

# Physics informed transformer-VAE for biophysical parameter estimation: PROSAIL model inversion in Sentinel-2 imagery

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## Abstract

We propose a physics-informed variational autoencoder (VAE) architecture, termed Transformer-PROSAILVAE, for retrieving vegetation biophysical parameters from Sentinel-2 satellite imagery. The model integrates a transformer-based encoder with a fixed PROSAIL radiative transfer model (RTM) decoder, embedding physical knowledge of canopy reflectance into a deep learning framework. This design enables self-supervised training on simulated reflectance data without any ground truth labels – the encoder learns to infer Leaf Area Index (LAI) and canopy chlorophyll content (CCC) by reconstructing spectral reflectances via the PROSAIL decoder. We thoroughly describe the architecture and training pipeline, and compare its performance to the original transformer-VAE approach of Z  rah et al. (2023) file-27hzu1p94gn7jorbww3kzm . Experiments on real Sentinel-2 images demonstrate that our Transformer-VAE achieves accurate LAI and CCC retrievals, outperforming both the baseline transformer-VAE and the operational SNAP biophysical processor. The transformer encoder effectively captures complex spectral–spatial context, yielding improved retrieval robustness across diverse landscapes. We report quantitative results on independent in-situ validation datasets (FRM4Veg and BelSAR campaigns) showing that the physics-informed Transformer-VAE attains lower estimation errors and higher consistency with field measurements. The proposed approach illustrates how integrating physical models with advanced deep networks can improve the inversion of RTMs, opening new prospects for large-scale, physically-constrained remote

sensing of vegetation traits.

## 1. Introduction

Physics-guided deep learning has applied to vegetation parameter retrieval by coupling the prosail radiative transfer model with neural network.

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Preliminary work. Under review by the International Conference on Machine Learning (ICML). Do not distribute.

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The footnote, “Preliminary work. Under review by the International Conference on Machine Learning (ICML). Do not distribute.” must be modified to “*Proceedings of the 42<sup>nd</sup> International Conference on Machine Learning*, Vancouver, Canada, PMLR 267, 2025. Copyright 2025 by the author(s).”

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The paper title should be set in 14 point bold type and centered between two horizontal rules that are 1 point thick, with 1.0 inch between the top rule and the top edge of the page. Capitalize the first letter of content words and put the rest of the title in lower case.

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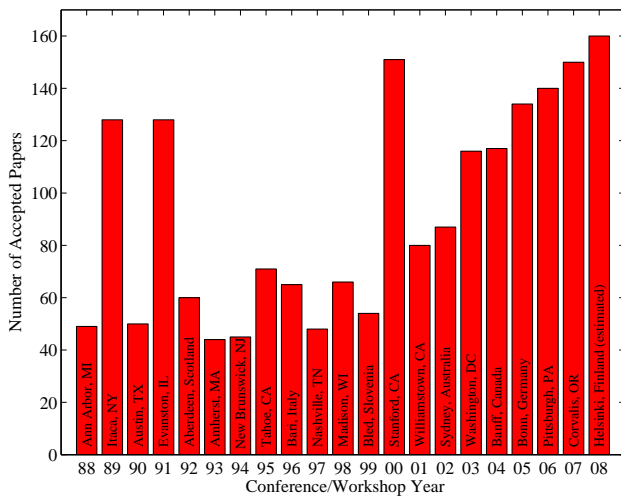


Figure 1. Historical locations and number of accepted papers for International Machine Learning Conferences (ICML 1993 – ICML 2008) and International Workshops on Machine Learning (ML 1988 – ML 1992). At the time this figure was produced, the number of accepted papers for ICML 2008 was unknown and instead estimated.

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## Algorithm 1 Bubble Sort

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**Input:** data  $x_i$ , size  $m$

**repeat**

Initialize  $noChange = true$ .

**for**  $i = 1$  **to**  $m - 1$  **do**

**if**  $x_i > x_{i+1}$  **then**

Swap  $x_i$  and  $x_{i+1}$

$noChange = false$

**end if**

**end for**

**until**  $noChange$  is  $true$

---

Table 1. Classification accuracies for naive Bayes and flexible Bayes on various data sets.

DATA SET	NAIVE	FLEXIBLE	BETTER?
BREAST	95.9±0.2	96.7±0.2	✓
CLEVELAND	83.3±0.6	80.0±0.6	×
GLASS2	61.9±1.4	83.8±0.7	✓
CREDIT	74.8±0.5	78.3±0.6	
HORSE	73.3±0.9	69.7±1.0	×
META	67.1±0.6	76.5±0.5	✓
PIMA	75.1±0.6	73.9±0.5	
VEHICLE	44.9±0.6	61.5±0.4	✓

serve this function.

Number figures sequentially, placing the figure number and caption *after* the graphics, with at least 0.1 inches of space before the caption and 0.1 inches after it, as in ???. The figure caption should be set in 9 point type and centered unless it runs two or more lines, in which case it should be flush left. You may float figures to the top or bottom of a column, and you may set wide figures across both columns (use the environment `figure*` in L<sup>A</sup>T<sub>E</sub>X). Always place two-column figures at the top or bottom of the page.

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## 2.9. Theorems and such

The preferred way is to number definitions, propositions, lemmas, etc. consecutively, within sections, as shown below.

**Definition 2.1.** A function  $f : X \rightarrow Y$  is injective if for any  $x, y \in X$  different,  $f(x) \neq f(y)$ .

Using ?? we immediate get the following result:

**Proposition 2.2.** *If  $f$  is injective mapping a set  $X$  to another set  $Y$ , the cardinality of  $Y$  is at least as large as that of  $X$*

*Proof.* Left as an exercise to the reader.  $\square$

?? stated next will prove to be useful.

**Lemma 2.3.** *For any  $f : X \rightarrow Y$  and  $g : Y \rightarrow Z$  injective functions,  $f \circ g$  is injective.*

**Theorem 2.4.** *If  $f : X \rightarrow Y$  is bijective, the cardinality of  $X$  and  $Y$  are the same.*

An easy corollary of ?? is the following:

**Corollary 2.5.** *If  $f : X \rightarrow Y$  is bijective, the cardinality of  $X$  is at least as large as that of  $Y$ .*

**Assumption 2.6.** The set  $X$  is finite.

*Remark 2.7.* According to some, it is only the finite case (cf. ??) that is interesting.

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## References

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