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Note: Thank you for your feedback. I revised my initial submission to be more precise and descriptive in various answers. In addition, although my math was correct, I inadvertently included my timed results with the samples giving us 25 samples instead of 24 samples. The calculations should reflect that change.

P1: Test a Perceptual Phenomenon

Statistics: The Science of Decisions Project Instructions

1. What is our independent variable? What is our dependent variable?

The independent variable, which is controlled, is the congruent condition and the dependent variable, which is measured, is time.

2. What is an appropriate set of hypotheses for this task? What kind of statistical test do you expect to perform? Justify your choices.

We are interested in the effects of reading congruent words vs. incongruent words and measuring whether there is a significant difference in time between the two conditions.

The Null Hypothesis states there is no significant difference ($H_0: \mu_C = \mu_I$). The Alternative Hypothesis states there is a difference ($H_A: \mu_C \neq \mu_I$).

We have 24 samples, which is a small sample size. We do not know the population standard deviation. However we can calculate the mean and standard deviation of the sample. Therefore we will be comparing sample means in a paired t-test, which will test whether the mean of the difference between paired observations is equal to a target value. The distribution of sample means is normal, i.e. the majority of participants will be within 1 – 2 standard deviation of the sample mean.

One statistical tests I expect to perform is a t-test, (small sample size & unknown population standard deviation), which I will use to reject or accept the null hypothesis.

The formula for t-statistic: $t = (\mu_C - \mu_I) / S / (\sqrt{n})$

A second statistical test I expect to perform is a confidence interval (CI) for the mean population difference, which is a range of values we suspect the population parameter lies between. I will use a 95% confidence level.

The formula for confidence interval (CI): $M_D \pm t_{\text{critical}} (S_D / \sqrt{n})$

A third statistical test I will perform is Cohen's d, the effect size measure or margin of error. This calculation will give us the distance between means in standardized units.

The formula for Cohen's d: $M_D - S_D$

3. Report some descriptive statistics regarding this dataset. Include at least one measure of central tendency and at least one measure of variability.

The data below illustrates measures of central tendency including Mean, and Median. Measures of variability include Variance and Standard Deviation for the differences in sample means.

Congruent	Incongruent	Difference		
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12.079	19.278	-7.199	0.586
16.791	18.741	-1.950	36.178
9.564	21.214	-11.650	13.581
8.630	15.687	-7.057	0.824
14.669	22.803	-8.134	0.029
12.238	20.878	-8.640	0.456
14.692	24.572	-9.880	3.668
8.987	17.394	-8.407	0.196
9.401	20.762	-11.361	11.534
14.480	26.282	-11.802	14.724
22.328	24.524	-2.196	33.279
15.298	18.644	-3.346	21.333
15.073	17.510	-2.437	30.556
16.929	20.330	-3.401	20.828
18.200	35.255	-17.055	82.632
12.130	22.158	-10.028	4.257
18.495	25.139	-6.644	1.744
10.639	20.429	-9.790	3.331
11.344	17.425	-6.081	3.549
12.369	34.288	-21.919	194.720
12.944	23.894	-10.950	8.911
14.233	17.960	-3.727	17.959
19.710	22.058	-2.348	31.548
16.004	21.157	-5.153	7.906

			-7.965		
14.051	22.016	<-- mean		23.667	<-- variance
14.357	21.018	<-- median		4.865	<-- stdv

