

Computer Vision

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Sumary

- Low level image processing
 - Arithmetic operations
 - Pixel relations
- Intensity level slicing / threshold
- Histograms
 - Contrast Stretching
 - Histogram equalization
- Filtering
 - Image smoothing
 - Image sharpening
- Geometrical transformations



Summary

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Aritmetics operation

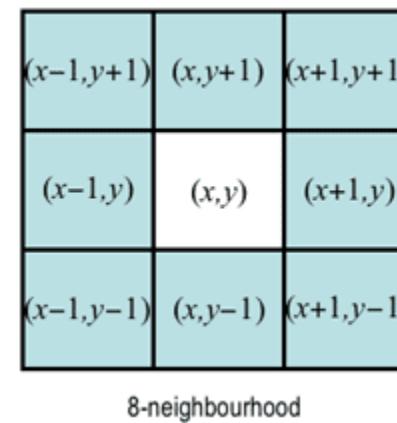
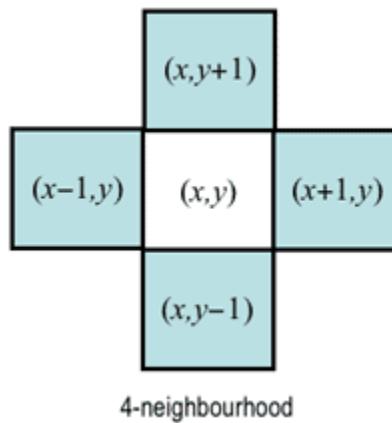
- It is possible to apply several arithmetic operations in images
 - Addition
 - Substraction
 - Multiplication
 - Division
- and logical operations (AND, OR, NOT...)



https://docs.opencv.org/4.x/d0/d86/tutorial_py_image_arithmetics.html

Pixel neighbours

- Many image processing operations make use of spatial relationships between pixels.
- A number of methods have been devised to specify pixel neighbours and calculate distance.
- The 4-neighbours of a pixel (x,y) are the closest pixels in horizontal and vertical directions (D4).
- The 8-neighbors are the 4-neighbors plus the four closest pixels in diagonal direction (D8).





Pixel Distance

- The distance between pixels (x,y) and (u,v) can be calculated in several ways:
 - Euclidean (L2): $D = \sqrt{[(x - u)^2 + (y - v)^2]}$
 - City-block (L1): $D = |x - u| + |y - v|$
 - Chessboard (Linf): $D = \max(|x - u|, |y - v|)$
 - ...
- Although Euclidean distance is more accurate, the sqrt makes it expensive to calculate.

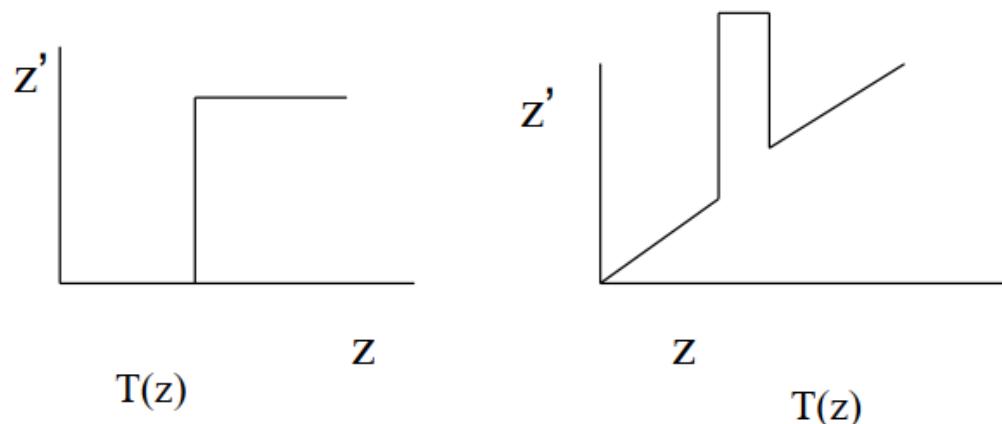


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Intensity level slicing

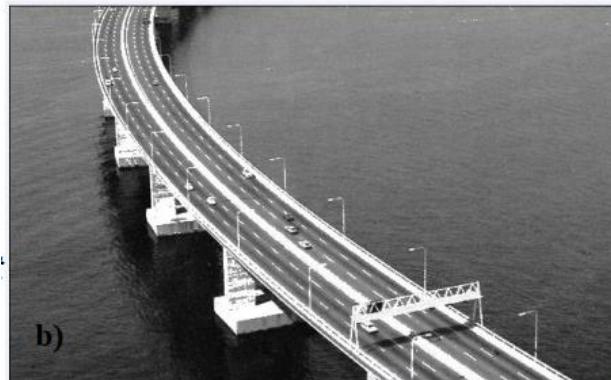
- Intensity level slicing means **highlighting a specific range of intensities** in an image.



a) Threshold

b) Highlight a band of interest

- Threshold** is a specific case of intensity level slicing

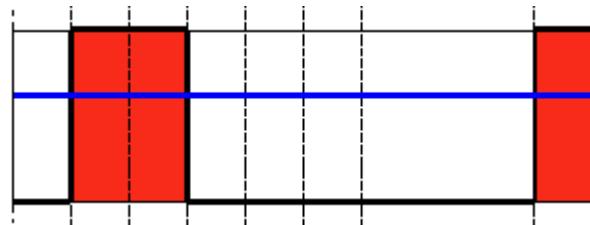




OpenCV - cv::threshold

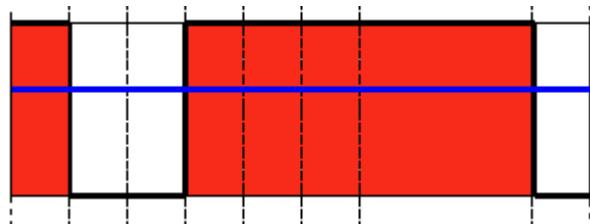
- Threshold Binary

$$dst(x, y) = \begin{cases} \text{maxVal} & \text{if } \text{src}(x, y) > \text{thresh} \\ 0 & \text{otherwise} \end{cases}$$



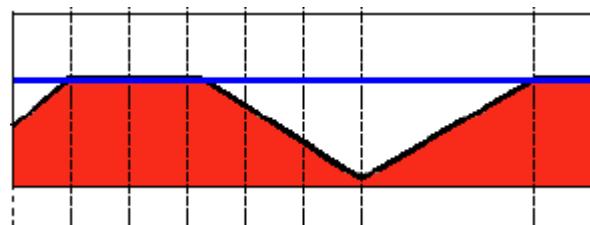
- Threshold Binary, Inverted

$$dst(x, y) = \begin{cases} 0 & \text{if } \text{src}(x, y) > \text{thresh} \\ \text{maxVal} & \text{otherwise} \end{cases}$$



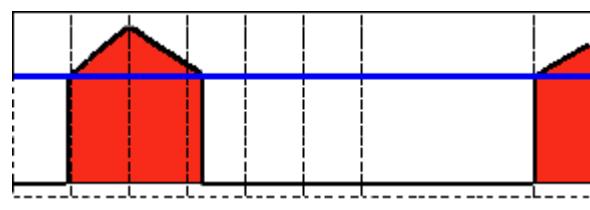
- Truncate

$$dst(x, y) = \begin{cases} \text{threshold} & \text{if } \text{src}(x, y) > \text{thresh} \\ \text{src}(x, y) & \text{otherwise} \end{cases}$$



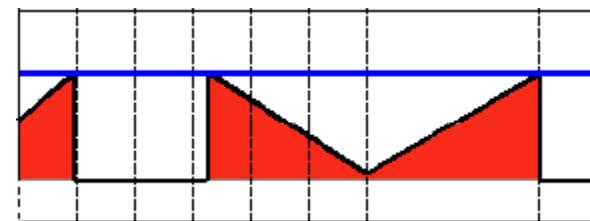
- Threshold to Zero

$$dst(x, y) = \begin{cases} \text{src}(x, y) & \text{if } \text{src}(x, y) > \text{thresh} \\ 0 & \text{otherwise} \end{cases}$$



