

Clustering Algorithms Explored:

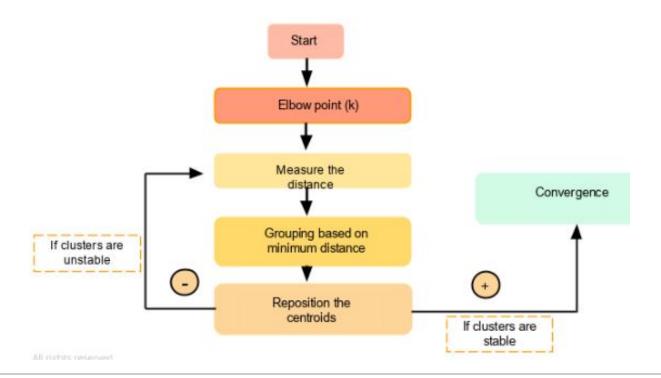
- Clustering algorithms are unsupervised machine learning algorithms so there is no label associated with data points.
- This technique involves grouping similar data points together into clusters based on certain characteristics.
- The goal of clustering is to discover inherent patterns or structures in the data without any predefined labels.

K-means Clustering: 😽 🔠 💵



K-means algorithm identifies k number of centroids, and then allocates every data point to the nearest cluster, while keeping the centroids as small as possible. The 'means' in the K-means refers to averaging of the data; that is, finding the centroid.

Here's how K-means clustering works:



1. Initialization: -

Choose the number of clusters K. Randomly initialize K cluster centers (centroids) in the feature space.

2. Assignment Step:

For each data point, calculate its distance to each cluster center. Assign the data point to the cluster with the nearest center.

3. Update Step:

Recalculate the cluster centers by taking the mean of all data points assigned to that cluster.

4. Repeat Assignment and Update:

Iteratively repeat the assignment and update steps until convergence or a maximum number of iterations.

K-means tries to minimize the within-cluster sum of squared (wcss) distances, which means that it aims to create clusters where the data points are close to the center of their own cluster.

Limitations of K-means Clustering:

- Sensitive to Initial Conditions: Different initializations might lead to different results.
- Number of Clusters: The number of clusters (K) must be specified in advance.
- Assumption of Spherical Clusters: K-means assumes that clusters are spherical and equally sized, which might not be true for all datasets.
- Outliers: K-means is sensitive to outliers as they can significantly affect cluster centroids.

Importing Libraries

```
In [1]: import pandas as pd
    import numpy as np
    import matplotlib.pyplot as plt
    import seaborn as sns
    import plotly.express as px
    sns.set()
    %matplotlib inline

import warnings
warnings.filterwarnings('ignore')
```

I Loading Dataset

```
In [2]: dataset = 'Bank-data.csv'
df = pd.read_csv(dataset)
df.head()
```

Out[2]:

l	Churr	duration	previous	Gender	credit	interest_rate	Index	
,	nc	117	0	1	0	1.334	0	0
i	yes	274	1	0	0	0.767	1	1
)	no	167	0	1	0	4.858	2	2
;	yes	686	0	0	0	4.120	3	3
)	nc	159	0	1	0	4.856	4	4

```
In [3]: df.drop('Index', axis=1, inplace=True)
```

☑ Data Cleaning

```
In [4]: # Remove duplicates

def drop_dup(df):
    if df.duplicated().any() == True:
        print('The total duplicate row before removing duplicate:', df.duplicated().sum())
        df.drop_duplicates(inplace=True , keep = 'last') # Remove duplicates
        df = df.reset_index(drop=True) #Reset the index
        print('The total duplicate row after removing duplicate:', df.duplicated().sum(), ' \nshape of datase
        else:
            return 'No duplicate entries'
        drop_dup(df)

The total duplicate row before removing duplicate: 5
        The total duplicate row after removing duplicate: 0
        shape of dataset after removing duplicate columns : (513, 6)
```

I Exploring Dataset

- The dataset consists of 517 rows and 6 columns.
- There are no missing values present in the dataset.
- The Churn column is object type , while the other columns contain numeric data.

```
In [6]: desc=df.describe().T
    def descriptive_stats(df):

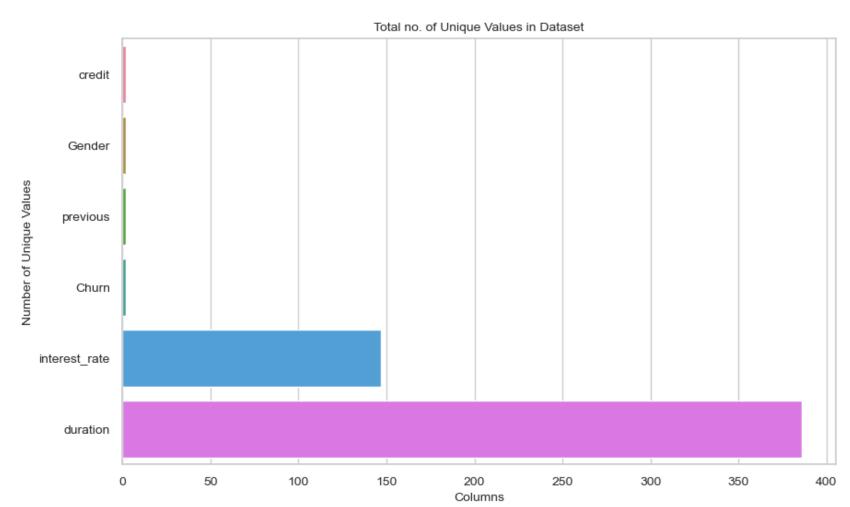
        plt.figure(figsize=(8,5))
        sns.heatmap(df, annot=True, cmap='rocket', fmt=".2f")
        plt.xticks(size = 12)
        plt.yticks(size = 12, rotation = 0)
        plt.title('Statistical Description')
        plt.show()

        descriptive_stats(desc)
```



