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## Supplementary information

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# Micro cold traps on the Moon

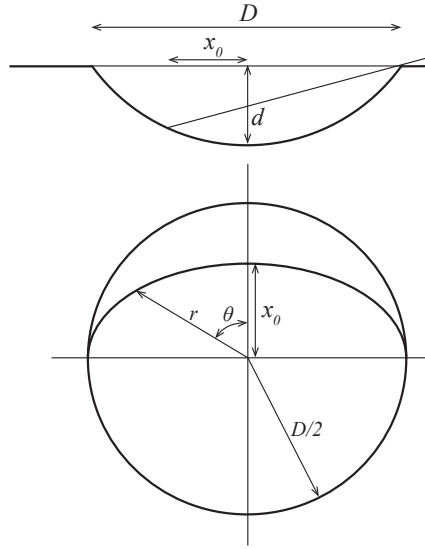
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In the format provided by the  
authors and unedited

*Supplementary Material for*  
**Micro cold traps on the Moon**

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**Supplementary Figures**



Supplementary Figure 1: Vertical and horizontal cross sections of spherical crater with shadow, with definitions for variables.

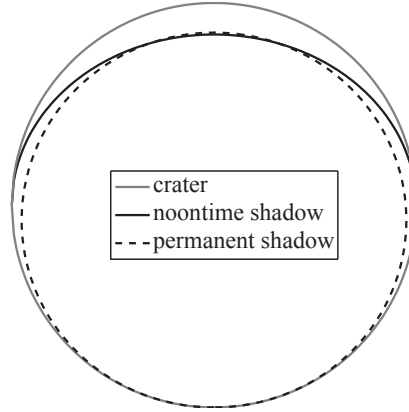
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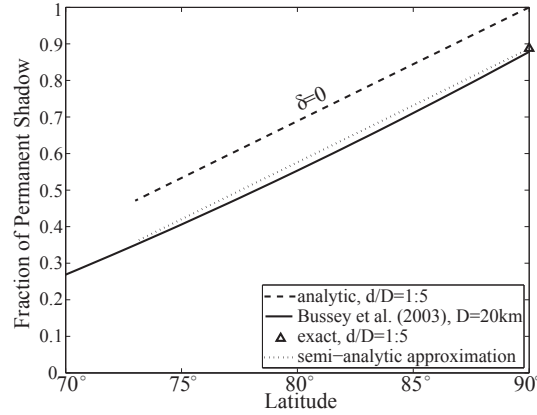
<sup>2</sup>Helen Kimmel Center for Planetary Science, Weizmann Institute of Science, Rehovot, Israel.

<sup>3</sup>Planetary Science Institute, Tucson, Arizona, USA.

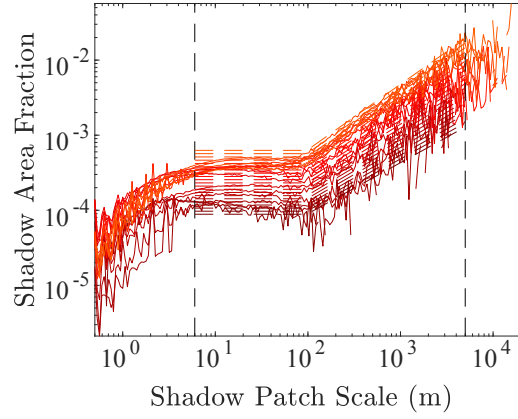
<sup>4</sup>Planetary Science Institute, Honolulu, Hawaii, USA



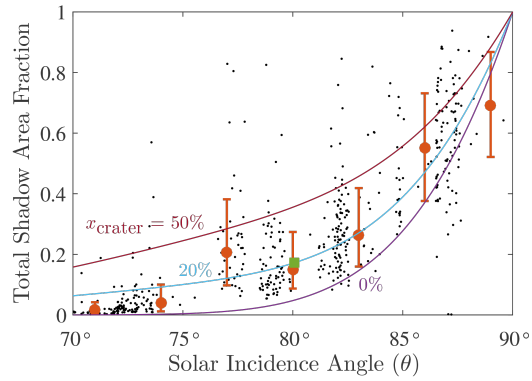
Supplementary Figure 2: Top view of circular crater with the exact noontime shadow boundary and the approximate extent of permanent shadow. The diameter to depth ratio of the crater is 5 and the maximum elevation of the Sun,  $e_0$ , is  $4^\circ$ .



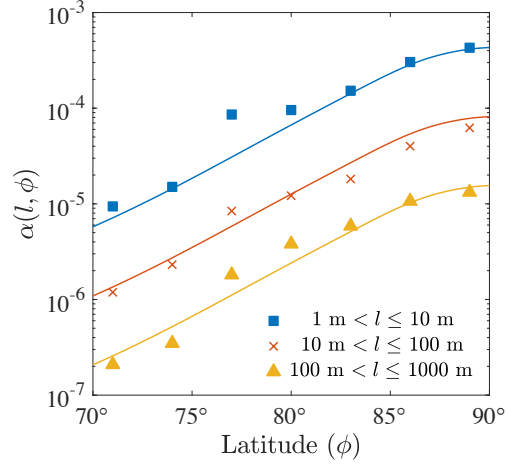
Supplementary Figure 3: Comparison between the numerical results of Bussey et al.<sup>1</sup>, the analytic result for zero declination (??), and approximation (??). The triangle shows the analytic result for the pole (??).



