Filament Recycling and Sustained Contractile Flows in an Actomyosin Cortex

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Abstract

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Author Summary

In this paper, we develop and analyze a minimal model for 2D active networks based on the cortical cytoskeleton of eukaryotic embryos. Our model introduces a drag-like slip between cross-linked filaments as means to dissipate stored stress, generating a macroscopic effective viscosity. We further introduce an active friction to active stress from microscopic properties. We generate computational simulations based on the model, and demonstrate that active stress is sufficient to drive network contraction only temporarily. By introducing filament recycling, we are able to set up steady state flow profiles such as those found in the cortex of developing embryos and migrating cells. The model is used to calculate phenomenological constants measured in prior experiments. Our analysis sheds insight on potential microscopic control parameters governing broad qualitative differences in 2D active networks. We make our model freely accessible and our methodology transparent to enable other researchers to clearly understand our modeling framework and to build upon our findings.

Introduction

Cortical flow is a fundamental and ubiquitous form of cellular deformation that underlies cell polarization, cell division, cell crawling and multicellular tissue morphogenesis [Bray and White, 1988, Hird and White, 1993]. These flows arise within the actomyosin cortex, a thin layer of cross-linked actin filaments and myosin motors that lies just beneath the plasma membrane [Salbreux et al., 2012]. The active forces that drive cortical flows are thought to be generated by myosin motors pulling against individual actin filaments [Munro et al., 2004]. These forces must be integrated within cross-linked networks to build macroscopic contractile stress. At the same time, cross-linked networks resist deformation and this resistance must be dissipated by network remodeling to allow macroscopic network deformation and flow. How force production and dissipation depend on motor activity, network architecture and remodeling remains poorly understood.

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Current models for cortical flow rely on coarse-grained descriptions of actomyosin networks as active fluids, whose motions are driven by gradients of active contractile stress and opposed by an effectively viscous resistance [Mayer et al., 2010]. In these models, gradients of active stress are assumed to reflect spatial variation in motor activity and viscous resistance is assumed to reflect the internal dissipation of elastic resistance due to local remodeling of filaments and/or crosslinks [Bois et al., 2011]. A key virtue of these models is that their behavior is governed by a few parameters (active stress and effective viscosity). By coupling an active fluid description to simple kinetic models for network assembly and disassembly and making active stress and effective viscosity depend on e.g network density and turnover rates, it is possible to capture phenomenological descriptions of cortical flow. Models based on this active fluids description can successfully reproduce spatiotemporal dynamics of cortical flow observed during polarization [Mayer et al., 2010], cell division [Turlier et al., 2014, Salbreux et al., 2009], cell motility [Keren et al., 2009, Marchetti et al., 2013] and tissue morphogenesis [Heisenberg and Bellaïche, 2013].

However, to understand how cells exert physiological control over cortical deformation and flow, or to build and tune networks with desired properties in vitro, it is essential to connect this coarse-grained description to the microscopic origins of force generation and dissipation within cross-linked actomyosin networks. Both active stress and effective viscosity depend sensitively on microscopic parameters including densities of filaments, motors and cross-links, force-dependent motor/filament interactions, cross-link dynamics and network turnover rates. Thus a key challenge is to understand how tuning these microscopic parameters controls the dynamic interplay between active force generation and passive relaxation to control macroscopic dynamics of cortical flow.

Studies in living cells have documented fluid-like stress relaxation on timescales of 10-100s of seconds [Mayer et al., 2010, Hird and White, 1993, Bray and White, 1988, Hochmuth, 2000, Evans and Yeung, 1989, Bausch et al., 1998]. These modes of stress relaxation are thought to arise both from the transient binding/unbinding of individual cross-links and from the turnover (assembly/disassembly) of actin filaments (ref). Studies of cross-linked and/or bundled actin networks in vitro suggest that cross-link unbinding may be sufficient to support viscous relaxation (creep) on very long timescales [Wachsstock et al., 1994, Lieleg et al., 2008, Lieleg et al., 2009, Yao et al., 2011, Liu et al., 2007, but is unlikely to explain the rapid large scale cortical deformation and flow observed in living cells. suggest that rapid actin turnover must play a significant role as well. Indeed, photokinetic and single molecule imaging studies studies reveal rapid turnover of cortical actin filaments in living cells on timescales of 10-100 seconds [Robin et al., 2014]. Previous theoretical models have explored the dependence of stress relaxation on cross-link binding and unbinding analytically [Broedersz et al., 2010, Müller et al., 2014 and others have explicitly modeled reversible cross-linking in combination with complex mechanics of filament bundles [Kim et al., 2011, Lieleg et al., 2009, Lieleg and Bausch, 2007. However, until very recently [Mak et al., 2016] very little attention has been paid to actin turnover as mechanism of stress relaxation.