☑ Exploratory Data Analysis (EDA)

```
In [7]: # Count the number of unique values in each column
        def check_unquie_count(df):
            unique_counts = df.nunique().sort_values()
            print('=='*30)
print(' '*10, 'Total no. of Unique Values')
            print('=='*30)
            print(unique_counts)
            print('=='*30)
        # Create a bar plot or count plot of unique values
            sns.set(style="whitegrid")
            plt.figure(figsize=(10, 6))
            sns.barplot(y=unique_counts.index, x=unique_counts.sort_values(),palette='husl' )
            plt.xticks(rotation=0, fontsize= 10)
            plt.yticks( fontsize= 10 )
            plt.xlabel('Columns', fontsize=10)
            plt.ylabel('Number of Unique Values', fontsize=10)
            plt.title('Total no. of Unique Values in Dataset', fontsize=10)
        # Display the plot
            plt.show()
        check_unquie_count(df)
```



Summarize dataset: 100% 19/19 [00:02<00:00, 10.26it/s, Completed]

Generate report structure: 100% 1/1 [00:01<00:00, 1.98s/it]

Render HTML: 100% 1/1 [00:00<00:00, 1.61it/s]

Overview

Dataset statistics

Number of variables	6
Number of observations	513
Missing cells	0
Missing cells (%)	0.0%
Duplicate rows	0
Duplicate rows (%)	0.0%
Total size in memory	44.2 KiB
Average record size in memory	88.3 B

Variable types

Numeric	2
Categorical	3
Boolean	1

Alerts

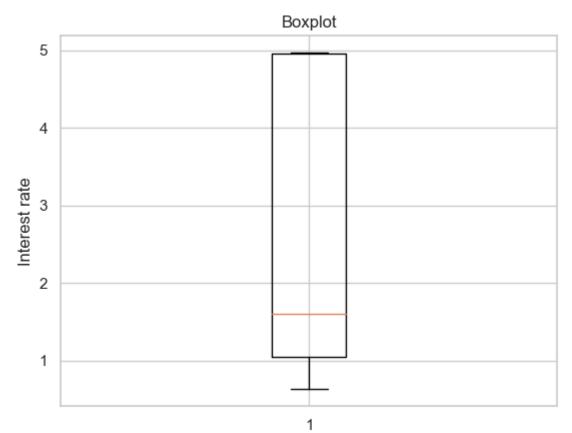
interest_rate is highly overall correlated with credit	High correlation
credit is highly overall correlated with interest_rate	High correlation
credit is highly imbalanced (78.1%)	Imbalance

Reproduction

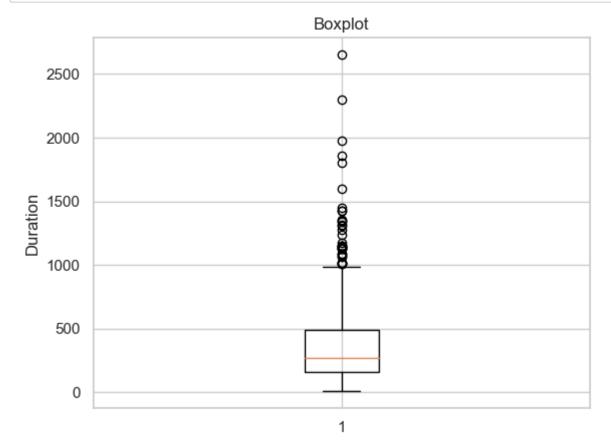
Analysis 2023-08-12 16:27:20.117621 **started**

Out[8]:

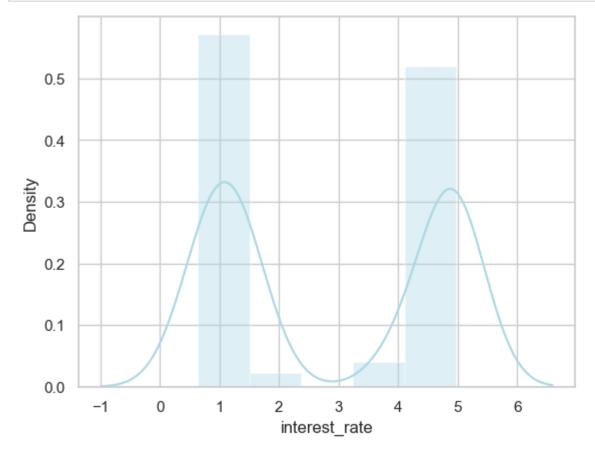
```
In [9]: sns.set_style("whitegrid")
  plt.boxplot(df.interest_rate)
  plt.ylabel('Interest rate')
  plt.title('Boxplot')
  plt.show()
```



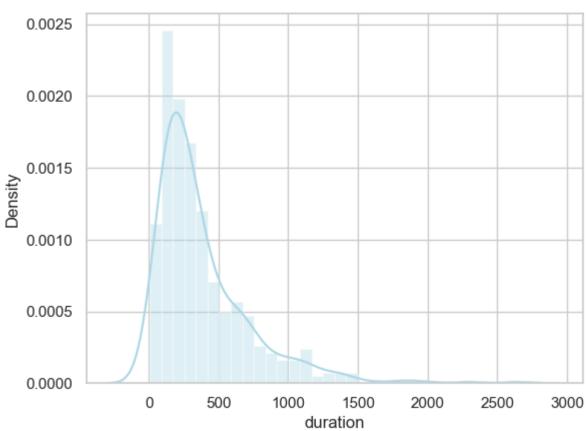
```
In [10]: plt.boxplot(df.duration)
    plt.ylabel('Duration')
    plt.title('Boxplot')
    plt.show()
```



