#### Introduction

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# Object of economic growth theory

- ▶ Dynamics of per capita aggregate income across long time, and space.
- ► Main questions
  - ▶ what is the meaning of "long time" (millenia, centuries, decennials) ?
  - ▶ what are the main factors explaining economic growth?
  - why rates of growth differ along historical times ?
  - ▶ why the rates of growth differ accross countries ?
  - why countries hold inequalities in the GDP per capita while having similar rates of growth?

## Main takeaways from the course

- Economic growth exists only if a reproduction mechanism exists
  - $\Rightarrow$  economic growth has an  $\mathbf{exponential}$  feature

$$y(t) \approx e^{\gamma t}$$

► The observed increase in the GDP per capita is not a reliable measure of economic growth: we should distinguish the transition from long term growth rate

$$\frac{\Delta y}{y}\Big|_{\text{observed}} = \gamma + \gamma_{\text{transition}}$$

- $\Rightarrow$  we need some **theory** to separate the two
- ▶ Level from rate of growth effects of shocks should be distinguished.
- ► (Side takeaway) In the very long run everything is endogenous.



## Beyond economic growth

Human impact on Earth's geological phases

#### The **Anthropocene**:

- ▶ consensus: there is a geological impact by human activity
- ▶ no consensus: periodization (when did it started ?)
  - ▶ around 8000 BCE ? (deforestation, increase in carbon concentration preventing a "natural" reduction in Earth's temperature)
  - ▶ around 1600 CE ? (exchange in animal and plant species brought about by human activity)
  - ▶ around 1800 CE ? (industrial revolution, increase in earth's temperature)
  - ▶ around 1944 CE ? (clear increase in temperature, start of the atomic era)
- ▶ see http://www.anthropocene.info

### Main growth factors

#### By increasing degree of variability

- Physical and biological environments: geography, size, resources, biology;
- ▶ Population: demography, human capital, social capital;
- ► Technology: capital accumulation, productivity growth (learning by doing, R&D );
- ► Aggregation: externalities, public goods ;
- ► Economic institutions: inclusive/exclusive, financial institutions, trade openness, patent protection;
- ▶ Political Institutions: in a broad sense (inclusive/exclusive, rule of law, enforcement, accountability) or a narrow sense (government intervention, governance)
- Luck (good or bad)

## Phases of economic growth

Secular long run perspective:

- ► Malthusian trap and first globalization (goods): (almost) constant rates of growth (6000 BCE to 1700 CE)
- ► Industrial Revolution: transition with modest increases in the rate of growth
- ▶ Modern economic growth and second globalization (goods): rapid economic growth and Great Divergence: post 1820 and until 1990 (according to some authors)
- ► Great convergence and third globalization (ideas): post 1990
- ▶ Nature strikes back: eventual natural limits to growth?

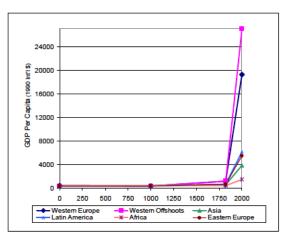


Figure 1: The Evolution of Regional Income Per Capita, 1-2000 CE (Source: Maddison, 2003)

Figure: Maddison on the evolution of income per capita

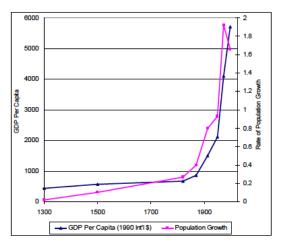


Figure 4: World Population Growth and Income Per Capita (Source: Maddison, 2001)

Figure: Maddison on the evolution of population

# Ancient growth experience Malthusian trap

- $\blacktriangleright$  low rates of growth: between 0% and 0.5%
- rises in income implied rises in population (not income p.c.)
- negative correlation between population growth and real wages
- ▶ big impact of demographic changes and (ex Black-Death (1347-1350)) and institutions (ex. different responses to it in E. and W.Europe);

# Ancient growth experience Malthusian trap

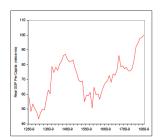


Figure 2: Fluctuations in Real GDP Per Capita in England, 1260-1870 CE (Source: Clark, 2005)



Figure 5: Population and Real Wages in England, 1250-1750 CE (Source: Clark, 2005)