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Recent work has also begun to reveal insights into mechanisms that govern active stress generation in disordered actomyosin networks. In vitro studies have confirmed that local interactions among actin filaments and myosin motors are sufficient to drive macroscopic contraction of disordered networks [Murrell and Gardel, 2012]. Theoretical studies suggest that asymmetrical compliance of actin filaments (stiffer under extension than compression) and spatial differences (dispersion) in motor activity are sufficient conditions for contraction in one [Lenz et al., 2012] and two [Lenz, 2014] dimensional networks, although other routes to contractility may also exist [Lenz, 2014]. Further work has explored how modulation of network architecture, crosslink dynamics and

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motor density, activity and assembly state can shape rates and patterns of network deformation [Köhler and Bausch, 2012, Alvarado et al., 2013, Banerjee and Marchetti, 2011] or network rheology [Liverpool et al., 2009, Koenderink et al., 2009].

Significantly, in vitro models for disordered actomyosin networks have used stable actin filaments, and these networks support only transient contraction, either because of network collapse (ref), or buildup of elastic resistance (ref?), or because network rearrangements (polarity sorting) dissipate the potential to generate contractile force (ref). This suggest that continuous turnover of actin filaments may play a key role in allowing sustained deformation and flow (refs). Recent theoretical and modeling studies have begun to explore how this could work [Hiraiwa and Salbreux, 2015, Mak et al., 2016, Zumdieck et al., 2007], and to explore dynamic behaviors that can emerge in contractile material with turnover [Dierkes et al., 2014]. However, there is much to learn about how the buildup and maintenance of contractile force during continuous deformation and flow depends local interplay of network architecture, motor activity and filament turnover.

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The goal of this work was to build a computational bridge between the microscopic description of cross-linked actomyosin networks and the coarse grained macroscopic description of an active fluid. We sought to capture the essential microscope features (dynamic cross-links, active motors and semi flexible actin filaments with asymmetric compliance and continuous filament recycling), but in a way that is sufficiently simple to allow systematic exploration of how parameters that govern network deformation and flow in an active fluid theory depend on microscopic parameters. To this end, we introduce several coarse-grained approximations into our representation of filament networks. First, we represent semi-flexible actin filaments as chains of simple springs with asymmetric compliance (stronger in extension than compression). Second, we replace dynamic binding/unbinding of elastic cross-links with a coarse-grained representation in terms of molecular friction [Vanossi et al., 2013, Spruijt et al., 2010, Filippov et al., 2004, such that filaments can slide past each other against a constant fictional resistance. Third, we used a similar scheme to introduce active motors at filament crossover points with a simple linear force/velocity relationship, and we introduce? dispersion? of motor activity by making only a subset of filament overlaps active [Banerjee et al., 2011]. Finally, we model filament turnover by regularly reseting a subset of filaments to a new unstrained position. Importantly, these simplification allows us to extend our single polymer models to dynamical systems of larger network models for direct comparison between theory and modeling results. This level of coarse graining will therefore make it easier to understand classes of behavior for varying compositions of cross-linked filament networks. In addition, it allows us to compute a new class of numerical simulations efficiently, which gives us concrete predictions for behaviors in widely different networks with measurable dependencies on molecular details.

Models

We choose to focus our attention on 2D networks both for their tractability as well as their relevance in the quasi-2D cytoskeletal cortex of many eukaryotic cells [Mayer et al., 2010]. In addition, recent developments in 2D in vitro systems [Murrell and Gardel, 2012, Sanchez et al., 2012], make 2D disordered models all the more interesting as a renewed focus of study. In the rest of this section, we underline the key points necessary for understanding our modeling framework and the key assumptions we have made in generating our equations of motion for the system.

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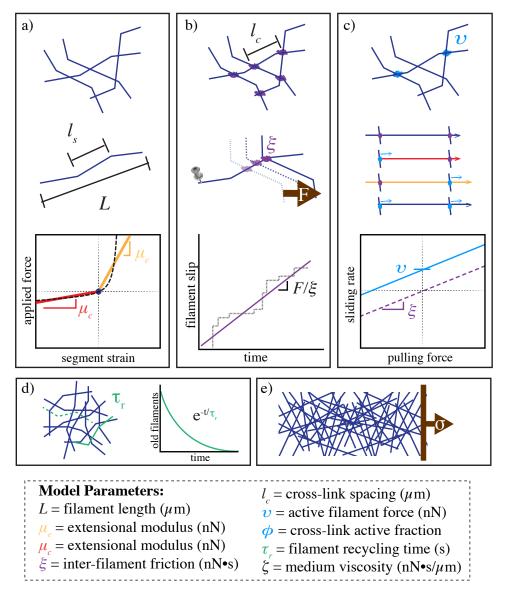


Figure 1. Schematic of modeling framework. a) Filaments are represented as connected chains of spring-like segments with asymmetric compliance.segments have a smaller spring constant for compression than for extension. b) Cross-linking is represented as filament coupling by an effective drag, such that their relative motion is proportional to any applied force. c) Motor activity manifests as a basal sliding rate even in the absence of an external force. d) Only a subset of filament cross-links are active, resulting in differential force exertion along the filament. e) Filaments are turned over at a constant rate, leading to a refreshing in the strain state of all filaments after a characteristic timescale.