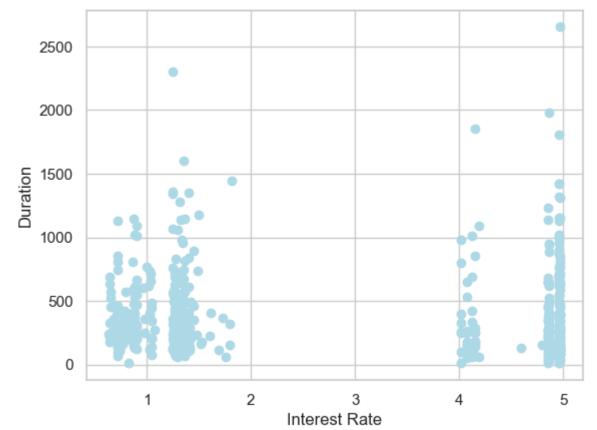
```
In [11]: #plt.hist(x["interest_rate"]) #Univariate
sns.distplot(df.interest_rate, color="lightblue", );
```



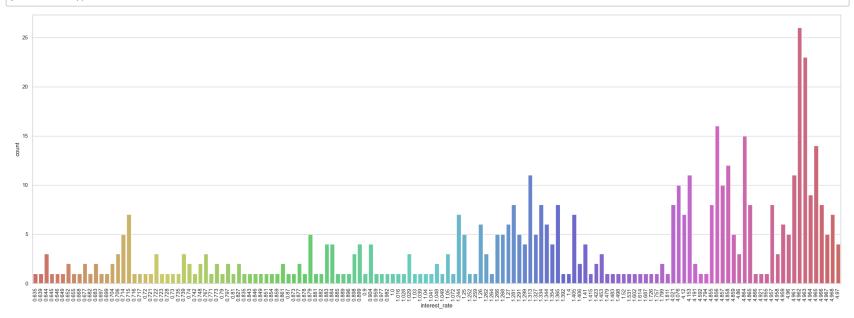
In [12]: #plt.hist(x["duration"])
sns.distplot(df.duration, color="lightblue");



```
In [13]: plt.scatter(df["interest_rate"], df["duration"], c ='lightblue' )
    plt.xlabel('Interest Rate')
    plt.ylabel('Duration')
    plt.show()
```

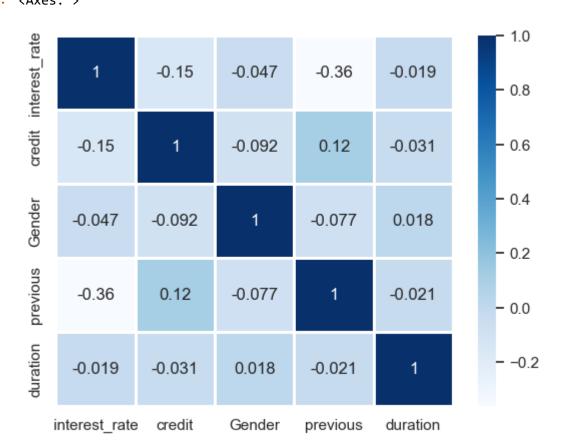


```
In [14]: plt.figure(figsize=(30, 10))
    sns.countplot(x="interest_rate", data=df, palette='hls',)
    plt.xticks(rotation=90)
    plt.show()
```



☑ Finding Correlation

In [15]: sns.heatmap(df.select_dtypes(include ='number').corr(), annot=True,linewidth=.8, cmap="Blues")
Out[15]: <Axes: >




```
In [16]: from sklearn.cluster import KMeans
    from sklearn.metrics import silhouette_score
    from sklearn.preprocessing import StandardScaler
```

Encoding Churn variable

```
In [17]: df['Churn'] = df['Churn'].astype('category').cat.codes
```

Modeling with 2 features: interest_rate, duration

```
In [18]: x2_train = df.loc[:, ['interest_rate','duration']].values
In [19]: sc = StandardScaler()
sc_x2 = sc.fit_transform(x2_train)
```

Inertia Calculation (Using Elbow Method):

