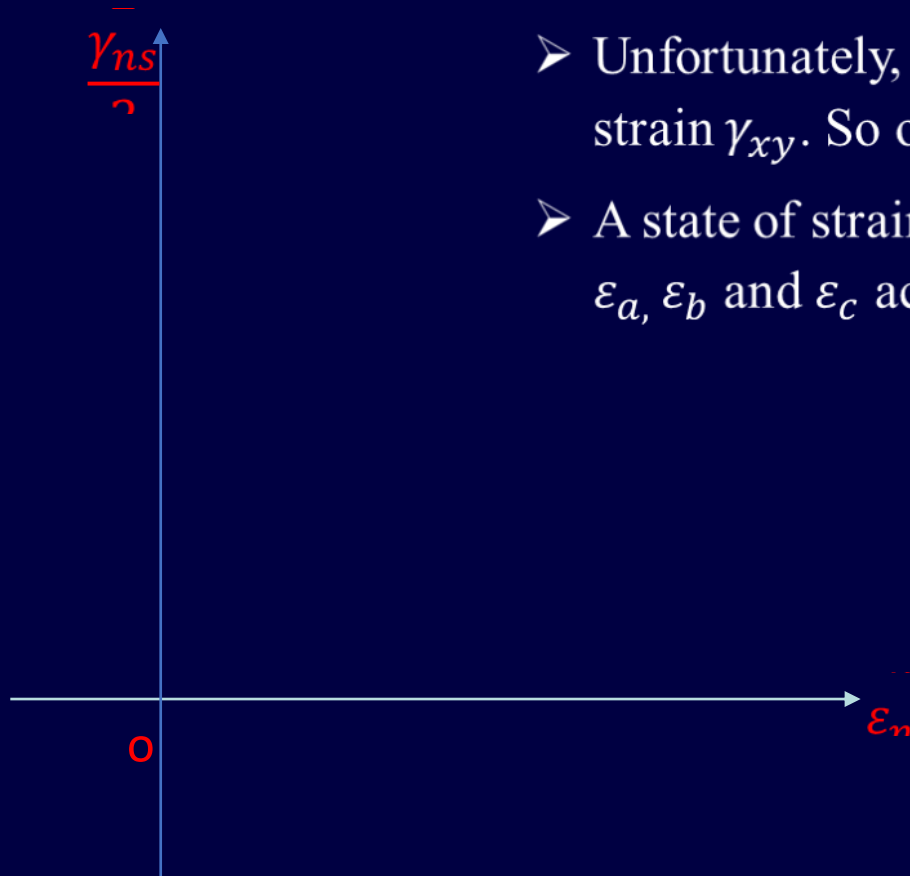
For the strains on an oblique plane we have two equations which are identical in form with the equation defining the direct stress on any inclined plane  $\theta$ .



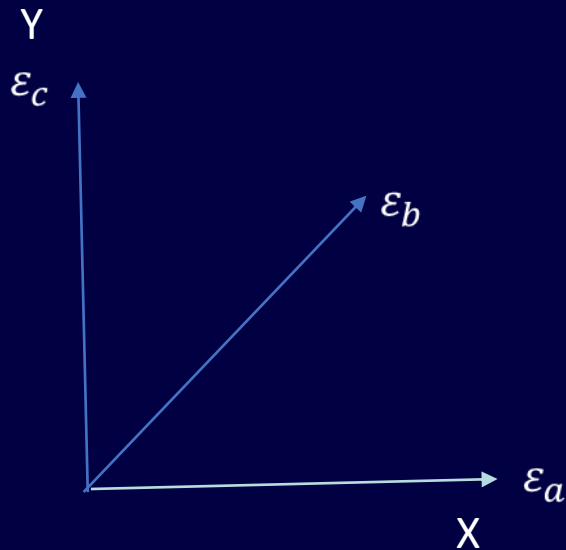


# MOHR'S CIRCLE ON STRAIN ROSETTE- GRAPHICAL SOLUTION.

- A single strain gage oriented in the direction of a uniaxial stress is sufficient for computing the stress.
- For biaxial stress, we are in need of three strains,  $\epsilon_x$ ,  $\epsilon_y$  and  $\gamma_{xy}$ .
- Unfortunately, there is no equipment that gives a direct measurement of the shearing strain  $\gamma_{xy}$ . So other methods are needed.
- A state of strain is uniquely determined by the measurement of three linear strains  $\epsilon_a$ ,  $\epsilon_b$  and  $\epsilon_c$  acting in three arbitrary direction  $\theta_a$ ,  $\theta_b$  and  $\theta_c$  at the same point.



- ❖ As a matter of practical convenience, the linear strains are obtained by using either of two combinations of three resistance strain gages
  1. Three gages set with their axes at  $45^\circ$  with each other,
  2. Three gages set with their axes at  $60^\circ$  with each other
- ❖ These combinations are known as strain rosettes.
- ❖ The three gages are electrically insulated from each other and are used to determine the strain at the surface of the structure to which they are attached.

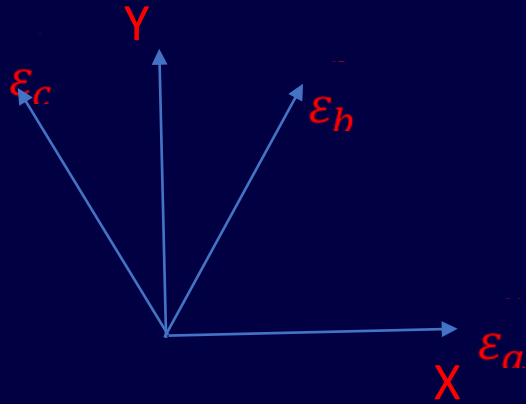


### The $45^\circ$ or Rectangular Strain Rosette

$$\theta_a = 0^\circ, \theta_b = 45^\circ, \theta_c = 90^\circ, \epsilon_x = \epsilon_a, \epsilon_y = \epsilon_c, \gamma_{xy}/2 = (\epsilon_a + \epsilon_c)/2 - \epsilon_b$$

This defines a state of strain from which the strain circle and the stress circle may be drawn.