Asymmetric Filament Compliance

We model individual filaments as chains of springs with relaxed length l_s . Filaments can therefore be represented as a sequence of nodes with positions $\mathbf{x_i}$ and nearest neighbor force interactions, $\mathbf{F_i^{\mu}}$, of the form

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$$|F_i^{\mu}| = \mu \cdot \frac{|\mathbf{x_{i+1}} - \mathbf{x_i}| - l_s}{l_s} + \mu \cdot \frac{|\mathbf{x_{i-1}} - \mathbf{x_i}| - l_s}{l_s}$$
(1)

where, μ represents an extensional modulus of a filament. Here, we take the modulus, μ , to have a different value depending on whether $|\mathbf{x_{i-1}} - \mathbf{x_i}| - l_s$ is greater or less than 0. This moduli is a composite quantity related to both filament and cross-linker compliance in a manner similar to a proposed effective medium theory [Broedersz et al., 2009]. In the limit of highly rigid cross-links and flexible filaments, our model reduces to the pure semi-flexible filament models of [Head et al., 2003, Wilhelm and Frey, 2003]. In the opposite regime of nearly rigid filaments and highly flexible cross links, our method is still largely similar to the model of [Broedersz et al., 2009] in small strain regimes before any nonlinear cross link stiffening. However, in departure from those models, the magnitude of the force on interior cross-links in our model is still the same as those on the exterior. This is a simplification of the varying levels of strain that would actually be present in these cross-linkers as addressed in [Broedersz et al., 2009], but we choose to ignore the slight variation in favor of an approximated, global mean approach.

Drag-like Coupling Between Overlapping Filaments

Cross-link binding and unbinding is an important element of the overall stress relaxation of a network. In contrast to previous models, we allow relaxation of the network's stored stress by letting the attachment points slip. We do this by replacing an elastic interaction between pairs of points along filament segments with a drag-like coupling between segments.

$$\mathbf{F}_{\mathbf{i}}^{\xi} = \xi \cdot \int_{s_{i-1}}^{s_{i+1}} ds \frac{l_s - |s - s_i|}{l_s} \left(\mathbf{v_i} - \mathbf{v_j} \right) p_{ij}(s)$$
 (2)

Where $p_{ij}(s)$ represents the locational distribution of cross-link points (equal to 1 at locations of cross-links and 0 elsewhere) and $\mathbf{v_i}$ and $\mathbf{v_j}$ represent the the velocities of the *i*th and *j*th filament segment. This model assumes a linear relation between applied force and the velocity difference between attached segments. This drag-like coupling has been shown to be an adequate approximation in the case of ionic cross-linking of actin [Ward et al., 2015, Chandran and Mofrad, 2010], and can be found in the theoretical basis of force-velocity curves for myosin bound filaments [Banerjee et al., 2011]. Although non-linearities can arise through force dependent detachment kinetics and/or non-linear force extension of cross-links, we assume that inhomogeneities from non-linear effects are of second or higher order. With this assumption, the motion for the entire network is governed by a dynamical equation of the form

$$L\zeta \mathbf{v_i} + \mathbf{F_i^{\xi}} = \mathbf{F_i^{\mu}} \tag{3}$$

Here, the first term in the integral is the filament's intrinsic drag through its embedding fluid, ζ , while the second comes from the drag-like coupling between filaments, ξ .

Active Coupling for Motor Driven Filament Interactions

To add motor activity we select a subset of cross-linked points and impart an additional force of magnitude v directed in the orientations of the individual filaments, $\mathbf{u_i}$. This leads to a modification of the equation of motion to

$$\mathbf{F}_{\mathbf{i}}^{\upsilon} = \hat{\mathbf{u}}_{\mathbf{i}} \cdot \upsilon \int ds \sum_{j} \frac{l_{s} - |s - s_{i}|}{l_{s}} p_{ij} q_{ij}$$

$$\tag{4}$$

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In this formulation, only at the subset of points where $p_{ij} = 1$ and $q_{ij} = 1$ will there be a force imparted. In our simulations we let q_{ij} be selected randomly such that $\bar{q} = \phi$, where \bar{q} indicates the mean of q.

$$L\zeta \mathbf{v_i} + \mathbf{F_i^{\xi}} = \mathbf{F_i^{\mu}} + \mathbf{F_i^{\upsilon}}$$
 (5)

2D Network Formation

We follow a mikado model approach by initializing a minimal network of connected unstressed linear filaments in a rectangular 2D domain. We generate 2D networks of these semi-flexible filaments by laying down straight lines of length, L, with random position and orientation. We then assume that some fixed fraction of overlapping filaments become cross-linked (defined in) at their point of overlap.