Inertia is within cluster sum of squares criteron (calculating error- sum square distance(Euclidean distance) between the centroid and each point). It is metric shows how internally coherent the clusters are. Inertia assumes the cluster

```
In [20]: # Elbow method : To find optimum number of clusters required for modeling
error = []
k = list(range(3, 15))

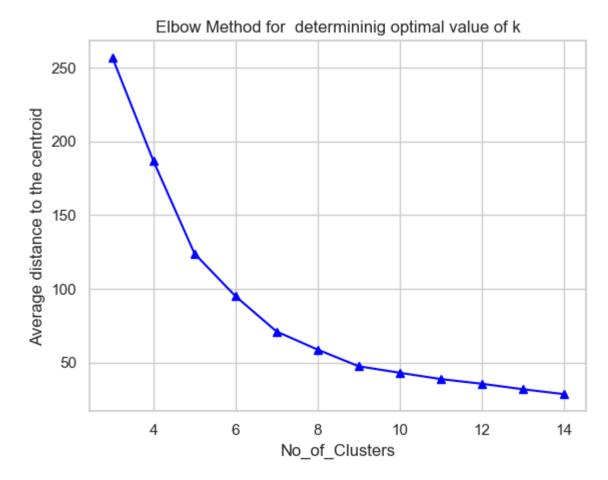
for i in k:
    kmeans = KMeans(n_clusters = i)
    kmeans.fit(sc_x2)
    error.append(kmeans.inertia_)
    print(f'For n_clusters = {i}, the intertia is {kmeans.inertia_}')

For n_clusters = 3, the intertia is 256.74571135356257
For n_clusters = 4, the intertia is 123.9285104929349
For n_clusters = 6, the intertia is 25.92845401
```

```
For n_clusters = 4, the intertia is 186.6160703941797
For n_clusters = 5, the intertia is 123.9285104929349
For n_clusters = 6, the intertia is 95.04326539845401
For n_clusters = 7, the intertia is 71.11739147621033
For n_clusters = 8, the intertia is 58.8400818768117
For n_clusters = 9, the intertia is 47.56772709171158
For n_clusters = 10, the intertia is 43.14045943905836
For n_clusters = 11, the intertia is 38.894387878157225
For n_clusters = 12, the intertia is 35.69839096427495
For n_clusters = 13, the intertia is 31.98454164431077
For n_clusters = 14, the intertia is 28.688022310816052
```

```
In [21]: plt.plot(k, error, color= 'blue', marker='^')
    plt.xlabel("No_of_Clusters")
    plt.ylabel("Average distance to the centroid")
    plt.title('Elbow Method for determining optimal value of k')
```

Out[21]: Text(0.5, 1.0, 'Elbow Method for determining optimal value of k')



```
In [22]: km5 = KMeans(n_clusters = 5)
km7 = KMeans(n_clusters = 7)

model_cluster =[('kMeans_clusters_5',km5, 5),('kMeans_clusters_7',km7, 7)]
```

```
In [23]: | for model_name, model, ncluster in model_cluster:
             model.fit(sc_x2)
             model_labels = model.labels_
             silhouette = silhouette_score(sc_x2, model_labels, random_state=1)
             df2= df.copy()
             df2['cluster'] = pd.Series(model_labels)
             print('--'*20)
             print(model_name)
             print('--'*20)
             print(f' silhouette score : {silhouette}')
             print()
             print( df2.iloc[:, 0:6].groupby(df2.cluster).mean())
             print('--'*40)
             color =['yellow', 'lightgreen', 'lightcoral', 'cyan', 'skyblue', 'pink', 'orange']
             for i in range(0, ncluster):
                 plt.scatter(x2_train[model_labels == i, 0], x2_train[model_labels == i, 1],
                             s=100, c=color[i], label ='Cluster '+str(i+1))
                 plt.title(model_name +' Clusters')
             plt.xlabel('interest_rate')
             plt.ylabel('duration')
             plt.legend( bbox_to_anchor=(1.2,0.5))
             plt.show()
```

kMeans_clusters_5

silhouette score : 0.6296905853234805

```
Churn
        interest_rate
                        credit
                                 Gender previous
                                                    duration
cluster
             3.048845 0.034483 0.241379 0.137931 392.775862 0.500000
0.0
1.0
            2.874554 0.010870 0.293478 0.130435
                                                  386.298913
                                                             0.500000
2.0
            2.791589 0.050761 0.253807 0.137056 384.781726 0.512690
3.0
            3.216981 0.037037 0.333333 0.055556 395.166667 0.444444
4.0
             2.851067 0.133333 0.133333 0.133333 354.866667 0.666667
```

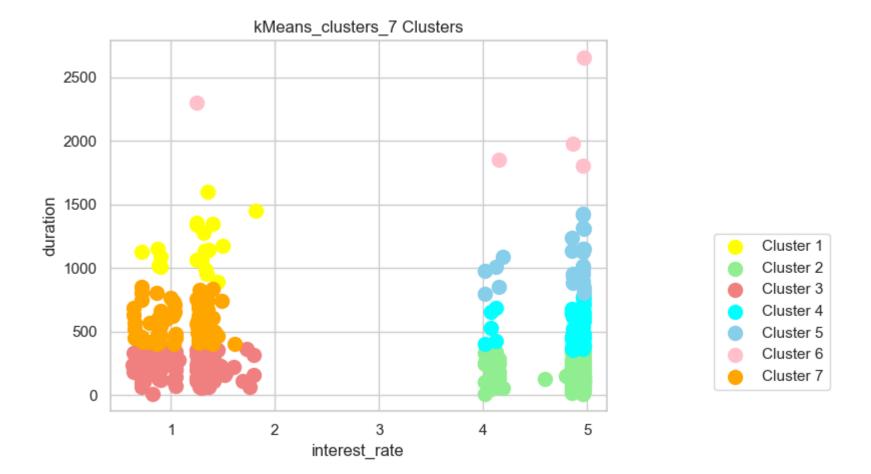
kMeans clusters 5 Clusters 2500 2000 duration 1500 1000 500 0 2 3 5 interest_rate

