



# Kinematic Synthesis of Planar Mechanisms

(Mechanisms Synthesis)

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## **Analysis vs. Synthesis**







In Kinematic Analysis one is given a mechanism & the task is to determine the various relative motion that can take place in that mechanism.

## **Synthesis**

- decision –making process
- Innovative or creative process
- process of creating new mechanism
- Selecting optimum/best configuration from no. of existing mechanism
- Determination of optimum dimensions of the elements of the mechanism on the basis of analysis

In Kinematic Synthesis one has to be come up with a design of mechanism to generate prescribed motion characteristic.



## Kinematics Synthesis of Plane Mechanisms or Linkages



### Aim:

Design or creation of a mechanism to obtain a desired set of motion characteristics.

#### **Objective**

- design of mechanisms to satisfy certain kinematic specification.
- In other words, motion characteristics are given & the mechanism is to be found

#### **Kinematic Synthesis Problems**

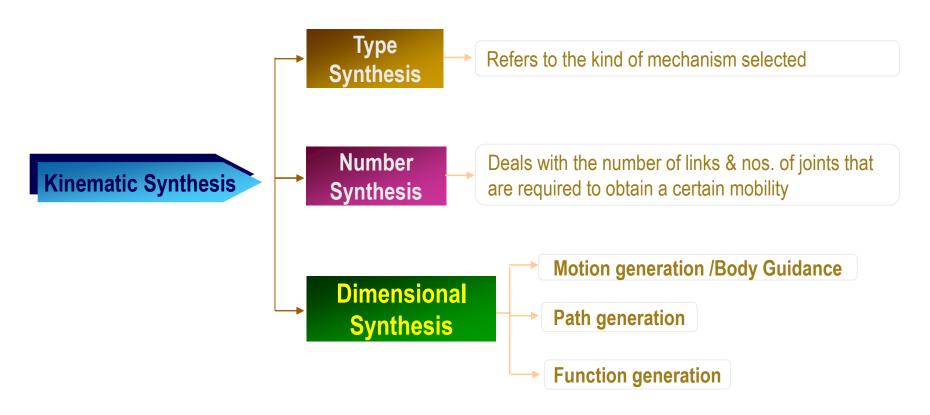
- Type Synthesis
- Number Synthesis
- Dimensional Synthesis



#### **Kinematic Synthesis of Mechanisms**



#### **Synthesis Problems**



By Dimensional Synthesis, we mean the determination of kinematic dimensions of the individual links of a mechanism to satisfy specified motion characteristics or specified tasks.



#### **Classification of Dimensional Synthesis Problems**



Depending on the required kinematic characteristics to be satisfied by the designed mechanism or linkage, dimensional synthesis problems can be broadly classified as given below:

#### **Motion generation /Body Guidance**

In this general class of synthesis problem, the linkage has to be so designed that a rigid body (i.e., one link of the mechanism, for example the coupler of a 4R linkage) can be guided in a prescribed manner.