Although real cytoskeletal networks may form with non-negligible anisotropy, we focus on isotropically initialized networks for simplicity. We define the density using the average distance between cross-links along a filament, l_c . A simple geometrical argument can then be used to derive the number of filaments filling a domain as a function of L and l_c [Head et al., 2003]. Here, we use the approximation that the number of filaments needed to tile a rectangular domain of size $W \times H$ is $2WH/Ll_c$, and that the length density is therefore $1/l_c$. In the absence of cross-link slip, we expect the network to form a connected solid with a well defined elastic modulus [Head et al., 2003, Wilhelm and Frey, 2003].

System of Equations for Applied Stress

We model our full network as a coupled system of differential equations satisfying 5. Although the general mechanical response of this system may be very complex, we focus our attention on low frequency deformations and the steady-state creep response of the system to an applied stress. To do this we introduce a fixed stress, σ along the midline of our domain. This stress points in the direction, $\hat{\mathbf{x}}$, producing extensional stress.

Finally, we add a 0 velocity constraint at the far edges of our domain of interest. We assume that our network is in the "dry," low Reynold's number limit, where inertial effects are so small that we can equate our total force to 0. Therefore, we have a dynamical system of wormlike chain filaments satisfying

$$L\zeta \mathbf{v_i} + \mathbf{F_i^{\xi}}(\mathbf{v_i}) = \mathbf{F_i^{\mu}}(\mathbf{x_i}) + \mathbf{F_i^{\upsilon}}(\mathbf{x_i}) + \sigma \hat{\mathbf{u}}(\mathbf{x_i})$$
(6)

subject to constraints such that $\mathbf{v_i}(\mathbf{x})$ is 0 with x=0. This results in an implicit differential equation for filament segments which can be discretized and integrated in time to produce a solution for the motion of the system.

Filament Recycling as a model for rapid filament turnover

To simplify the complex biochemical changes that can give rise to actin filament polymerization and depolymerization, we chose to use simple filament appearance and disappearance as a lowest order model of filament recycling. In this sense the average lifetime of a filament between it's appearance and disappearance would be τ_r . In order to do this without causing an unnecessary bias in the results, at a regularized interval $\tau_s < 0.01 \cdot \tau_r$, we selected τ_s/τ_r filaments, reset their extension or compression to 0, and relocated them to a random position and orientation. This has the effect of creating an approximately exponential decay in the number of old filaments over time.

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Computational Simulation Method

We tested our analytical conclusions on a computational model. More technical details of the model can be found in the Appendix, but we summarize the main modeling points here.

We discretize the filaments such that the equations of motion becomes a coupled system of equations for the velocities of filament endpoints, \mathbf{x} . The drag-like force between overlapping filaments results in a coupling of the velocities of endpoints.

$$\mathbf{A} \cdot \dot{\mathbf{x}} = \mathbf{f}(\mathbf{x}) \tag{7}$$

where **A** represents a coupling matrix between endpoints of filaments that overlap, and $\mathbf{f}(\mathbf{x})$ is the spring force between pairs of filament segment endpoints. We can then numerically integrate this system of equations to find the time evolution of the positions of all filament endpoints.

We generate a network by laying down filaments with random position and orientation within a domain of size D_x by D_y with periodic boundaries in the y-dimension. The external stress (shear or extensional/compressional) is applied to all filament endpoints falling within a fixed x-distance from the center of the domain. Finally, filament endpoints falling within a fixed x-distance from the edges of the domain are constrained to be nonmoving. All filament interactions, force fields, and constraints are smoothed over small regions such that the equations will contain no sharp discontinuities.

The nominal units for length, force, and time are μm , nN, and s, respectively. We explored parameter space around an estimate of biologically relevant parameter values, given in Table 1.

Table 1. Simulation Parameter Values

parameter	symbol	physiological estimate
extensional modulus	μ_e	10nN
compressional modulus	μ_c	0.1nN
cross-link drag coefficient	ξ	unknown
medium drag coefficient	ζ	$0.0005 \frac{nNs}{\mu m^2}$
filament length	L	$5\mu m$
cross-link spacing	l_c	$0.5 \mu m$
domain size	$D_x \times D_y$	$20 \times 50 \mu m$

Results and Discussion

We used our model to tease apart the complex interdependence of passive and active network properties on the patterning and rates of cortical flow. To begin, we addressed the effect of filament recycling on the deformation of a network without motor activity in the presence of a constant external force. After we had established the timescales of passive deformation, we approached the active case and made similar measurements of the timescales of internal stress buildup and dissipation. Finally, we were able to synthesize our understanding of the passive and active systems to analyze the behavior of a more complex situation of an actively flowing network.