## The 60° or Equiangular Strain Rosette



$$\theta_a = 0^\circ, \theta_b = 60^\circ, \theta_c = 120^\circ,$$

$$\varepsilon_x = \varepsilon_a, \quad \varepsilon_y = \frac{1}{3}(2\varepsilon_b + 2\varepsilon_c - \varepsilon_a), \quad \frac{\gamma_{xy}}{2} = \frac{(\varepsilon_c - \varepsilon_b)}{\sqrt{3}}$$

A strain circle is readily transformed into a stress circle by means of

$$R_\sigma = R_\varepsilon \frac{E}{1 + \mu}; \quad OC_\sigma = OC_\varepsilon \frac{E}{1 - \mu}$$

**PROBLEM 1:** Determine principal stresses, maximum and minimum shear stresses and stress components on plane whose normal makes an angle  $30^\circ$  with x- direction.

$$\varepsilon_x = -400 * 10^{-6}, \quad \varepsilon_y = +200 * 10^{-6}, \quad \gamma_{xy} = +800 * 10^{-6}, \quad E = 200 \text{ GPa}, \quad \mu = 0.30$$

State of strain of x-plane is denoted by point A. A  $(\varepsilon_x, \frac{\gamma_{xy}}{2})$ , A  $(-400 * 10^6, 400 * 10^6)$ ,

State of strain of y-plane is denoted by point B. B  $(\varepsilon_y, -\frac{\gamma_{xy}}{2})$ , B  $(200 * 10^6, -400 * 10^6)$ ,

**Mohr's Circle for Strain:**

Scale 1 cm =  $100 * 10^{-6}$

Measure OC of strain circle, OC =

Measure R of strain circle, R =

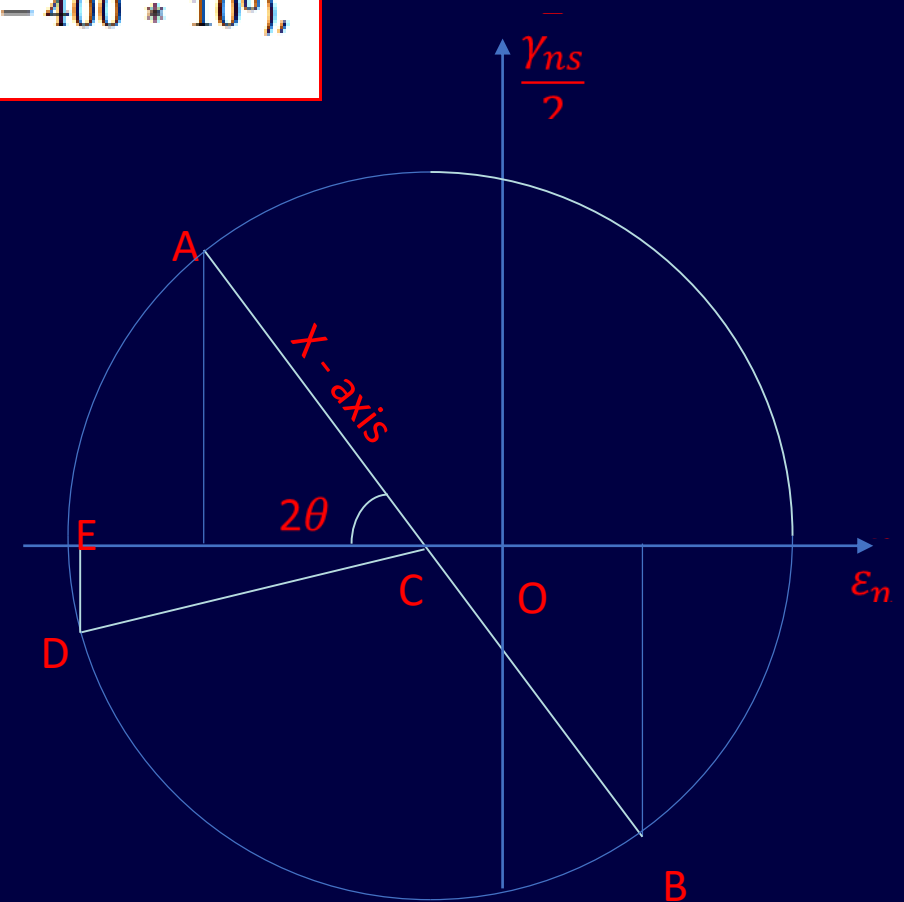
Maximum Principal Strain,  $\varepsilon_{max} = OC + R$

Minimum Principal Strain,  $\varepsilon_{min} = OC - R$

Maximum Shearing Strain,  $\frac{\gamma_{max}}{2} = R$

Minimum Shearing Strain,  $\frac{\gamma_{min}}{2} = -R$

Measure angle  $2\theta$ ,  $2\theta = 53^\circ$



Strain components on plane whose normal makes an angle  $30^\circ$

In the Mohr's Circle at an angle  $60^\circ$  anticlockwise we are getting point D on the Mohr's Circle.

Drop a perpendicular from D on  $\varepsilon_n$  axis DE

Co-ordinate of point D (OC + CE, ED)

Measure these lengths and multiply by scale to get normal and shearing strain components.

	Magnitude	Direction with x-axis (anticlockwise)
$OC_\varepsilon$		
$R_\varepsilon$		
$\varepsilon_{max}$		$\theta + 90^\circ$
$\varepsilon_{min}$		$\theta$
$\frac{\gamma_{max}}{2}$		$\theta + 135^\circ$
$\frac{\gamma_{min}}{2}$		$\theta + 45^\circ$
$\varepsilon_n$		$30^\circ$
$\frac{\gamma_{ns}}{2}$		$30^\circ$

## Transformation of strain circle to a stress circle

$$R_{\sigma} = R_{\varepsilon} \frac{E}{1 + \mu}; OC_{\sigma} = OC_{\varepsilon} \frac{E}{1 - \mu}$$

Calculate OC of stress circle, OC =

Calculate R of stress circle, R =

Maximum Principal Stress,  $\sigma_{max} = OC + R$

Minimum Principal Stress,  $\sigma_{min} = OC - R$

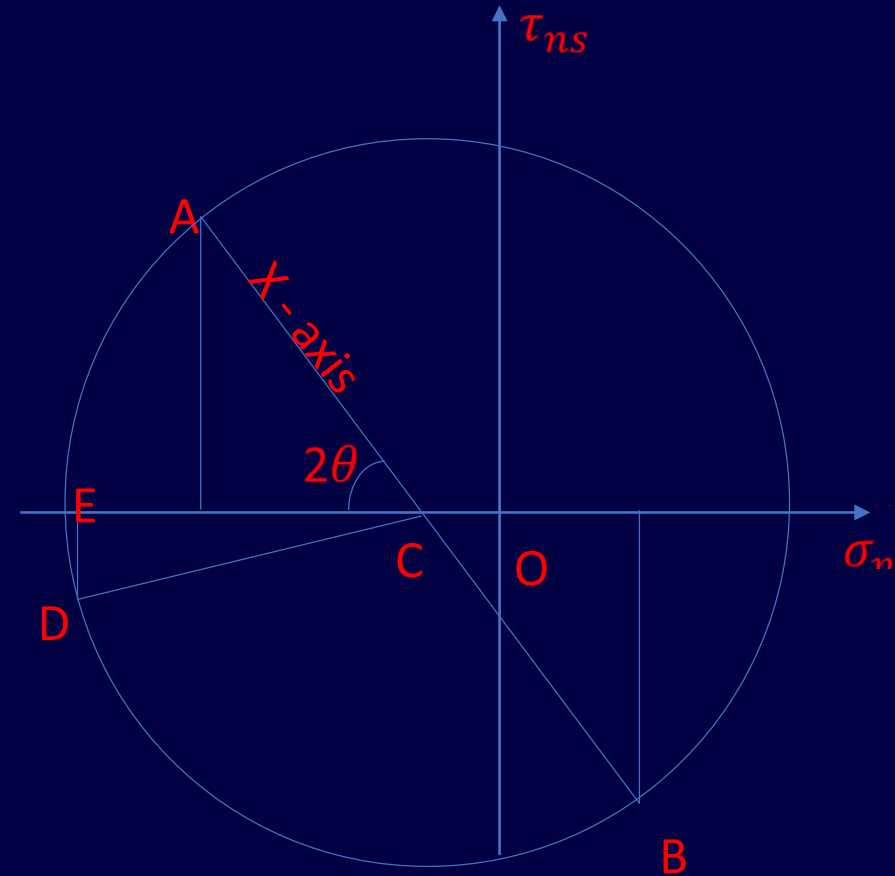
Maximum Shearing Stress,  $\tau_{max} = R$

