

Linear-Regression.R

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2020-12-05

```
library(ISLR)

## Warning: package 'ISLR' was built under R version 4.0.2

data("Carseats")
attach(Carseats)

set.seed(123)
indx <- sample(2,nrow(Carseats), replace=T, prob = c(0.8, 0.2))
train <- Carseats[indx ==1, ]
test <- Carseats[indx ==2, ]

#lm - linear model (~)
#lm(num target ~ inputs, data= train)

lmModel <- lm(Sales ~ ., data= train)
summary(lmModel)

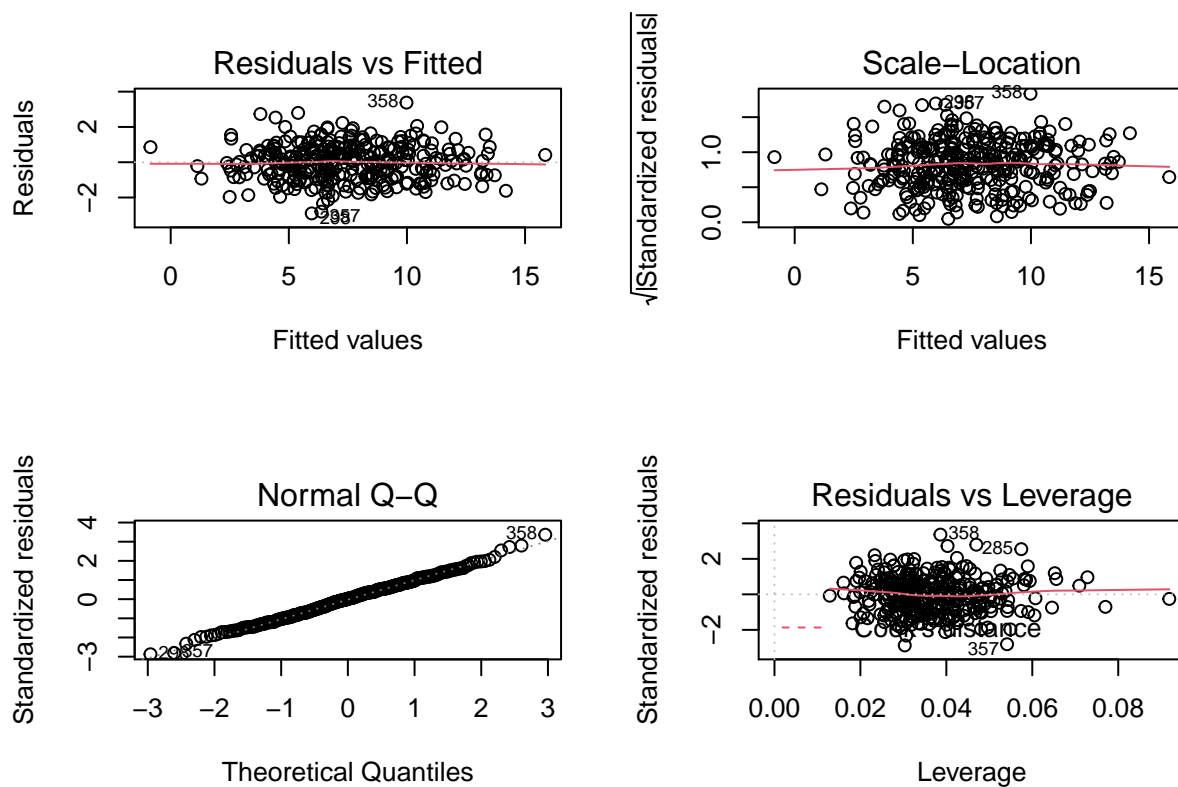
##
## Call:
## lm(formula = Sales ~ ., data = train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8993 -0.7146  0.0192  0.6676  3.3789
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   5.843e+00  6.790e-01   8.605 3.75e-16 ***
## CompPrice     9.105e-02  4.495e-03  20.254 < 2e-16 ***
## Income       1.659e-02  2.069e-03   8.017 2.18e-14 ***
## Advertising  1.228e-01  1.222e-02  10.047 < 2e-16 ***
## Population   8.435e-06  4.182e-04   0.020  0.984
## Price       -9.555e-02  2.896e-03 -32.999 < 2e-16 ***
## ShelveLocGood 4.857e+00  1.703e-01  28.511 < 2e-16 ***
## ShelveLocMedium 1.884e+00  1.387e-01  13.583 < 2e-16 ***
## Age         -4.679e-02  3.610e-03 -12.960 < 2e-16 ***
## Education    -1.783e-02  2.249e-02  -0.793  0.428
## UrbanYes     1.947e-01  1.251e-01   1.556  0.121
## USYes       -1.624e-01  1.672e-01  -0.971  0.332
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 1.024 on 313 degrees of freedom
## Multiple R-squared:  0.876, Adjusted R-squared:  0.8716
## F-statistic: 201 on 11 and 313 DF, p-value: < 2.2e-16
```

```
#estimate- coefficient of each variable in the linear model
#if coefficient is larger-> means variable is more important & sign means direction of relationship
#if we increase price, sales decrease.