- Threshold to Zero, Inverted

$$dst(x, y) = \begin{cases} 0 & \text{if } \text{src}(x, y) > \text{thresh} \\ \text{src}(x, y) & \text{otherwise} \end{cases}$$



https://docs.opencv.org/3.4/db/d8e/tutorial_threshold.html



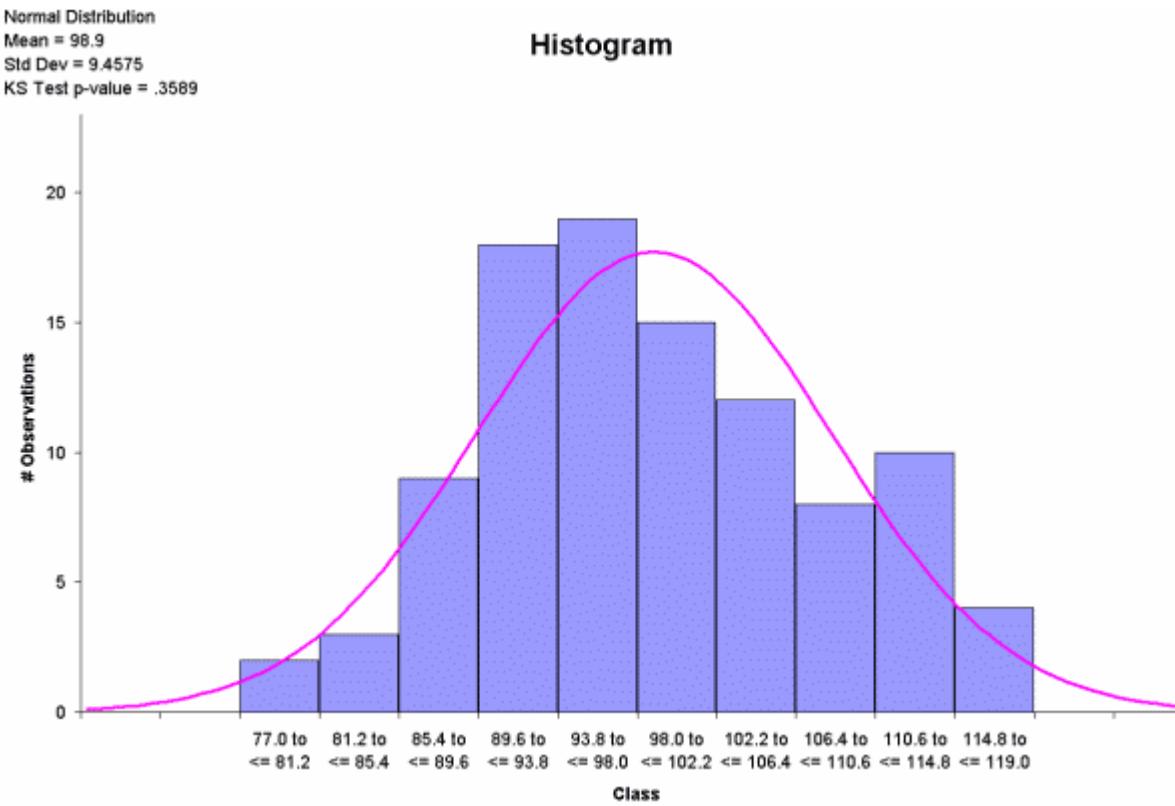
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Histograms

- An histogram is a graphical display of tabulated frequencies.
- Typically represented as a bar chart



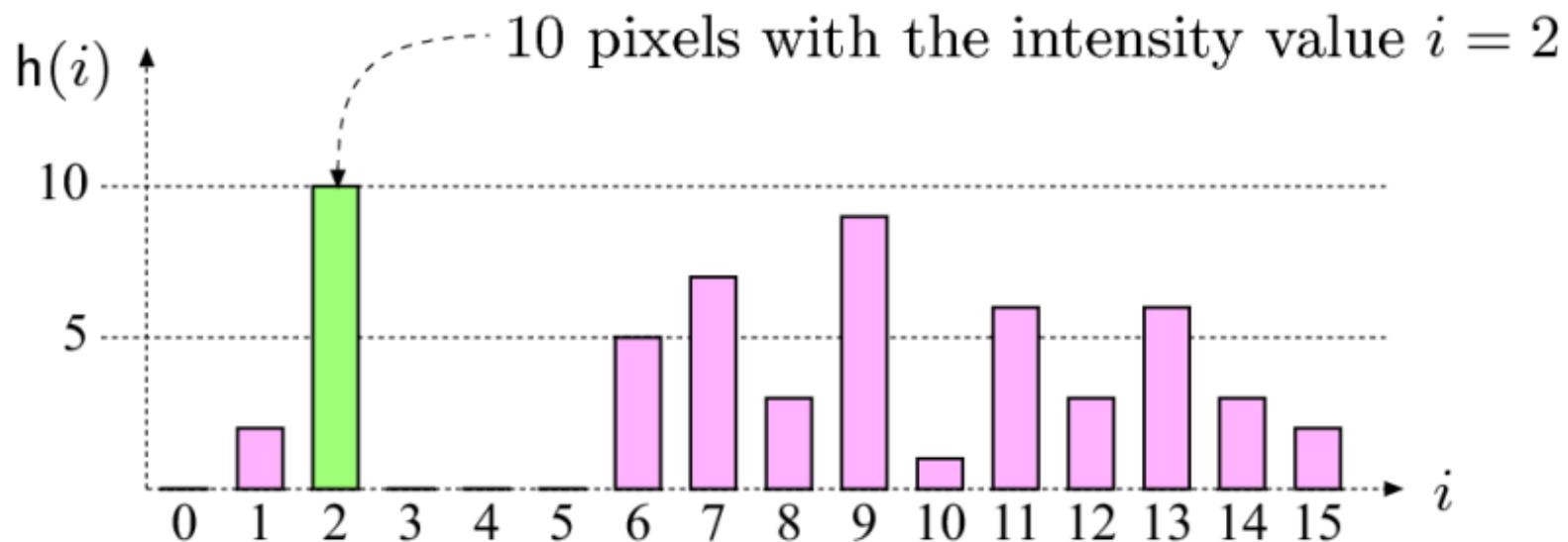


Histograms

- In images, histograms allow us to see the colour or intensity distribution.
- The collected counts of data can be organized into a set of predefined bins.
- Important parts of an histogram:
 - dims: The number of parameters you want to collect data.
 - bins: The number of subdivisions in each dim.
 - range: The limits for the values to be measured.
- Operation based on histogram typically have two phases:
 - Determination and analysis of histogram
 - Image improvement based on the histogram.



Histograms

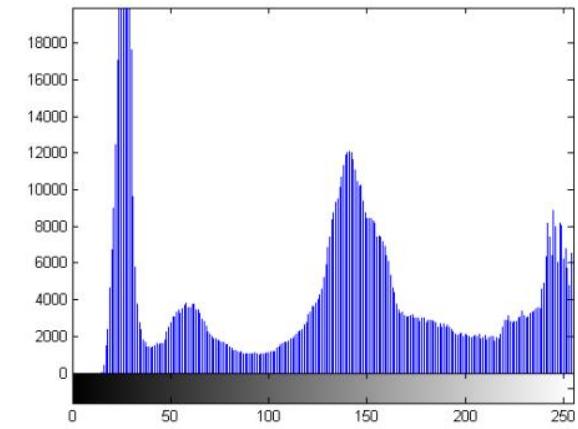
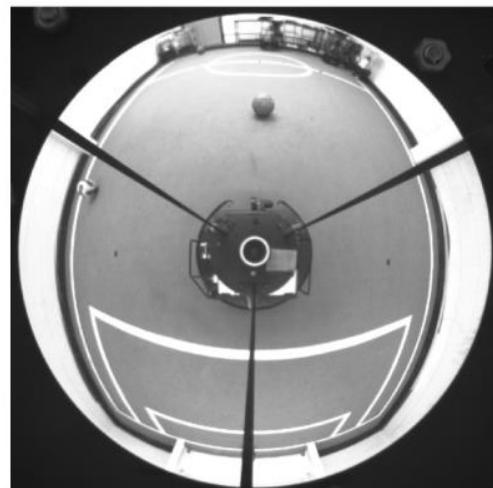
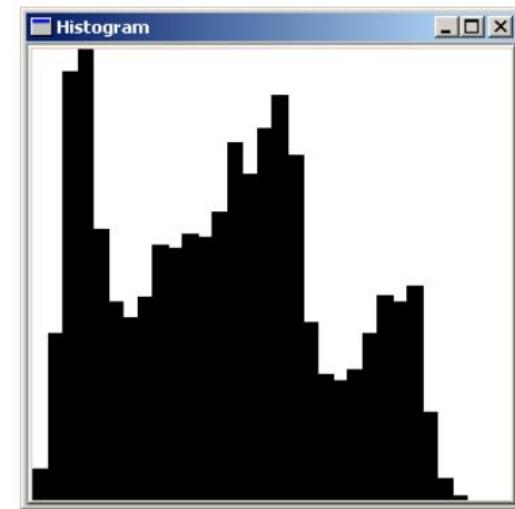


$h(i)$	0	2	10	0	0	0	5	7	3	9	1	6	3	6	3	2
i	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15



Histograms

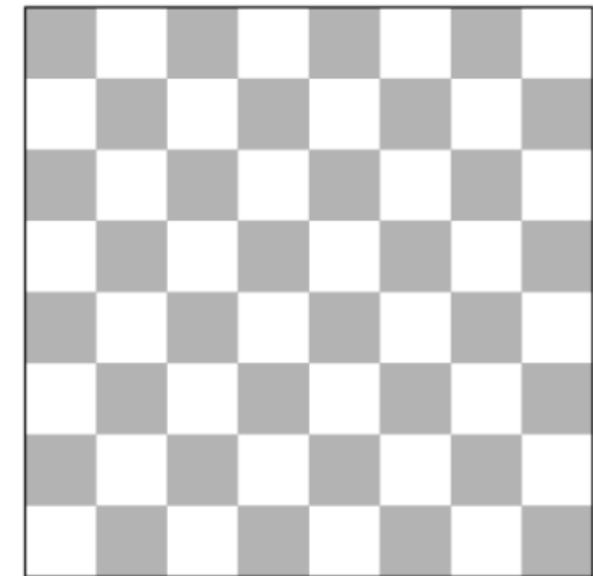
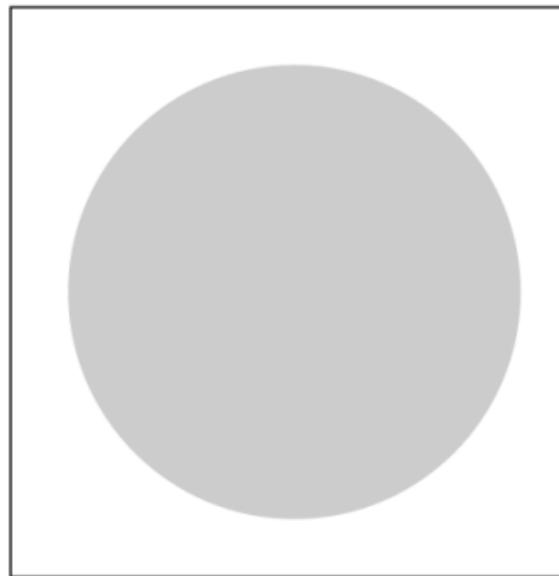
- Examples





Histograms

- Histograms... same or different?