Minimum Shearing Stress,  $\tau_{min} = -R$

Measure angle  $2\theta$ ,  $2\theta = 53^{\circ}$

## Mohr's Circle for Stress

Scale 1 cm =

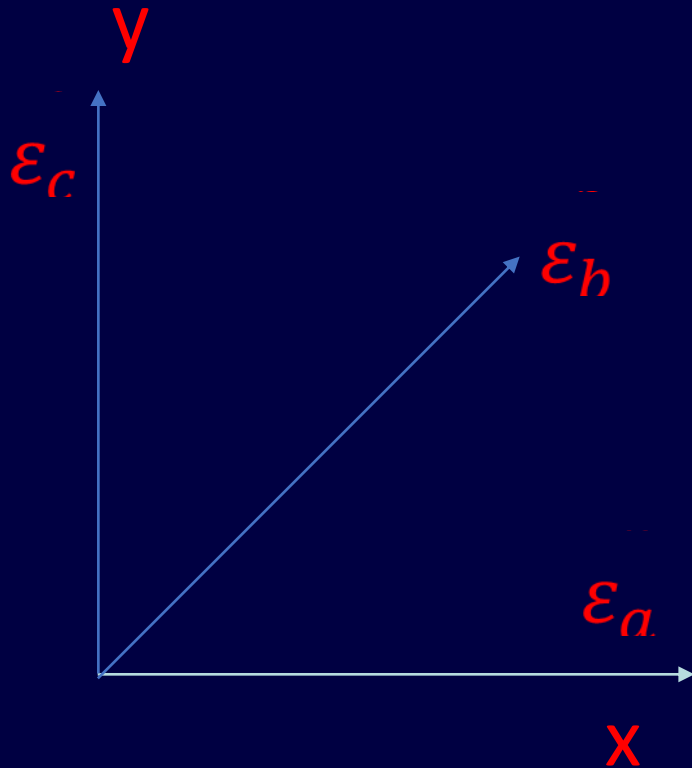


**Write answers in tabular form as shown**

	Magnitude	Direction with x-axis (anticlockwise)
$OC_\sigma$		
$R_\sigma$		
$\sigma_{max}$		$\theta + 90^\circ$
$\sigma_{min}$		$\theta$
$\tau_{max}$		$\theta + 135^\circ$
$\tau_{min}$		$\theta + 45^\circ$
$\sigma_n$		$30^\circ$
$\tau_{ns}$		$30^\circ$

Determine principal stresses and their directions for the following strain rosettes:

a) 45° STRAIN ROSETTE:  $\varepsilon_a = 400 * 10^{-6}$ ,  $\varepsilon_b = -200 * 10^{-6}$ ,  $\varepsilon_c = -100 * 10^{-6}$ ,  
 $E = 200 \text{ G Pa}$ ,  $\mu = 0.30$



We will draw Strain Circle by Graphical Method.

- Draw  $\varepsilon_n$  axis and  $\frac{\gamma_{ns}}{2}$  axis as shown, o1 is the origin.
- Draw vertical lines for linear strains  $\varepsilon_a = 400 * 10^{-6}$ ,  $\varepsilon_b = -200 * 10^{-6}$  and  $\varepsilon_c = -100 * 10^{-6}$
- Consider the middle strain within  $\varepsilon_a$ ,  $\varepsilon_b$ , and  $\varepsilon_c$ .
- In this problem  $\varepsilon_c$  is the middle strain.
- Take a line element on this vertical line.
- In the strain rosette if you rotate  $\varepsilon_c$  45° clockwise you will meet  $\varepsilon_b$
- Rotate the line element 45° clockwise to meet  $\varepsilon_b$  line, you will get C1B line between  $\varepsilon_c$  and  $\varepsilon_b$
- Rotate the line element 90° clockwise to meet  $\varepsilon_c$  line, you will get C1A line between  $\varepsilon_c$  and  $\varepsilon_a$

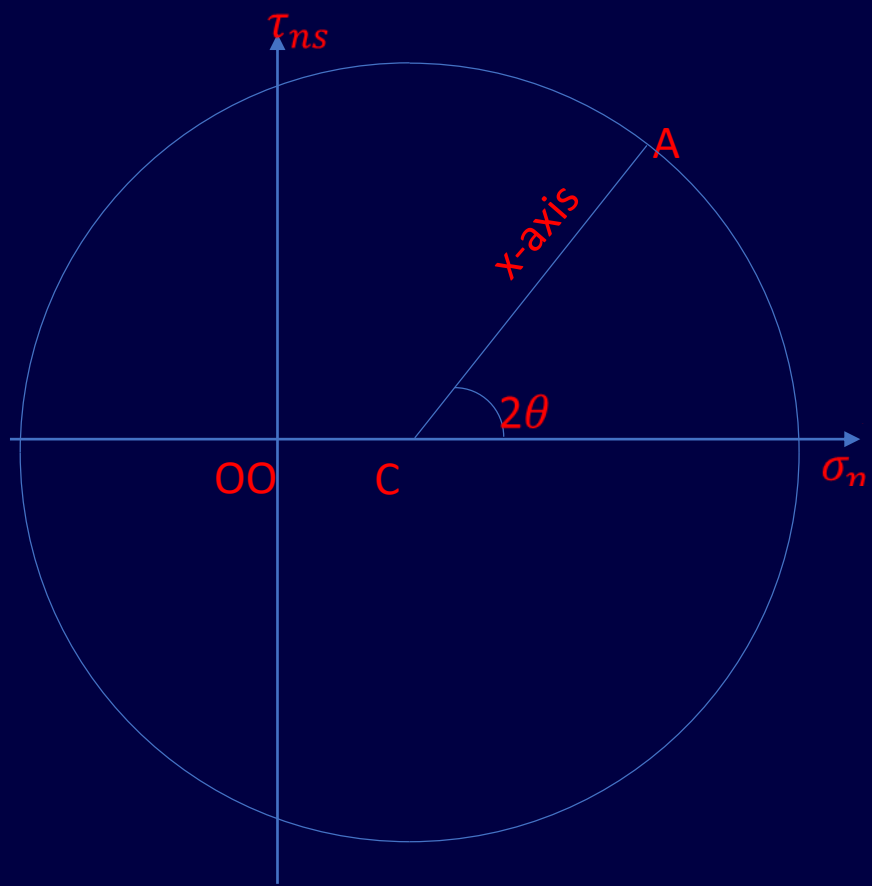




	Magnitude	Direction with x-axis (anticlockwise)
$OC_\varepsilon$		
$R_\varepsilon$		
$\varepsilon_{max}$		$180^\circ - \theta$
$\varepsilon_{min}$		$90^\circ - \theta$
$\frac{\gamma_{max}}{2}$		$45^\circ - \theta$
$\frac{\gamma_{min}}{2}$		$135^\circ - \theta$