#Pr(>|t|) -p value, whether there is a significant relationship between each variable & target variable
#we want r-squared to be large-> indicates good fit of model
```

```
#Population around the store does NOT affect sales much, also education level, if urban, and if store
#is in USA.
```

```
layout(matrix(c(1,2,3,4), 2, 2))
plot(lmModel)
```



```
#Residuals vs Fitted - we don't want to see any pattern, points should be
#scattered at random, should be a horizontal line.
```

```
#Scale-Location - variation of residuals,
```

```
#line should be horizontal-> means variation is the same around all points.
```

```
#Normal Q-Q - check that residuals have normal distribution, should be a 45 degree line.
```

```
#Residual vs Leverage - helps identify influential points.
```

```
#no influential points in our model.
```

```
#mean squared error
```

```
predictions <- predict(lmModel, newdata = test)
```

```
mean(test$Sales-predictions)^2
```

```
## [1] 0.02526576
```

```
## [1] 0.02526576
```

```
fitted(lmModel) #predictions for train values
```

##	1	2	3	6	7	9	10
##	7.2693060	12.4507357	9.2402292	9.6306823	6.2254075	5.9884113	5.7511180
##	12	13	14	15	17	18	19
##	11.8857466	3.6424874	11.9994924	9.7372705	8.4807905	11.8130859	13.4272856
##	22	23	25	26	27	28	29
##	11.0571063	5.6971609	10.0417359	13.3295228	8.4885686	5.2803506	4.4454580
##	30	33	34	35	36	37	38
##	6.0668329	6.0220505	8.4851409	4.6304094	10.7017747	10.3866801	6.8584153
##	39	40	41	42	43	44	45
##	6.0058871	3.5331958	2.5449354	6.3672818	11.1237596	5.2098291	5.0108004
##	46	47	48	49	51	52	53
##	4.5872270	13.1382248	5.9582987	4.5511468	3.2848487	4.4343502	6.3665817
##	54	55	56	57	58	60	61
##	5.8141527	5.4517724	4.8474780	10.7231549	1.1296053	5.4679492	7.6704002
##	62	63	64	66	69	70	71
##	6.1489426	2.6642567	8.5466955	4.2324048	12.0583265	7.7517985	8.8863066
##	72	73	74	75	76	77	78
##	6.5024091	6.6215248	12.4179257	6.7438237	7.6016180	9.7698190	9.0002717
##	79	80	81	82	83	84	85
##	3.7699877	8.6020352	8.8635338	6.9142139	11.4557584	5.4618893	2.4697572
##	86	90	91	92	93	94	95
##	7.5931012	7.0873896	5.5345446	4.4726039	6.6617929	8.8084471	7.7737958
##	96	97	98	99	100	101	102
##	4.4707773	9.5354571	8.3550421	11.7676154	4.7176400	6.4509471	7.9326659
##	103	105	108	109	110	112	113
##	5.7861497	4.7487846	8.5572415	4.1713119	7.5677528	6.5211431	8.4928989
##	115	116	117	119	120	121	122
##	8.0142510	6.6360939	5.1125049	7.1075613	6.6994382	6.8114068	10.1622093
##	123	124	125	127	128	129	130
##	6.8602358	7.3747072	10.0336247	10.2818861	6.5870004	5.1698321	5.4567005
##	131	133	134	135	136	138	140
##	9.3542231	8.1206412	7.3834173	4.0988631	6.1154506	5.0621901	12.4997467
##	141	142	143	144	146	147	148
##	7.3419574	5.3890577	6.8001966	2.4965773	9.5848436	3.2055311	11.7137735
##	149	150	152	153	154	155	156
##	6.6702131	11.2350095	10.0421596	9.0823040	6.8775373	8.5496426	8.1198106
##	157	158	159	160	161	162	163
##	7.0798805	9.4509942	12.3782124	9.2628074	6.1252373	2.9107908	3.4056489
##	164	165	166	167	168	169	170
##	6.4847315	7.1343353	1.3006147	5.9343354	6.8603161	7.6837136	11.6327807
##	171	172	174	175	176	177	178
##	6.7618378	10.4302468	6.5365718	-0.8566772	6.8281249	5.9033687	10.9715933
##	180	182	183	184	185	186	187
##	6.6465984	8.2432202	5.2208305	6.6606922	8.7186323	9.2122351	8.8270538
##	188	191	192	194	196	197	198
##	4.8452222	10.0001740	6.9872075	13.2032633	4.5790024	2.5536377	3.1991896
##	199	200	201	203	204	205	207

```
