

# Performance Modeling and System Design Insights for AI Foundation Models

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*NERSC, Berkeley Lab*



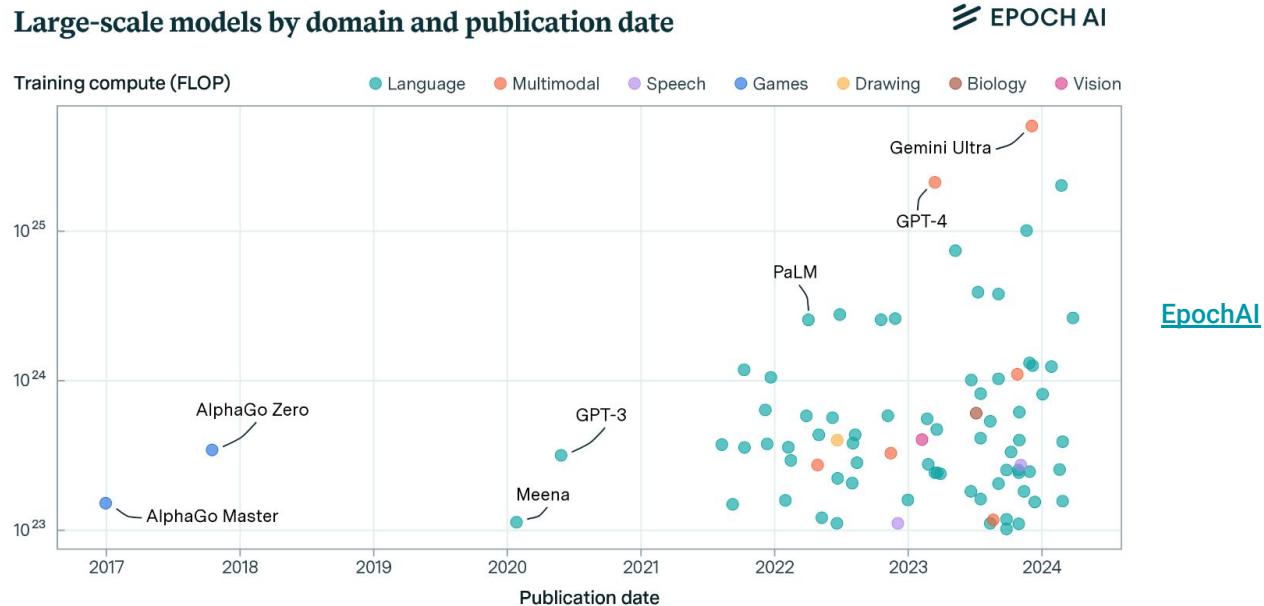
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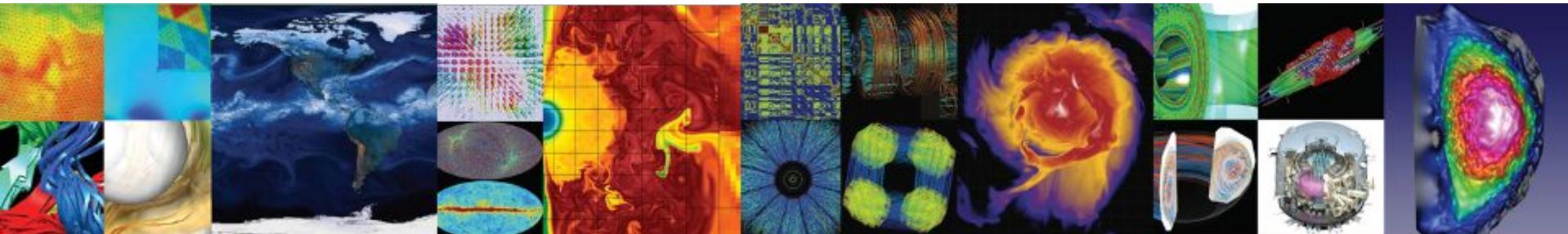
Comprehensive Performance Modeling and System Design Insights for Foundation  
Models, PMBS, SC24, [arXiv](#), [Github](#)

# AI Foundation Models are **Expensive**



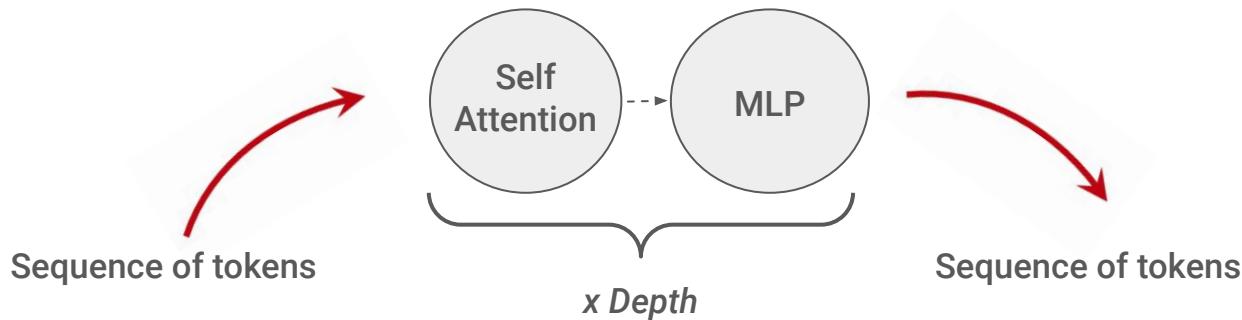
- Transformers are the workhorse: Scaling properties, flexible, SOTA results

# Large-scale AI Models are Growing in Science



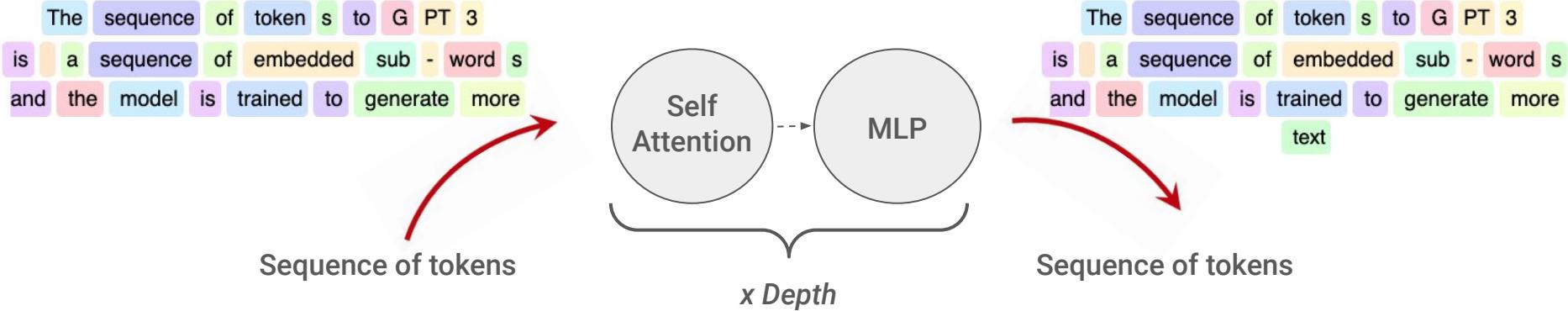
- Range of scientific simulation tasks is enormous
  - weather/climate, fusion, seismic, fluids, proteins, material sciences, high-energy physics, ...
- Surge of transformer models as possible *foundations* for downstream tasks
  - forecasting, superresolution, inversion, reconstruction, UQ, ...

# Transformers in Science can Amplify the Cost



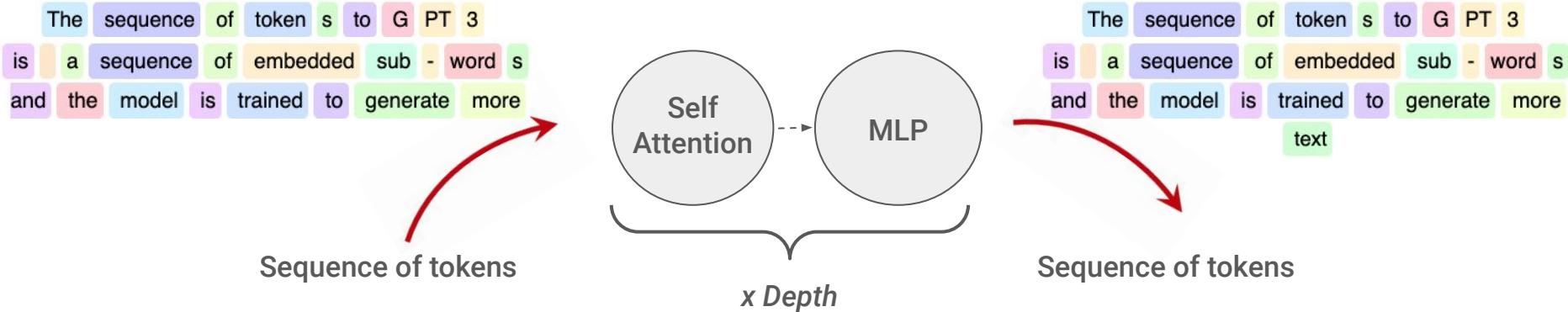
- Transformers in science may operate in different computational regimes

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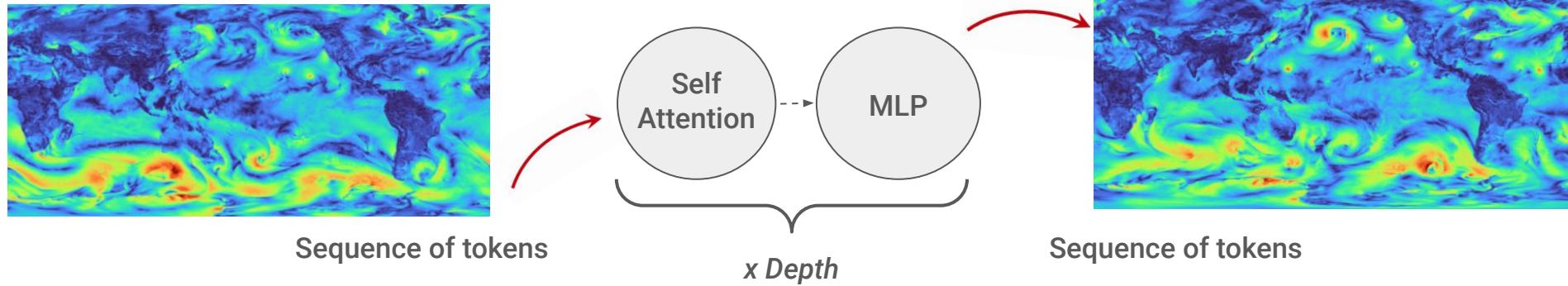
- A Large Language Model (LLM) example: GPT3