Cluster 1 Cluster 2 Cluster 3 Cluster 4 Cluster 5

kMeans_clusters_7

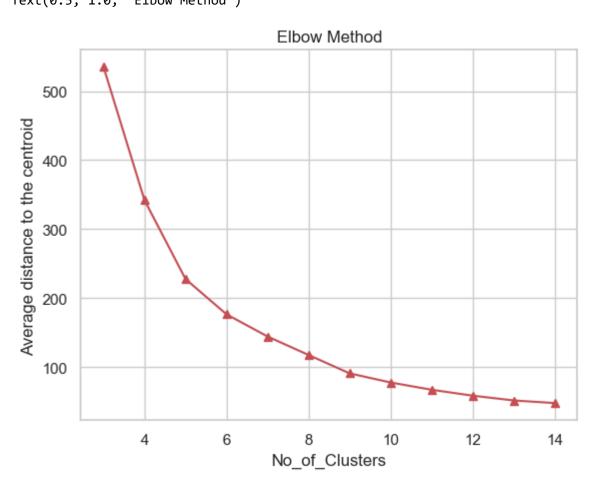
silhouette score : 0.5753250691907946

	interest_rate	credit	Gender	previous	duration	Churn
cluster						
0.0	3.100421	0.105263	0.421053	0.157895	366.105263	0.421053
1.0	2.904631	0.012739	0.286624	0.133758	403.076433	0.496815
2.0	2.811314	0.041420	0.230769	0.142012	394.337278	0.538462
3.0	3.006475	0.033898	0.322034	0.084746	351.542373	0.559322
4.0	3.125462	0.000000	0.307692	0.038462	361.192308	0.307692
5.0	3.450800	0.000000	0.200000	0.000000	504.600000	0.600000
6.0	2.825096	0.068493	0.246575	0.136986	366.945205	0.479452



Modeling with 3 features: interest_rate, duration, Churn

```
In [24]: x3 = df.loc[:, ['interest_rate','duration', 'Churn',]].values
         sc_x3 = sc.fit_transform(x3)
         error3 = []
         k = list(range(3, 15))
         for i in k:
             kmeans = KMeans(n_clusters = i)
             kmeans.fit(sc_x3)
             error3.append(kmeans.inertia_)
             print(f'For n_clusters = {i}, the intertia is {kmeans.inertia_}' )
         plt.plot(k, error3, 'r^-')
         plt.xlabel("No_of_Clusters")
         plt.ylabel("Average distance to the centroid")
         plt.title('Elbow Method')
         For n_clusters = 3, the intertia is 535.2870606652542
         For n_{clusters} = 4, the intertia is 341.99897529325335
         For n_{clusters} = 5, the intertia is 227.76158050959037
         For n_clusters = 6, the intertia is 176.6691790591495
         For n_clusters = 7, the intertia is 144.51450419165573
         For n_{clusters} = 8, the intertia is 117.73405232225687
         For n_clusters = 9, the intertia is 91.12974068533914
         For n_clusters = 10, the intertia is 77.91532496028883
         For n_clusters = 11, the intertia is 67.38281236972449
         For n_clusters = 12, the intertia is 58.810443399324676
         For n_{clusters} = 13, the intertia is 51.91088164614595
         For n clusters = 14, the intertia is 48.086950615696765
Out[24]: Text(0.5, 1.0, 'Elbow Method')
```



Out[25]:

	interest_rate	duration	Churn
0	-0.827129	-0.782880	-1.005865
1	-1.129090	-0.326688	0.994169
2	1.049610	-0.637596	-1.005865
3	0.656581	0.870452	0.994169
4	1.048545	-0.660841	-1.005865
508	-0.827129	-0.530086	-1.005865
509	-1.079029	1.219134	0.994169
510	-1.069443	-0.280197	-1.005865
511	-1.070508	0.251542	0.994169
512	1.106594	-0.710238	-1.005865

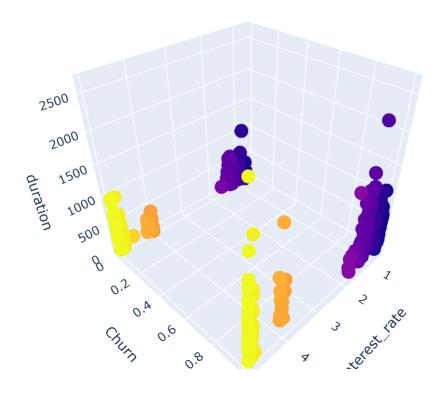
513 rows × 3 columns

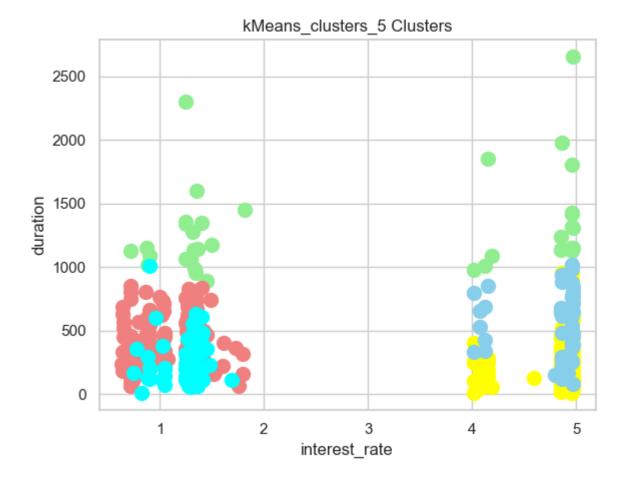
```
In [26]: for model_name, model, ncluster in model_cluster:
             model.fit(sc_x3)
             model_labels = model.labels_
             pred = model.predict(sc_x3)
             silhouette = silhouette_score(sc_x3, model_labels, random_state=1)
             df3 = df.copy()
             df3['cluster'] = pd.Series(model_labels)
             print('--'*20)
             print( model_name)
             print('--'*20)
               print('Trained data', model_labels)
               print('predicted data',pred)
             print(f' silhouette score : {silhouette}')
             print()
             print( df3.iloc[:, 0:6].groupby(df3.cluster).mean())
             print('--'*40)
             fig = px.scatter_3d(df3, x ='interest_rate', y= 'Churn', z='duration', color ='interest_rate')
             fig.show()
             color =['yellow', 'lightgreen', 'lightcoral', 'cyan', 'skyblue', 'pink', 'orange']
             for i in range(0, ncluster):
                 plt.scatter(x3[model_labels == i, 0], x3[model_labels == i, 1], s=100, c=color[i], label ='Cluster'
                 plt.title(model_name +' Clusters')
             plt.xlabel('interest_rate')
             plt.ylabel('duration')
             plt.legend( bbox_to_anchor=(1.2,0.5))
             plt.show()
```