## 4.2647069 5.6602425 5.3017797 3.7333899 2.9051601 9.5343270 4.4268623
##      208      209      210      211      212      213      214
## 5.3937343 6.8942761 3.9532442 3.7886330 8.8614246 12.1089720 8.3309733
##      215      216      217      218      221      223      224
## 6.5457253 2.3791112 5.6559879 3.9812124 10.0910918 7.1298377 4.5342890
##      225      226      227      228      229      231      232
## 5.3413905 6.4286845 7.7511719 7.7351550 5.0695438 4.3891536 7.7745751
##      233      234      235      236      237      239      241
## 12.6058744 9.1639460 8.1574246 5.4903078 9.4029116 5.9549368 10.6296185
##      242      243      244      245      246      247      250
## 10.3772065 4.1998998 7.7054614 9.1667266 10.3775925 7.6177916 4.1136495
##      251      252      253      254      255      256      257
## 7.6539196 5.2429787 8.6788989 5.3312258 10.7566131 7.6513321 4.6186521
##      258      259      263      265      266      267      268
## 7.2154583 4.9503808 6.6255777 6.5730107 5.0693283 10.7895976 6.8026194
##      269      270      272      273      274      275      276
## 8.0131995 5.2299713 5.2645851 13.7184162 9.9185985 8.6822732 5.5392131
##      278      279      280      281      282      283      284
## 8.5010857 6.4700292 4.7297836 3.1309884 11.2277740 8.3790868 6.6363156
##      285      286      287      288      289      290      291
## 4.4387722 8.3166803 7.2759106 6.5059319 5.8611104 7.9092930 8.9143538
##      292      293      295      298      299      300      301
## 7.3112624 13.1880103 13.3738165 5.9692861 9.7799873 10.6090493 7.9778469
##      302      303      304      305      306      307      308
## 7.0522786 4.3623586 11.0311400 10.6939608 7.5186100 5.1730926 5.5940017
##      309      310      311      312      313      314      315
## 8.2445785 10.0934330 9.7805712 6.5237696 6.0504319 10.5363559 8.7214363
##      318      319      322      323      324      325      326
## 7.1242762 8.9349126 9.1637972 9.1818061 9.8106525 2.7837925 11.0344024
##      328      329      331      332      333      335      336
## 6.7117069 4.3700741 5.4849993 8.4604242 7.4115345 7.2647218 7.5453393
##      337      338      339      341      342      343      344
## 4.6252253 6.6341776 6.5666191 8.2739531 6.2091645 8.5548294 5.4276928
##      345      346      348      349      350      351      353
## 8.8829301 4.8935931 7.8735736 14.1888310 10.7123828 9.4902091 11.4564821
##      354      355      357      358      359      361      362
## 9.2532619 4.3656946 6.3784885 9.9811372 5.1952094 9.9755176 8.3115072
##      364      365      366      367      368      369      370
## 10.6671625 9.9862564 3.7980568 5.6405996 13.5035464 10.7964694 10.8238967
##      371      372      374      375      377      378      379
## 7.1825044 8.2551579 6.5400318 7.6387671 15.8549829 6.6835138 6.4169409
##      381      382      383      384      385      387      388
## 7.7114663 2.5632389 6.6772413 9.1624060 12.1634356 6.2885357 8.7721120
##      389      390      392      393      394      395      396
## 9.5610293 9.0200603 6.2595241 5.6717540 6.3903289 5.8986975 13.1526578
##      397      398      399
## 6.7352176 7.0322852 5.5213980
```