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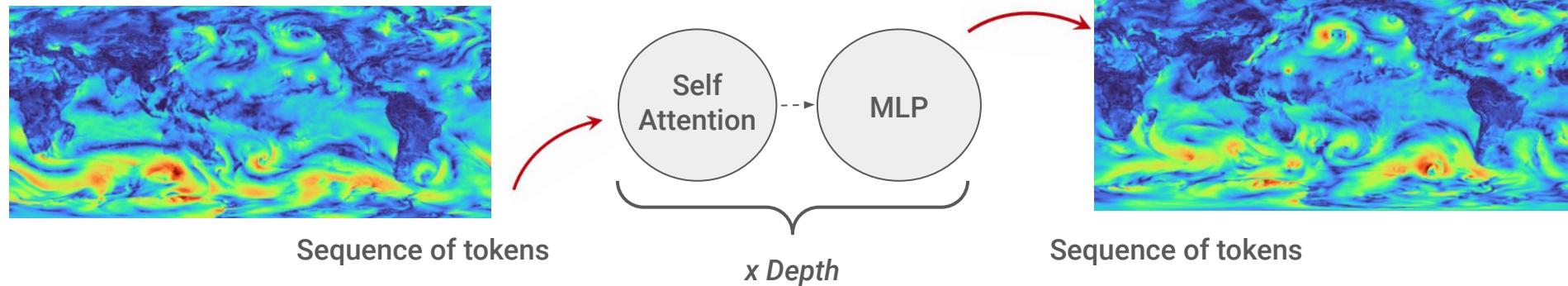
- A Large Language Model (LLM) example: GPT3
  - #Parameters can be huge ~ **billions to trillions** of parameters
  - Process a sequence of O(1K) tokens (usually **2K, 4K** tokens in pre-training)
  - MLP FLOPs are large (compared to S/A)
  - GPT3-1T on **3072 A100 GPUs** takes **84 days** to train on 450B tokens
  - Understood reasonably well

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- A Scientific Surrogate example: Transformer for global weather forecasting

# Transformers in Science can Amplify the Cost



- A Scientific Surrogate example: Transformer for global weather forecasting
  - #Parameters are moderate ~ **million to billion** parameters
  - Process a sequence of **O(1M) tokens** (usually downsampled to O(10K) tokens)
  - S/A FLOPs are large (compared to MLP)
  - **A small model could be more expensive than a trillion parameter LLM!**
  - [?] Days on [?] GPUs on [?] tokens. Less understood

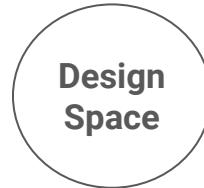
# Performance Modeling can be Valuable

- Understand **Costs/Bottlenecks** and analyze **Sensitivity of Performance**
  - What bottlenecks w.r.t parallelization strategies?
  - Different Transformer regimes (LLMs vs Science)?
  - Different system hardware (specifically network/NVLINK effects)?
  - Different system scales (10s vs 1000s of accelerators)?

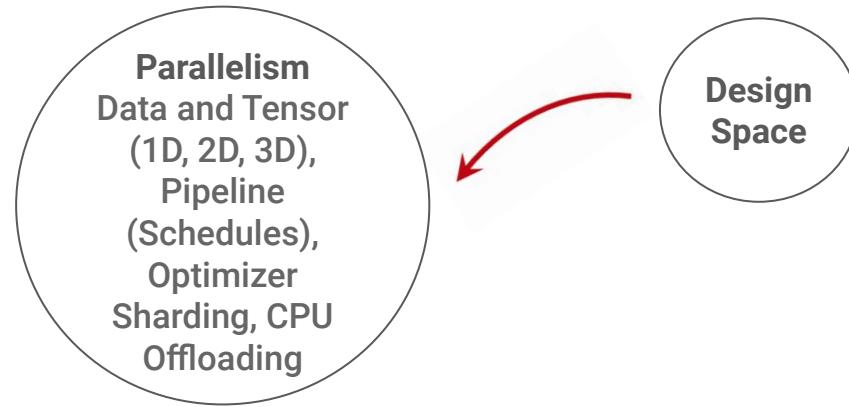
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- **Value-add for:**
  - Users (researchers, engineers)
    - Optimal ways to parallelize AI models? Architecture search with performance in mind?
  - Systems design
    - Which aspects of the HPC system are crucial? Alternate design choices?

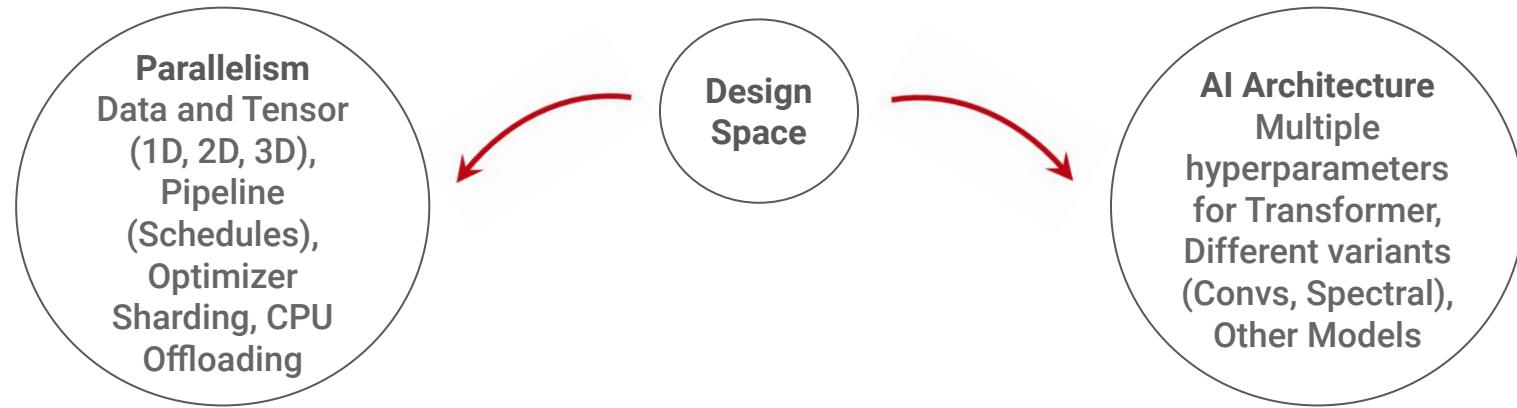
# AI Performance Modeling is Challenging



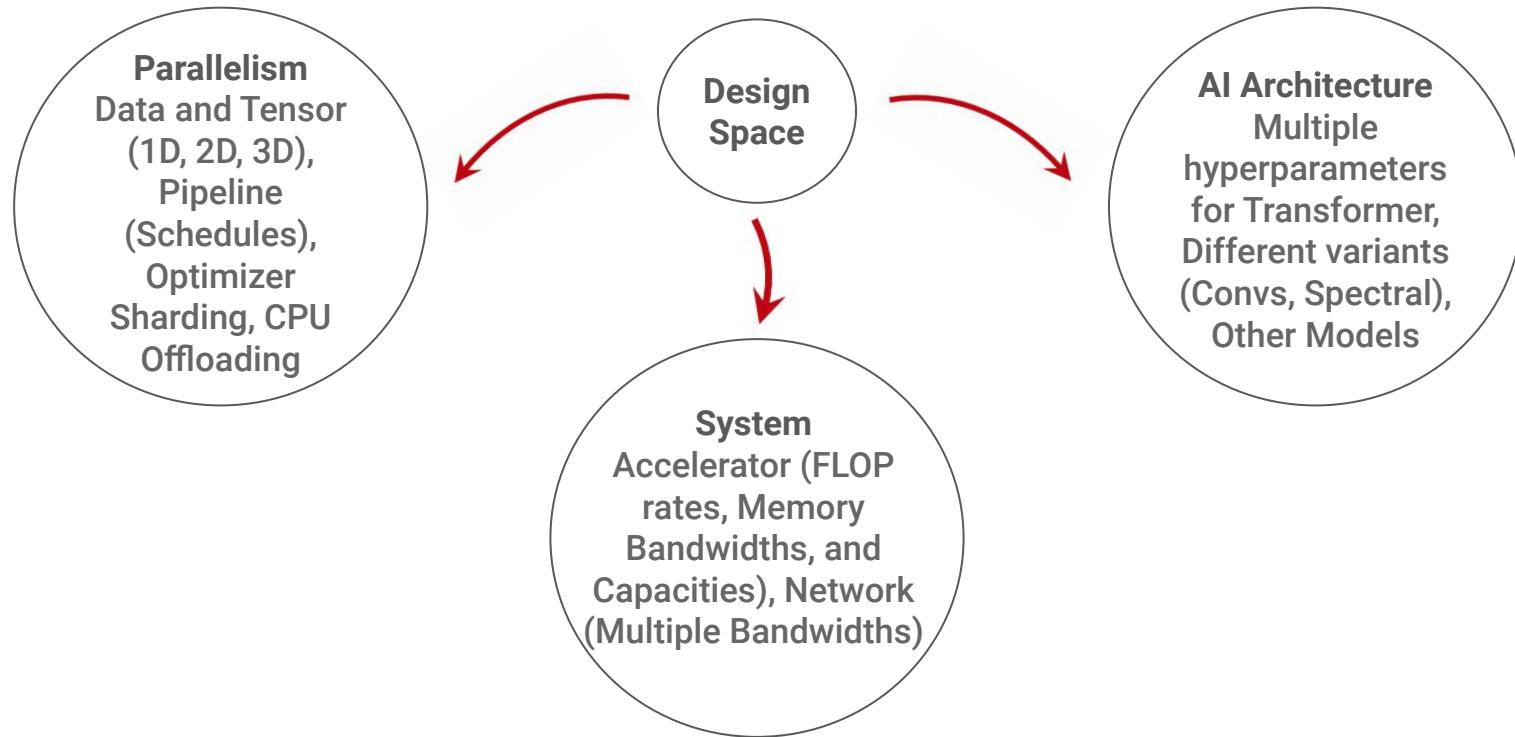
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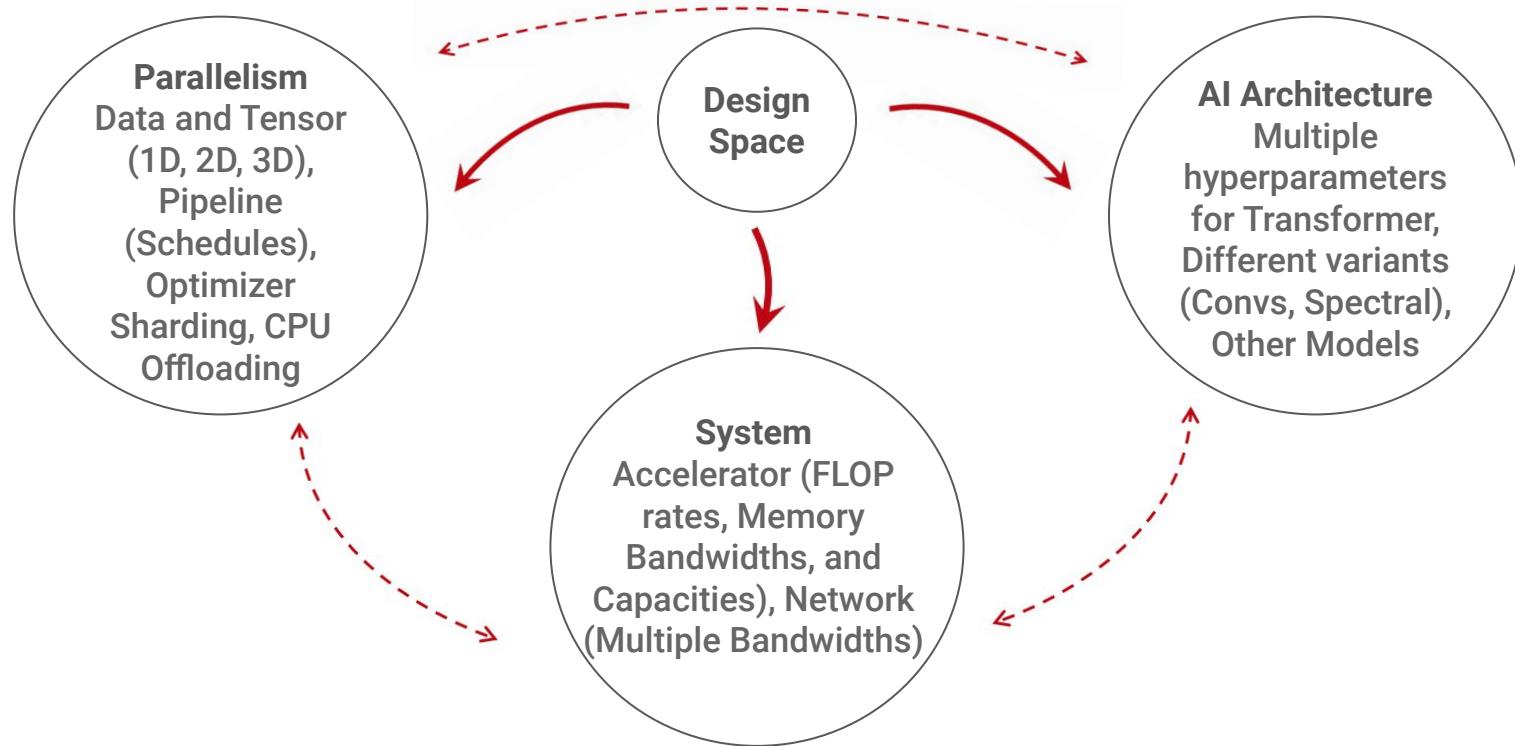
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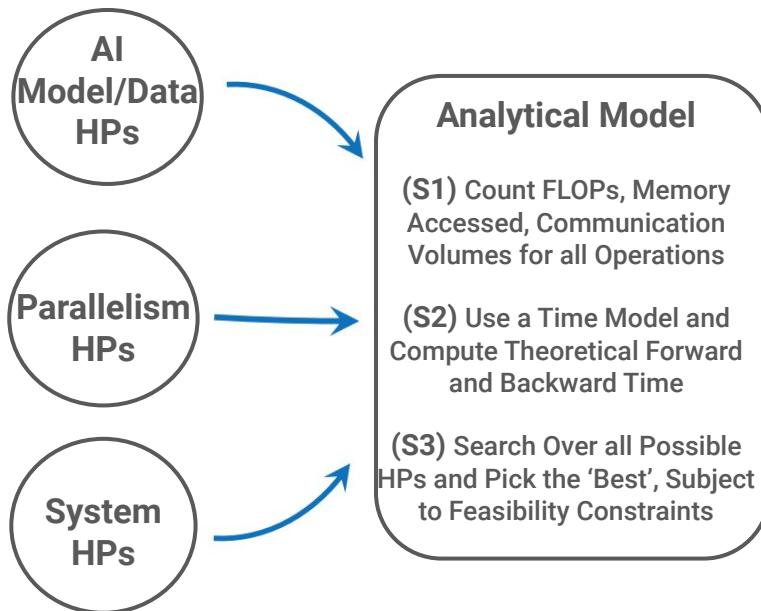
# Analytical and Parameterized Models can be Valuable

