

⇒ Inferential
Statistics :-

↳

Hypothesis testing

↳ 1) (t-test (z-test))

2) Anova

3) Chi²-Square

→ [Confidence Interval] → (Add on for this session)

⇒ Hypothesis - ?

- 1- Null Hypothesis →
- 2- Alternate hypothesis

2- friends which are having a debate on any topic

↳ difference in opinion

- P-1 → "statement"
- P-2 → will oppose.

⇒ Try to explain him via facts (google, show some data, etc)



1) $p < 0.05 \Rightarrow$ we accept the alternate hypothesis

2) $p > 0.05 \Rightarrow$ We failed to reject the (Null Hypothesis)

$\left\{ \begin{array}{l} H_0 \Rightarrow \text{Assumption, thought process, status quo.} \\ H_a \Rightarrow \text{Opposing the thought process} \end{array} \right.$

* $\alpha = \text{critical value} /$
threshold value / significant
threshold.

$p > \alpha =$ we failed to reject the Null hypo (H_0) |

$\left\{ \begin{array}{l} p < \alpha \\ \hookrightarrow \text{accept} \end{array} \right\}$ simple words (\rightarrow we accept H_0)

⇒ Eg:

factory → ice-cream

(Dairy product)

↓
{milk}

↳ Salmonella
Bacteria

> 0.03 mg/L

↓
(milk is not fit for any
consumption)

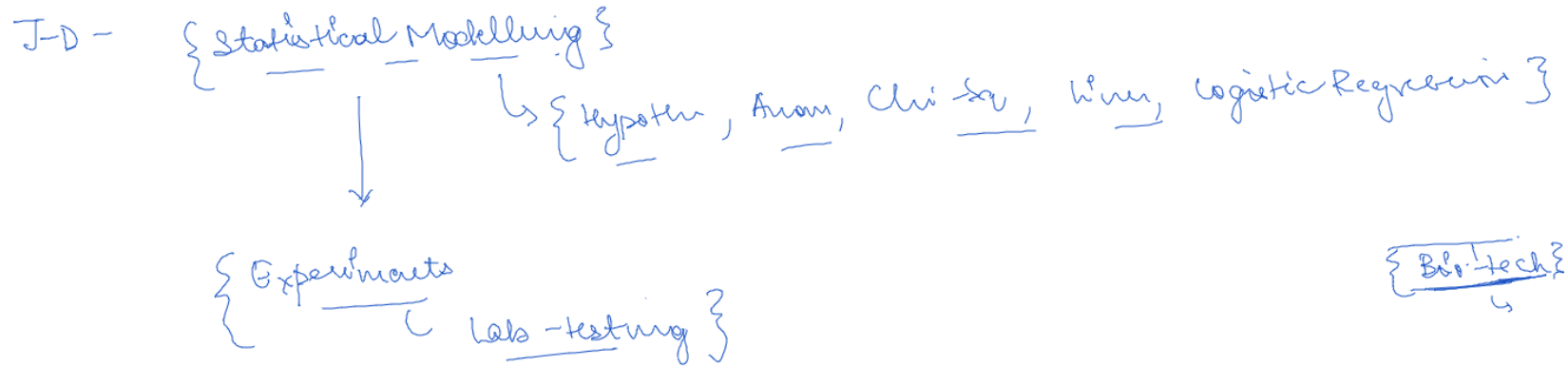
⇒ Inspector → (fssai)

→

{ $H_0: \beta > 0.03$
 $H_a: \beta < 0.03$

{ plant manager
↓
samples (collected from Random
Batches of milk)
↓
Lab test
↳ (Reading) →

⇒ t-statistic value → p-value → compare with
α-value & Make final decision



⇒ Steps - Involved:-

1→ formulate hypothesis eqn

2→ check which test to apply

3→ Calculate t/z Statistical value

4) using t-Statistical value → calculate p-value

5) then check for the threshold (critical value (α);
this value is given by SME (Subject Matter Expert) / if not
then we go with $0.05 \Rightarrow \alpha$ -value.

6) \rightarrow then p value is compared with α -value

\hookrightarrow 6.1) $\rightarrow p < \alpha \Rightarrow$ we accept the alternate hypothesis

6.2) $\rightarrow p > \alpha \Rightarrow$ we failed to reject the Null hypothesis.