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Filament recycling prevents cortical tearing and modulates the viscous stress relaxation of passive filament networks

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Networks with passive cross-links and no filament turnover undergo three stages of deformation in response to an extensional force. We first probed the network's passive response by imposing an external force on our simulated network in the absence of recycling. As shown in Figure 2.a, by applying a force at the boundary of a patch of network, we induced a rightward deformation or strain, γ , equal to the change in patch size divided by the original size, ($\gamma = \Delta x/x_0$). The deformation occurred in three phases corresponding to the three example networks in Figure 2.a. On short timescales the networked quickly responded by elastically approaching a fixed strain γ_0 , similar to that predicted by [Head et al., 2003]. On longer timescales, we found that the network continued deforming more slowly as filaments were able to slip past each other. Finally, as the network continued to dilate viscously, the connectivity of the network decreased. Eventually connected patches became isolated and the network teared, resulting in the highly heterogeneous network structure shown in the t=440 example of Figure 2.a.

We next analyzed the force and velocity data of the network at individual time points to determine what kind of deformation the material was undergoing. As shown by the data in Figure 2.b corresponding to the simulation at time t=88s, during this stage, the stress profile (blue) is nearly constant throughout the material while the velocity profile (orange) is linear in space. These are two indications that a purely viscous description is adequate for this stage of deformation. By measuring the mean material stress and strain rate (v_i/x_i) at every time point, we generated a measurement of the material strain through time as shown in Figure 2.c. From this measurement, we can identify phases of deformation outlined in Figure 2.a. It's clear that there are two phases in the stress and strain profile: one characterized by a rapid buildup of internal stress and strain, and one where the internal stress remains constant and the strain increases more slowly. We define the transition time between this fast, elastic response and the slower, viscous response as τ_c . For times longer than τ_c the material underwent a steady continuous straining at a nearly constant rate. This linear relationship between strain and time characterizes a material with an effective viscosity, η , given by the ratio of the applied stress to the strain rate (i.e $\sigma/\dot{\gamma}$). At very long times, this constant strain rate behavior begins to break down. As the network strains beyond 30% or so, network connectivity decreases, and the strain rate of the network begins to increase. This strain thinning behavior can be seen in the hockey-stick shape of the inset of Figure 2.c.

Network architecture sets the rate and timescales of deformation. To better understand the origins of the timescale of viscous behavior and the effective viscosity, we measured these features for a variety of network parameters and applied stresses. Across a wide swath of parameter space, the network was shown to be always capable of reaching a point of viscous deformation with a characteristic effective viscosity. By measuring the rate of deformation during the phase of constant strain rate, we could measure the effective viscosity and determining which network parameters were responsible for setting its value. From our observations, we were able to determine that the effective viscosity of a network was proportional to the friction coefficient of the individual cross-links, ξ , as well as the square of the number of cross-links on a given filament $(L/l_c-1)^2$. A simple theoretical derivation (See Supp.) allowed us to estimate a numerical constant of proportionality of $\pi/4$. As shown in Figure 3.a, the theoretical prediction agrees very well with the measured values form the simulation.

We were also interested in determining what sets the timescale of the transition from elastic to viscous behavior. In many simple viscoelastic materials, the ratio of the elastic modulus, G_0 , to the viscosity, η_c is a general indicator of the transition timescale from

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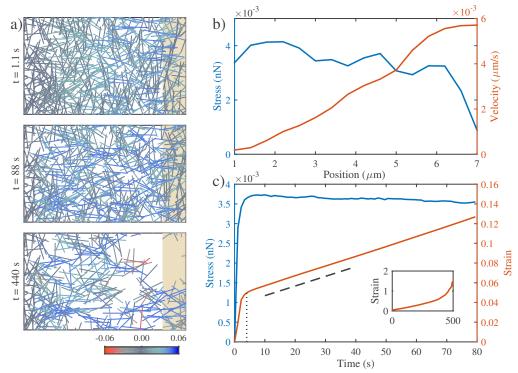


Figure 2. Networks with passive cross-links and no filament turnover undergo three stages of deformation in response to an extensional force. a) Three successive time points from a simulation of a $4 \times 10 \ \mu m$ network deforming under an applied extensional stress of $0.005 \ nN/\mu m$. In this and all subsequent figures, filaments are color-coded with respect state of stress (blue = tension, red = compression). Network parameters: $L = 1 \ \mu m$, $l_c = 0.3 \ \mu m$, $\xi = 100 \ nN \cdot s$. b) Mean filament stress and velocity profiles for the network in (a) at t=88s. Note that the stress is nearly constant and the velocity is nearly linear as predicted for a viscous fluid under extension. c) Plots of the mean stress and strain vs time for the simulation in (a), illustrating the three stages of deformation: (i) A fast initial phase accompanies rapid buildup of internal network stress; (ii) after a characteristic time τ_c s (indicated by vertical dotted line) the network deforms like a material with a constant effective viscosity, η_c , as indicated by the slope of the dashed line. (inset) At long times, the strain accelerates as the network undergoes strain thinning and eventually tears.

elastic to viscous behavior. Using the approximation of the equation for elastic modulus from [Head et al., 2003], $G_0 \approx \mu/l_c$, we predict a crossover time, $\tau_c \approx L^2 \xi/l_c \mu$. By measuring the time at which the strain rate became nearly constant we were able to determine an estimate of this time for a wide variety of simulation parameters as well. Indeed, as shown in Figure 3.b, our approximation is in good agreement with the observed transition time. This served as a good indication that our model was consistent with known models for viscoelastic semi flexible polymer networks.