# Transformation of strain circle to a stress circle

$R_{\sigma} = R_{\epsilon} \frac{E}{1 + \mu}; OC_{\sigma} = OC_{\epsilon} \frac{E}{1 - \mu}$



Calculate OC of stress circle, OC =

Calculate R of stress circle, R =

Maximum Principal Stress,  $\sigma_{max} = OC + R$

Minimum Principal Stress,  $\sigma_{min} = OC - R$

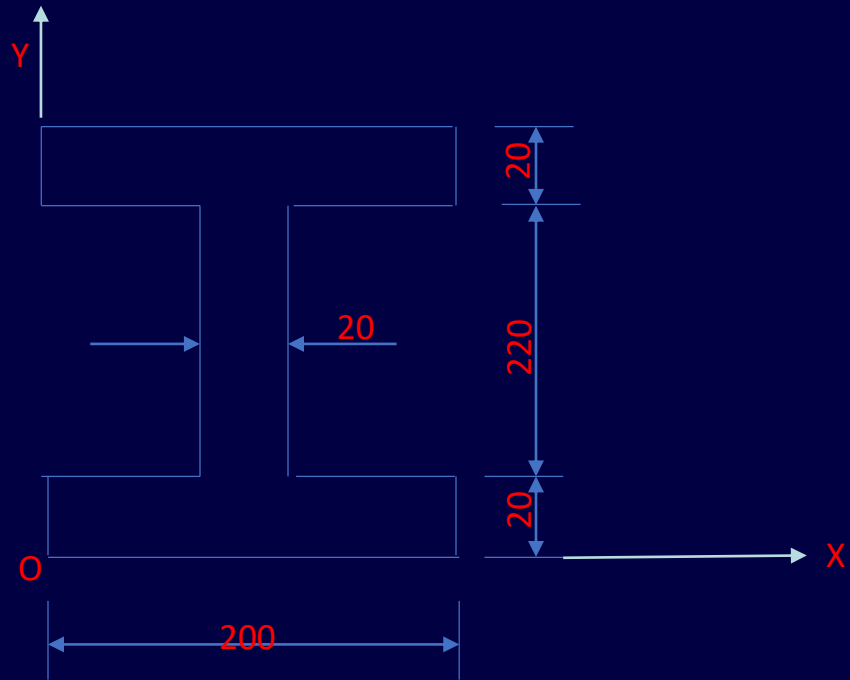
Maximum Shearing Stress,  $\tau_{max} = R$

Minimum Shearing Stress,  $\tau_{min} = - R$

Measure angle  $2\theta$ ,  $2\theta =$

	Magnitude	Direction with x-axis (anticlockwise)
$OC_{\sigma}$		
$R_{\sigma}$		
$\sigma_{max}$		$180^{\circ} - \theta$
$\sigma_{min}$		$90^{\circ} - \theta$
$\tau_{max}$		$45^{\circ} - \theta$
$\tau_{min}$		$135^{\circ} - \theta$

Find out the principal moment of inertia about centroid and their orientation from centroidal axis for the following sections.



Take X and Y axes as shown in the figure. O is the origin  
To get centre of gravity use formula

$$\bar{x} = \frac{\sum_{i=1}^n A_i x_i}{\sum_{i=1}^n A_i}; \bar{y} = \frac{\sum_{i=1}^n A_i y_i}{\sum_{i=1}^n A_i}$$

$$\bar{x} = \frac{A_1 x_1 + A_2 x_2 + A_3 x_3}{A_1 + A_2 + A_3} \quad \bar{y} = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3}$$

TOP FLANGE

$$A_1 = 4000 \text{ mm}^2 = 40 \text{ cm}^2; x_1 = 100 \text{ mm} = 10 \text{ cm}; y_1 = 250 \text{ mm} = 25 \text{ cm};$$

BOTTOM FLANGE

$$A_2 = 4000 \text{ mm}^2 = 40 \text{ cm}^2; x_2 = 100 \text{ mm} = 10 \text{ cm}; y_2 = 10 \text{ mm} = 1 \text{ cm};$$

WEB

$$A_3 = 4400 \text{ mm}^2 = 44 \text{ cm}^2; x_3 = 100 \text{ mm} = 10 \text{ cm}; y_3 = 130 \text{ mm} = 13 \text{ cm};$$

$$\bar{x} = \frac{A_1 x_1 + A_2 x_2 + A_3 x_3}{A_1 + A_2 + A_3} = \frac{40 * 10 + 40 * 10 + 44 * 10}{40 + 40 + 44} = \frac{1240}{124} = 10 \text{ cm}$$

$$\bar{y} = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3} = \frac{40 * 25 + 40 * 1 + 44 * 13}{40 + 40 + 44} = \frac{1612}{124} = 13 \text{ cm}$$

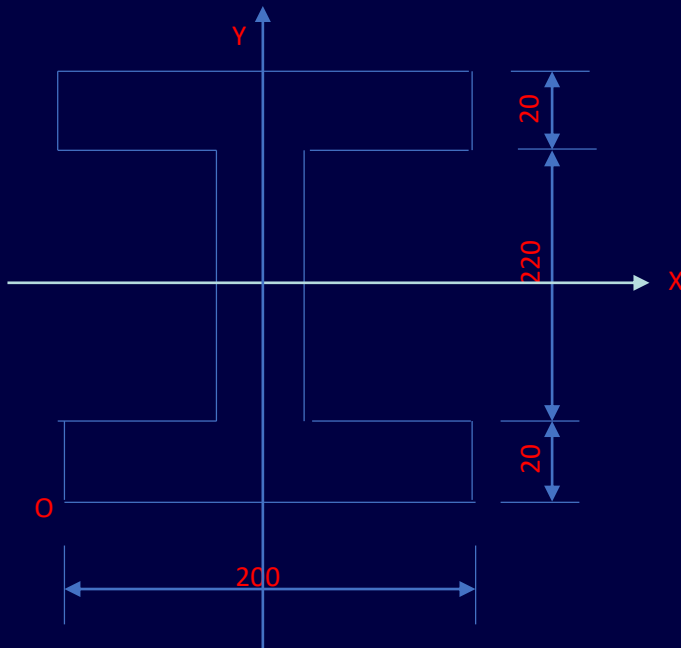
Calculate moment of inertia about x-axis,  $I_x$ , about y-axis,  $I_y$  and product of inertia  $P_{xy}$ .