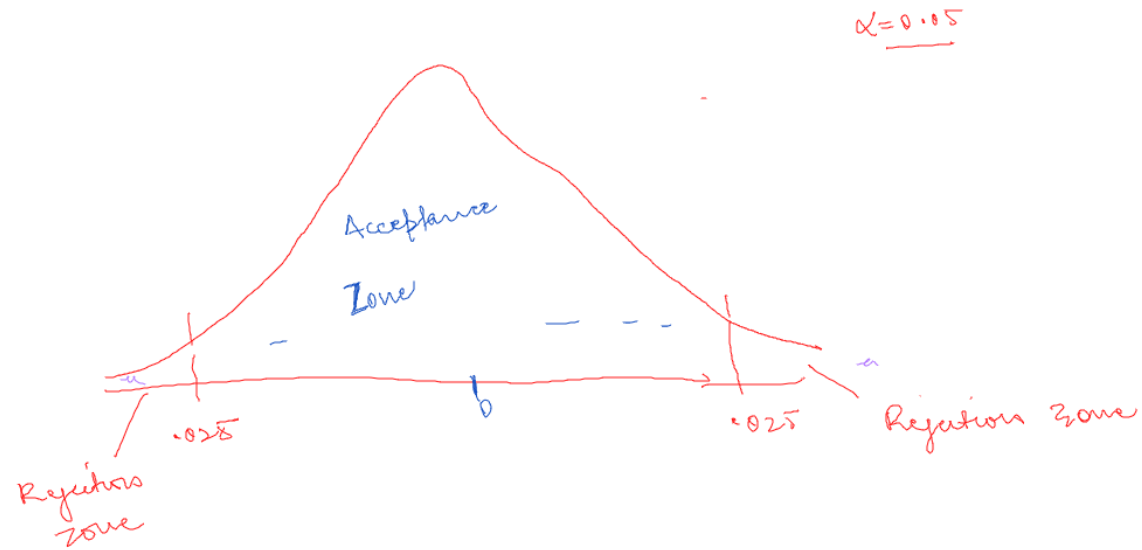
\Rightarrow

How α -value is calculated?

95% $\Rightarrow .95$

$\alpha = 1 - \text{Confidence Interval.}$

$$\begin{aligned} \Rightarrow \alpha &= 1 - .95 \\ &= \underline{0.05} \end{aligned}$$



$(p < 0.05) \rightarrow$ Acceptance zone

$p > 0.05 \Rightarrow$ Rejection zone

⇒ Difference between t-test & z-test (p-test)

As per theory

t-test

- 1) Sample set is less than 30
- 2) It is used when sample std deviation is given along with the sample mean

z-test

- 1) When sample size > 30
- 2) - It is used when (population std dev) is given

⇒ In reality pop-std dev is absolutely impossible

∴ we always use (t-test)

⇒ f-test ⇒ test of variance — f-ratio
↓
Anova

⇒ How the t-statistical value is calculated?

$$\underline{t\text{-st}} = \frac{x - \mu}{\sigma / \sqrt{n}}$$

x = Reference Value

μ = Sample mean

σ = Sample Std deviation

∴ after this you use t → p conversion table
for p-value.

⇒ t-test ⇒ 2-Samples (Continuous Variables)

⇒ Anova ⇒ >2-Samples (Continuous Variable)

⇒ Chi-Square ⇒ when you have categorical variables



Chi-Square :

Eg- problem statement

→ Is there any relationship between

Marital Status & Education

$\chi^2_{\text{tabular}} > \chi^2_{\text{calculated}} \Rightarrow$ failed to reject Null hypo

$\chi^2_{\text{cal}} > \chi^2_{\text{tab}} \Rightarrow$ we accept Alternate hypothesis

⇒ What is Pearson Correlation Coefficient?

$$\text{variance}(x) = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$$

\bar{x} = Mean of
the sample

x_i = data point

n = sample size

$$\frac{\text{Co - Variance}}{(\text{Cor}(x, y))} = \sum_{i=1}^n \left(\frac{(x_i - \bar{x})(y_i - \bar{y})}{n-1} \right)$$

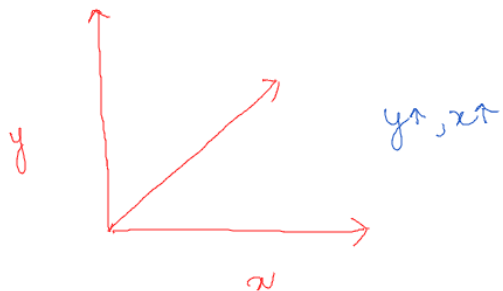
$$\begin{aligned} & (a-b)^2 \\ &= (a-b)(a-b) \end{aligned}$$