Filament recycling rescues network tearing and modulates effective viscosity. We next explored how the deformation profile changed in the presence of filament recycling. To do so we ran a series of simulations with identical filament lengths and network densities and filament slip rates, while varying the rate at which filaments were reset to a refreshed, unstressed state. When the filament recycling

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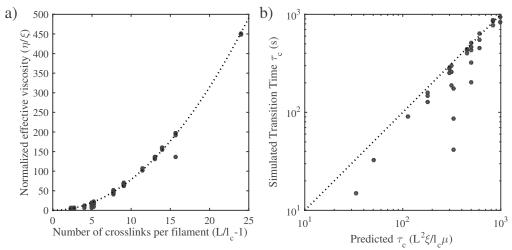


Figure 3. Network architecture sets the rate and timescales of deformation. a) The effective viscosity depends on the drag coefficient and the density of the network. Data points are the normalized effective viscosity from simulations (effective viscosity measured in fluid phase divided by the cross link friction coefficient) vs the number of cross links per filament (L/lc - 1). Dotted line indicates the relationship predicted by a simple theory, $\eta_c = \xi(L/l_c - 1)^2$ b) The transition to viscous behavior occurs at a characteristic time, τ_c , that is set by the ratio of the elastic modulus predicted in [Head et al., 2003] (i.e. $G_0 \approx \mu/l_c$) to the effective viscosity, η_c .

lifetime is reduced, we noticed a striking change in the long time behavior of the network strain. Instead of the network tearing at large strains and the viscosity decreasing over time, we found that the network remained more intact and the viscosity remained constant. As shown in Figure 4.a, for the network in the presence of recycling, $\tau_r=10$ s, we see less network thinning at $\gamma=0.4$ than we do in the recycling free $(\tau_r=\infty)$ case. In essence, material has been pulled to the right in the τ_∞ case, creating gaps in the network microstructure. In the presence of recycling, however, these gaps are filled in by recycled filaments as they appear. This leads to

As is also made clear by Figure 4.b, we found that the presence of recycling could dramatically affect the effective viscosity of the network at intermediate timescales as well. The strain rate for the $\tau_r=10$ s condition was much higher than the $\tau_r=\infty$ condition despite being subjected to the same external stress. In general, Figure 4.b show that lower recycling timescales led to lower viscosities. We believe that this is caused by increasing the networks ability to undergo the faster deformation rate of the elastic phase. By constantly reseting filaments to their unstrained state, the network is able to repeatedly extend filaments, thereby allowing the network to deform at a rate similar to its rapid deformation phase continuously. However, it was clear that there was some thresholding to this behavior since longer recycling lifetimes (e.g. $\tau_r=1000$ s in Figure 4.b), had almost no effect compared to the recycling free case $(\tau_r=\infty)$. As we discuss further in Figure 8, we found that this threshold timescale was approximately τ_c .

Taken together, our results for the passive network under extension suggest that the passive stress relaxation of our network model is modified strongly by the presence of filament recycling. Given high enough levels of recycling, we find that network tearing can be prevented and that a steady state effective viscosity is established. Our model also suggests a simple microscopic derivation of viscosity which depends on the strength of inter filament cross-linking, the networks architecture, and the timescale of filament

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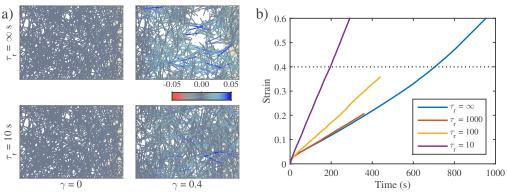


Figure 4. Filament recycling rescues network tearing and modulates effective viscosity. a) Examples of $20 \times 12 \mu m$ network under $0.001 \ nN/\mu m$ extensional stress with recycling $(\tau_r = 10s)$ and without, $(\tau_r = \infty)$. Both images are taken when the patches had reached a net strain of 0.4. The network with recycling doesn't appear to change shape because its components have been recycled to remain in the original domain. Network parameters: $L = 3 \ \mu m, \ l_c = 0.5 \ \mu m, \ \xi = 10 \ nN \cdot s$. b) Strain buildup for networks with parameters as in a) in the presence of different filament recycling rates. Dotted line indicates the strain state at which the snapshots in panel a) were taken. Note that the strain rate for $\tau_r = 1000$ is essentially identical to that of $\tau_r = \infty$, indicating that recycling does not govern the relaxation rate if the recycling time is above a threshold.

recycling. Finally, these findings point to the possibility that different phases of network behavior are possible depending on the relative timescales of competing processes.