$$I_x = \frac{1}{12} [b h^3 - b_1 h_1^3] = \frac{1}{12} [20 * 26^3 - 18 * 22^3] = 13321 \text{ cm}^4$$

$$I_y = 2 * \frac{1}{12} b_3 h_3^3 + \frac{1}{12} b_4 h_4^3 = 2 * \frac{1}{12} 2 * 20^3 + \frac{1}{12} 22 * 2^3 = 2681 \text{ cm}^4$$

$$P_{xy} = 0$$

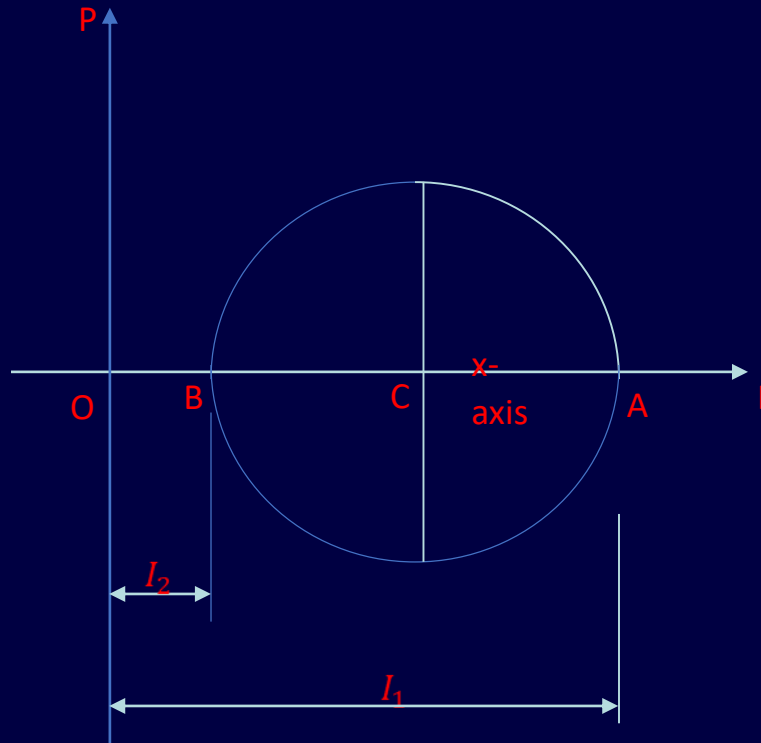
If an area has an axis of symmetry, this axis together with any axis perpendicular to it will form a set of axes for which the product of inertia is zero.



# Mohr's Circle for moment of inertia

<https://www.youtube.com/watch?v=XjKWxqCwX00>

$A (I_x, P_{xy}), B (I_y, -P_{xy}),$



Scale : 1 cm =

Measure OC and radius of Mohr's Circle R

Maximum moment of inertia,  $I_1 = OC + R, \theta = 0^\circ$

Minimum moment of inertia,  $I_2 = OC - R, \theta = 90^\circ$

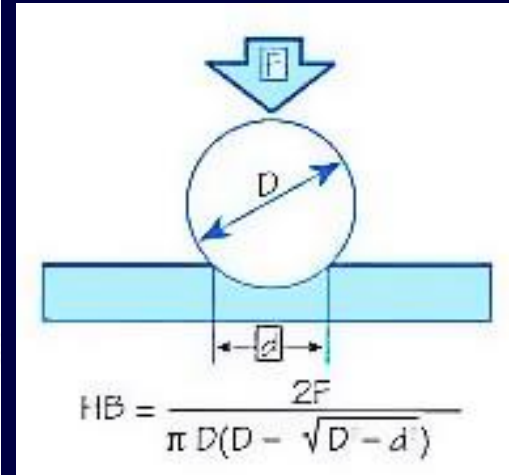
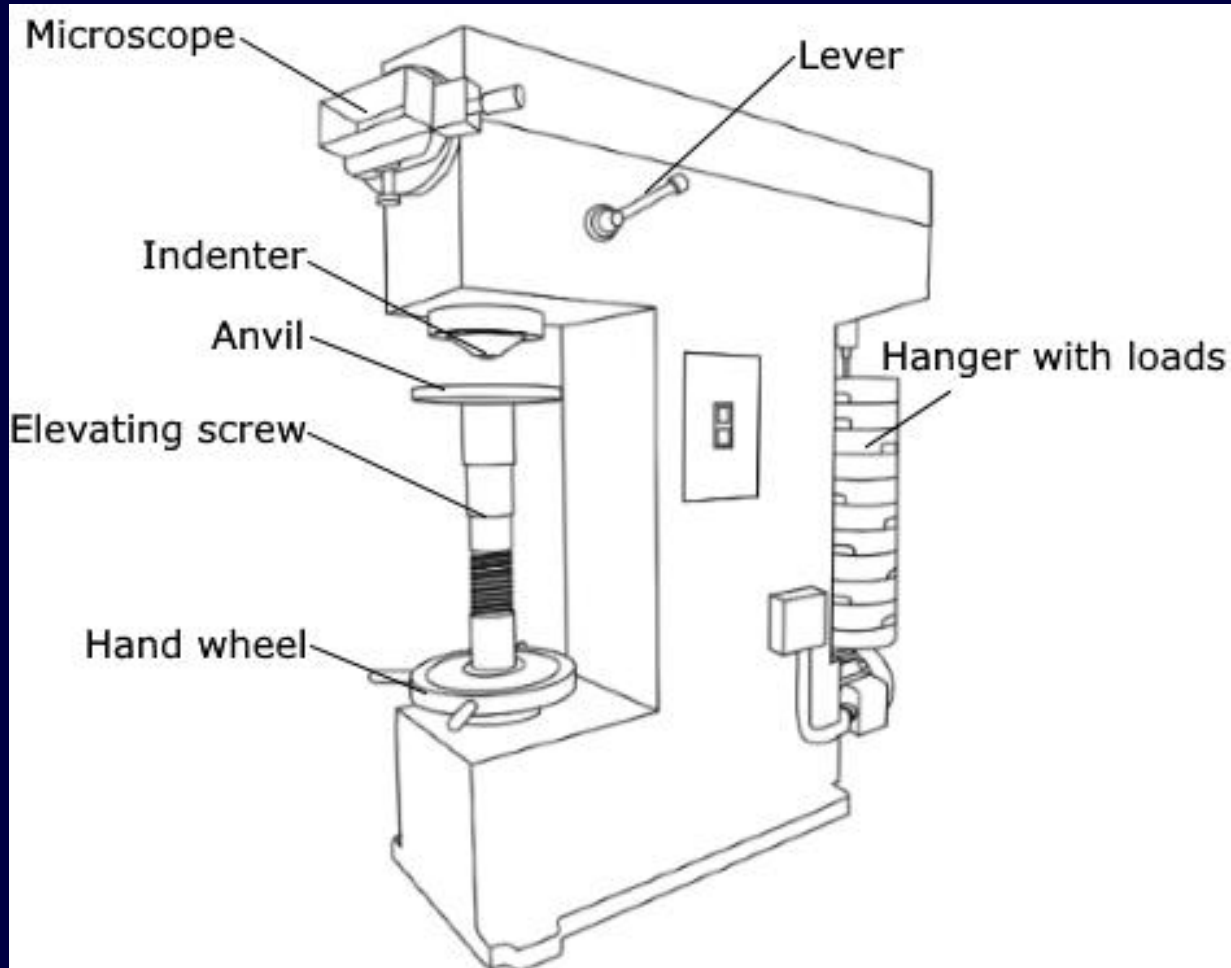
Maximum product of inertia,  $P_1 = R, \theta = 45^\circ$