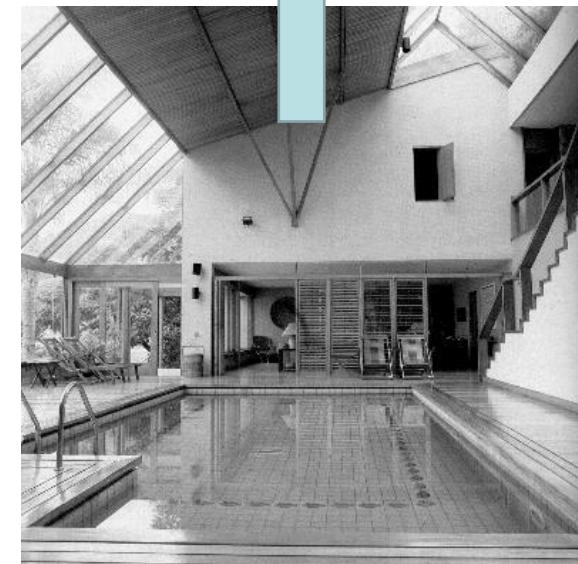
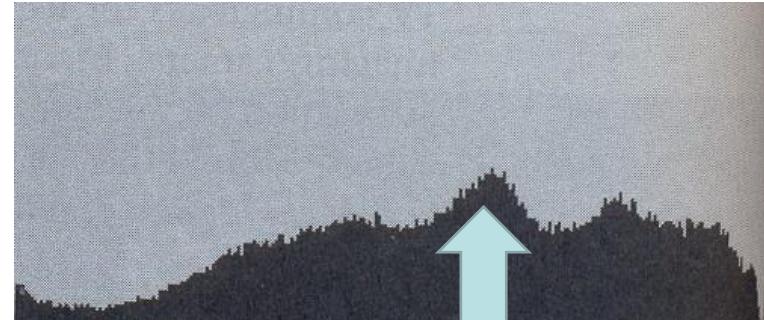
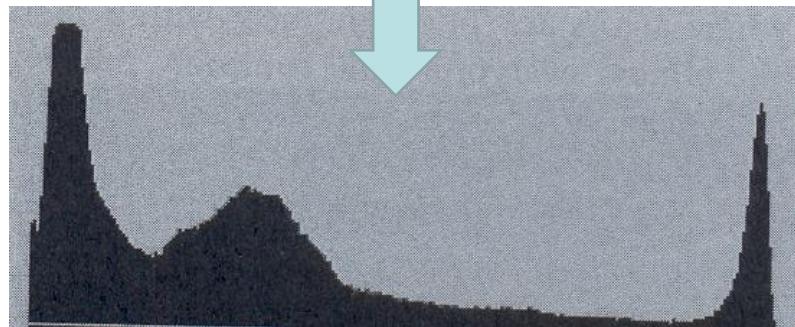
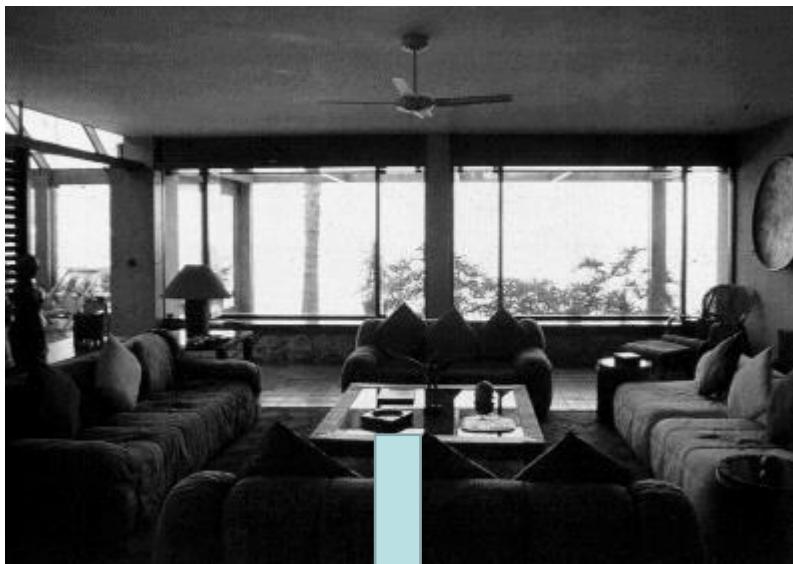


Burger and Burge



Histograms

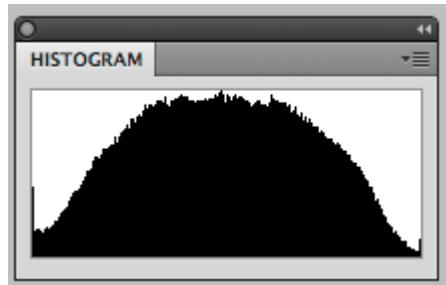
- Which histogram to which image



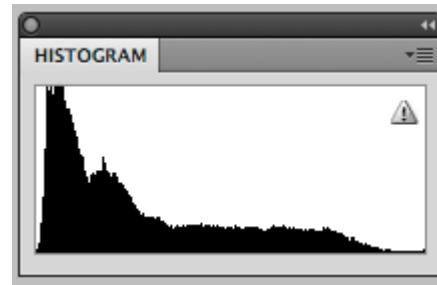


Histograms

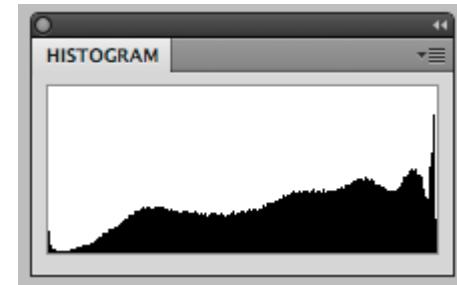
- Histograms



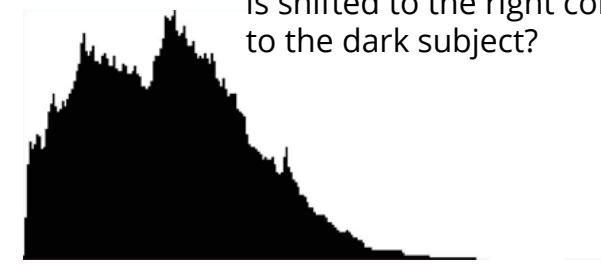
This is how an ideal histogram might look, evenly distributed, edge to edge, not up the sides.



This is a histogram for a dark subject. It is not wrong; it is just more shifted to the left to represent the tones of the subject.



This is a histogram for a light subject (e.g., a white cat) with mostly light tones in the scene and few dark areas. See how it is shifted to the right compared to the dark subject?



This graph shows an overexposed image; notice the gap on the left side indicating a lack of any blacks in the image. It also means you will lose lots of detail in the white areas that may not be recoverable. In this case, shift to give your image less exposure and shoot the scene again.

This histogram shows the opposite. Now we see a gap on the right side of the graph indicating there are no whites represented, so the image will be dark – too dark. You can safely give the image more exposure until you see the tones just touch the right edge of the histogram.