Filament recycling allows persistent stress buildup in active networks

In the absence of filament recycling, active networks with free boundaries contract and then stall against passive resistance to network compression. We found that our simulation axioms were able to produce transient contraction of a patch of free-floating network. As shown in Figure 5.a, when an intitially unstrained network has internal motor activity "switched on" at t=0, the . By 100 s, the network has contracted by 40%, and many internal filaments can be seen to have reached a compressed state (indicated by orange). By 150 s, the compression has stalled, but filament sliding has begun to force some filaments away from the center. Over long time periods, this filament sorting actually rearranges the entire network, undoing the initial contraction (see supplemental video).

By monitoring both the network and individual filament strains, as in Figure 5.b, we see that the networks macroscopic deformation can be explained entirely by a buildup of internal compression on individual filaments. Due to the strong stiffness assymetry, there is far more compressive strain than there is extension in the network. It is this asymmetry that generates the net contraction in a disordered network despite myosin activity being equally capable of generating both. The network contraction stalled over the same timescale as individual filaments, further indicating the essential role of filament compression in generating contractility.

The final contraction extent was strongly dependent on the magnitudes of both the filament stiffness asymmetry (i.e. the ratio of the extensional and compressive stiffnesses μ_e/μ_c) and the motor activity scale (v). As shown in Figure 5.c, small

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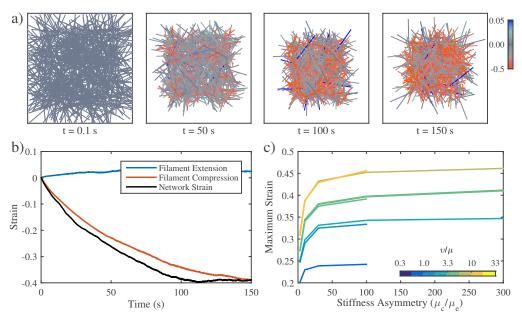


Figure 5. In the absence of filament recycling, active networks with free boundaries contract and then stall against passive resistance to network compression. a) Example of an active network contracting. Note the buildup of compressive stress as contraction approaches stall between 100 s and 150 s. Network parameters: $L=5~\mu m,~l_c=0.3~\mu m,~\xi=100~nN\cdot s,~v=0.1~nN.$ b) Plots showing time evolution of total network strain and the average extensional (blue) or compressive (red) strain on individual filaments. c) The network's ability to deform requires asymmetric filament compliance. Total network strain also increases with the applied myosin force v.

Active networks can only exert a transient force against a fixed boundary in the absence of filament recycling. Due to the complication of making measurements in the presence of such large-scale rearrangements of the network, we decided to additionally analyzed the stress buildup in a patch that was constrained to maintain its original area. The results from Figure 6.a echo those from Figure 5.a, with a consistent buildup of internal filament strain (represented by the colored lines) that stabilizes and persists indefinitely. However, in contrast the network in Figure 6.a doesn't demonstrate any apparent large-scale rearrangement as any net deformation is impossible since the patch sets in a domain with periodic boundaries.

Under these conditions, we found that a net stress was generated throughout the material, but that the net stress could not be maintained and would decay after characteristic time. As shown in Figure 6.b, the results showed a period of net stress

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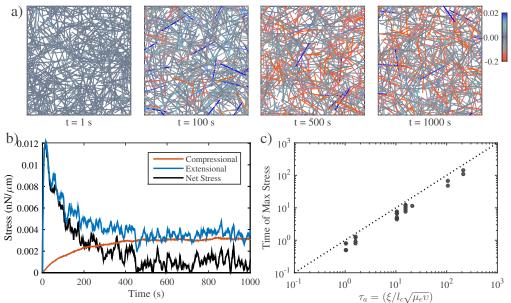


Figure 6. In the absence of filament recycling, active networks can only exert a transient force against a fixed boundary. a) Simulation of an active network with fixed boundaries illustrating progressive buildup of internal stress through local filament rearrangement and deformation. Note the progressive buildup of compressive stress on individual filaments. Network parameters: $L=5~\mu m,~l_c=0.3~\mu m,~\xi=100~nN\cdot s,~v=0.1~nN.$ b) Plots of total network stress and the average extensional (blue) and compressive (red) stress on individual filaments for the simulation shown in (a). Rapid buildup of extensional stress allows the network transiently to exert force on its boundary, but this force is dissipated at longer times as as internal extensional and compressive stresses become balanced. c. Measurement and prediction of the characteristic time (τ_a) at which the maximum stress is achieved.

Filament recycling allows network to exert sustained stress on a fixed boundary. We next added filament recycling to the simulation setup with and found that the presence of recycling allowed for persistent. Similar to the mechanism for preserving integrity in passive networks, the recycling appears to refresh the network such that subsets of filaments are continually transitioning from an unstressed to their stressed state before being recycled back to the unstressed state. The presence of recycling therefore both repaired structural inhomogeneities and reset the net strain of individual filaments. The panels in 7.a show the differences in structure for identical starting architectures in the presence of different recycling timescales. Clearly, longer recycling times allow the network to reach a more strongly reorganized and internally stressed network.