```
coefficients(lmModel) #coefficients of regression
```

```
##      (Intercept)      CompPrice      Income      Advertising      Population
## 5.842839e+00 9.105120e-02 1.658512e-02 1.227960e-01 8.434767e-06
##      Price      ShelfLocGood      ShelfLocMedium      Age      Education
## -9.555257e-02 4.856521e+00 1.884479e+00 -4.679088e-02 -1.783126e-02
##      UrbanYes      USYes
```

```
##      1.946842e-01    -1.624238e-01
```

```
residuals(lmModel) #residuals from actual train values - predicted train values
```

##	1	2	3	6	7	9
##	2.230694030	-1.230735704	0.819770826	1.179317660	0.404592547	0.551588688
##	10	12	13	14	15	17
##	-1.061118049	0.074253427	0.337512644	-1.039492364	1.432729453	-0.900790488
##	18	19	22	23	25	26
##	0.476914082	0.482714358	1.072893677	-0.617160949	0.098264051	1.570477230
##	27	28	29	30	33	34
##	-0.158568562	-0.010350553	-1.455458019	1.743167126	0.177949539	0.284859082
##	35	36	37	38	39	40
##	-1.960409363	0.368225301	-1.496680105	-1.908415281	0.584112912	-0.293195755
##	41	42	43	44	45	46
##	-0.474935404	1.592718155	-0.693759606	-1.089829057	-0.850800387	-0.027226995
##	47	48	49	51	52	53
##	-0.698224835	-1.578298726	-0.641146792	-1.864848716	-0.014350196	1.543418266
##	54	55	56	57	58	60
##	1.105847319	-0.551772363	2.002522027	1.186845148	-0.219605349	-0.257949217
##	61	62	63	64	66	69
##	0.649599794	1.171057359	-0.844256730	-0.076695497	0.667595210	1.331673510
##	70	71	72	73	74	75
##	0.238201538	0.573693350	-0.002409133	-1.101524754	0.192074307	-0.543823736
##	76	77	78	79	80	81
##	0.948382009	0.870180973	-1.300271663	0.660012304	0.537964840	-0.853533793
##	82	83	84	85	86	90
##	0.605786098	0.164241631	-1.041889288	-0.239757190	0.876898810	0.862610434
##	91	92	93	94	95	96
##	-0.204544558	0.337396123	-2.131792916	0.051552936	0.616204205	1.109222668
##	97	98	99	100	101	102
##	-0.055457085	-0.905042128	0.722384610	0.162359956	-2.340947097	-1.732665897
##	103	105	108	109	110	112
##	-0.486149727	-0.128784582	-0.007241515	-0.701311868	1.412247213	0.098856851
##	113	115	116	117	119	120
##	-1.822898941	1.295748957	1.903906079	-0.032504917	0.462438692	0.670561808
##	121	122	123	124	125	127
##	0.058593189	1.507790674	0.019764208	0.815292805	-1.163624695	0.988113927
##	128	129	130	131	133	134
##	-0.067000358	-0.209832125	-0.986700529	-0.944223132	1.419358770	0.236582738
##	135	136	138	140	141	142
##	-0.428863087	0.324549366	1.457809894	-0.199746712	-1.311957432	1.140942340
##	143	144	146	147	148	149
##	0.639803368	-1.966577256	-0.814843590	0.694468902	-1.203773476	0.889786936
##	150	152	153	154	155	156
##	0.244990458	0.727840370	-1.442303972	-0.947537326	-1.659642585	-0.409810576
##	157	158	159	160	161	162
##	0.410119514	0.759005836	0.151787620	0.057192641	-1.455237342	0.019209227
##	163	164	165	166	167	168
##	0.224351142	-0.804731508	1.085664683	-0.930614715	0.775664562	-0.150316057
##	169	170	171	172	174	175
##	-0.383713630	-0.152780662	1.248162171	2.059753194	-0.156571838	0.856677157
##	176	177	178	180	182	183
##	