The guidance may or may not be coordinated with the input motion

#### Path generation

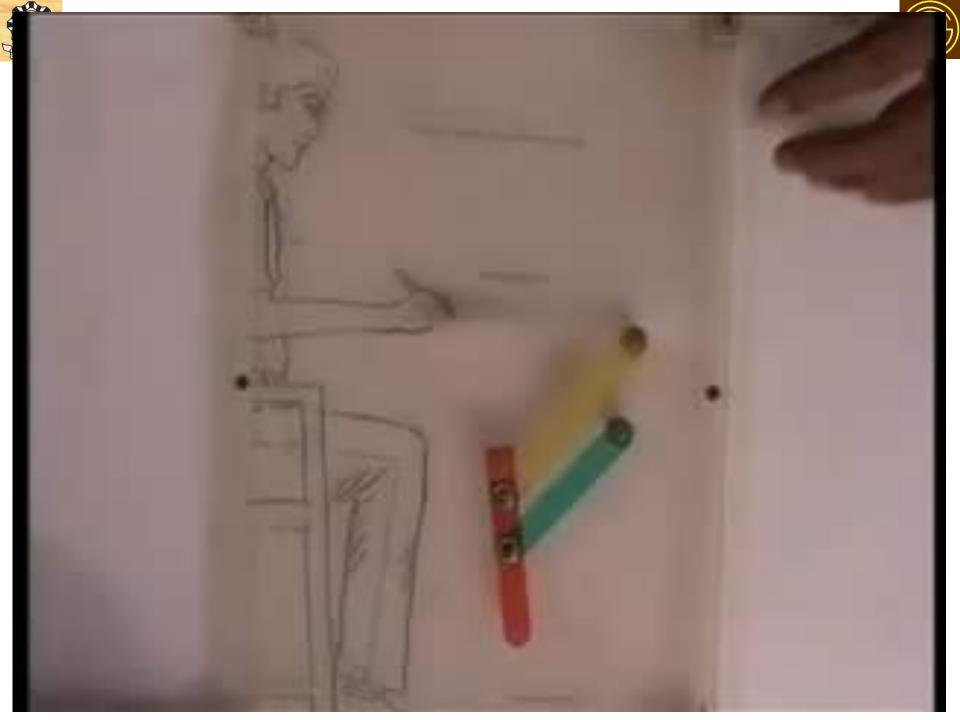
If a point on the floating link (i.e. link not connected to the frame, like coupler) of a mechanism has to be guided along a prescribed path, then such a problem is classified as a path-generation problem.

This refers to a problem in which a coupler point is to generate a path having a prescribed shape

The generation of a prescribed path may or may not be coordinated with the input motion

#### **Function generation**

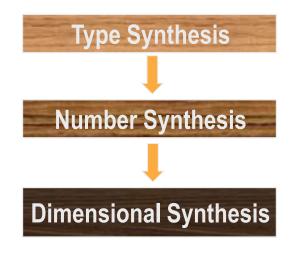
In this class of problem, the motion parameters (displacement, velocity, acceleration etc.) of the output & input links are to be coordinated so as to satisfy a prescribed functional relationship. The output & input motion characteristics have to maintain a specified functional relationship

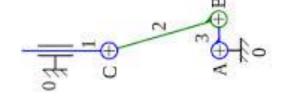




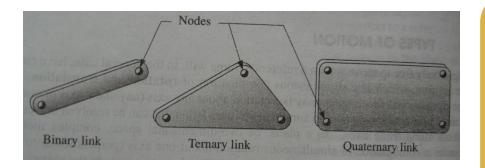
#### **Steps in Kinematics Synthesis of Plane Mechanisms**



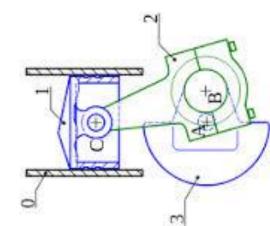




#### What is Kinematic dimensions?



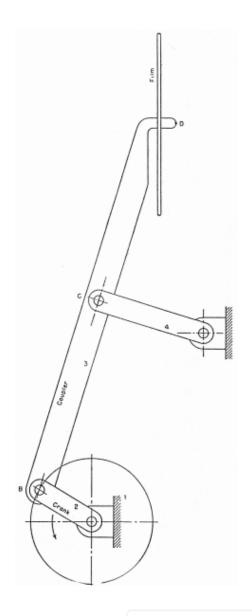
Node-node
distance
or
joint centre to
centre
distance etc.