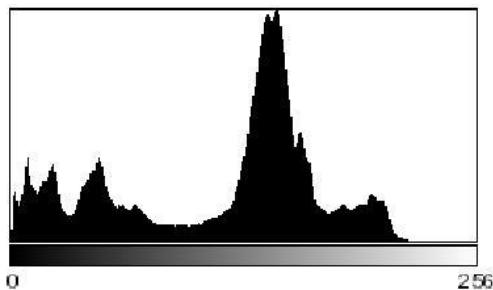
<https://digital-photography-school.com/how-to-read-and-use-histograms/>



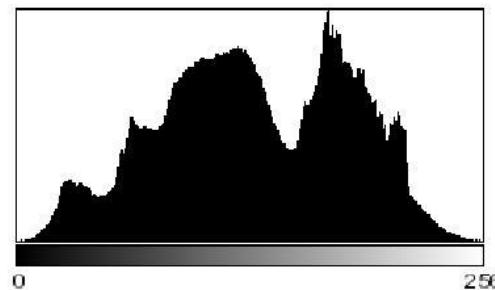
Histograms

- Properties: exposition

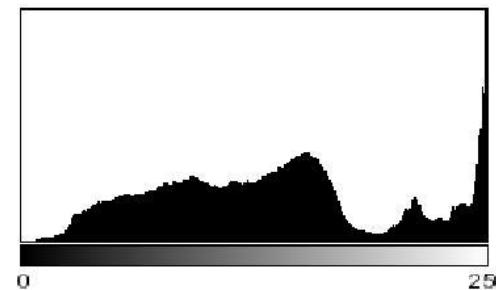
Burger and Burge



(a)



(b)



(c)

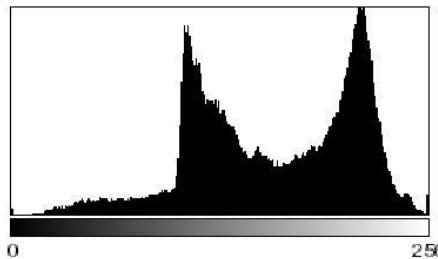
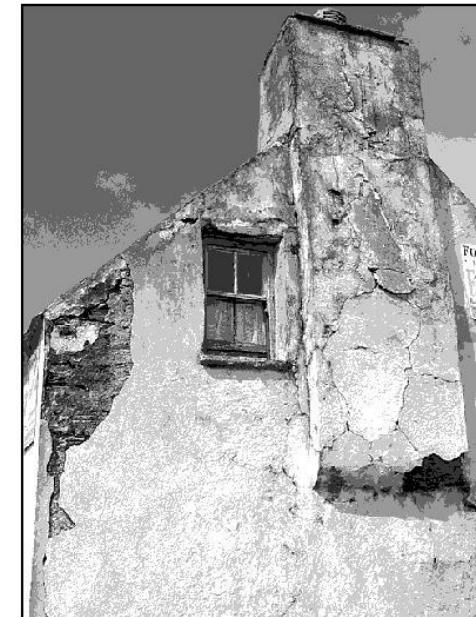
a - **underexposed** image – loss of details in dark areas

b - ok

c - **overexposed** – loss of details in bright areas

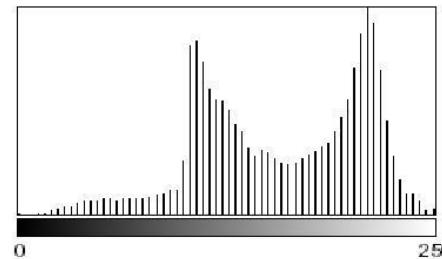
Histograms

- Properties: intensity levels

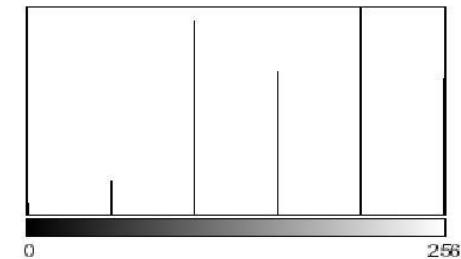


(a)

256, 64 and 6



(b)



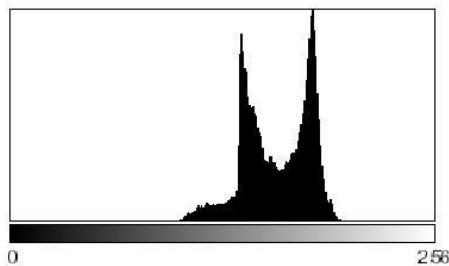
(c)

Burger and Burge

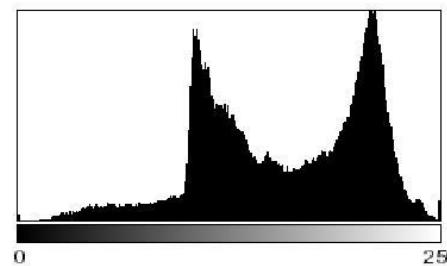


Histograms

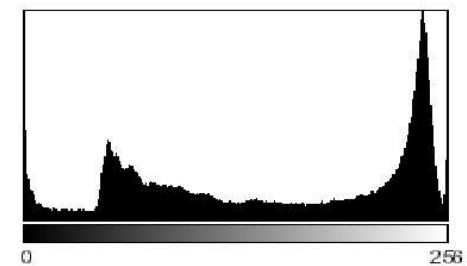
- Properties: contrast



(a)



(b)



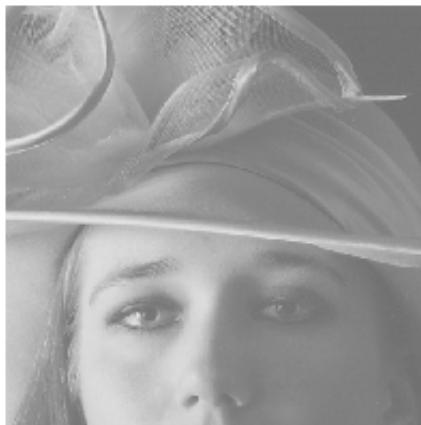
(c)