kMeans_clusters_5

silhouette score : 0.655579576321065

	interest_rate	credit	Gender	previous	duration	Churn
cluster						
0.0	2.916305	0.011299	0.299435	0.129944	401.305085	0.497175
1.0	3.155857	0.057143	0.314286	0.085714	440.000000	0.485714
2.0	2.921125	0.023810	0.238095	0.148810	386.053571	0.523810
3.0	2.606053	0.106667	0.240000	0.120000	382.266667	0.506667
4.0	3.006283	0.037736	0.301887	0.075472	308.792453	0.471698





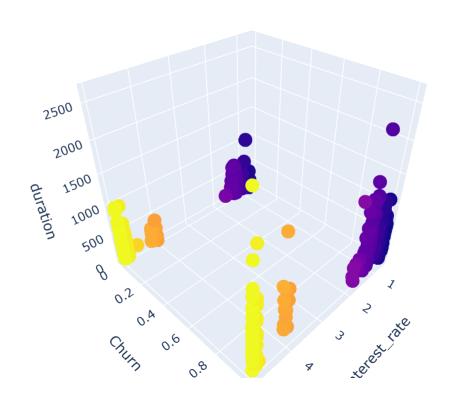


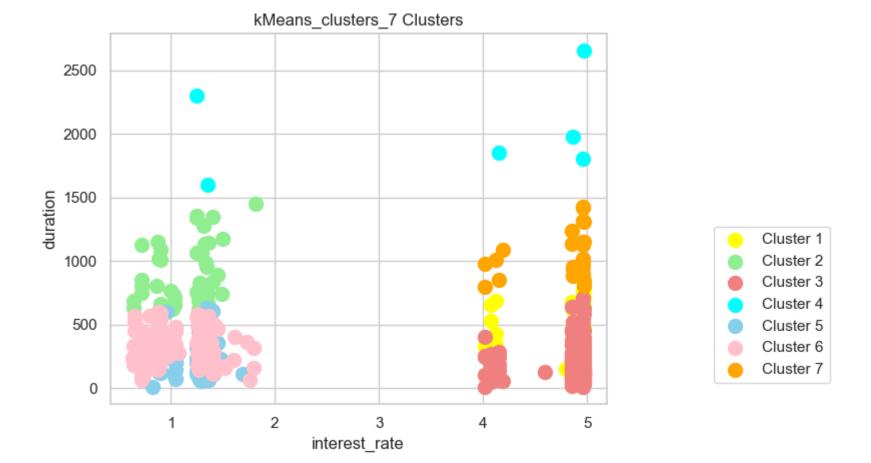
kMoans clustons 7

kMeans_clusters_7

silhouette score : 0.6556484427282129

	interest_rate	credit	Gender	previous	duration	Churn
cluster						
0.0	2.959286	0.047619	0.309524	0.071429	317.785714	0.547619
1.0	3.087977	0.046512	0.302326	0.162791	350.930233	0.488372
2.0	2.925971	0.011494	0.293103	0.132184	406.189655	0.505747
3.0	3.702667	0.000000	0.166667	0.000000	588.666667	0.666667
4.0	2.575608	0.108108	0.229730	0.121622	386.121622	0.513514
5.0	2.880503	0.027972	0.244755	0.146853	389.608392	0.517483
6.0	3.125462	0.000000	0.307692	0.038462	361.192308	0.307692





☑ Modeling with 4 features: interest_rate, duration, Churn and Gender

```
In [27]: x4 = df.loc[:, ['interest_rate','duration', 'Churn', 'Gender']].values
    sc_x4 = sc.fit_transform(x4)
    pd.DataFrame(sc_x4, columns =['interest_rate','duration', 'Churn','Gender'])
```

Out[27]:

	interest_rate	duration	Churn	Gender
0	-0.827129	-0.782880	-1.005865	1.640319
1	-1.129090	-0.326688	0.994169	-0.609637
2	1.049610	-0.637596	-1.005865	1.640319
3	0.656581	0.870452	0.994169	-0.609637
4	1.048545	-0.660841	-1.005865	1.640319
508	-0.827129	-0.530086	-1.005865	1.640319
509	-1.079029	1.219134	0.994169	-0.609637
510	-1.069443	-0.280197	-1.005865	-0.609637
511	-1.070508	0.251542	0.994169	-0.609637
512	1.106594	-0.710238	-1.005865	-0.609637