Upon the addition of filament recycling, we found that the network maintained a

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nonzero net stress for timescales much longer than τ_a . We refer to this as the steady state stress because, based on our simulations, it doesn't appear that this stress ever subsides. As can be seen in Figure 7.b, The profile of stress buildup changes dramatically by changing the recycling timescale in identical networks corresponding to those in Figure 7.a. It's important to notice that the effect of changing recycling time is not an entirely simple dependence. As the recycling time is decreased from 333 to 33.3, we can see that the long-term steady state increases from nearly 0.05 to a closer to 0.15. Nevertheless, the final steady state is still lower than the peak stress for those curves. In contrast, for the faster recycling rates (3.33, 0.33, 0.033), the final steady state decreases monotonically with decreasing recycling time. In addition, for these shorter timescales, the stress never reaches a peak but rather rises immediately to its steady state level. We attribute this to the strain resetting whereby individual filaments repeatedly are set to an unstrained state and then transition too having more strain until they are again reset.

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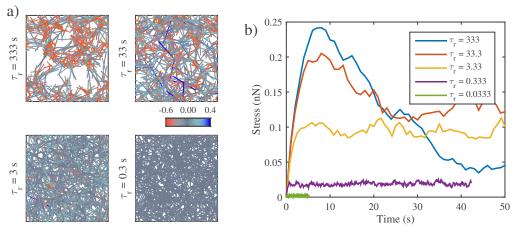


Figure 7. Filament recycling allows network to exert sustained stress on a fixed boundary. a) Example simulations of active networks and fixed boundaries for different timescales of filament recycling. Network parameters are the same as in Figure 6, except that the active force (v=1) has been increased to emphasize the effects of internal network remodeling under stress. Note that significant remodeling occurs for longer recycling times. b) Plots of net stress for different recycling times; for long-lived filaments, stress is built rapidly, but then dissipates. Increasing filament turnover rates reduces stress dissipation by recycling compressed filaments; however, very short recycling times prevent any stress from being built up in the first place.

Filament recycling tunes the balance between active stress buildup and viscous stress relaxation

we found that the steady state stress was well predicted by the comparison between the timescale of recycling, τ_r and that of peak activity, τ_a .

and tunes the flow rate in polarized networks

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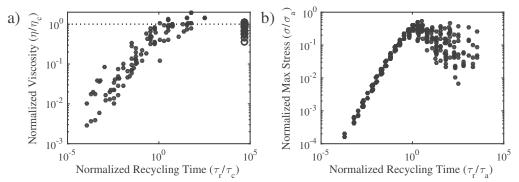


Figure 8. Filament recycling tunes the magnitude of effective viscosity and steady state stress. a) Normalized effective viscosities as a function of the normalized recycling time. When the recycling timescale is significantly less than the passive relaxation timescale (see Figure 3), the viscosity of the network becomes dependent on recycling time. b) Normalized steady state stress as a function of normalized recycling time. The steady state stress is set by the timescale at which the network strain is refreshed relative to the timescale at which the max stress is reached.

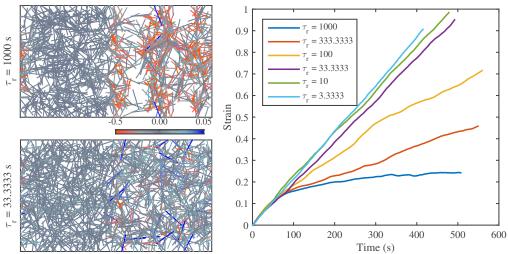


Figure 9. Filament recycling allows sustained flows in networks with non-isotropic activity. a) Example simulations of non-isotropic networks with long ($\tau_r = 1000$) and short ($\tau_r = 33$) recycling timescales. In these networks the left half of the network is passive while the right half is active. Network parameters: $L = 5 \ \mu m, \ l_c = 0.3 \ \mu m, \ \xi = 100 \ nN \cdot s, \ v = 1 \ nN$. b) Graph of strain for identical networks varying recycling timescales. With long recycling times, the network stalls; reducing the recycling timescale allows the network to persist in its deformation. However, for the shortest recycling timescales, the steady state strain appears to approach an asymptotic limit.

Supporting Information

Acknowledgments

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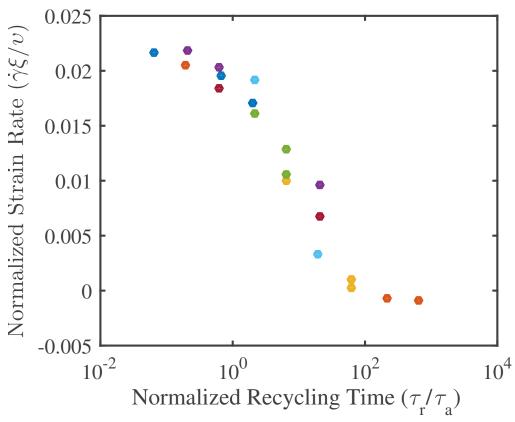


Figure 10

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