Minimum product of inertia,  $P_2 = -R, \theta = 135^\circ$

Write the results in a tabular form

	$cm^4$	Direction from x-axis in the anticlockwise sense.
OC		
R		
$I_1$		
$I_2$		
$P_1$		
$P_2$		

# Brinell Hardness Test



$$HBW = \frac{2P}{\pi D[D - \sqrt{(D^2 - d^2)}]}$$

$$HBW = 0.102 \times \frac{2F}{\pi D[D - \sqrt{(D^2 - d^2)}]}$$

## Test Method Illustration

$P$  = Load in Kg

$D$  = Ball diameter (mm)

$d$  = impression diameter (mm)

HBW = Brinell result (Kg/mm<sup>2</sup>)

$F$  = load in Newton

# Brinell Hardness Test - Procedure

## STEPS:

1. When you click on a Brinell test file, a new window will open as shown below.

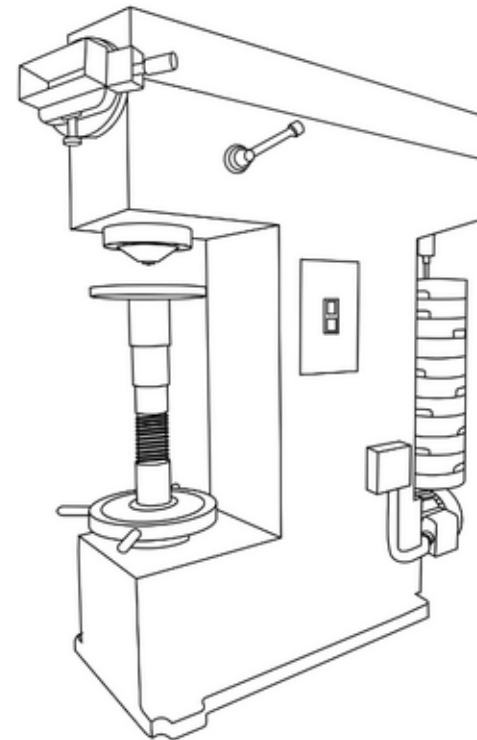
## BRINELL HARDNESS TEST

### Objective :

To determine the indentation hardness of mild steel, cast iron, brass, aluminium etc. using Brinell hardness testing machine.

### Apparatus used :

Brinell hardness testing machine





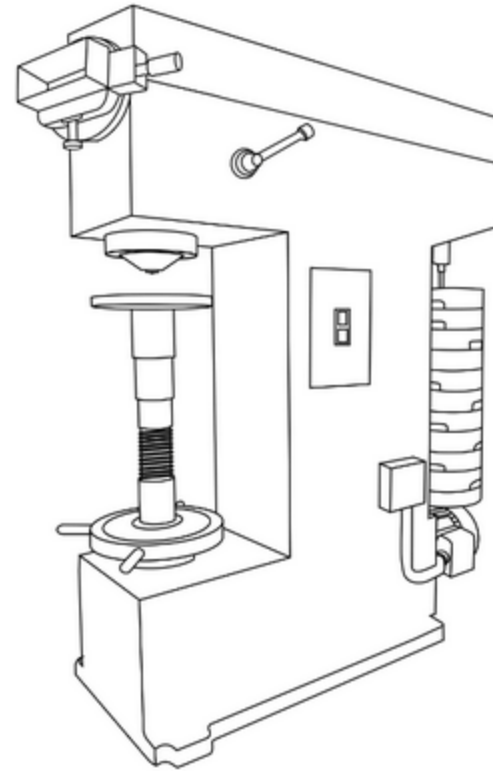
# BRINELL HARDNESS TEST

## Objective :

To determine the indentation hardness of mild steel, cast iron, brass, aluminium etc. using Brinell hardness testing machine.

## Apparatus used :

Brinell hardness testing machine



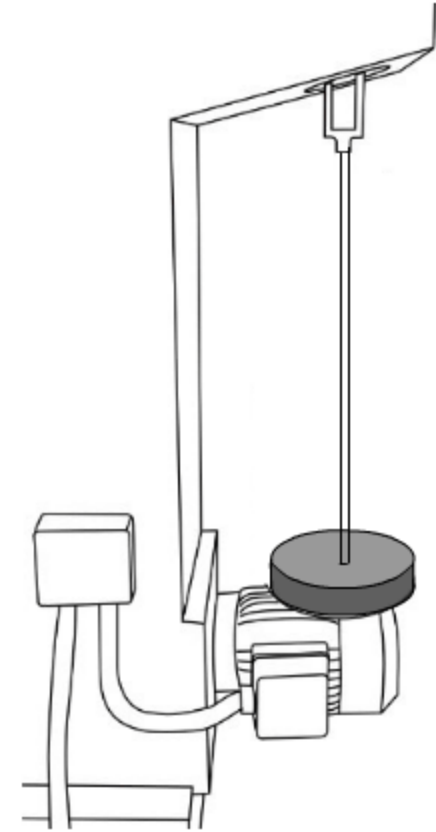
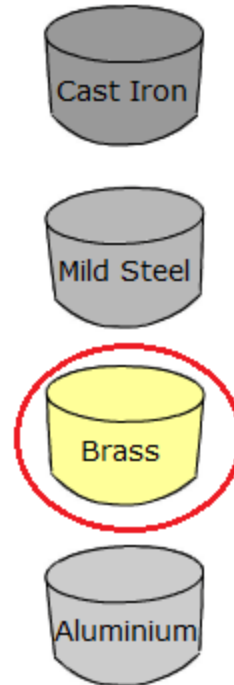
Click on the NEXT button at the bottom right corner to move to the next step.

Click on the material to select the required specimens and the load to be applied on that is shown, and then click on NEXT button.

## BRINELL HARDNESS TEST

**STEP 1** Diameter of the indenter  $D = 10\text{mm}$ . Select the load  $P$  based on the type of material selected (Mild steel, Cast Iron, Brass, Aluminium).

Select material :



The load to be applied on the selected specimen is displayed here, click NEXT button to mount the specimen on setup.

# BRINELL HARDNESS TEST

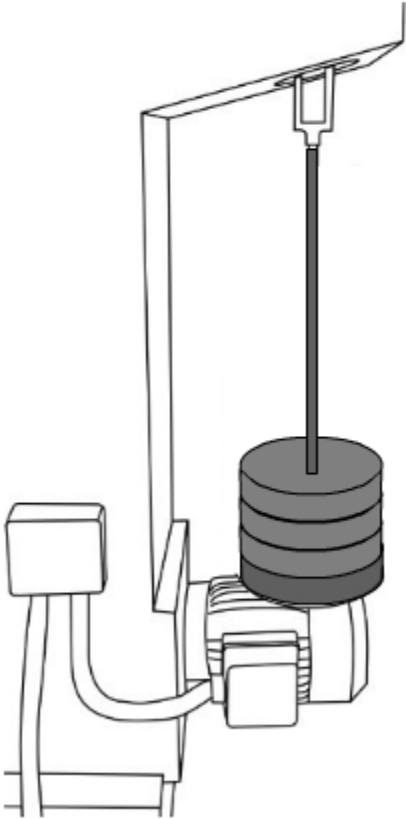
**STEP 1** Diameter of the indenter  $D = 10\text{mm}$ . Select the load  $P$  based on the type of material selected (Mild steel, Cast Iron, Brass, Alluminium).