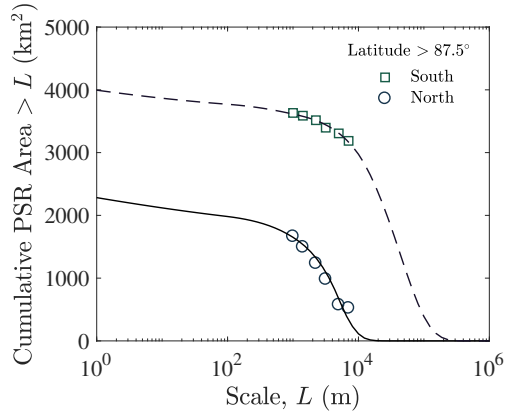
Supplementary Figure 4: Instantaneous shadow fraction from LROC-NAC images for a range of solar incidence angles ( $68^\circ$ ,  $69^\circ$ , ...,  $88^\circ$ , lighter tones representing increasing incidence angle), binned in logarithmically spaced shadow patch scales from 0.5 m to 50 km. Dashed lines represent a fit to the data.



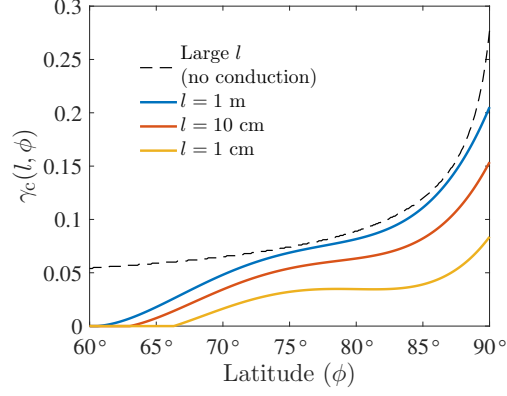
Supplementary Figure 5: Comparison of shadow fraction from LROC image data (points) to the model (curves). Error bars indicate the mean and standard deviations within each solar incidence angle bin, and  $x_{\text{crater}}$  is the area occupied by craters within the rough terrain.



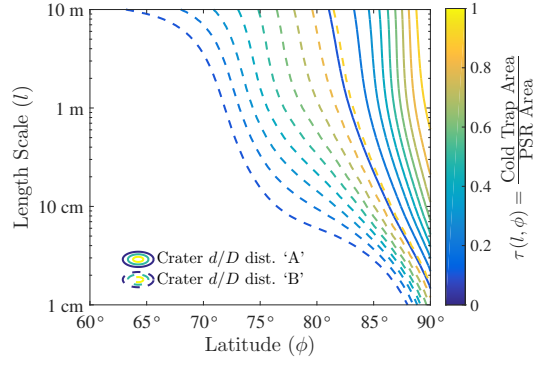
Supplementary Figure 6: Fraction  $\alpha$  (units of  $\text{m}^{-1}$ ) of the total surface area occupied by permanent shadows as a function of latitude  $\varphi$  and length scale  $l$ . The model curves shown assume a crater fraction of 20% and inter-crater plains with RMS slope  $\sigma_s = 5.7^\circ$



Supplementary Figure 7: Cumulative fraction of the total surface area occupied by permanent shadows with length scale  $l > L$ . Data points are from Mazarico et al.<sup>2</sup>, for each polar region,  $> 87.5^\circ$ .

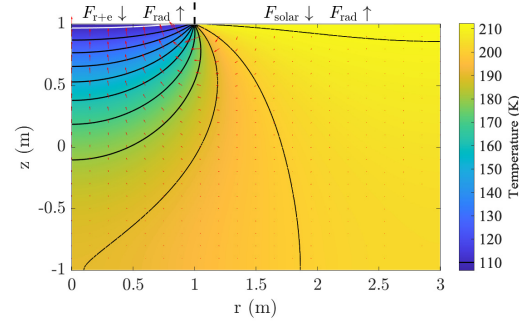


Supplementary Figure 8: Critical depth/diameter ratio  $\gamma_c$  of craters, for which  $\gamma < \gamma_c$  indicates the PSR is a cold trap for water ice.

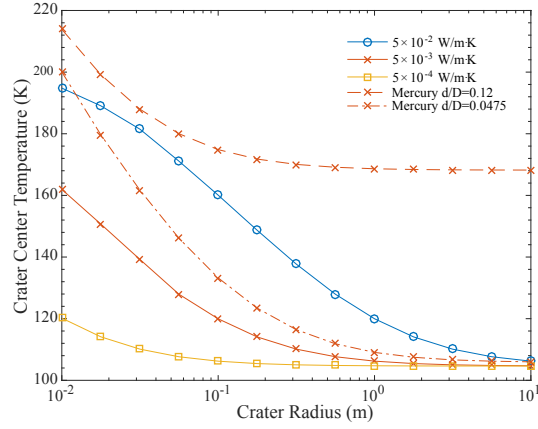


Supplementary Figure 9: Fraction of permanently shadowed regions (PSR) inside craters that are cold traps for water ice,  $T_{\max} < 110$  K. Results are shown for two log-normal probability distributions ‘A’ (deeper craters,  $\mu = 0.14$ ) and ‘B’ (shallower craters,  $\mu = 0.076$ ). Contours are plotted for  $\tau = 0.1, 0.2, \dots, 0.9$ .

a)



b)



Supplementary Figure 10: Solution to the heat equation in a cylindrically symmetric geometry. a) Cross section through the domain showing temperature contours and heat flow directions. b) Temperature at the center of a crater (representing the minimum temperature) for different thermal and orbital assumptions.

## References

- [1] Bussey, D. B. J. *et al.* Permanent shadow in simple craters near the lunar poles. *Geophys. Res. Lett.* **30**, 1278 (2003).
- [2] Mazarico, E., Neumann, G. A., Smith, D. E., Zuber, M. T. & Torrence, M. H. Illumination conditions of the lunar polar regions using LOLA topography. *Icarus* **211**, 1066–1081 (2011).