Figure: Clark on the UK's population and real wages

# Ancient growth experience Limits to growth

- ▶ labor was the main factor of production
- ▶ land had an impact on growth because of decreasing returns;
- ▶ there were some gains in productivity, although not related to a purposeful activity as R&D;

# Ancient growth experience

First globalization

▶ there was a small difference in GDP per capita across the world (Eurasian continent)

Table: Ratio richest to poorest region: before the great divergence

1000	1500	1820
1.1:1	2:1	3:1

- ► E. and SW. Asia were richer (see Frankopan (2016))
- ▶ first globalization: a first decoupling between production and consumption took place with trade in a small number of (luxury) goods (Silk road)
- physical distance was a major factor

# Modern economic growth

- modern economic growth: permanent positive rates of growth;
- ▶ it may have started in the UK around 1800;
- ▶ it was contemporaneous with a demographic revolution, but growth became independent from the growth population;
- ▶ non-Malthusian features: rise in wages and almost stationary rate of return of capital

# Modern economic growth

Main factors

▶ two driving forces: increases in productivity and capital accumulation (physical, human, social)

- physical capital accumulation: massive, helped by the development of financial system
- ► technologic progress: rise in productivity as a purposeful activity, huge reduction in transport costs;
- unprecedented accumulation of human capital: schooling and knowledge (Scientific Revolution)
- social capital: institutions (protection of property rights, contract enforcement, reduction of transactions costs, reduction in uncertainty, etc)
- ▶ non-renewable natural resources: no decreasing returns?

# Modern economic growth

#### Great divergence

► The Great divergence:

Table: Ratio richest to poorest region: after the great divergence

1820	1870	1913	1950	2001
3:1	5:1	9:1	15:1	18:1

- ▶ increase in disparities and change of the economic center
- second globalization (inter-industrial trade): huge reduction in transport costs lead to an increase in the trade in goods and the Ricardo comparative advantage mechanism start working massively;
- ► relative free capital movement re-inforced this movement and lead to an international alignment of interest rates;
- ▶ increasing agglomeration of economic activity in a few centers (at national and international levels)

# Present epoch: a new phase?

Great convergence

- ► technical progress: driven by IT lead to a reduction of costs in the movement of **ideas**, robotization;
- ▶ third globalization (intra-industrial trade): a large part of international trade is related to the supply chains of some multinational corporations;
- ▶ allowed high increases in wages in a few (7) countries (technology from the "North" and wages from the "South") and competition between countries for parts of the supply chains;
- ▶ institutional consequences: rebalances of the inclusive/exclusive attitudes around the world?
- ▶ limits to growth as a result of the environmental impact of human activity ?

- ► Long run growth arises only for a very particular mathematical structure:
- ► Let

$$\dot{y} \equiv \frac{dy(t)}{dt} = \mu(y)$$

- logistic growth:  $\mu(y) = \alpha y(\beta y)$ ,
- exponential growth:  $\mu(y) = \gamma y$ ,
- **power law** growth:  $\mu(y) = y^{\phi}$  for  $\phi > 1$ ,
- ► razor edge property of growth models: although the exponential case is very particular it this the structure underlying (almost) all growth theories

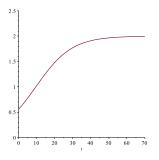


Figure: Logistic growth  $\mu(y) = \alpha y(\beta - y)$ 

- ▶ there is short run (transition) growth
- but there is no long-run growth

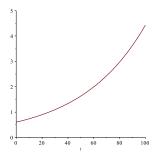


Figure: Exponential growth  $\mu(y) = \gamma y$ 

- ▶ there is no short run (transition) growth
- but there is long-run growth
- ▶ gdp becomes infinite  $(y(t) \to \infty)$  in **infinite** time

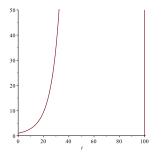


Figure: Power law growth  $\mu(y) = y^{\phi}$  for  $\phi > 1$ 

- ▶ gdp becomes infinite  $(y(t) \to \infty)$  in **finite** time
- ▶ and collapses afterwards