Path generation



#### **Function generation problem**



In function generation, rotation (or translation) motion of input and output links must be correlated. The kinematic Synthesis task may be to design a linkage to commetate input and output Such that ors the input moves by x', the output makes by y=f(x) for the range x < X < xuri

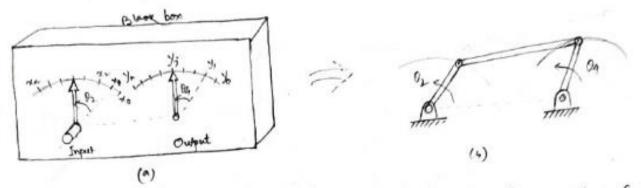
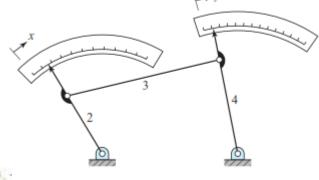


Fig. 1 Function-generated mechanism (a) exterior view, (b) Schemotic of the mechanism inside.

(i.e. four-bar linkage function generator)

In the case of rotatey input and output, the angles of rotation of linear amalogs of x and y respectively.

When the input is rotated to a value of the independent parameter in the black box' causes the output link to torn to the corresponding value of the dependent variable y = f(x). This may be regarded as a simple case of a mechanical analy computer.





#### **Function generation problem**



Fig. 2 Shows a Six-link function generator mechanism in which two four-link mechanisms are joined in a Series. The objective in this linkage is to provide a measure of the Dethug are joined in a Series. The weir where the input is the vertical translation 'x' of the inates level, trate (i.e y) through the weir where the input is the vertical translation 'x' of the inates level,

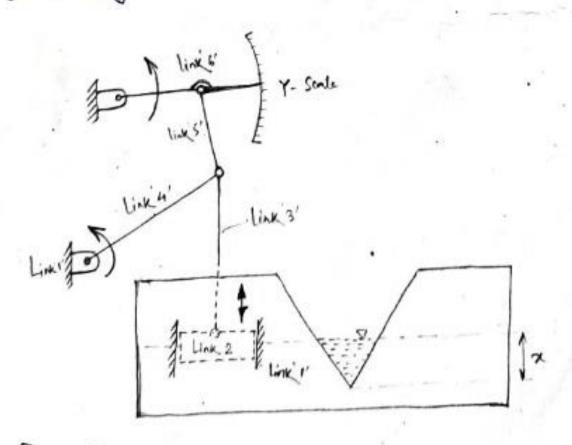
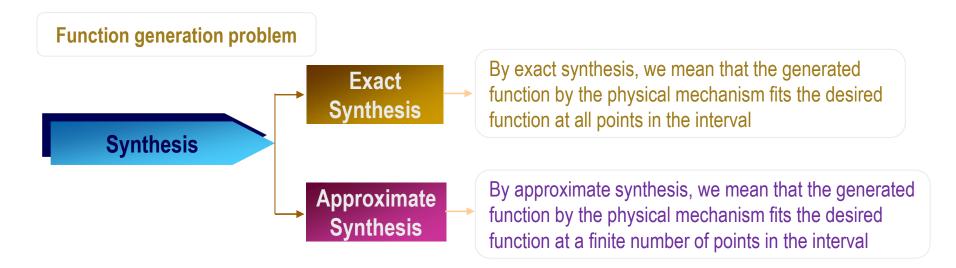


Fig. 2: Flow rate indicator mechanism. yof(x)



#### **Dimensional Synthesis Problems**



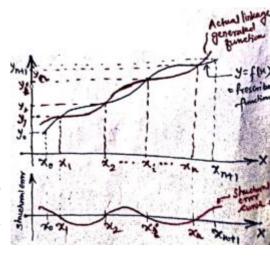


#### **Accuracy points / Precision points**

The points at which the generated and desired functions agree

#### **Structural Error**

It is defined as the theoretical difference between the function generated by the synthesized linkage & the function originally prescribed





#### **Chebyshev's Spacing of Accuracy Points**



Let y=f(x) be the function desired to be generated in an interval  $x_0 \le x \le x_{n+1}$ :

Let the mechanism generated function be  $F(x, R_1, R_2, ......, R_k)$  where  $R_1, R_2, .....$   $R_k$  are design parameters