AI  
Model/Data  
HPs

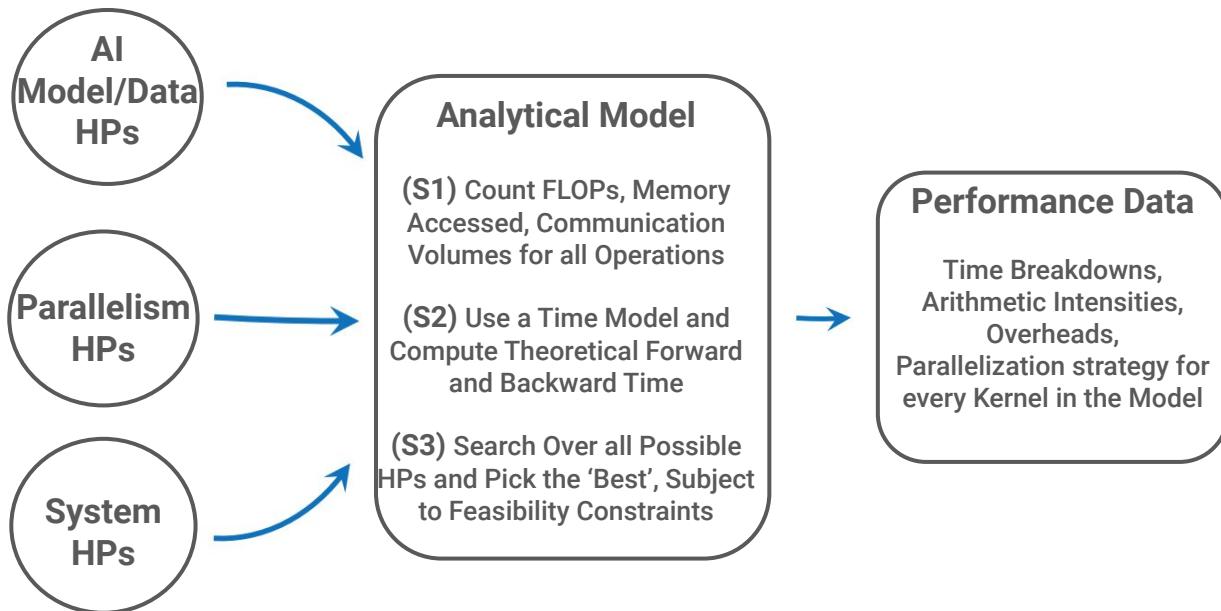
Parallelism  
HPs

System  
HPs

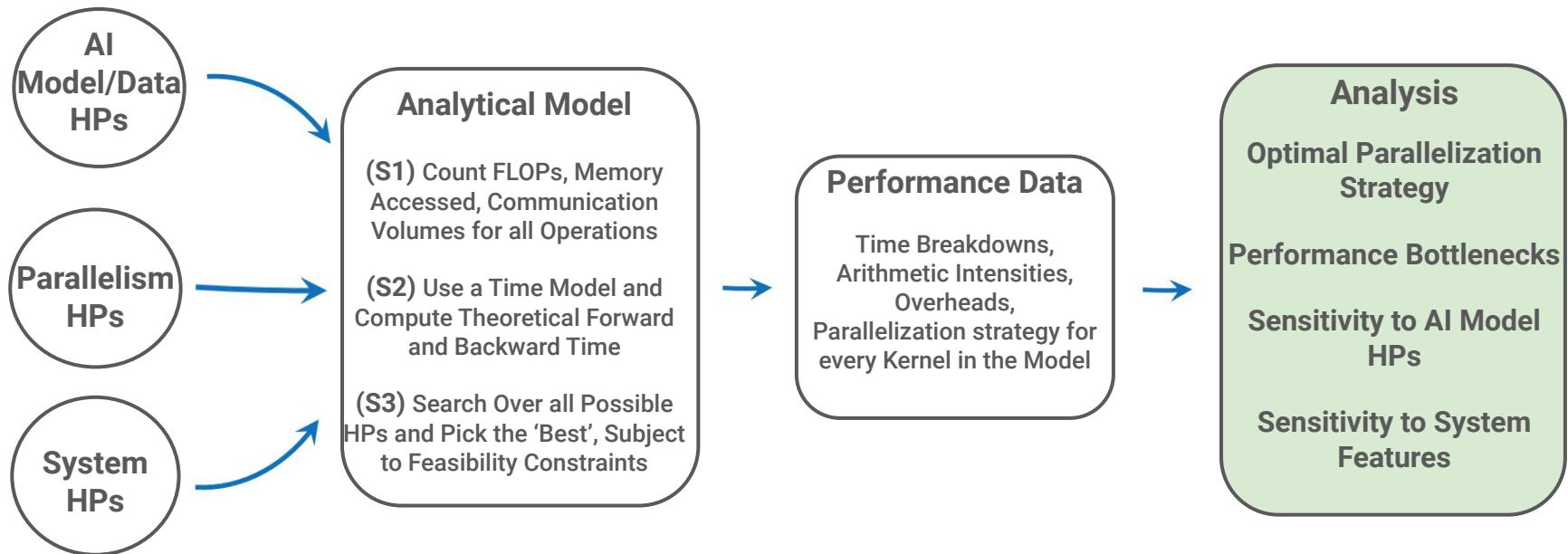
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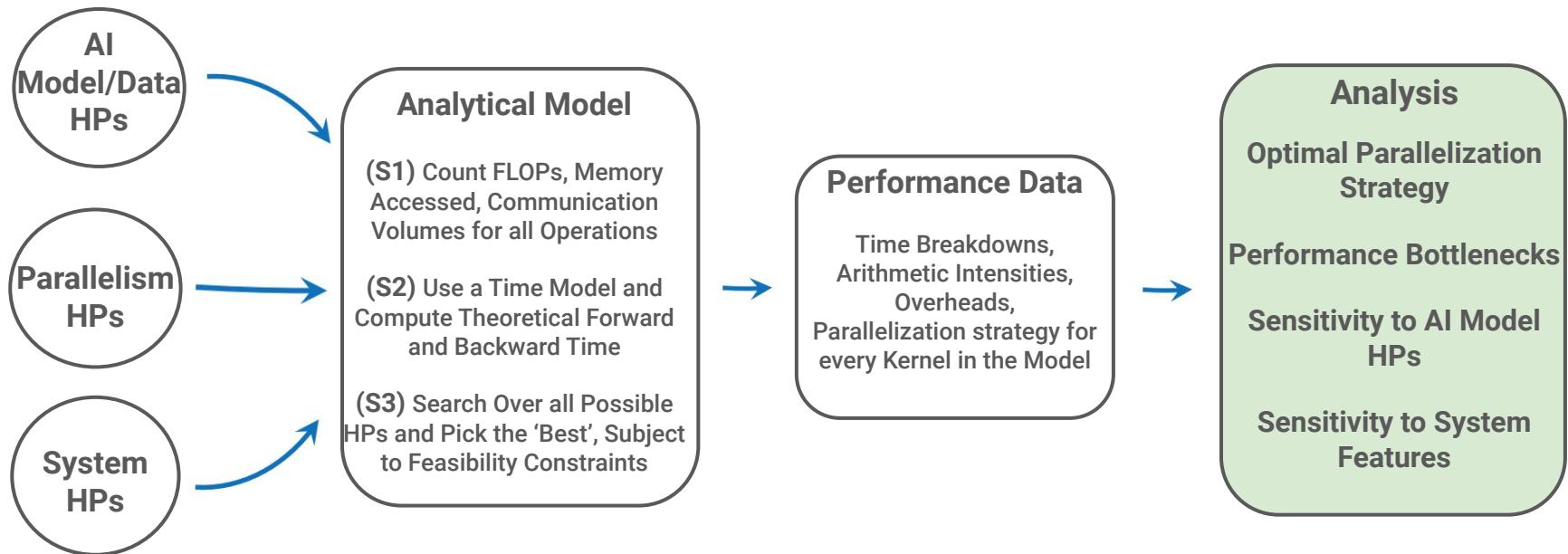
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# Analyze Varying Needs for Transformers in Science

- Counting FLOPs, communication volume is dependent on the parallelism
- Long sequence lengths may necessitate 4D parallelism

Operation	Partitioned Tensor Shapes	Type	Vol
<b>2D TP over <math>n_1 \times n_2</math> grid of GPUs</b>			
SA			
$\tilde{\mathbf{X}} = \text{LN}(\mathbf{X})$	$\tilde{\mathbf{X}} : (b, \frac{l}{n_2}, e), \mathbf{X} : (b, \frac{l}{n_1 n_2}, e),$	$\mathcal{AG}$	$b \frac{l}{n_2} e$
$\mathbf{Q} = \tilde{\mathbf{X}} \mathbf{W}_{\mathbf{Q}}$	$\mathbf{Q} : (b, \frac{h}{n_1}, \frac{l}{n_2}, e_h), \mathbf{W}_{\mathbf{Q}} : (e, \frac{e}{n_1}),$	-	0
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# Analyze Varying Needs for Transformers in Science