#### Puzzle 2: growth and distribution

► Consider the former equation

$$dy(t) = \mu(y)dt$$

▶ let  $\rho(y, t)$  be the density of population having the income  $y \in [y_0(t), y_1(t)] \in (0, \infty)$ , such that

$$\int_0^\infty \rho(y, t) dy = 1,$$

▶ the dynamics of the distribution is given by

$$\frac{\partial \rho(y,t)}{\partial t} + \frac{\partial}{\partial y} (\mu(y)\rho(y,t)) = 0$$

#### Puzzle 2: growth and distribution

We can determine

▶ the average per capita income

$$\bar{y}(t) = \int_0^\infty \rho(y, t) y dy$$

▶ its variance

$$\sigma(t) = \int_0^\infty \rho(y, t) (y - y(t))^2 dy$$

▶ the Gini index

$$G(t) = \frac{1}{\bar{y}(t)} \int_0^\infty R(y, t) (1 - R(y, t)) dy \in (0, 1)$$

where 
$$R(x,t) = \int_0^x \rho(y,t) dy$$



Puzzle 2: growth and distribution

- ▶ there are four important properties that interest us
  - ▶ long run growth: does  $\lim_{t\to\infty} y(t) = \infty$ ?
  - ergodicity: does  $\lim_{t\to\infty} \sigma(t) = \bar{\sigma}$  finite and constant (independent from the initial distribution )?
  - **dispersion**: does  $\sigma(t) = 0$  or  $\lim_{t \to \infty} \sigma(t) = 0$ ?
  - ▶ inequality: does  $G(t) \in (0,1)$  stays stationary, increases, decreases, f or  $\lim_{t\to\infty} \sigma(t) = 0$ ?

#### Puzzle 2: growth and distribution

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  - ergodicity: does  $\lim_{t\to\infty} \sigma(t) = \bar{\sigma}$  finite and constant (independent from the initial distribution )?
  - ▶ dispersion: does  $\sigma(t) = 0$  or  $\lim_{t\to\infty} \sigma(t) = 0$ ? or  $\lim_{t\to\infty} \sigma(t) = +\infty$ ? or  $\lim_{t\to\infty} \sigma(t) = 0$ ?
  - ▶ inequality: does  $G(t) \in (0,1)$  stays stationary, increases, decreases,
- examples, starting from an initial heterogeneous distribution:
  - ightharpoonup case1: logistic  $\mu(k) = ay(b-y)$
  - case 2: constant  $\mu(k) = \bar{\mu}$
  - ightharpoonup case 3: exponential  $\mu(k) = \gamma k$
- ► can we have long-run growth without an increase in inequality?

Puzzle 2: growth and distribution

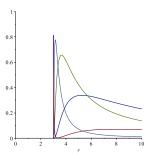


Figure: case 1: ergodicity, long run equality, but no growth (obs: increasing time moves distribution to the left)

Puzzle 2: growth and distribution

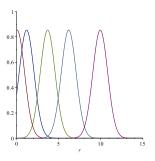


Figure: case 2: permanent ergodicity and dispersion and growth:  $\mu(k) = \bar{\mu}$ 

Puzzle 2: growth and distribution

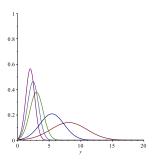


Figure: case 3: no ergodicity, increasing dispersion, permanent inequality and growth:  $\mu(k) = \gamma k$ 

### Some historical facts

#### Inequality

▶ Inequality in the very long run: Scheidel (2017) and

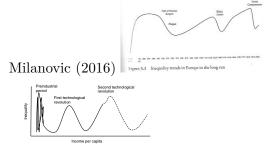


FIGURE 2.4. Expected pattern of changes in inequality versus income per capita from the preindustrial through the postindustrial period and into the future (dotted line)

- ▶ Pre IR: compression (short) and distension (longer) periods
- ➤ Post IR: distension (IR WWI, 1970 present) and compression (WWI- 1970)



#### References

- ► Anthropocene: Lewis and Maslin (2018)
- ▶ Long-run growth facts: Maddison (2007)
- ➤ Stylized facts on economic growth: (Acemoglu, 2009, ch. 1, 2), (Barro and Sala-i-Martin, 2004, ch. 10,11,12)
- ▶ Pre-modern and modern economic growth: (Galor, 2011, ch 2)
- ▶ Inequality: Milanovic (2016), Scheidel (2017)

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