Burger and Burge

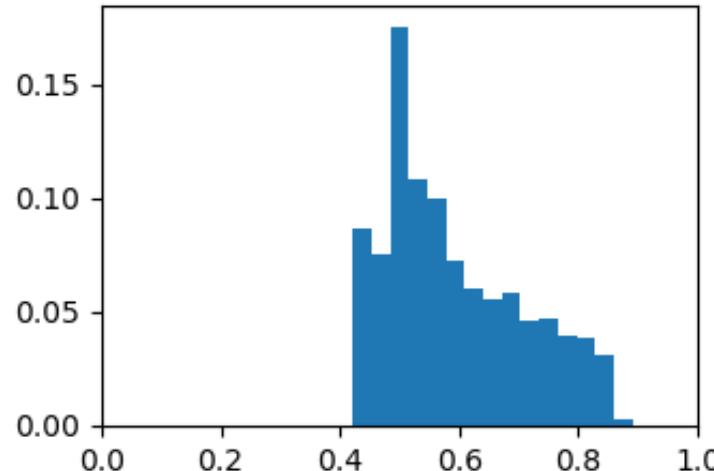
Histograms

- Contrast stretching

Low contrast original



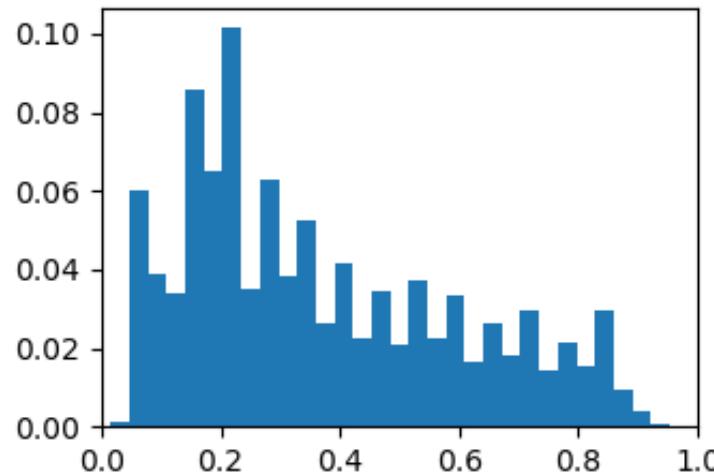
Histogram of low contrast image



Contrast Stretched



Histogram of contrast stretched image

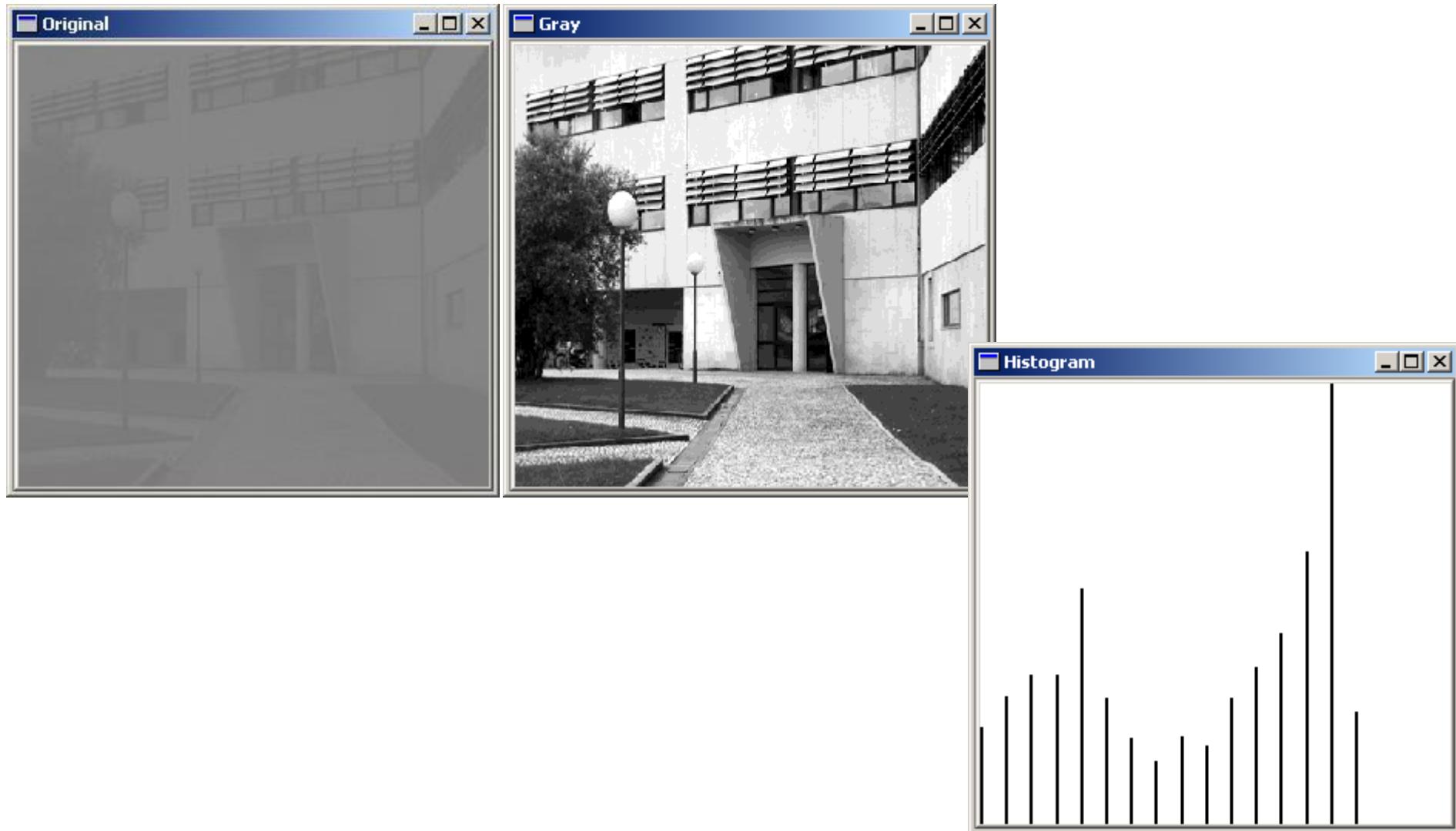


$$g = \frac{f - f_{\min}}{f_{\max} - f_{\min}}$$



Histograms

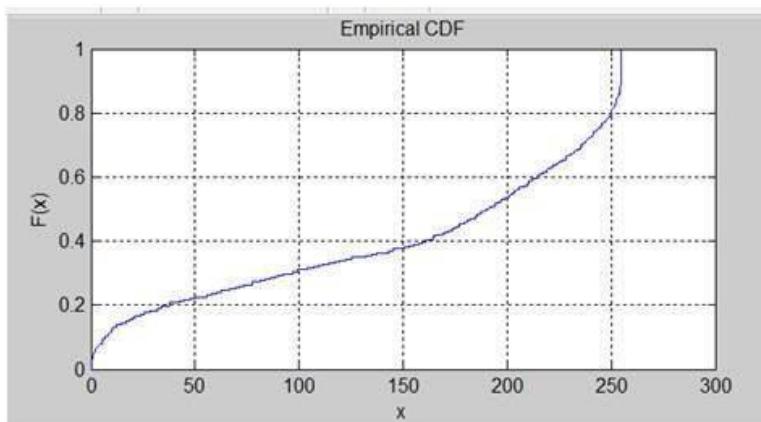
- Contrast stretching (another exemple)





Histograms

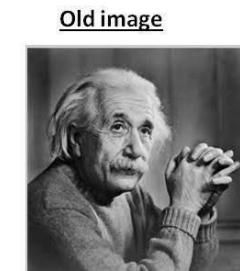
- Histogram equalization
 - Can be seen as an **extension of contrast stretching**
 - Histogram is analysed by a function $T(z)$ to **reshape the image** to make its **histogram flat and wide**
 - A typical solution is to use the **cumulative histogram** (integral of intensity histogram) as the intensity mapping function.



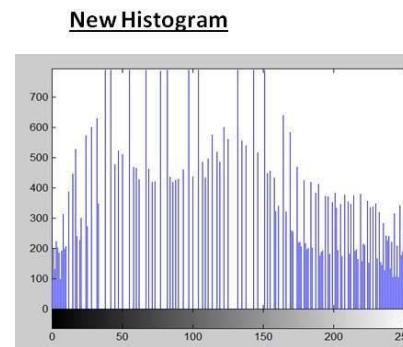
Cumulative Distributive function of the image



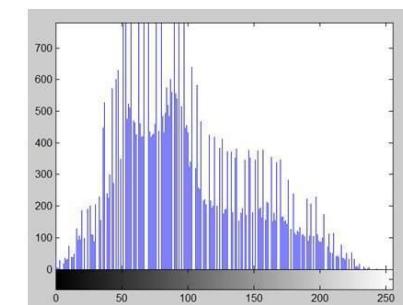
New Image



Old image



New Histogram

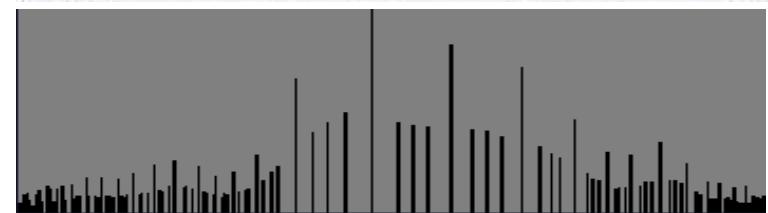
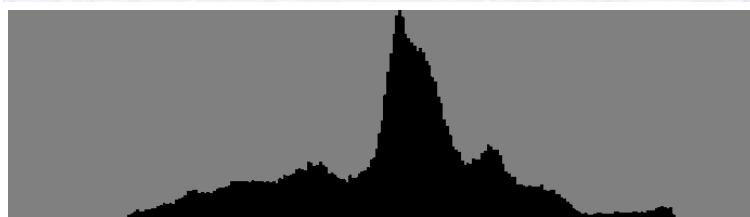


Old Histogram



Histograms

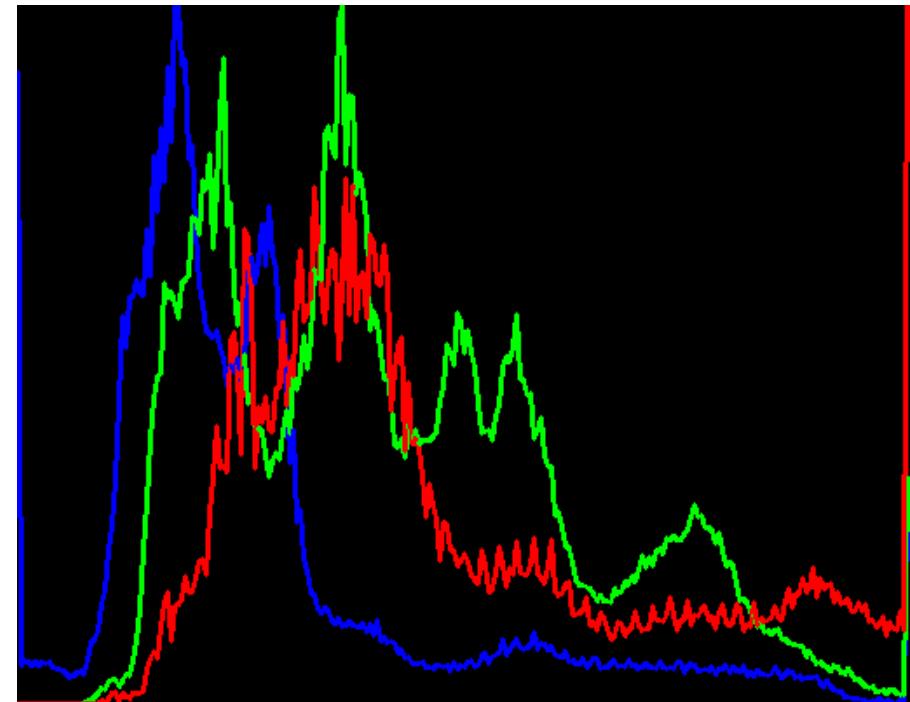
- Histogram equalization





Histograms

- Colour histogram





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- **Filtering**
 - Image smoothing
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Filtering

- Image smoothing or blurring
 - Also known as **neighbourhood averaging**
 - Used to **remove noise** or a **pre-processing for edge detection**
 - Filtering operation in which a **weighted array** is moved over the original image while computing the pixel as a **weighted average**:
 - $I'(u, v) = \sum_{i=0, j=0}^{n, m} R(i, j) \cdot I(u - \left(\frac{n-1}{2}\right) + i, v - \left(\frac{m-1}{2}\right) + j)$