- Long sequence lengths may necessitate 4D parallelism
- Different choices for Matrix Multiplies: SUMMA also possible

Operation	Partitioned Tensor Shapes	Type	Vol
<b>2D TP with SUMMA over <math>n_1 \times n_2</math> grid of GPUs</b>			
SA			
$\tilde{\mathbf{X}} = \text{LN}(\mathbf{X})$	$\tilde{\mathbf{X}} : (b, \frac{l}{n_2}, \frac{e}{n_1}), \mathbf{X} : (b, \frac{l}{n_2}, \frac{e}{n_1})$	$\mathcal{AR}$	$b \frac{l}{n_2} e$
$\mathbf{Q} = \tilde{\mathbf{X}} \mathbf{W}_Q$	$\mathbf{Q} : (b, \frac{h}{n_1}, \frac{l}{n_2}, e_h), \mathbf{W}_Q : (\frac{e}{n_2}, \frac{e}{n_1})$	$\mathcal{B}$	$V_1$
$\mathbf{A} = \mathbf{Q} \mathbf{K}^T$	$\mathbf{A} : (b, \frac{h}{n_1}, \frac{l}{n_2}, l), \mathbf{K} : (b, \frac{h}{n_1}, l, e_h)$	$\mathcal{AG}$	$bl \frac{e}{n_1}$
$\mathbf{S} = \mathbf{A} \mathbf{V}$	$\mathbf{S} : (b, \frac{h}{n_1}, \frac{l}{n_2}, e_h), \mathbf{V} : (b, \frac{h}{n_1}, l, e_h)$	$\mathcal{AG}$	$bl \frac{e}{n_1}$
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MLP			
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$\mathbf{Z} = \tilde{\mathbf{Y}} \mathbf{W}_1$	$\mathbf{Z} : (b, \frac{l}{n_2}, \frac{f}{n_1}), \mathbf{W}_1 : (\frac{e}{n_2}, \frac{f}{n_1})$	$\mathcal{B}$	$V_2$
$\mathbf{X} = \mathbf{Z} \mathbf{W}_2$	$\mathbf{X} : (b, \frac{l}{n_2}, \frac{e}{n_1}), \mathbf{W}_2 : (\frac{f}{n_2}, \frac{e}{n_1})$	$\mathcal{B}$	$V_3$

$$V_1 = ble/n_2 + e^2/n_1$$

# Two Transformer Variants on Different Systems

- Large GPT3 (1T, 2K) on ~trillion tokens
- Large ViT (80B, 64K) on 40 years of weather data



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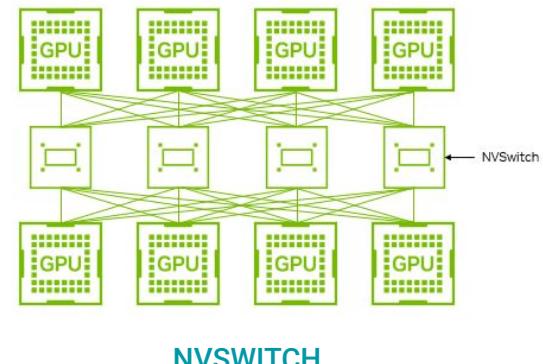
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- Large GPT3 (1T, 2K) on ~trillion tokens
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System

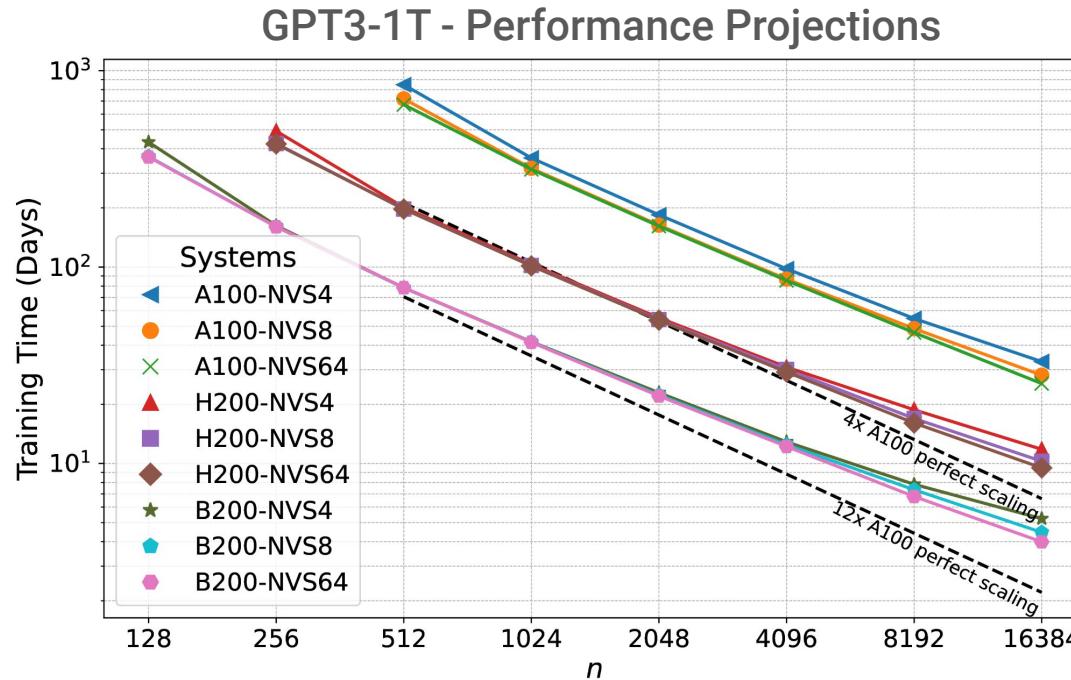
- Three NVIDIA GPU generations: A100, H200, B200
- Three NVLINK/NVSWITCH domain sizes: 4, 8, 64

Multi-GPU Configuration with NVSwitch

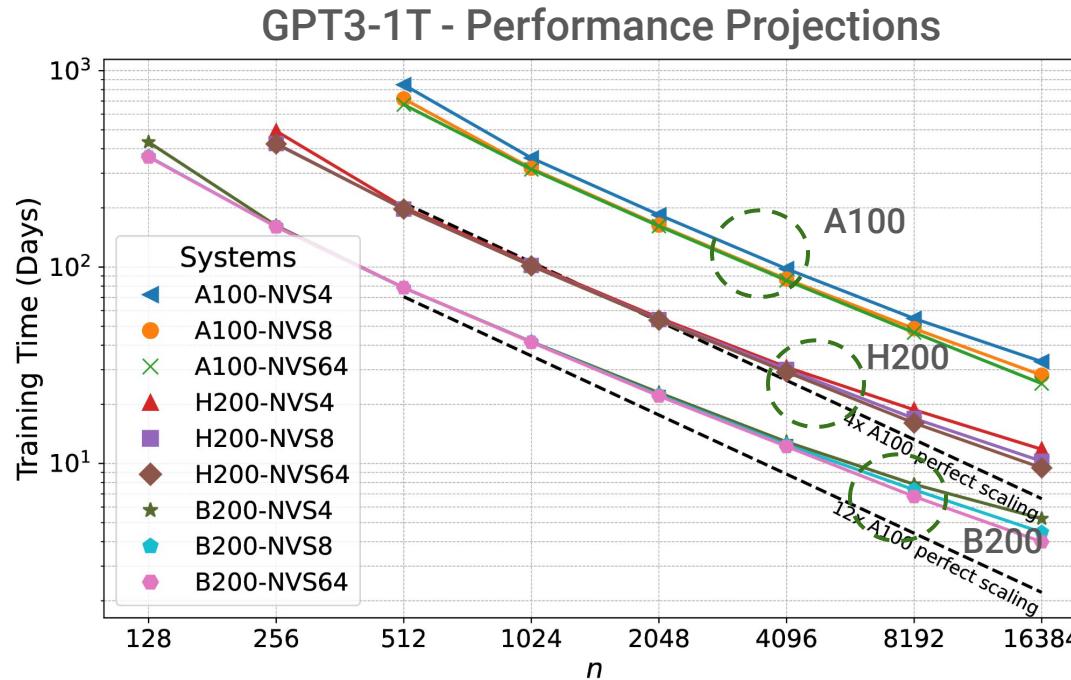


NVSWITCH

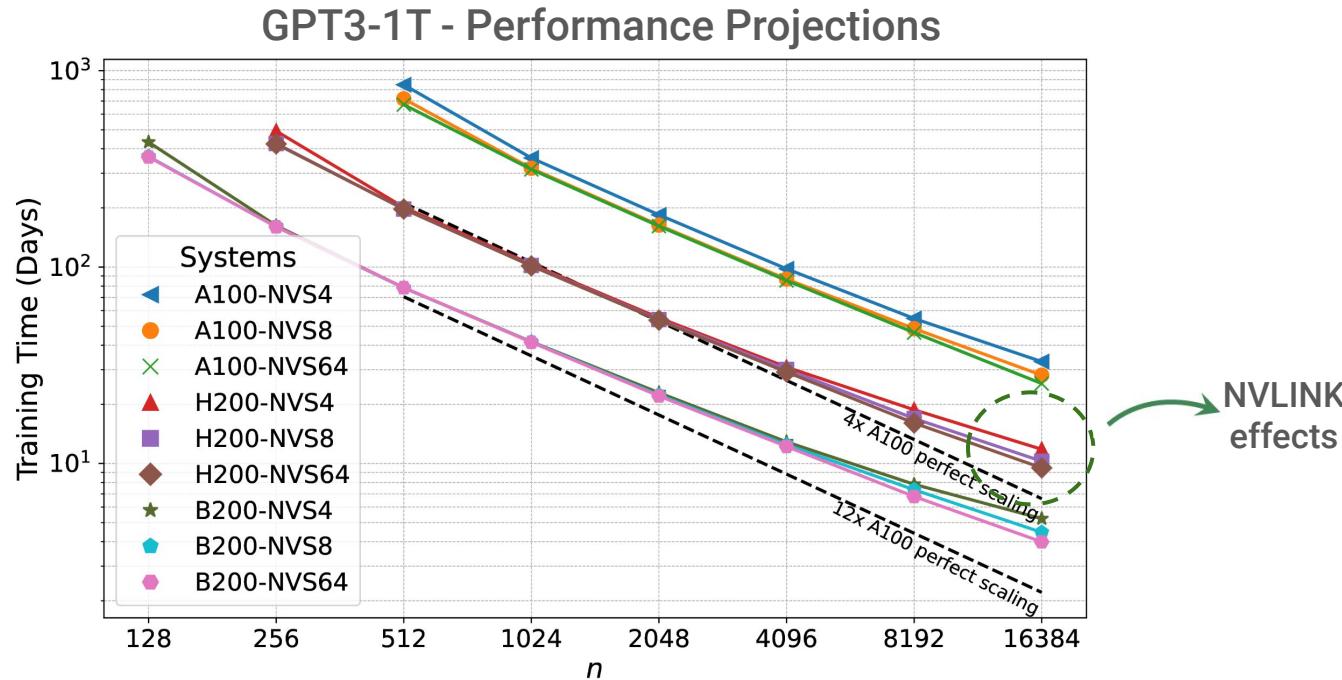
# Provides a High-level View of Scaling Behavior