#### **Structural Error**

$$E(x)=f(x)-F(x, R_1, R_2,..., R_k)$$

The best choice for the spacing of accuracy points will be that which gives the min. value of E(x) between any two adjacent points:

However, Chebyshev's spacing of accuracy points can always be taken as a first approximation

A very good trial for the spacing of these precision positions is called Chebyshev Spacing



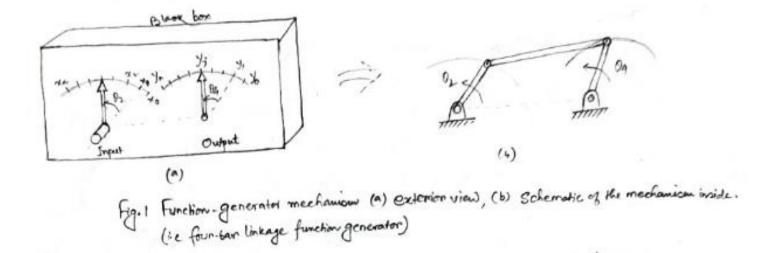
#### **Chebyshev's Spacing of Accuracy Points**



For 'n' precision positions in the range  $x_0 \le x \le x_{n+1}$ , the Chebyshev's spacing is

$$x_j = \left(\frac{x_{n+1} + x_0}{2}\right) - \left(\frac{x_{n+1} - x_0}{2}\right) G_s \left\{\frac{(2j-1)\pi}{2n}\right\} \quad \text{where } j = 1, 2, \dots, n.$$

Determine the three accuracy points with Chebyshev's spacing for a 4 bar linkage to generate the function  $y=x^{0.8}$  in the interval  $1 \le x \le 3$ ,







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Here 
$$n=3$$
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#### **Function generation problem**



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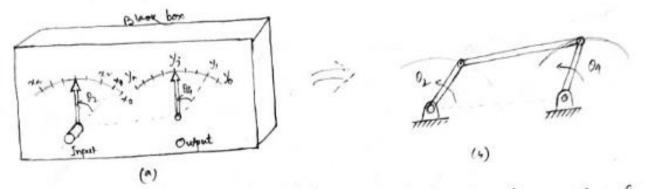
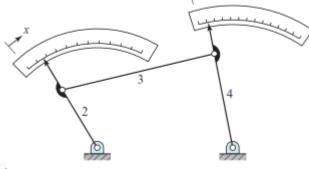


Fig. 1 Function-generator mechanism (a) externior view, (b) Schematic of the mechanism inside.

(i.e. four-tern linkage function generator)

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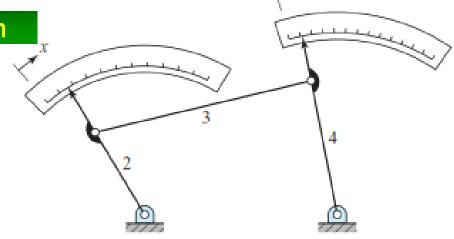
#### **Scale Factor for Input & Output motion**

**Mechanized variables:** 

02 4 04

**Functional variables:** 

x'1 y'



The orientation of the driver link (02) represents the independent variable 'x'.

The orientation of the driven link (04) represents the dependent variable 'y'.

The mechanized variables 02 f 04 are proportional to the functional variables x' 1 y'.

The relation bet ax and 102 f that bet by and 104 is usually assumed to be linear.

With the mappings bet function variable space (x, y) and mechanism joint space (2, 2) theorem, we can map the three function precision points to corresponding precision joint angles.