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

3x3 average filter with 1/9 weight,
anchored in center of array



Filtering

- Image smoothing or blurring

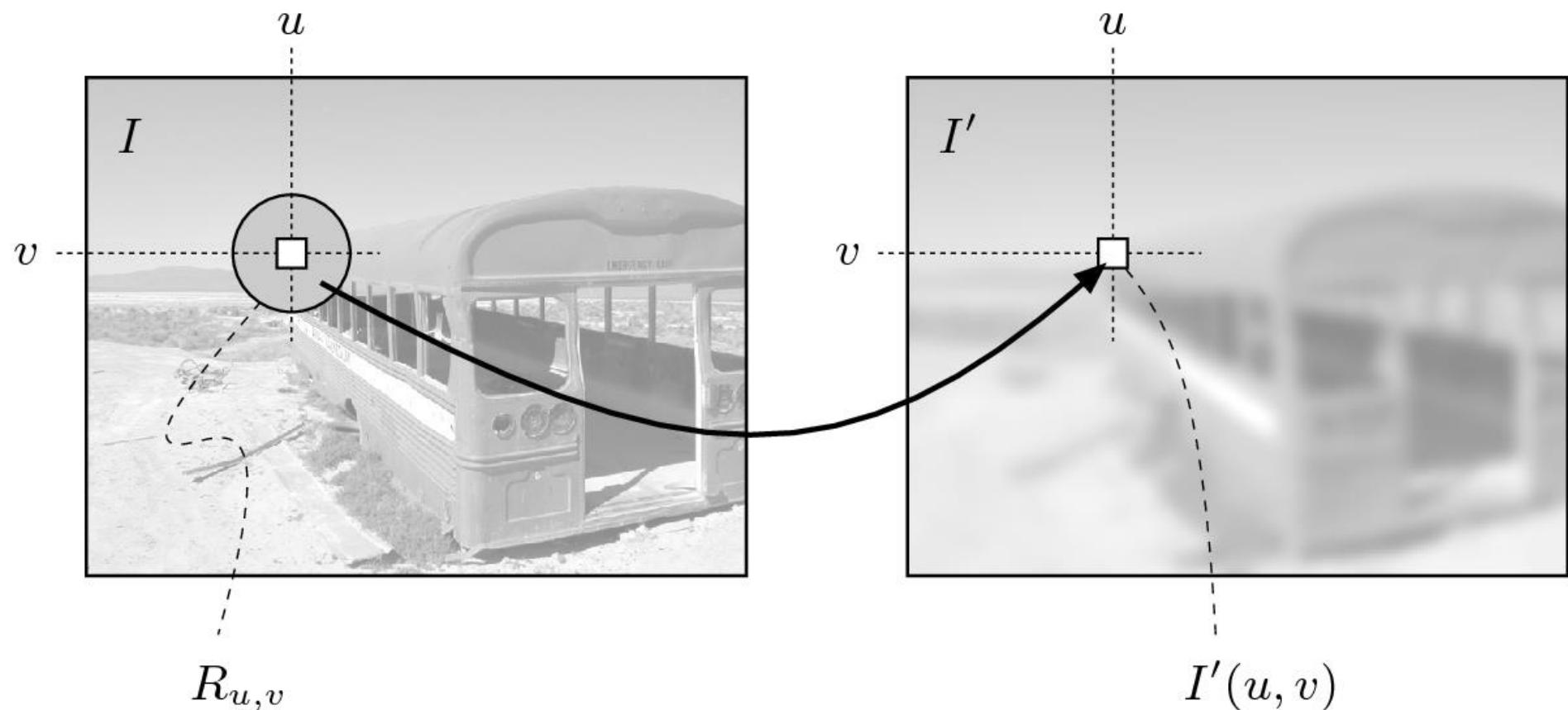


Burger and Burge



Filtering

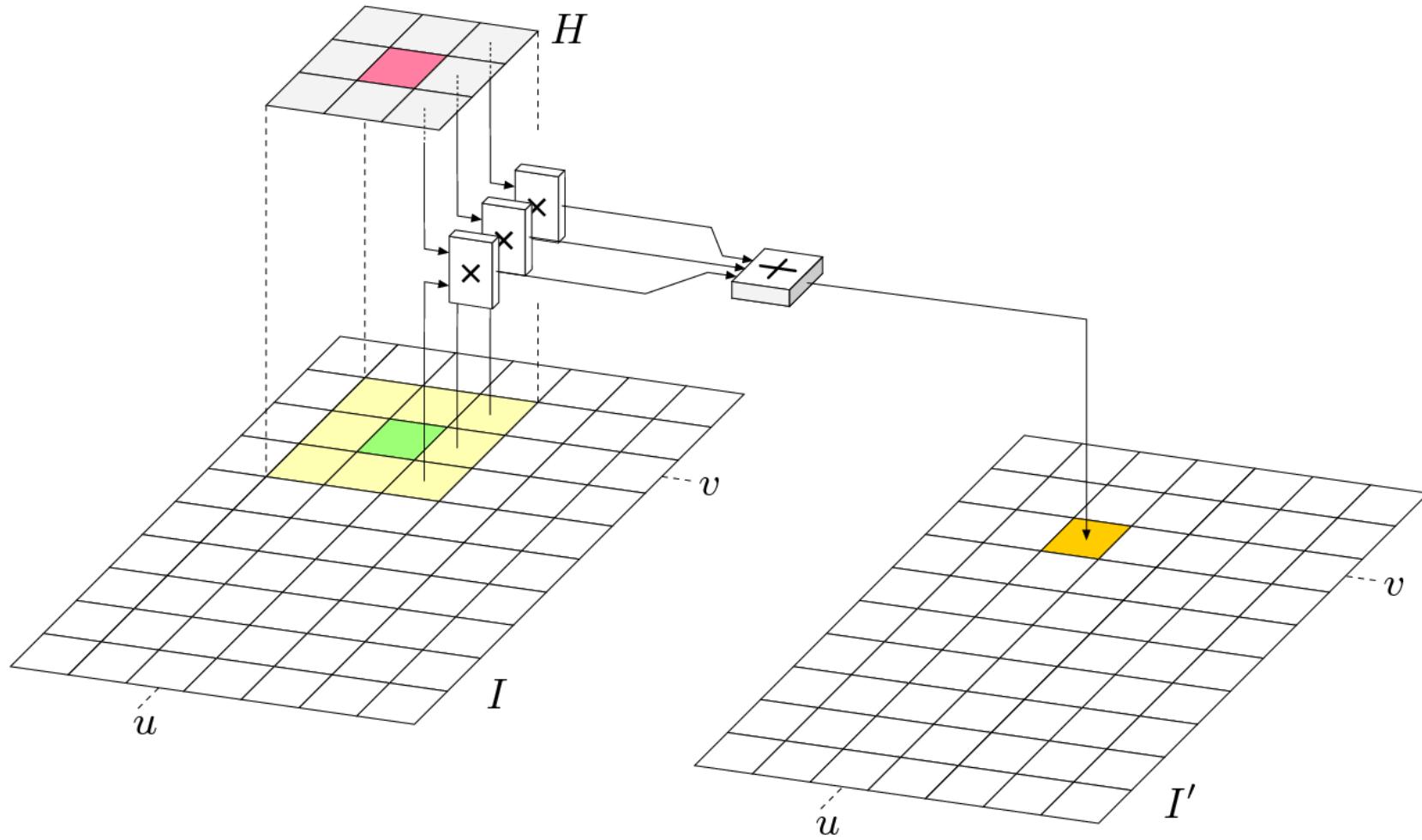
- Image smoothing or blurring

 $R_{u,v}$ $I'(u, v)$



Filtering

- Image smoothing or blurring

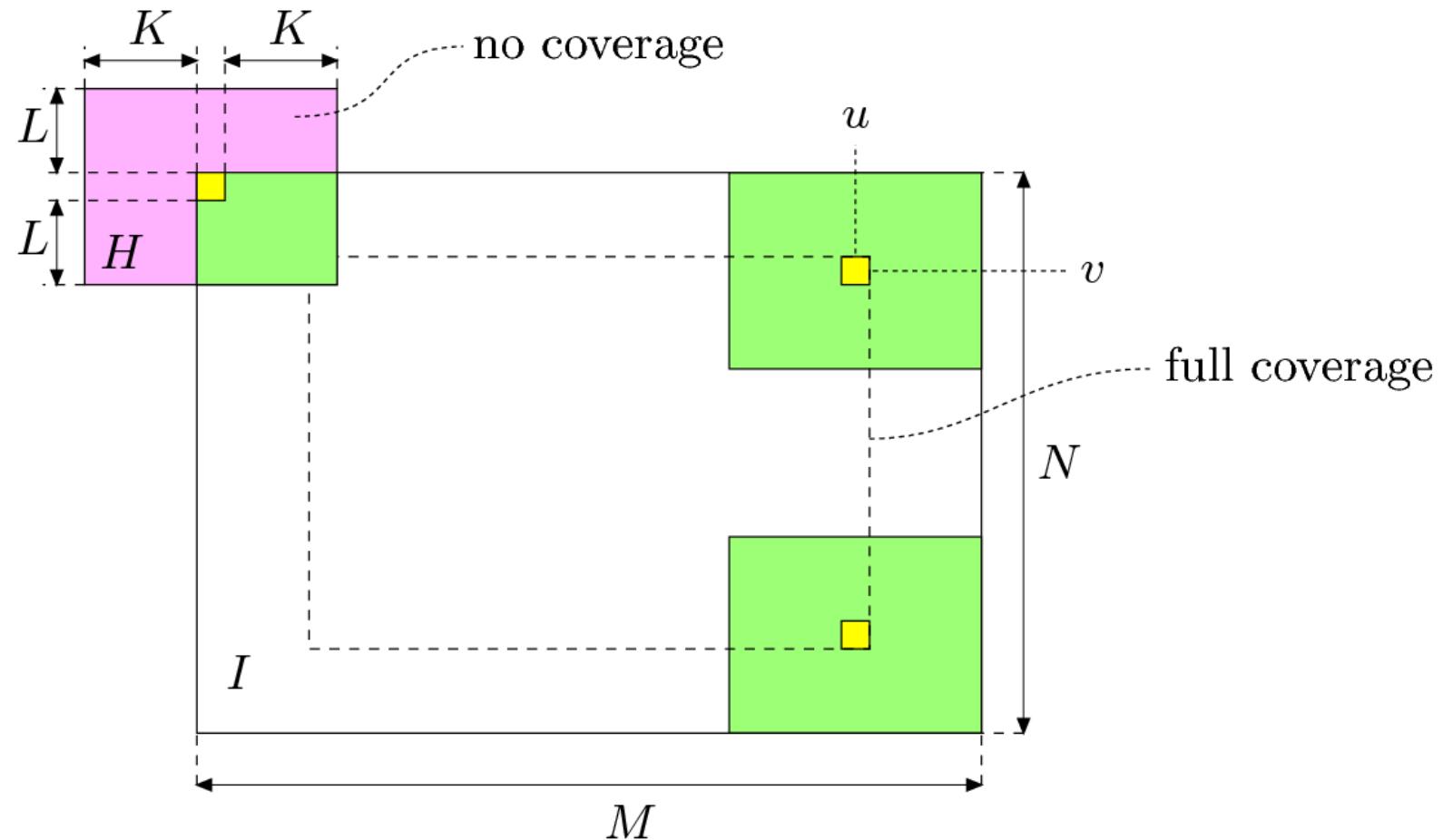


Burger and Burge



Filtering

- Image smoothing or blurring
 - What to do at borders





Filtering

- Image smoothing or blurring
 - What to do at borders



Constant Value



Value of closest border



Mirrored at image Boundary



Periodically repeat along axis

Burger and Burge



Filtering

- Average filter for noise reduction
 - Kind of the **low pass filter**, the larger the size, the larger the cut-off frequency.