⇒ 3-types of Relationships $(-1, 1)$

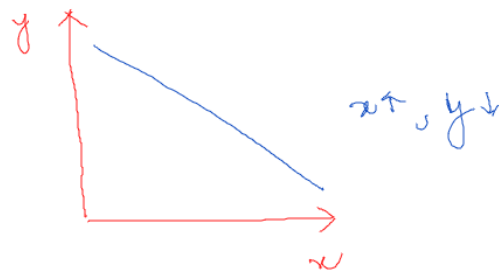
-ve - ve relation

+ve = +ve relation

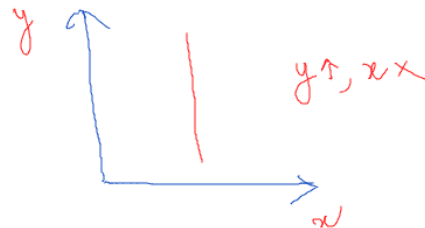
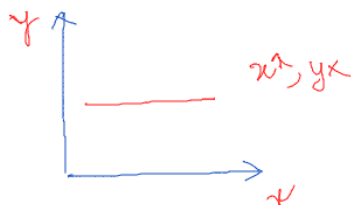
+ve relationship



-ve relationship



0 of No relationship



⇒ Pearson's Co-efficient / ratio (r)

$$\Rightarrow \frac{\text{Cov}(x, y)}{(\text{Std of } x) * (\text{Std of } y)} = (-1, 1)$$

⇒

t-test

↳

1) 1-tail test

2) 2-tail test

3) 1 sample 1-tail test

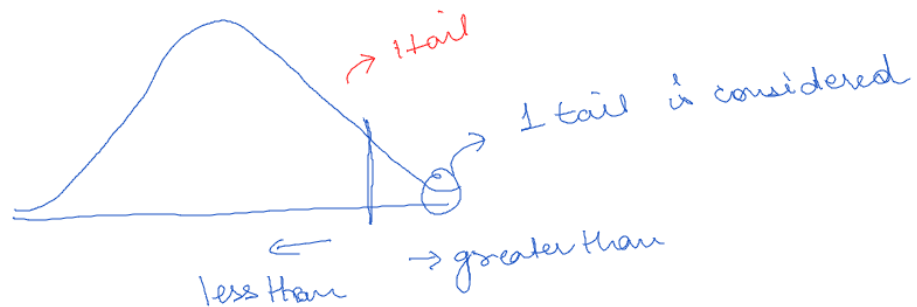
4) 2-sample 2-tail test

5) 2-proportion Test

Sample ⇒ No. of datapets
used for analysis

1-tail test \Rightarrow in the problem statement -

$>$, $<$, tall short, high low,



2-tail test \Rightarrow equal to Not equal, diff, No diff



$$\text{Eg} = \begin{bmatrix} 2=2 \\ 2 \neq 2 \end{bmatrix}$$

⇒ Anova

1-way Anova ⇒ 2-Independent Variables

2-way Anova ⇒ >2-Independent Variables

⇒ Degree of freedom in Anova

12

A	B	C

$$\underline{f\text{-Ratio}} = \frac{\text{Variance between the group}}{\text{Variance within the group}}$$

⇒ Total Variables = 3

⇒ DoF freedom

1 → Inter group = $3 - 1 = (2)$

2 → Intra group = $3 \times (12 - 1) = 3(11)$
(for intra group variance) 33

$$Z = 95\% = 1.96$$

⇒ Confidence Interval :

$$\Rightarrow \text{C.I.} = \bar{x} \pm Z \frac{S}{\sqrt{n}}$$

Eg → weather forecast

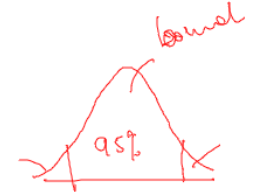
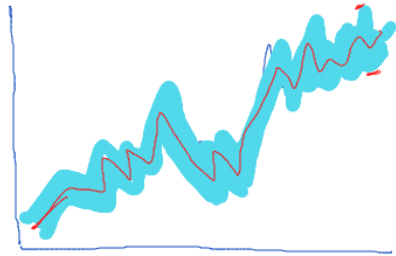
\bar{x} = Mean Value (point estimate) (Red line)

Z = confidence, S = std dev, n = sample size.

Min temp & Max temp, X Never tell 1 temp for day



upper bound & lower bound
} decided basis confidence interval



⇒ Red line = Absolute values

⇒ Blue zone = the area within which your value might oscillate.