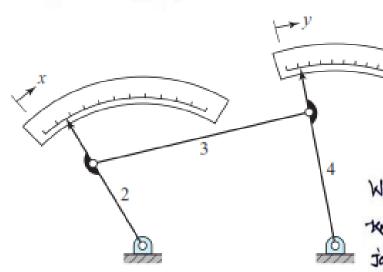


Let  $\theta_2^{(i)}$  be the initial value of  $\theta_2$  representing Bq be " " " 1 89

$$\frac{\int_{\text{cole form}} x_{-\frac{4\theta_{2}}{4x}} \frac{\theta_{2}^{(f)} - \theta_{2}^{(f)}}{\chi_{n+1} - \chi_{0}} = \frac{\theta_{2} - \theta_{2}^{(f)}}{\chi - \chi_{0}}$$

$$m_{y} = \frac{4\theta_{1}}{4y} = \frac{\theta_{1}^{(f)} - \theta_{1}^{(i)}}{y_{n+1} - y_{0}} = \frac{\theta_{1} - \theta_{1}^{(i)}}{y - y_{0}}$$

denote the initial of final values of



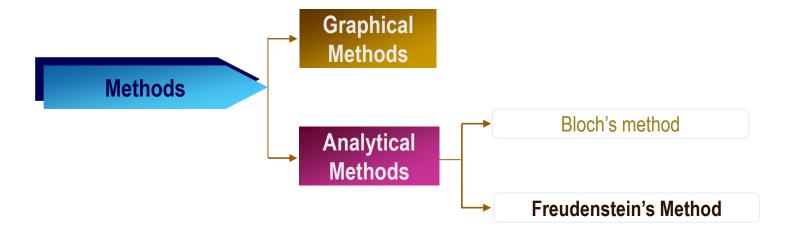
$$\theta_2 - \theta_2^{(i)} = m_x(x - x_0) = 0$$
  $\theta_2 = \theta_2^{(i)} + m_x(x - x_0)$  where  $m_x = \frac{\theta_2^{(f)} - \theta_2^{(i)}}{x_{n+1} - x_0}$   $\theta_4 - \theta_4^{(i)} = m_y(y - y_0) = 0$   $\theta_4 = \theta_4^{(i)} + m_y(y - y_0)$  where  $m_y - \frac{\theta_4^{(f)} - \theta_4^{(i)}}{y_{nn} - y_0}$ 

With the mappings bet function variable space (x, y) and mechanism joint space (8, 4) tensor, we can map the three function precision points to corresponding precision







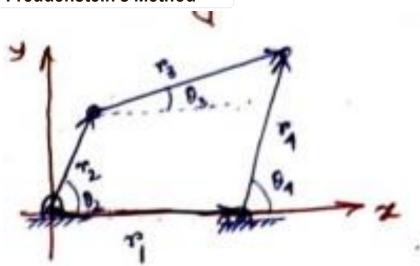


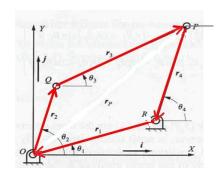


#### Displacement Analysis of 4R linkage



#### Freudenstein's Method





Two Scaler egas.

#### **Loop Closure Equation in Scalar Form**







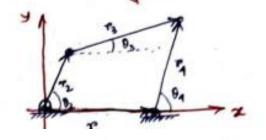


## FREUDENSTEIN'S METHOD: Function Generation with Three Accuracy Points.



With three accuracy points, the number of design parameters that can be determined is three.

Example , Four-bar Function Generators with Three Accuracy Points



Substituting the three related pairs (0,0) + (0,0), (0,0) + (0,0) and (6,0)+ (0,0), Successively) in eq (A), we obtain three linear Simultanemore, in k1, k2 1 kg.