Selected material : Brass      Load : 1000Kg



Material	Load 'P' (Kg), diameter 'D' (mm) (Diameter of the indenter $D=10\text{mm}$ )
Cast Iron & Mild Steel	$P=30, D^2 = 3000\text{Kg}$
Brass, copper & bronze	$P=10, D^2 = 1000\text{Kg}$
Aluminum, Magnesium & Zinc	$P=5, D^2 = 500\text{Kg}$

( Each weight is equivalent to 250Kg, supporting hanging rod and base plate is 250Kg )

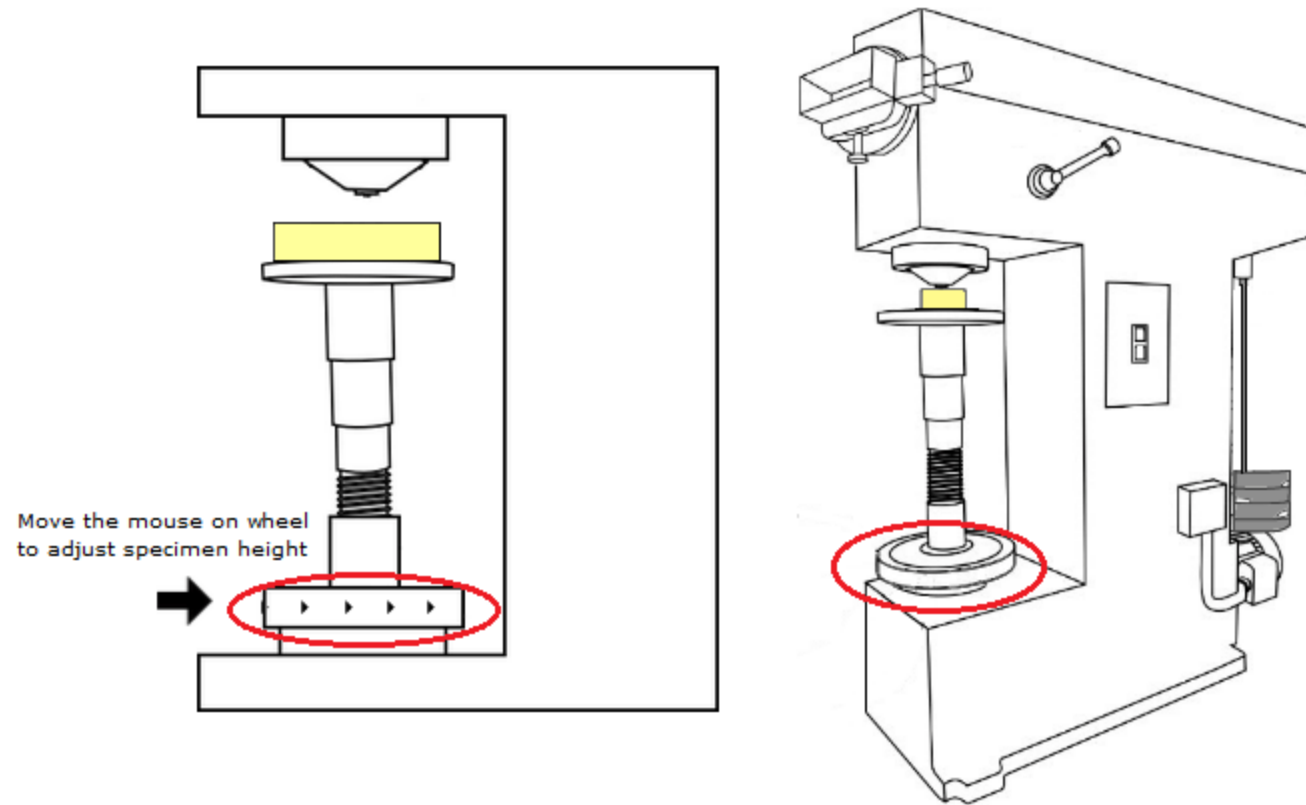


Click on hand wheel then move mouse pointer over the hand wheel to rotate it in clockwise direction till the specimen is in position, after adjusting the specimen in specified position then move to the next step by clicking on NEXT button.

## BRINELL HARDNESS TEST

**STEP 2** The specimen is placed on the supporting table, then the hand wheel below the table is turned in clockwise direction until the gap between the surface of the specimen and the indenter is 5mm.

**TRIAL : 1**

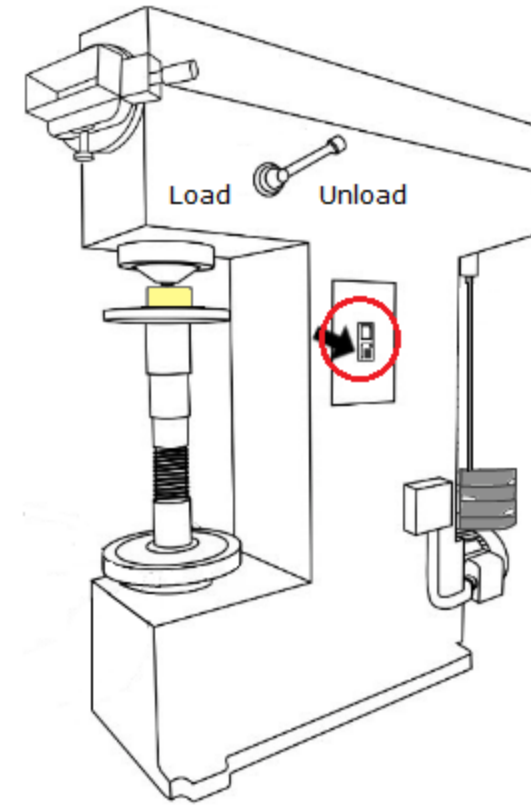


Switch on the machine and click on hand lever to apply load, again click on unload after applying load of 10 to 15 sec for ferrous material and up to 30sec for nonferrous material.

## BRINELL HARDNESS TEST

**STEP 3** The motor is switched ON. The hand lever is pulled into load position. The load is applied for a period of 10 to 15 seconds.