 - This is an approximation since smoothing operation is performed in space and not in frequency domain.



Filtering

- Average filter for noise reduction



Original



Noisy

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

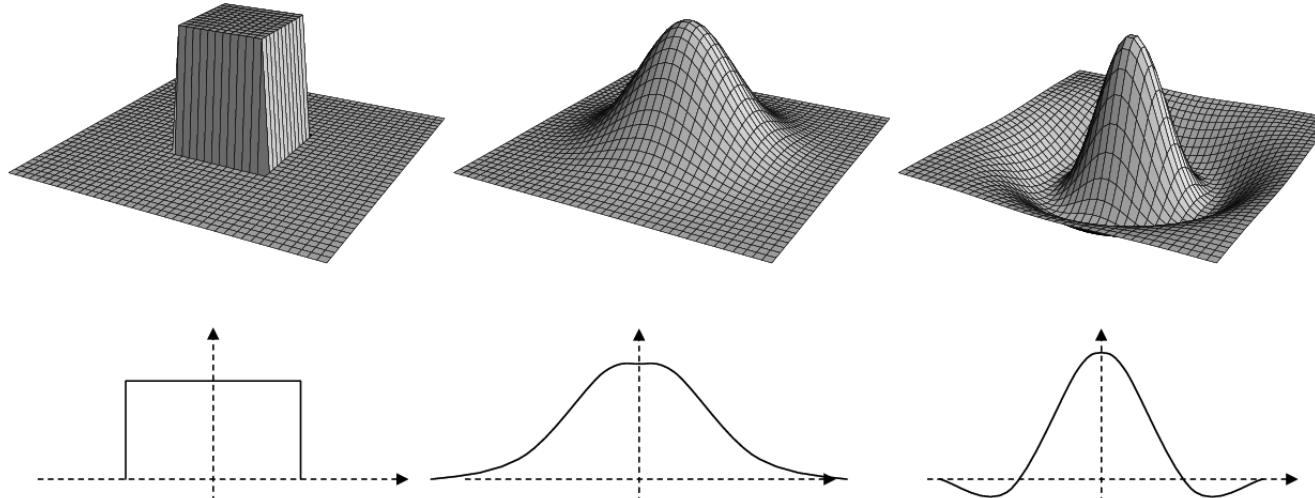


Blurred image

Filtering



- Typical linear filter



0	0	0	0	0
0	1	1	1	0
0	1	1	1	0
0	1	1	1	0
0	0	0	0	0

(a)

a - Box filter

0	1	2	1	0
1	3	5	3	1
2	5	9	5	2
1	3	5	3	1
0	1	2	1	0

(b)

b - Gaussian Filter

0	0	-1	0	0
0	-1	-2	-1	0
-1	-2	16	-2	-
0	-1	-2	-1	0
0	0	-1	0	0

(c)

c – “Laplace” or “Mexican hat” filter

Burger and Burge



Filtering

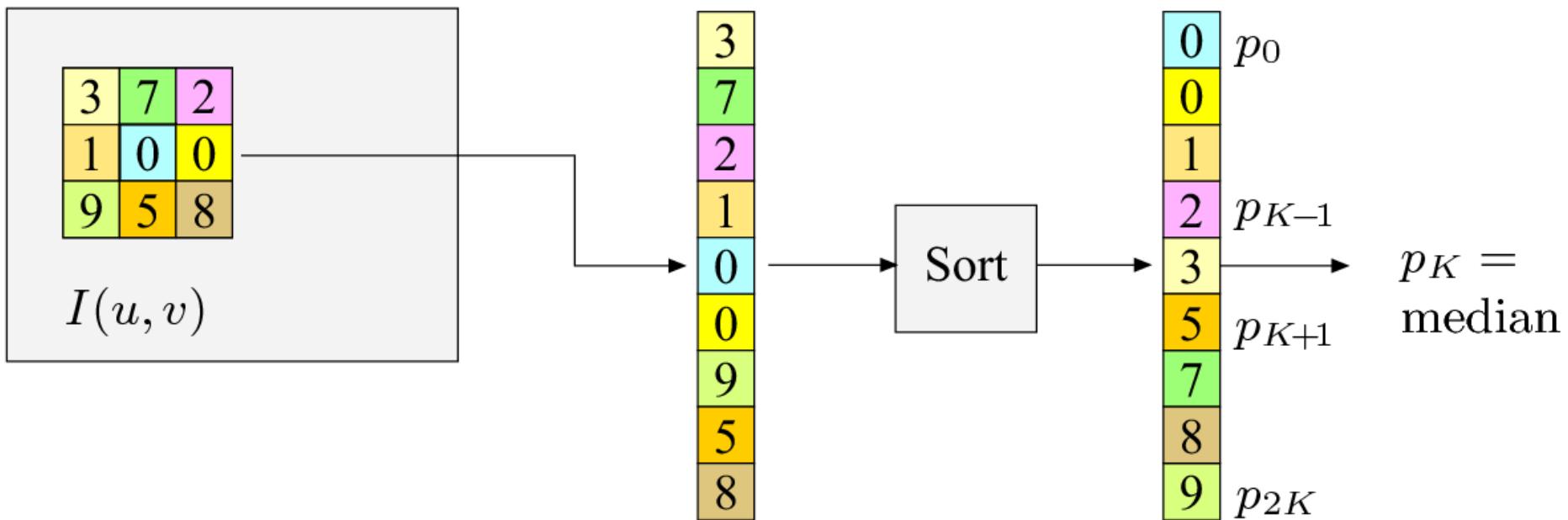
Blurring in openCV





Filtering

- Median Filter





Filtering

- Average vs median Filter



(a)



(b)



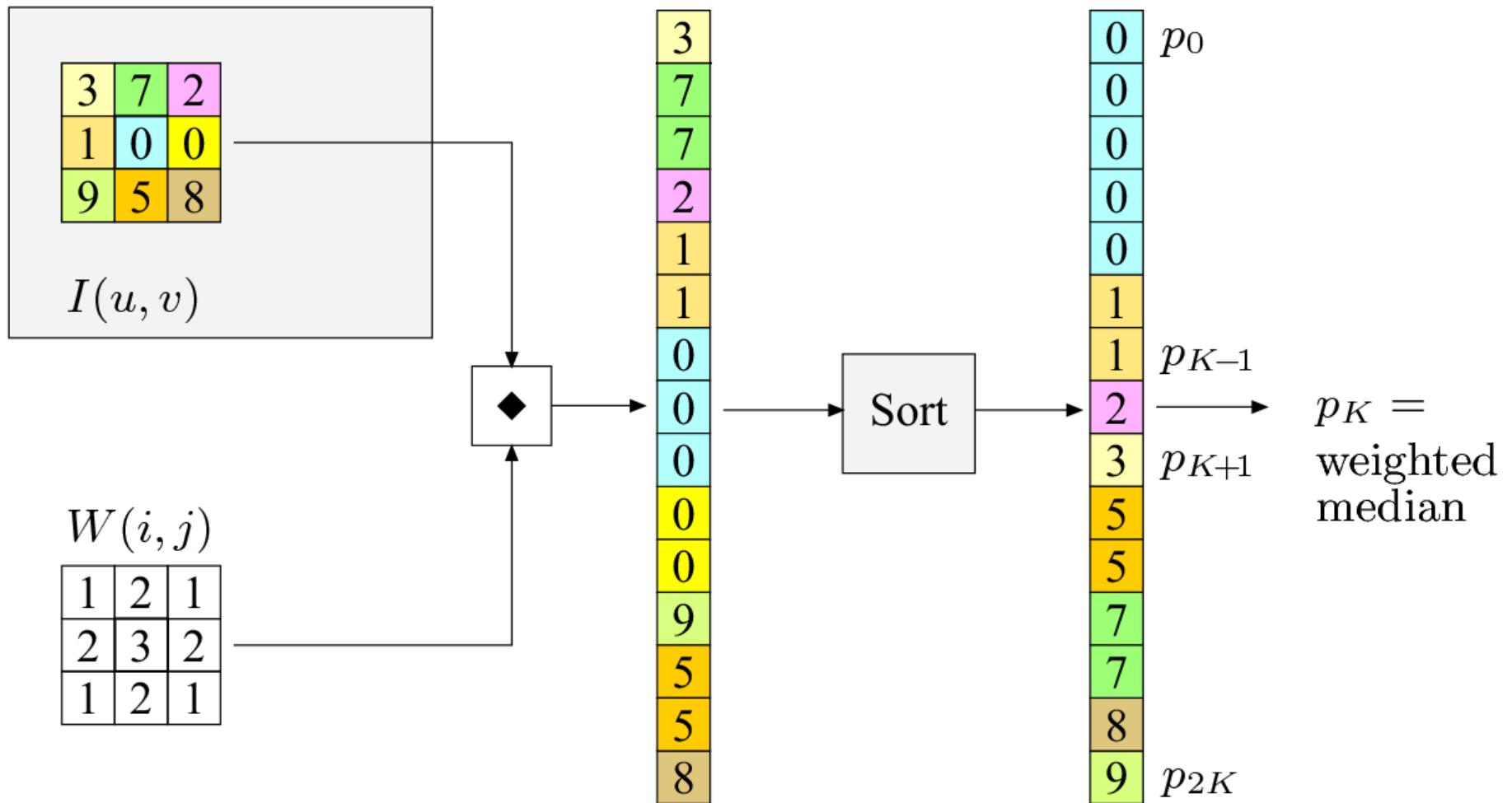
(c)