513 rows × 4 columns

```
In [28]: | for model_name, model, ncluster in model_cluster:
                     model.fit(sc_x4)
                     model_labels = model.labels_
                     silhouette = silhouette_score(sc_x4, model_labels, random_state=1)
                     df4 = df.copy()
                     df4['cluster'] = pd.Series(model_labels)
                     print('--'*20)
                     print(model_name)
                     print('--'*20)
                     print(f' silhouette score : {silhouette}')
                     print()
                     print( df4.iloc[:, 0:6].groupby(df4.cluster).mean())
                     print('--'*40)
               kMeans_clusters_5
                silhouette score : 0.5505974722438397
                             interest_rate credit
                                                                       Gender previous duration
                                                                                                                            Churn
               cluster
                                    2.913070 0.028169 0.232394 0.154930 381.985915 0.542254
               0.0
               1.0
                                 2.725623 0.043210 0.277778 0.123457 420.851852 0.555556

      2.0
      2.991891
      0.065217
      0.391304
      0.108696
      424.500000
      0.456522

      3.0
      3.009923
      0.032967
      0.252747
      0.142857
      351.780220
      0.406593

      4.0
      3.066269
      0.014925
      0.283582
      0.059701
      333.805970
      0.462687

               kMeans_clusters_7
               _____
                silhouette score : 0.5925088849802866
                             interest_rate credit Gender previous duration
                                                                                                                            Churn
               cluster
               0.0
                                    2.924522 0.086957 0.217391 0.086957 461.739130 0.652174

      2.193733
      0.166667
      0.300000
      0.133333
      414.900007
      0.000007

      2.926657
      0.027972
      0.237762
      0.153846
      381.202797
      0.538462

      2.823424
      0.015152
      0.295455
      0.121212
      419.689394
      0.530303

      3.116900
      0.020000
      0.260000
      0.060000
      331.700000
      0.420000

      3.034844
      0.033333
      0.255556
      0.133333
      353.922222
      0.400000

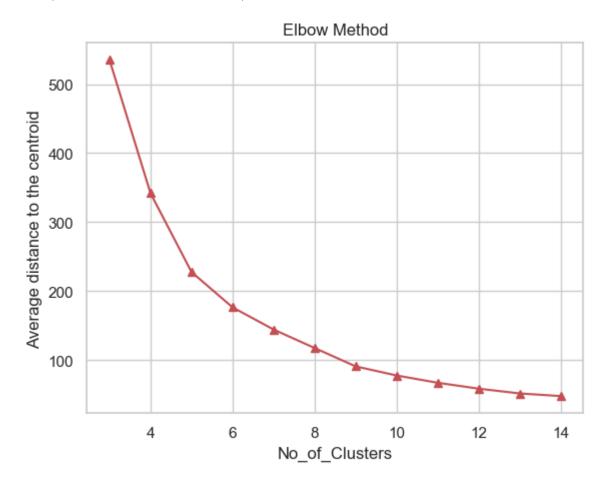
      2.972900
      0.025000
      0.375000
      0.125000
      372.650000
      0.425000

               1.0
               2.0
               3.0
               4.0
               5.0
               6.0
```

Modeling with all features

```
In [29]: | x_all = df.iloc[:,:]
         sc_x = sc.fit_transform(x_all)
         error = []
         k = list(range(3, 15))
         for i in k:
             kmeans = KMeans(n_clusters = i)
             kmeans.fit(sc_x)
             error.append(kmeans.inertia_)
             print(f'For n_clusters = {i}, the intertia is {kmeans.inertia_}' )
         plt.plot(k, error3, 'r^-')
         plt.xlabel("No_of_Clusters")
         plt.ylabel("Average distance to the centroid")
         plt.title('Elbow Method')
         For n_{clusters} = 3, the intertia is 1759.219425163075
         For n clusters = 4, the intertia is 1312.5647507569627
         For n_{clusters} = 5, the intertia is 1005.1254345057963
         For n_{clusters} = 6, the intertia is 780.778024214083
         For n_{clusters} = 7, the intertia is 653.5824962754772
         For n_clusters = 8, the intertia is 573.2075443889329
         For n_clusters = 9, the intertia is 491.86959403883264
         For n_{clusters} = 10, the intertia is 413.93497789435935
         For n_clusters = 11, the intertia is 364.9169104089628
         For n_clusters = 12, the intertia is 328.30554004879815
         For n_clusters = 13, the intertia is 293.87842334652925
         For n_clusters = 14, the intertia is 266.94971985690347
```