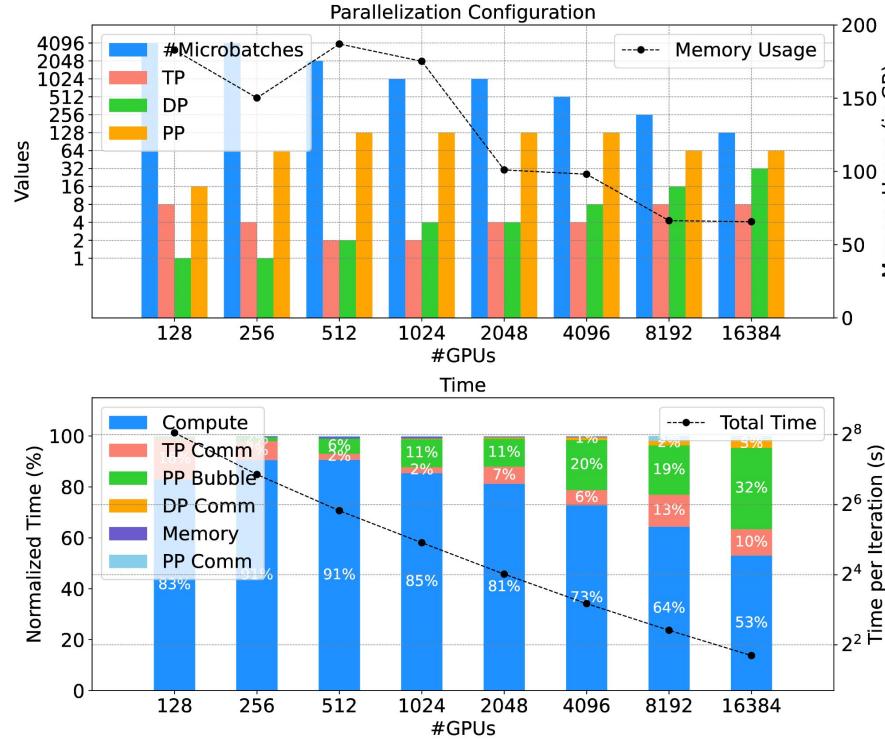
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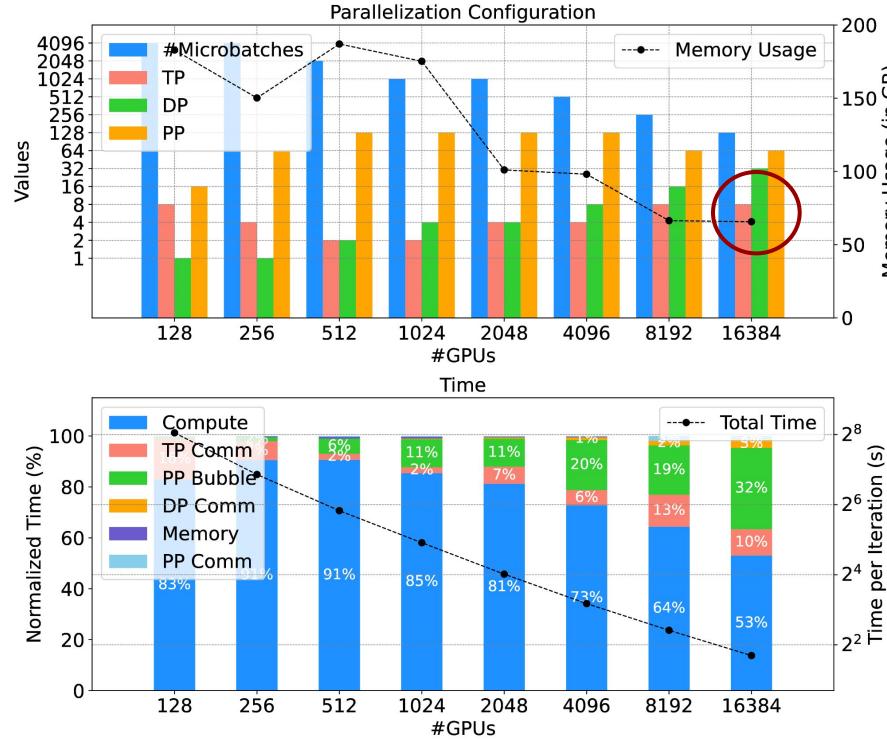


# Expose Bottlenecks and Optimal Parallelism

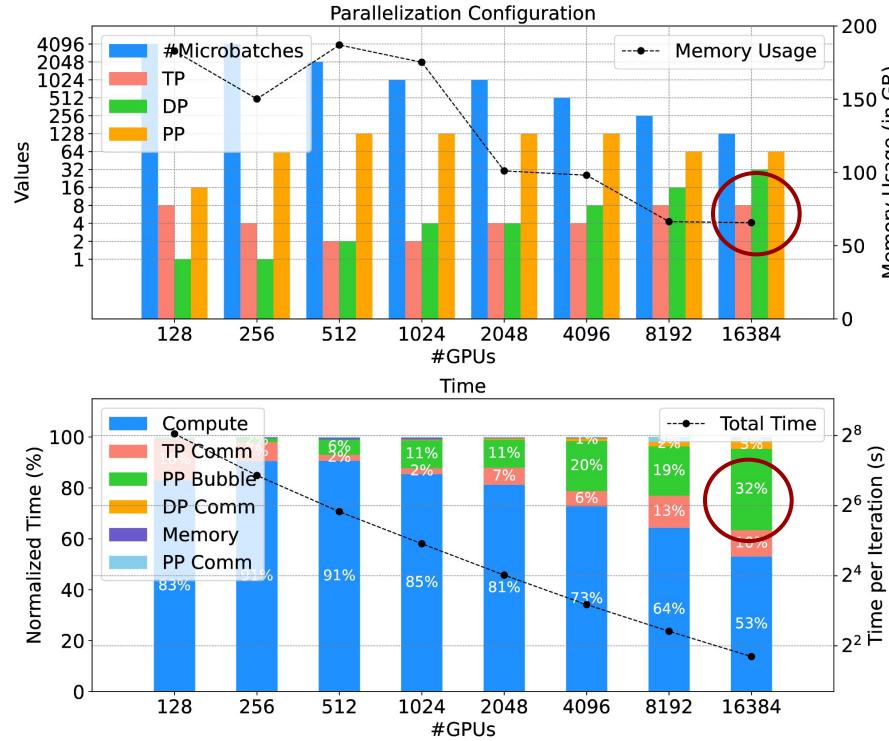


B200, NVS8

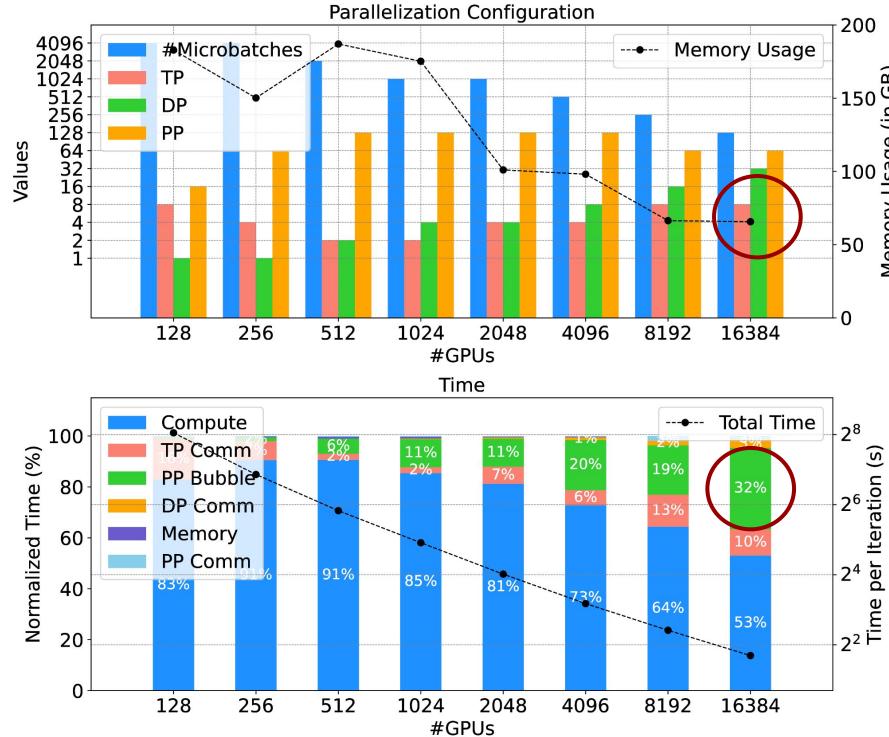
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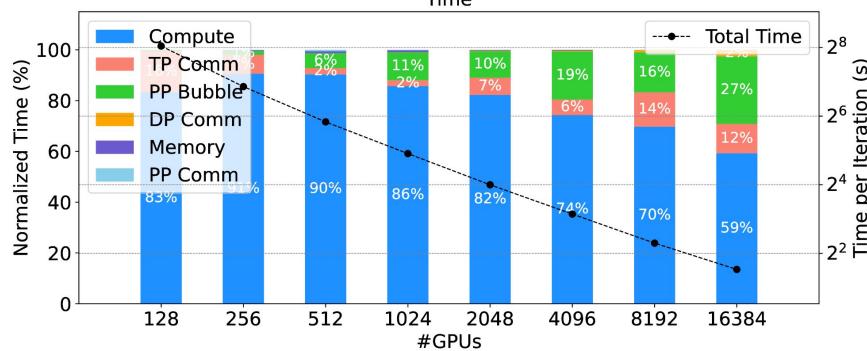
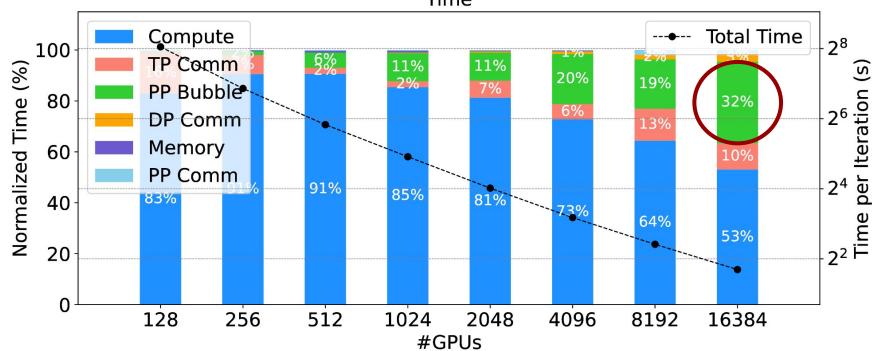
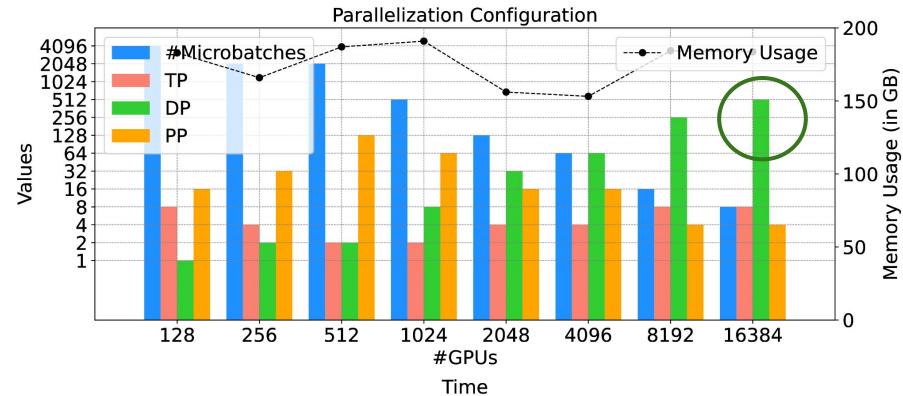
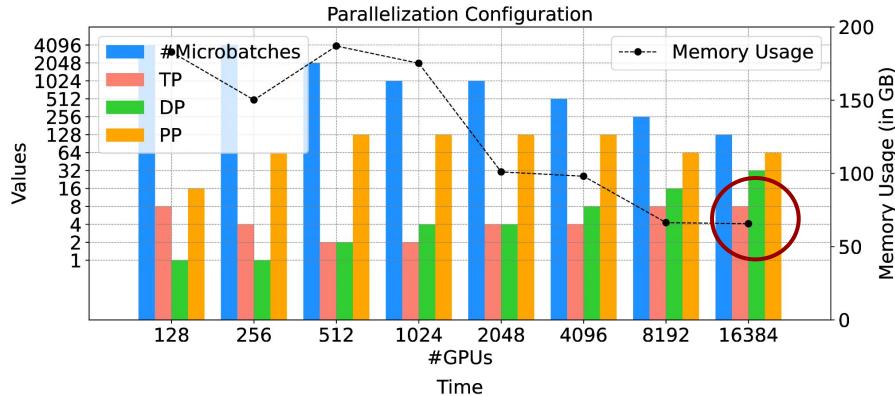
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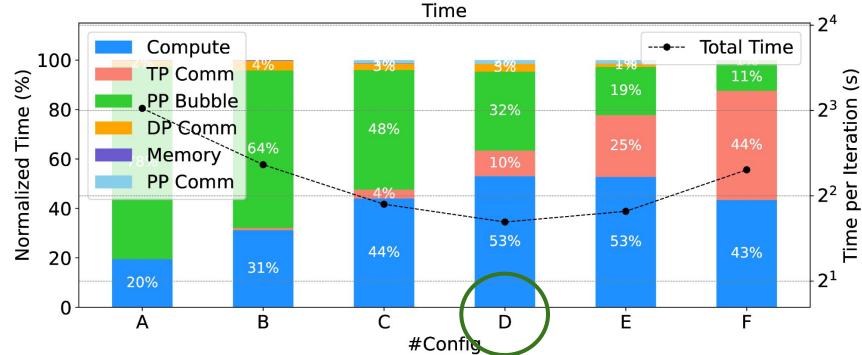
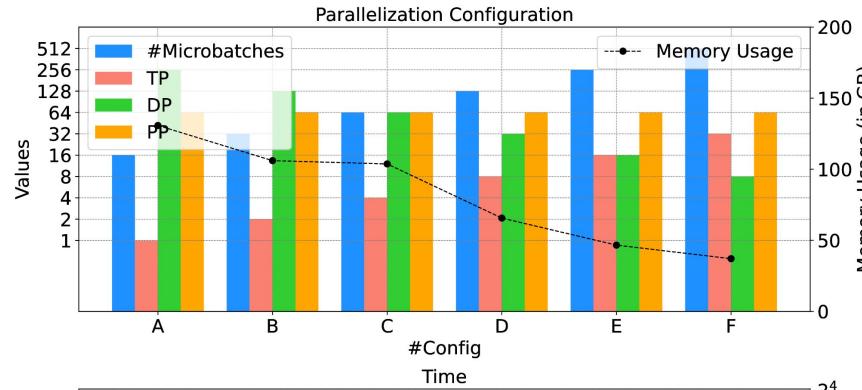