Mean of congruent = 14.051

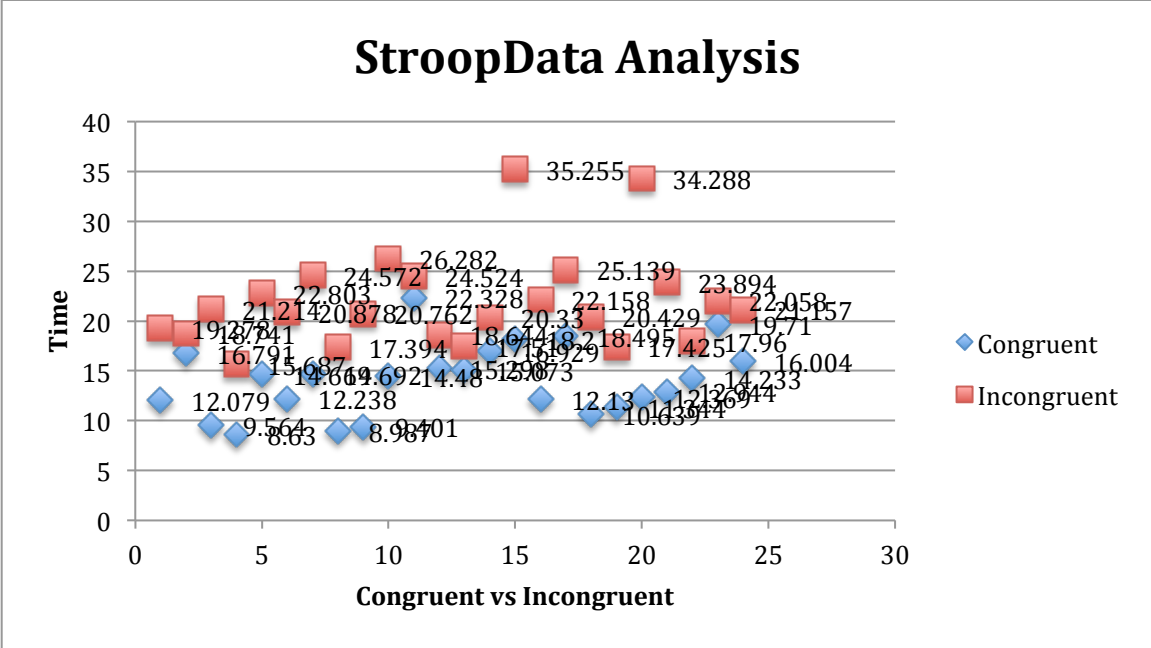
Mean of incongruent = 22.016

Variance of the differences = 23.667 (using Bessel's correction $n - 1$)

Standard deviation of the differences (S) = 4.865 (sqrt of the variance)

4. Provide one or two visualizations that show the distribution of the sample data. Write one or two sentences noting what you observe about the plot or plots.

Based on the scatter plot chart below of our sample data, the distribution of incongruent performance results is narrower than that of congruent results and contains fewer outliers. The incongruent times are higher on average than congruent times, indicating that it takes longer to read an equally sized list of words.



5. Now, perform the statistical test and report your results. What is your confidence level and your critical statistic value? Do you reject the null hypothesis or fail to reject it? Come to a conclusion in terms of the experiment task. Did the results match up with your expectations?

This statistical test is a dependent t-test for a paired sample, whereby the subject takes the same test twice. The Null Hypothesis (defined above) states that two population means will be the same. The Null assumes the difference in means will equal 0 (alternatively assumes they will not equal 0). We are testing to see if there is a significant difference in times between 2 population means and whether that is significantly different than 0.

Testing based on the following sample data:

Congruent	Incongruent
12.079	19.278
16.791	18.741
9.564	21.214
8.630	15.687
14.669	22.803
12.238	20.878
14.692	24.572
8.987	17.394
9.401	20.762
14.480	26.282
22.328	24.524
15.298	18.644
15.073	17.510
16.929	20.330
18.200	35.255

Difference	Sq Diff
-7.199	0.586
-1.950	36.178
-11.650	13.581
-7.057	0.824
-8.134	0.029
-8.640	0.456
-9.880	3.668
-8.407	0.196
-11.361	11.534
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			-7.965		
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Results:

Point estimation or difference between population of errors ($\mu_c - \mu_i$) = **-7.97**

Math: 14.051-22.016

Standard error (S) of the differences / stdv of each difference = **4.87**

Math: sqrt of 23.667

t-statistic ($(\mu_c - \mu_i) / S / (\sqrt{n})$) = **-8.02**

Math: -7.965/(4.865/4.899)

t-critical value ($\alpha = 0.05$) = +/- **2.069**

Math: using the t-table, 0.025 in each tail, and a df of 23 (n-1)

Cohen's d / effect size measure or margin of error ($M_D - S_D$) = **-1.64**

Math: -7.965/4.865

Confidence interval ($M_D \pm t_{\text{critical}} (S_D / \sqrt{n})$) = **-10.02 -5.91**

Math: -7.965 +/- 2.069 (4.865/4.899)

Conclusions:

Reject the Null (**Reject H_0**), since the t-statistic is in the critical region, past the t-critical value. Participant's times were significantly faster reading congruent vs. incongruent words. As a causal statement, the type of word had an effect on time. We can conclude on average participants were 1.6X faster reading congruent words vs. incongruent words.

Sources: Udacity, Wikipedia, Google