Out[29]: Text(0.5, 1.0, 'Elbow Method')



```
In [30]: for model_name, model, ncluster in model_cluster:
                   model.fit(sc_x)
                   model_labels = model.labels_
                   silhouette = silhouette_score(sc_x, model_labels, random_state=1)
                   df_all = df.copy()
                   df_all['cluster'] = pd.Series(model_labels)
                   print('--'*40)
                   print(model name)
                   print('--'*40)
                   print(f' silhouette score : {silhouette}')
                   print()
                   print( df_all.iloc[:, 0:6].groupby(df_all.cluster).mean())
                   print('--'*40)
             kMeans_clusters_5
               silhouette score : 0.4627904912095595
                           interest_rate credit Gender previous duration
                                                                                                                 Churn
             cluster
             0.0
                                 2.735064 0.044586 0.286624 0.121019 423.242038 0.554140

      2.995393
      0.038251
      0.262295
      0.114754
      376.896175
      0.486339

      2.660914
      0.000000
      0.258621
      0.155172
      401.448276
      0.586207

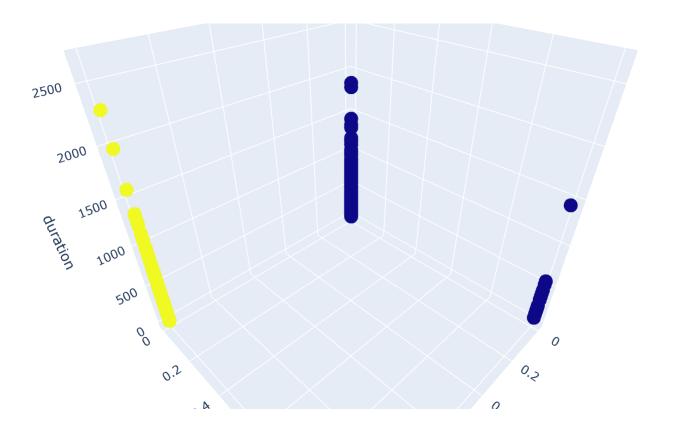
      3.069174
      0.043478
      0.260870
      0.130435
      341.445652
      0.402174

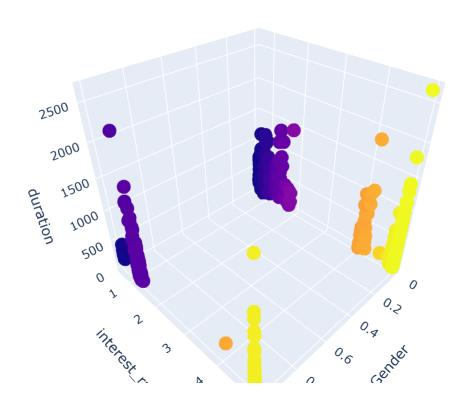
      3.217667
      0.000000
      0.3333333
      0.166667
      344.777778
      0.500000

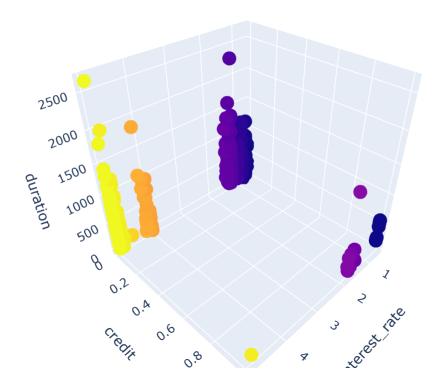
             1.0
             2.0
             3.0
             kMeans_clusters_7
               silhouette score : 0.5459210972300551
```

	interest_rate	credit	Gender	previous	duration	Churn
cluster	_					
0.0	3.033375	0.034091	0.250000	0.136364	349.625000	0.397727
1.0	2.721227	0.045455	0.279221	0.123377	429.019481	0.564935
2.0	2.928851	0.042553	0.202128	0.148936	376.159574	0.531915
3.0	3.217667	0.000000	0.333333	0.166667	344.777778	0.500000
4.0	3.041514	0.081081	0.459459	0.081081	420.243243	0.432432
5.0	2.660914	0.000000	0.258621	0.155172	401.448276	0.586207
6.0	3.153763	0.016949	0.271186	0.067797	323.559322	0.423729

```
In [31]: fig1 = px.scatter_3d(df_all, x ='Gender', y= 'credit', z='duration', color ='Gender')
fig2 = px.scatter_3d(df_all, x ='Gender', y= 'interest_rate', z='duration', color ='interest_rate')
fig3 = px.scatter_3d(df_all, x ='interest_rate', y= 'credit', z='duration', color ='interest_rate')
fig1.show()
fig2.show()
fig3.show()
```







☑ Overall Evaluation (Silhouette Analysis)

The evaluation of a K-means clustering model is often performed using a metric called the silhouette distance. The silhouette distance metric yields values within the range of [-1, +1]. A higher silhouette distance value indicates a better quality model, with values approaching +1 suggesting that the clusters are well-separated and distinct.

In summary, the silhouette distance serves as a measure to assess the effectiveness of a K-means clustering model. A silhouette distance closer to +1 signifies that the clusters formed are distinct and well-defined, indicating a stronger and more reliable clustering solution.

Out[32]:

	features	n_cluster (k)	silhouette_distance
0	feature_2	5	0.63
1	feature_2	7	0.57
2	feature_3	5	0.65
3	feature_3	7	0.65
4	feature_4	5	0.55
5	feature_4	7	0.59
6	feature_all	5	0.46
7	feature_all	7	0.54

```
In [33]: crosstab_result1 = pd.crosstab(silhouette_df['features'], silhouette_df['n_cluster (k)'], values=silhouette_d
crosstab_result1
```

Out[33]:

n_cluster (k)	5	,
features		
feature_2	0.63	0.57
feature_3	0.65	0.65
feature_4	0.55	0.59
feature all	0.46	0.54

```
plt.ylabel('silhouette_score')
Out[34]: Text(0, 0.5, 'silhouette_score')
                                                                             n_cluster (k)
               0.6
               0.5
           silhouette_score
               0.4
               0.3
               0.2
               0.1
               0.0
                           feature 2
                                                                                  feature_all
                                                    features
In [35]: crosstab_result2 = pd.crosstab(silhouette_df['n_cluster (k)'], silhouette_df['features'], values=silhouette_
          crosstab_result2
Out[35]:
               feature_3 feature_4 feature_all
           n_cluster (k)
                                                         0.46
                    5
                            0.63
                                     0.65
                                               0.55
                    7
                            0.57
                                     0.65
                                               0.59
                                                          0.54
In [36]: crosstab_result2.plot(kind ='bar')
          plt.ylabel('silhouette_score')
Out[36]: Text(0, 0.5, 'silhouette_score')
               0.6
               0.5
            silhouette_score
               0.4
               0.3
                                                    features
                                                      feature_2
                                                      feature_3
               0.1
                                                      feature_4
                                                      feature all
               0.0
                                                 n_cluster (k)
```

☑ Conclusion

In [34]: crosstab_result1.plot(kind ='bar')

- The model is efficient in clustering with features =3 and no of clusters =7
- Model build using feature =3, k=7 has obtained a silhouette_score 0.655