# Larger NVLINK Favor High Data Parallelism



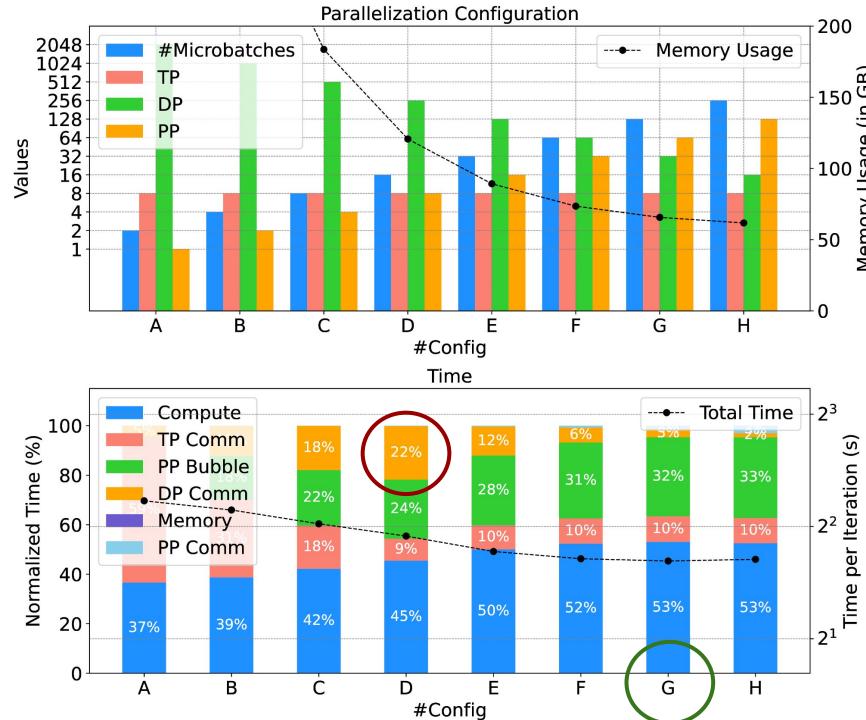
NVS 64

# Probe the Model to Get Deeper Insights

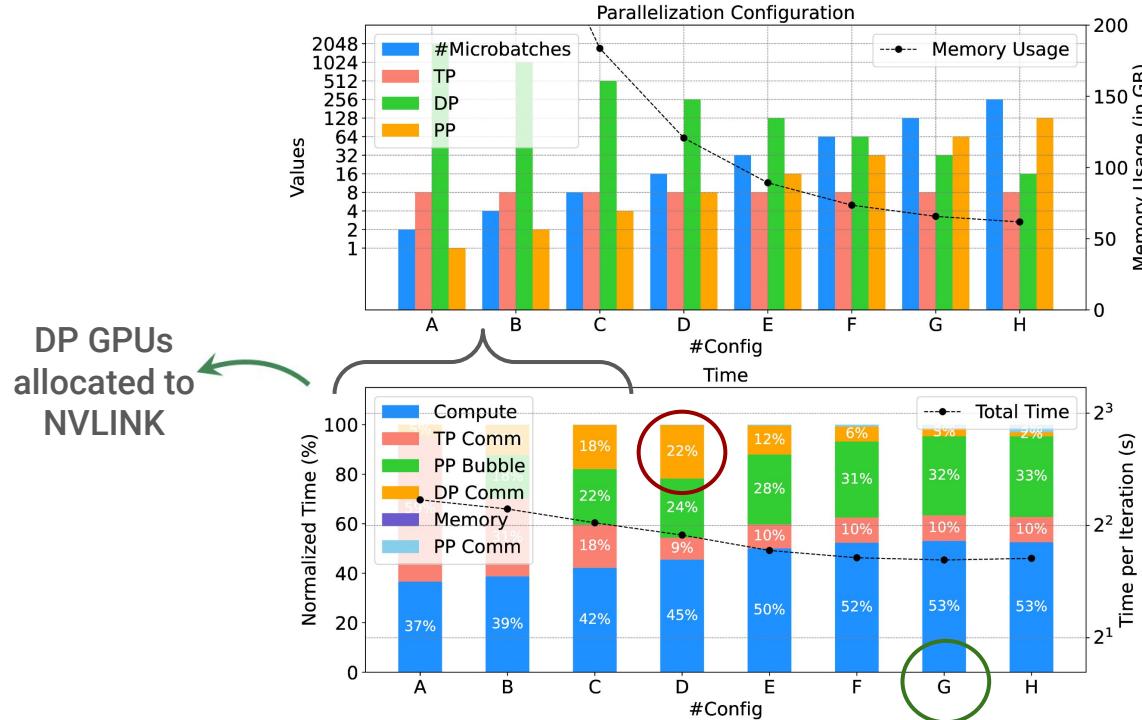


Fix #GPUs and look around the optimal configuration

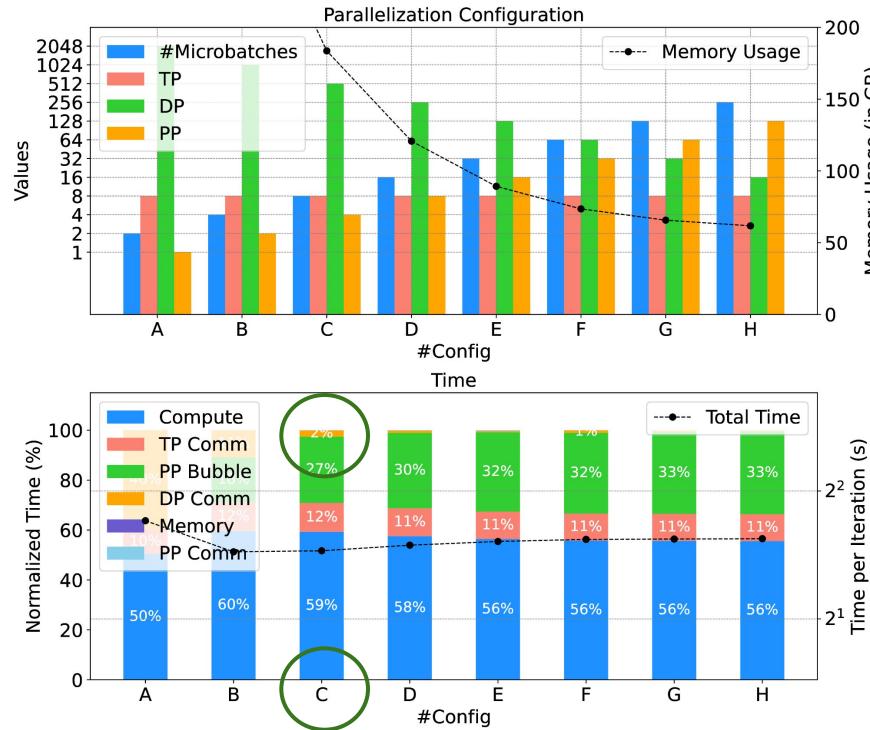
# Placement of GPUs Matters



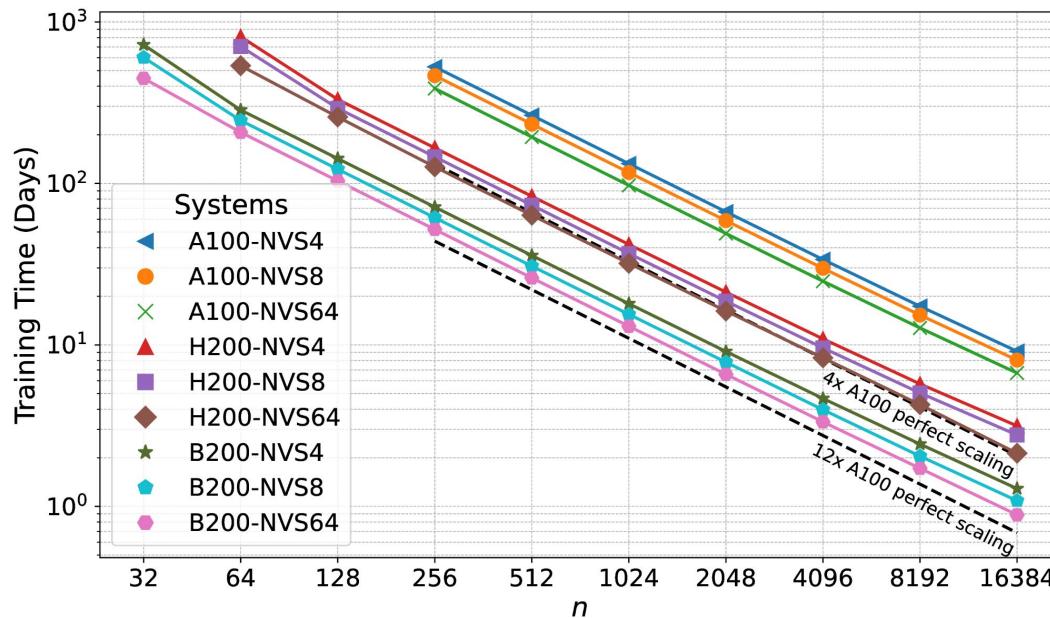