Solving above linear egos, we get the ky ky they is link length raters (design parameters) (1) - (1): K, [G, 0] - G, 0, ) - K2 [G, 0, - G, 0, ()] = G, (0, - 0, ) -G, (0, -0) (1) - (1) : K, [G, 0, (6) - G, 0, (1)] - K2 [G, 0, (6) - 6, (1)] = cm (0, (1) - 6, (0) - 6, (

Some two ego for two uniqueness





#### Example # 2

Determine the lengths of the links of a 1 bar linkage to generate  $y = lag_{10} \times$  in the interval 1 < x < 10. The length of the Smalless link is 5 cm. Use three accuracy points with chebysher's spacing? Give 03(1)= 45°, 02(1)= 105°, 04 = 135° + 841 = 2550 45° < 02 < 105° ; 135 < 04 < 225°

Given deta: 
$$N = 3$$
 $x_j = {x_{n+1} + x_0 \choose 2} - {x_{n+1} + x_0 \choose 2} G_s \left\{ {x_{j-1} \choose 2n} \right\}$ 
 $x_0 = 1$ 
 $x_1 = 10$ 

is

 $x_j = {x_{n+1} + x_0 \choose 2} - {x_{n+1} + x_0 \choose 2} G_s \left\{ {x_{j-1} \choose 2n} \right\}$ 
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$$x_0 = 1$$
  $\Rightarrow y_0 = \log_{10}(1) = 0$   $\Rightarrow y_4 = \log_{10}(1) = 1$ .



#### **Scale Factor for Input & Output motion**

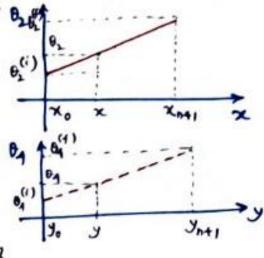


Let 
$$\theta_2^{(r)}$$
 be the initial value of  $\theta_2$  representing to  $\theta_3^{(r)}$  be " " " of  $\theta_3$  "  $\theta_3$  = f(x<sub>0</sub>)

The input of contput weale factors mx 1 my resp. are defined so: Bath

$$Scale for m_{\frac{4}{4}} = \frac{\theta_{2}^{(f)} - \theta_{2}^{(f)}}{x_{n+1} - x_{0}} = \frac{\theta_{2} - \theta_{2}^{(i)}}{x - x_{0}}$$

$$m_{y} = \frac{46_{1}}{4y} = \frac{\theta_{1}^{(f)} - \theta_{1}^{(i)}}{y_{n+1} - y_{o}} = \frac{\theta_{1} - \theta_{1}^{(i)}}{y - y_{o}}$$



The Superscripes 'i' & if denote the initial & final values of

$$m_{\chi} = \frac{105 - 45^{\circ}}{10 - 1} = \frac{\theta_2 - 45^{\circ}}{2 - 1}$$

$$m_y = \frac{225 - 135}{1 - 0} = \frac{64 - 135}{y - 0}$$

$$\theta_1 = 90(y - 0) + 135$$





	7,000	9 100113	or Pracision Pri		n (i)
Position		-		00	4
1	1.6	490	0.204	14-69	153.36
2	5.5	750	0.341	14-69	201169
3	9.4	1010	0.974	19246	222160

Freudenskin 'eg"

TK,= 2.0; K2=-0.7015; K3= 1.081





$$TK_{3} = \frac{x_{1}^{2} + x_{2}^{2} + x_{3}^{2} - x_{3}^{2}}{2x_{2}x_{4}} = 1.081$$

$$\frac{x_{1}^{2} + x_{1}^{2} + \left(\frac{x_{1}}{0.3015}\right)^{2} - x_{3}^{2}}{2x_{1}/2 \cdot \left(\frac{x_{1}}{0.3015}\right)^{2} - x_{3}^{2}} = 1.081$$

$$+ \left[\frac{x_{1}^{2} + x_{1}^{2}/4 + \left(\frac{x_{1}}{0.3015}\right)^{2} - x_{3}^{2}}{x_{1}^{2}}\right] = -\frac{1.081}{0.3015}$$

$$1 + \frac{1}{4} + \left(\frac{1}{0.3015}\right)^{2} - \left(\frac{x_{3}}{3}\right)^{2} = -\frac{1.081}{0.3015}$$