Burger and Burge



Filtering

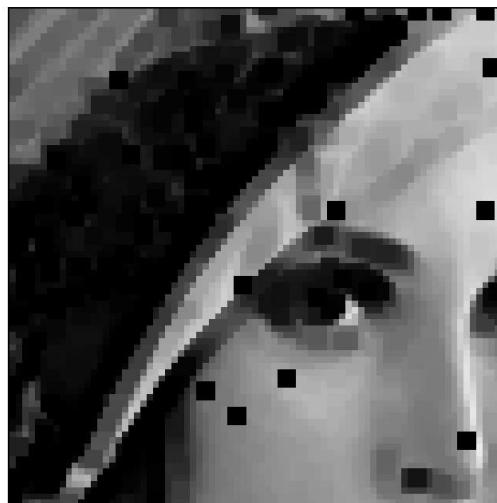
- Weighted Median Filter





Filtering

- Minimum vs Maximum filter



(a)

(b)

(c)

Burger and Burge



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Geometrical transformations

- Geometric operation transform a given image I to a new image I'

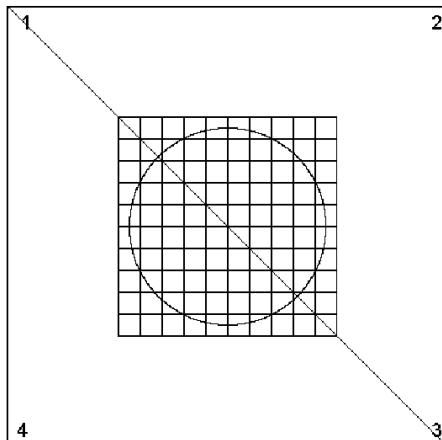
$$I'(x',y') \leftarrow I(x, y)$$

- Value of image I at original location (x,y) moves to new position (x',y') in transformed image I' based on a geometric mapping T

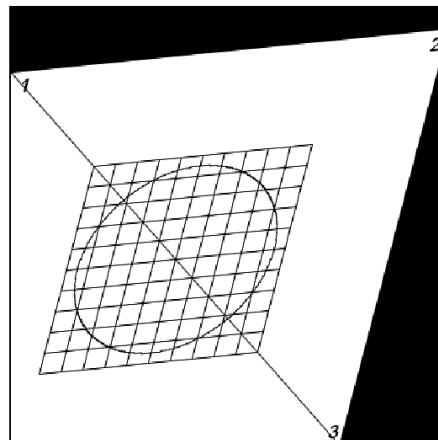
$$(x',y') = T(x, y)$$



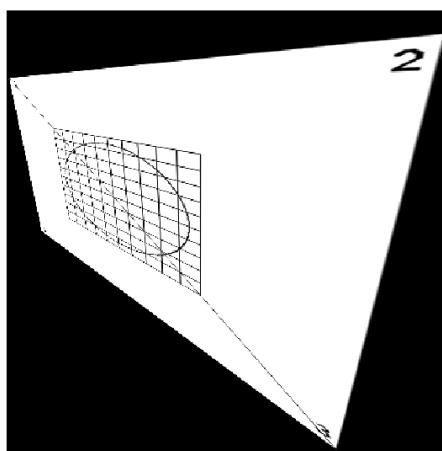
Geometrical Transformation



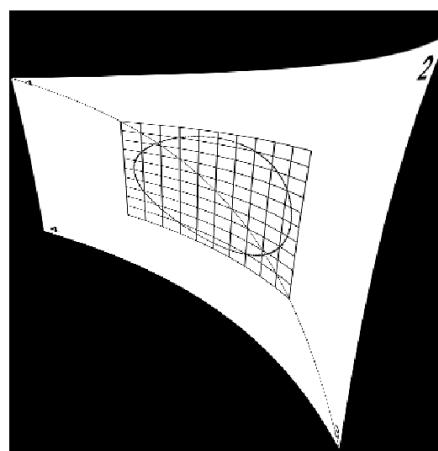
(a)



(b)



(c)



(d)

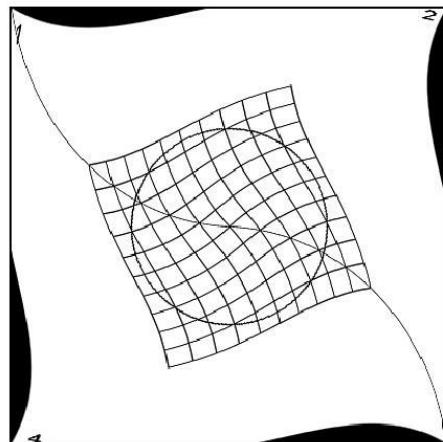
Linear:

- Affine
 - Translation, rotation, and scaling
 - Preserves lines and parallelism
- Projective
 - Particular case of affine
 - Does not preserve parallelism

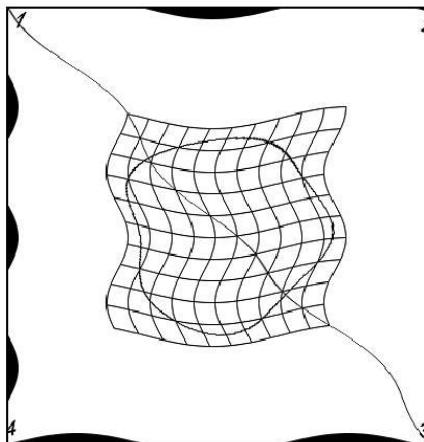


Geometrical Transformation

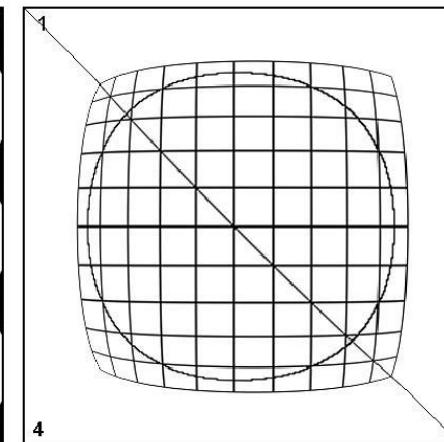
- Non linear: twirl, ripple, sphere, ...



Twirl



Ripple



Sphere

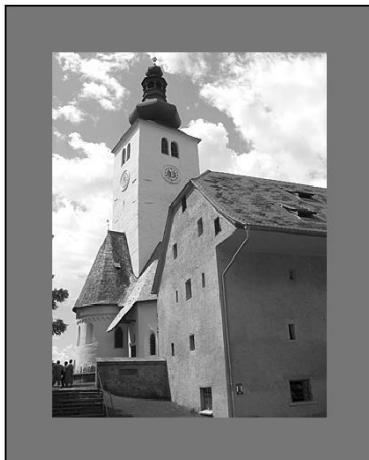


Burger and Burge



Geometrical Transformation

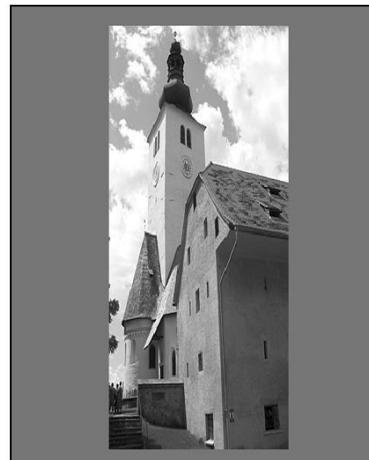
- Which ones



Original



Translation



Scaling (contract [x] and stretch [y])



Rotation



Projective



Non Linear

Burger and Burge

Geometrical transformations

- Geometrical transformations used for:
 - Correction of distortion
(Camera lens correction)
 - Texture mapping (Computer Graphics)
 - Morphing (Special effects in movies)