# Placement of GPUs Matters



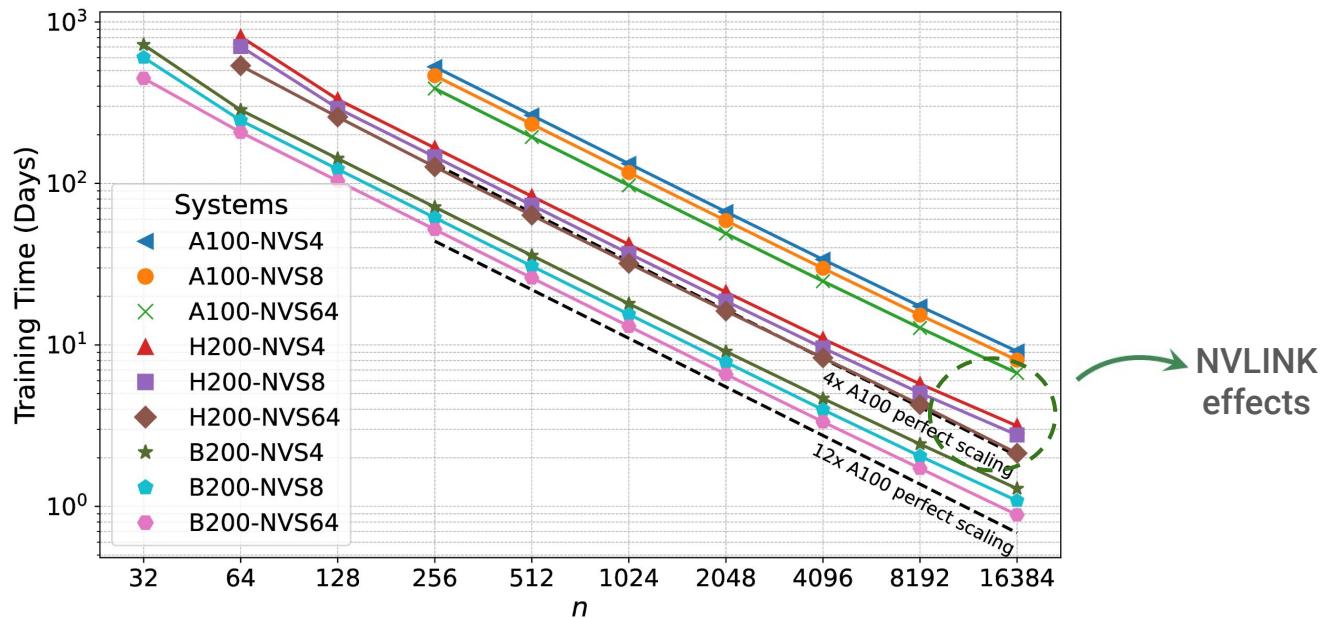
# Placement of GPUs Matters for Large NVLINK



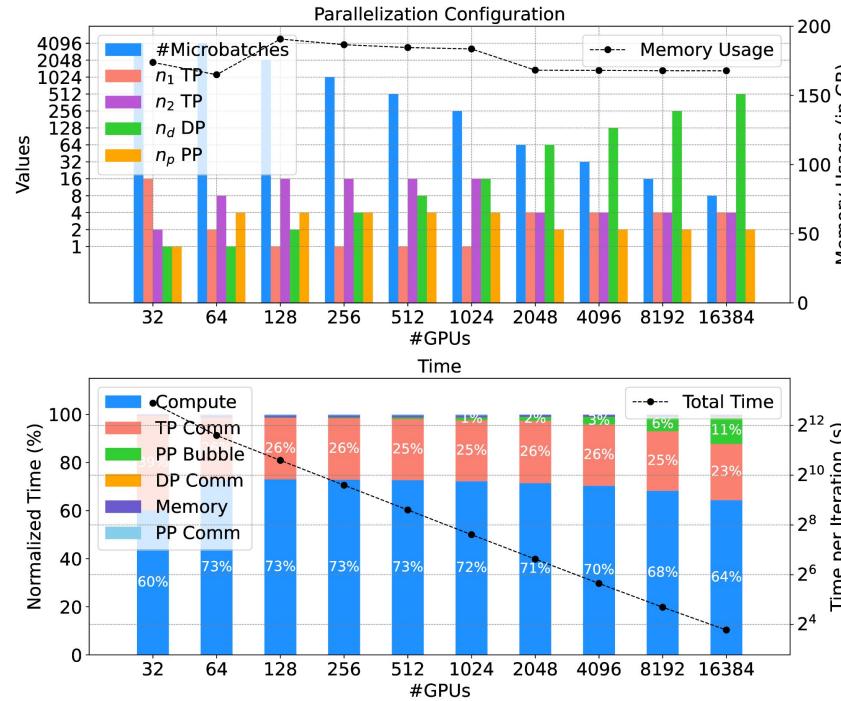
# Transformer in Science is More Sensitive to the Network



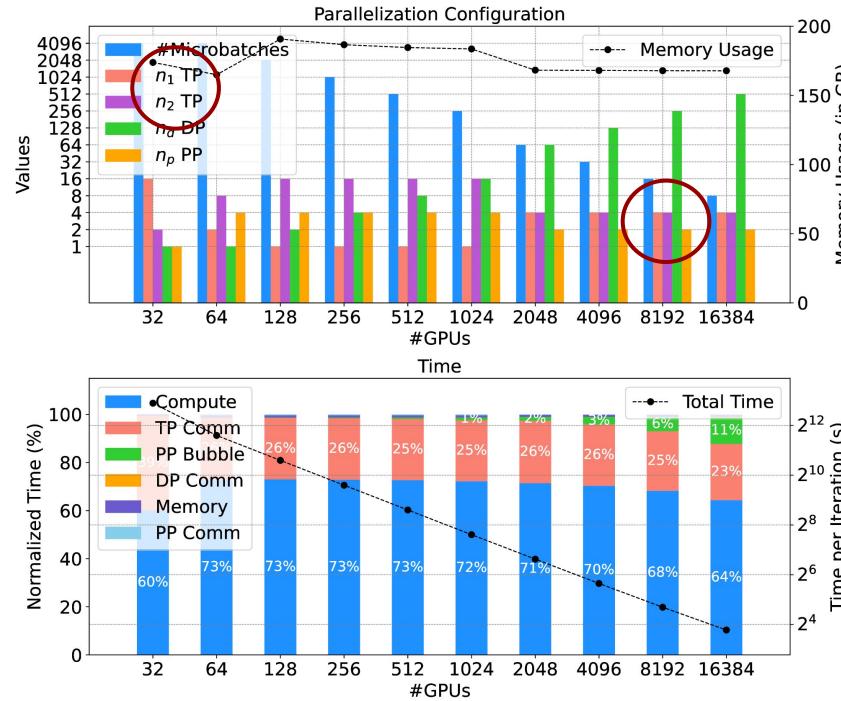
# Transformer in Science is More Sensitive to the Network