$$\left(\frac{x_{3}^{2}}{3}\right)^{2} = (2.1962)^{2} \qquad \frac{x_{3}^{2}}{3} = 2.1962$$

$$\frac{x_{1}^{2}}{3} = 0.462$$





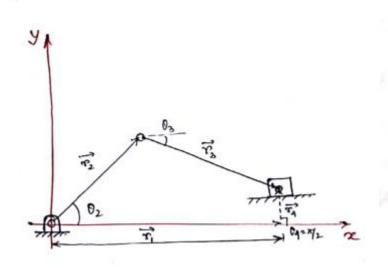
from above it is clear that 
$$T_{3} = 0.462$$

from above it is clear that  $T_{3} = 0.462$ 
 $T_{2} < T_{1}$ 
 $T_{2} < T_{1}$ 
 $T_{3} < T_{4}$ 
 $T_{4} < T_{5}$ 
 $T_{5} < T_{1} < T_{2}$ 
 $T_{7} < T_{1} < T_{2}$ 
 $T_{1} < T_{2} < T_{1} < T_{3}$ 
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## Synthesis of the Slider-Crank Mechanism with three accuracy points



Loop - closure ego  

$$\overrightarrow{R_2} + \overrightarrow{P_3} = \overrightarrow{R_1} + \overrightarrow{P_4}$$
  
Scalar Component of the ego.  
 $P_2 \cos\theta_2 + r_3 \cos\theta_3 = r_1 \cos\theta_1 + r_4 \cos\theta_4$   
 $P_2 \sin\theta_2 + r_3 \sin\theta_3 = r_1 \sin\theta_1 + r_4 \sin\theta_4$ 

$$r_3 \cos \theta_3 = r_1 + 0 - r_2 \cos \theta_2$$
 $r_3 \sin \theta_3 = 0 + r_4 - r_2 \sin \theta_2$ 
Squarity + adding
$$r_3^2 = (r_1 - r_2 \cos \theta_2)^2 + (r_4 - r_2 \sin \theta_2)^2$$

where 9=0°, 09=172





$$T_{3} \cos \theta_{3} = r_{1} + 0 - r_{2} \cos \theta_{2}$$

$$T_{3} \sin \theta_{3} = 0 + r_{4} - r_{2} \sin \theta_{2}$$

$$Squaring + adding$$

$$T_{3}^{2} = (r_{1} - r_{2} \cos \theta_{2})^{2} + (r_{4} - r_{2} \sin \theta_{2})^{2}$$

$$T_{3}^{1} = r_{1}^{2} + r_{2}^{2} + r_{4}^{2} - 2r_{1}r_{2} \cos \theta_{2} - 2r_{2}r_{4} \sin \theta_{2}$$

$$2r_{1}r_{2} \cos \theta_{2} + 2r_{2}r_{4} \sin \theta_{2} - (r_{2}^{2} - r_{3}^{2} + r_{4}^{2}) = r_{1}^{2}$$

 $K_1 S (cs\theta_2 + K_2 S ln\theta_2 - K_3 = S^2)$ , where  $K_1 = 2r_2$ Substituting the three rotated pairs  $K_3 = r_2^2 - r_3^2 + r_4^2$  $\left[g_2^{(i)}, s_3^{(i)}\right], \left[g_2^{(2)}, s_3^{(3)}\right] + \left[g_3^{(3)}, s_3^{(3)}\right]$  Vanisher  $r_1 = S$  (Sliding)





K15 6302 + K2 SIDB2 - K3 = 52

Successively in above eq", we obtain three linear Simultaneous eq.





Example #

Design a Whicher-Crank mechanism in which the white displacement is proportional to the square of the voronce interval in the interval of \$135°. The initial and final volue of Slicer displacement Asition are 10 and \$3 an respectively. Use the three point chebyshar spacing. The dreets of Slicer mother is parallel to 4. mish