

Economic Growth Theory:

Problem set 9:

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Growth and government debt

1. Consider a growth model with a government that finances expenditures with debt. Let the consumer problem be

$$\max_C \int_0^\infty \ln(C(t)e^{-\rho t}) dt, \rho > 0$$

subject to $\dot{K} + \dot{B} = Y + rB - C - T$ given $B(0)$, $K(0)$ and a non-Ponzi game condition. The production function be $Y = K^\alpha G^{1-\alpha}$ with $0 < \alpha < 1$. (Hint: G and T are taken by the consumer as externalities). Notation: consumption, C , physical capital stock K , government debt B and r is the interest rate. The government budget constraint is $\dot{B} = G - T + rB$. There are two policy instruments: taxes are defined as $T = \tau Y$ and there is a rule of keeping the debt ratio constant as $B/Y = \bar{b} > 0$.

- (a) Write the DGE in (z, g) where $z = C/K$ and $g = G/Y$ and provide an intuition why this represents the detrended DGE dynamic system.
- (b) Find the long-run growth rate.
- (c) Study the growth facts associated to the model.