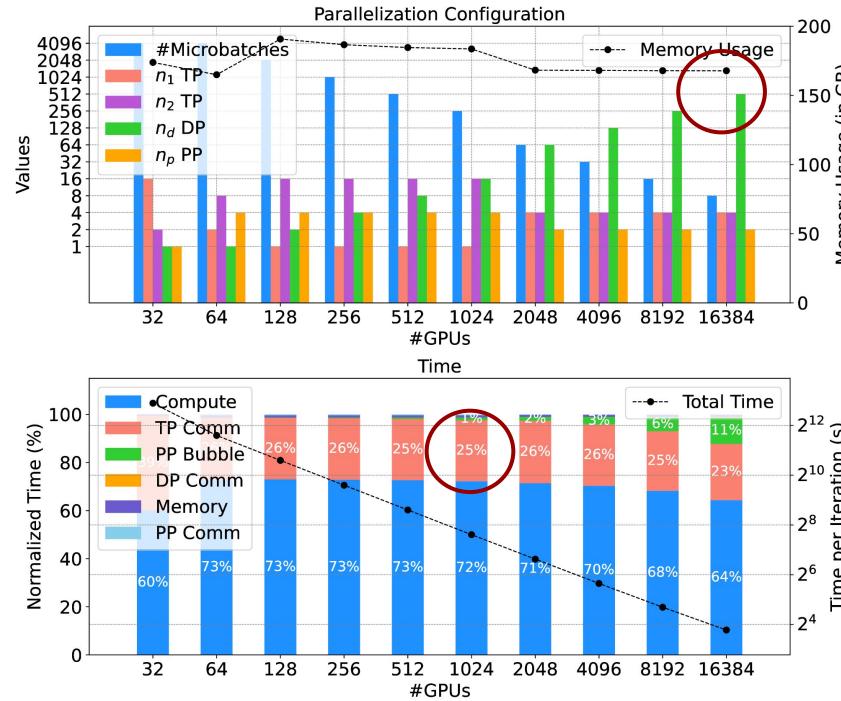
# Long Contexts Need 4D Parallelism



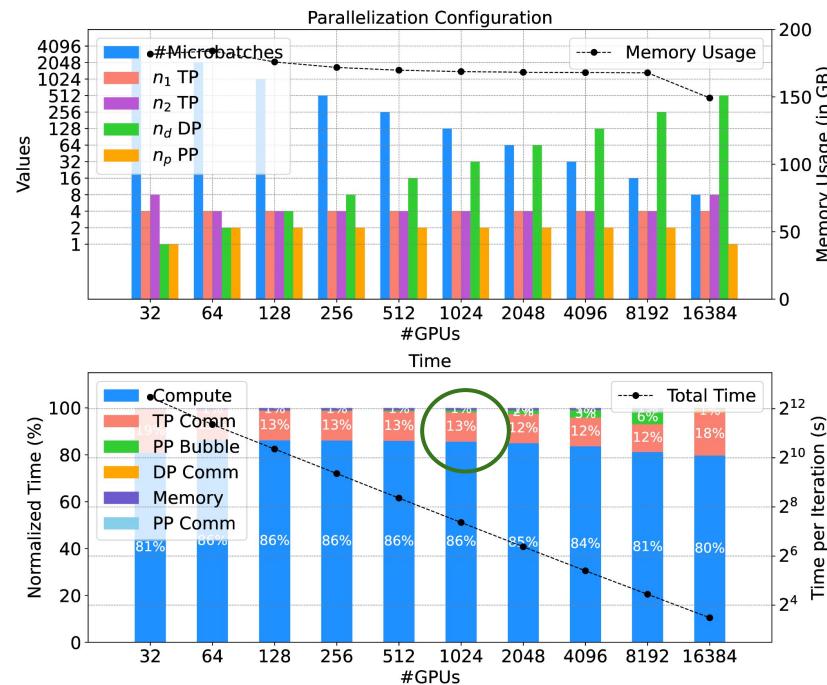
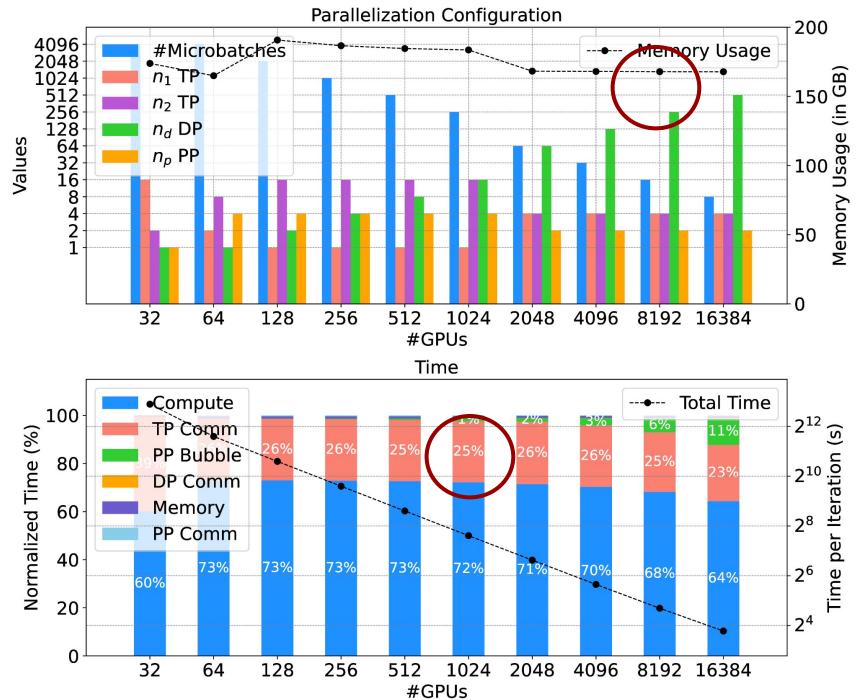
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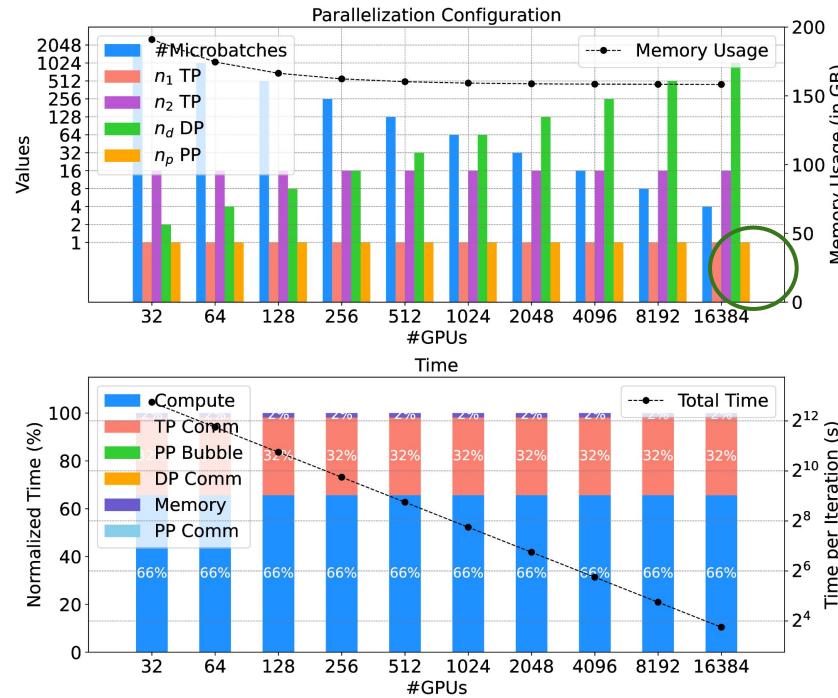
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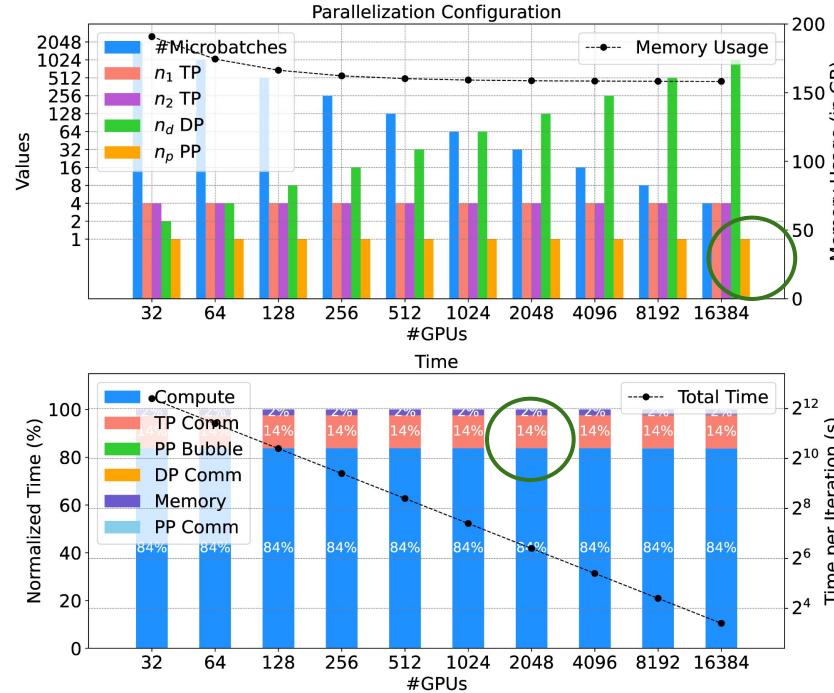
# Larger NVLINK Drops Communication Costs



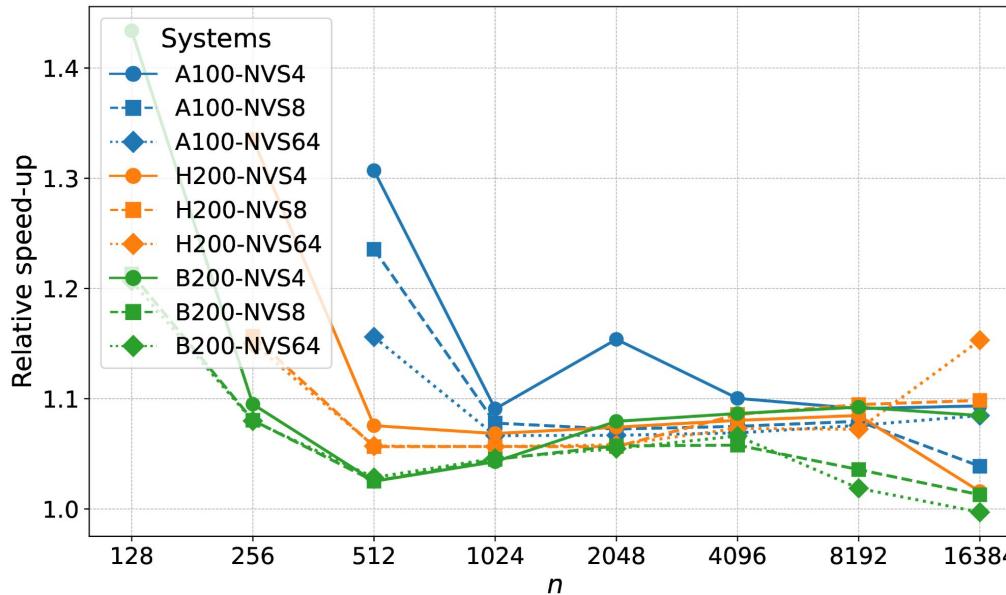
# SUMMA Presents More Uniform Strategies



# Larger NVLINK Drops Communication Costs

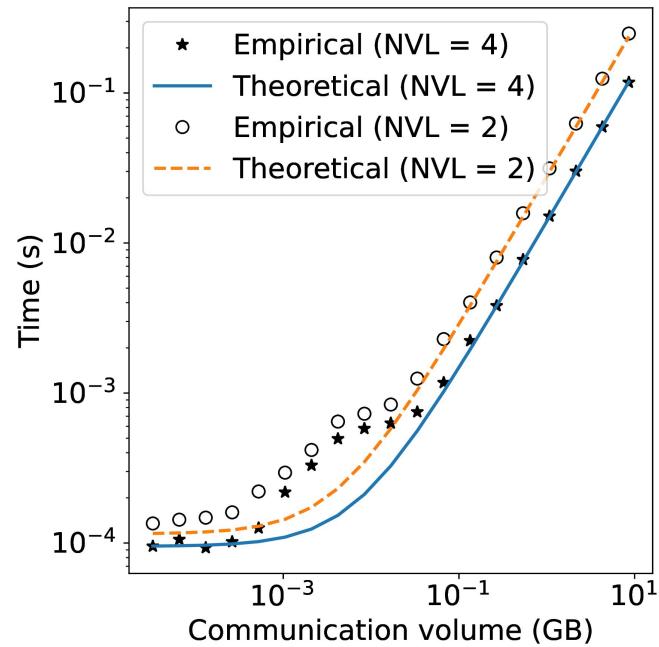


# 4D Parallelism Increases Throughput Compared to 3D



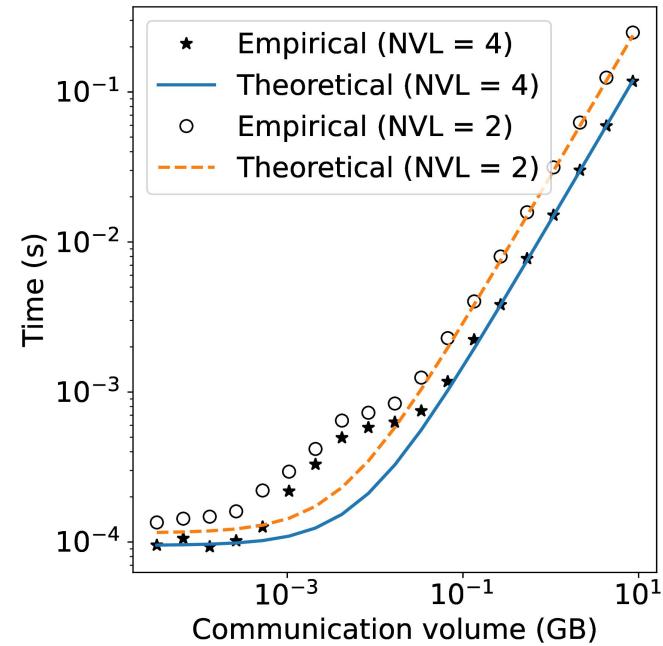
# Validation with Megatron-LM

- Validated time models on the Perlmutter supercomputer
  - 4-way NVLINK domain



# Validation with Megatron-LM

- Validated time models on the Perlmutter supercomputer
  - 4-way NVLINK domain
- Validated throughput numbers on 512 GPUs
  - GPT3 (175B) and ViT (32K)
- ~10% errors in iteration time
  - Controlled GPU placement with Megatron flags
  - Overlap flags, *FlashAttention*, other optimizations in sync with model
  - Validated sub-optimal configurations as well
- SUMMA validation challenging
  - ColossalAI in future work



# Some Key Takeaways

- Placement of GPUs on high-bandwidth domain affects the optimal parallelism
  - Software codebases to be flexible to this
- LLMs benefit from large NVLINKs at pre-training scales
  - Fine-tuning scales can leverage other parallelization strategies to be less sensitive
  - HBM capacity is underutilized for the largest scales
- Science Transformers benefit uniformly from NVLINK due to memory pressure
  - Demand 4D parallelism (data + pipeline + 2D tensor + optimizer sharding)
  - Capacity is more critical (High capacity, low bandwidth alternatives?)
- 4D parallelism is useful for moderate speedups

# Thank You!

