

⑩ Use example from problem ⑨ with a slight modification.

Let  $A_n = [0, \frac{1}{n}]$ , a closed interval

note that, as before,  $A_{n+1} \subset A_n$

And  $\lim_{n \rightarrow \infty} A_n = [0, 0] = \{0\}$  a single element

Proof: given an arbitrary  $n$ ,

$$A_n = [0, \frac{1}{n}] \text{ and } A_{n+1} = [0, \frac{1}{n+1}]$$

note that  $\frac{1}{n+1} < \frac{1}{n}$  so each element of  $A_{n+1}$  exists in  $A_n \Rightarrow A_{n+1} \subset A_n$

Also,  $\lim_{n \rightarrow \infty} A_n = [0, 0] = \{0\}$  a single element

And the intersection of any  $A_n$  with  $[0, 0]$  will be the single element  $\{0\}$