0.711875090	-0.293368677	-0.491593310	1.133401565	-0.813220184	-0.480830451
##	184	185	186	187	188	191

##	-1.340692228	1.231367699	0.857764905	-0.147053843	1.184777764	-1.210174011
##	192	194	196	197	198	199
##	-0.317207490	0.076736663	-0.389002427	1.546362317	-0.679189629	-0.644706852
##	200	201	203	204	205	207
##	0.759757481	0.258220315	0.366610134	-0.855160144	-0.794326991	0.543137732
##	208	209	210	211	212	213
##	2.796265738	0.885723929	-0.933244249	0.571366991	0.528575444	-0.068971996
##	214	215	216	217	218	221
##	-0.100973299	-1.715725255	-0.039111244	0.074012066	0.358787602	0.498908226
##	223	224	225	226	227	228
##	0.360162349	-1.084289032	-1.241390490	0.251315512	0.048828059	0.954845045
##	229	231	232	233	234	235
##	0.330456157	0.770846439	0.315424851	0.534125599	-0.513946015	1.272575437
##	236	237	239	241	242	243
##	0.039692244	-0.082911572	1.405063249	-0.319618495	1.632793502	0.480100221
##	244	245	246	247	250	251
##	0.114538605	-0.386726567	-0.377592535	-0.717791553	0.936350531	1.506080422
##	252	253	254	255	256	257
##	-1.522978686	-0.368898920	0.308774204	-1.176613076	0.058667897	-0.418652120
##	258	259	263	265	266	267
##	1.454541697	-1.480380813	-0.255577670	0.376989273	0.240671724	-1.689597634
##	268	269	270	272	273	274
##	-0.972619387	-1.483199517	-0.219971333	-0.714585093	-0.738416223	0.121401494
##	275	276	278	279	280	281
##	-1.462273184	1.130786877	-0.701085729	0.749970793	-1.309783596	-0.270988415
##	282	283	284	285	286	287
##	-0.037773995	-0.639086750	-1.276315555	2.531227797	-0.716680319	0.254089378
##	288	289	290	291	292	293
##	0.374068148	1.118889649	0.840707010	0.575646249	-0.671262426	-1.368010275
##	295	298	299	300	301	302
##	-0.713816466	-2.899286090	1.200012750	-1.209049287	0.592153081	0.357721358
##	303	304	305	306	307	308
##	0.917641417	-1.021139992	1.236039216	0.511390016	-0.393092577	0.305998264
##	309	310	311	312	313	314
##	0.995421550	1.086567015	-0.250571201	-0.373769624	0.749568058	-1.206355943
##	315	318	319	322	323	324
##	-1.001436329	-0.714276207	1.145087355	-1.643797249	-0.021806078	0.549347475
##	325	326	328	329	331	332
##	-0.123792486	0.665597581	-0.481706880	-1.220074099	-0.494999319	1.639575790
##	333	335	336	337	338	339
##	-1.671534537	0.365278177	-1.365339314	0.544774705	1.975822420	-0.596619135
##	341	342	343	344	345	346
##	-0.773953143	1.170835487	-0.744829401	0.562307168	-0.452930144	-0.083593073
##	348	349	350	351	353	354
##	-0.993573632	-1.618830960	-1.392382757	-0.850209132	1.983517946	0.196738102
##	355	357	358	359	361	362
##	0.934305384	-2.798488538	3.378862813	-1.025209406	-1.205517634	0.368492828
##	364	365	366	367	368	369
##	-0.407162452	0.513743585	2.731943190	0.339400418	0.866453568	-0.086469417
##	370	371	372	374	375	377
##	-0.563896737	0.497495578	0.824842109	-0.960031808	1.801232868	0.415017124
##	378	379	381	382	383	384
##	0.126486208	-0.306940862	1.928533721	1.336761074	-1.727241323	0.187593957
##	385	387	388	389	390	392

```
## 0.686564379 -0.968535721 -0.102111983 -1.421029263 -0.580060304 -0.159524076
##          393          394          395          396          397          398
## -1.141754048 -0.820328934 -0.548697514 -0.582657813 -0.595217563  0.377714820
##          399
## 0.418602026
```