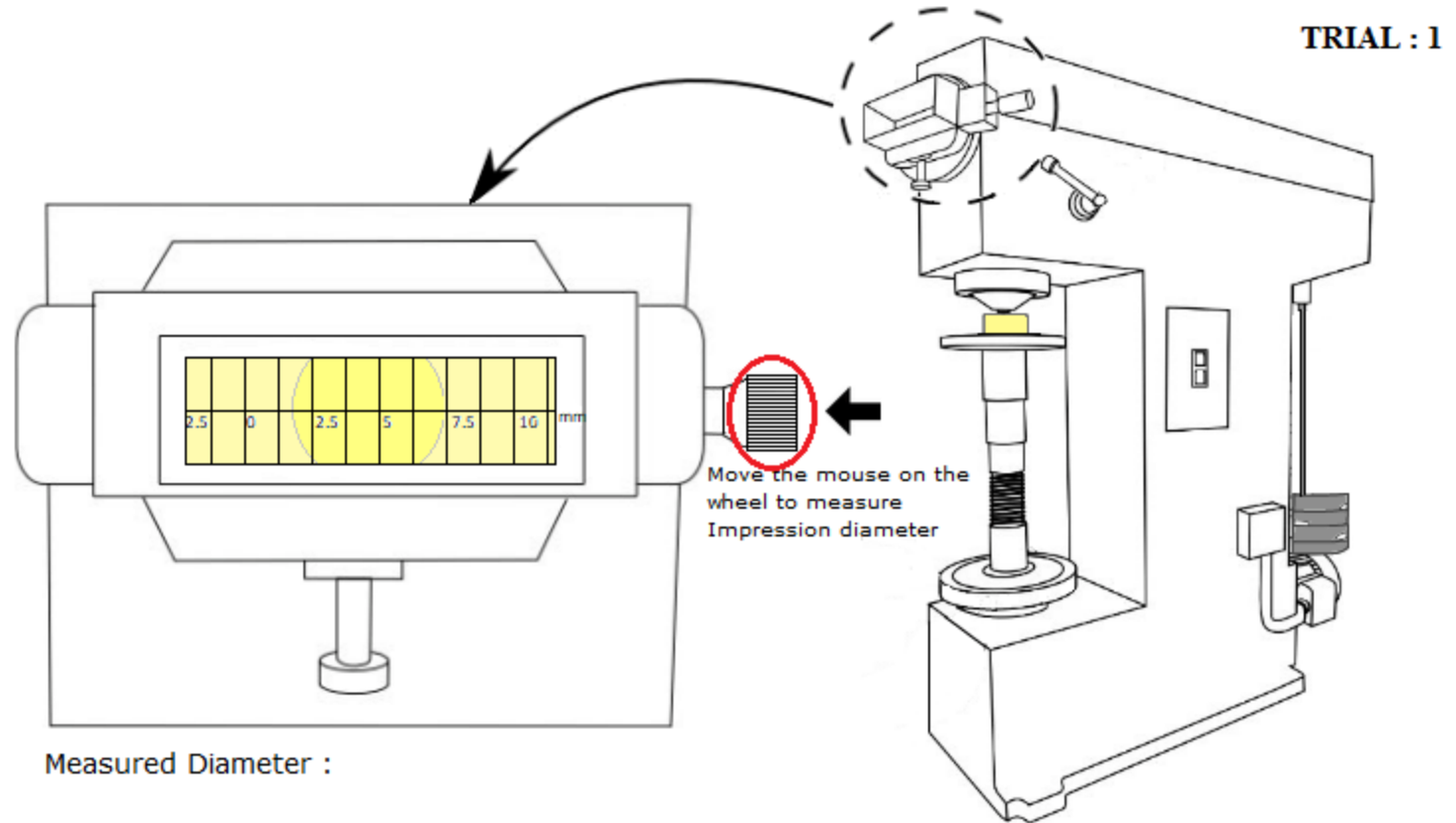
**TRIAL : 1**



Scroll mouse over the microscope adjusting screw to view the indentation, adjust the indentation corner to zero.

## BRINELL HARDNESS TEST

**STEP 4** The hand lever is pulled back into unload position. The diameter of the impression is measured through a microscope attached to the apparatus.

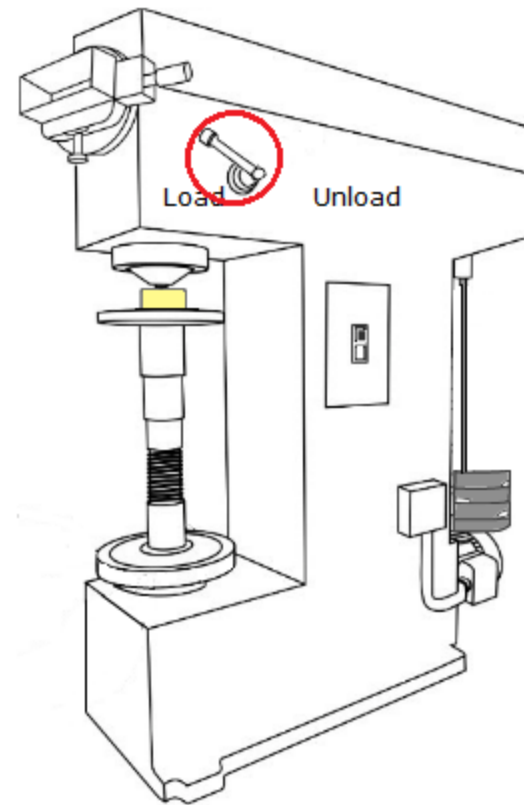
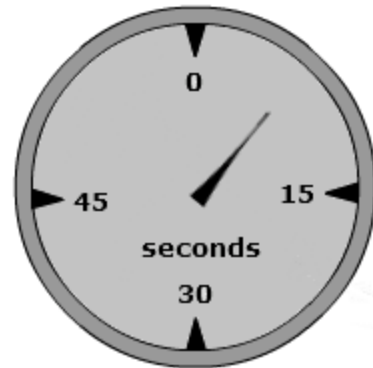


Click on hand lever again to stop the loading process.

## BRINELL HARDNESS TEST

**STEP 3** The motor is switched ON. The hand lever is pulled into load position. The load is applied for a period of 10 to 15 seconds.

**TRIAL : 1**



The observation of trial 1 is given; repeat the same steps for other trials.

## BRINELL HARDNESS TEST

### Observations:

Calculate the Brinell Hardness Number (HBW)

**TRIAL : 1**

*[HBW (H from hardness, B from brinell and W from the material of the indenter, tungsten (wolfram) carbide)]*

Material	Diameter of indenter D ( mm )	Load P ( Kg )	P/D <sup>2</sup>	Diameter of indentation ( mm )		Average diameter d <sub>i</sub> ( mm )	d/D	HBW (Kg/mm <sup>2</sup> )
				d <sub>ix</sub> ( mm )	d <sub>iy</sub> ( mm )			
Brass	10	1000	10	3.79	3.79	3.79	0.379	85.38

$$HBW = \frac{2 P}{\pi D [D - \sqrt{(D^2 - d^2)}]}$$

$$\text{Average diameter, } d_1 = \frac{d_{1x} + d_{1y}}{2}$$





The final average hardness value from different trials is given here.

## BRINELL HARDNESS TEST

### Observations:

Trial	Material	Diameter of indenter D ( mm )	Load P ( Kg )	Average diameter $d_i$ ( mm )	HBW ( Kg/mm <sup>2</sup> )	Average HBW ( Kg/mm <sup>2</sup> )
1	Brass	10	1000	3.79	85.38	93.64
2				3.48	101.9	

# Charpy Impact Test

















