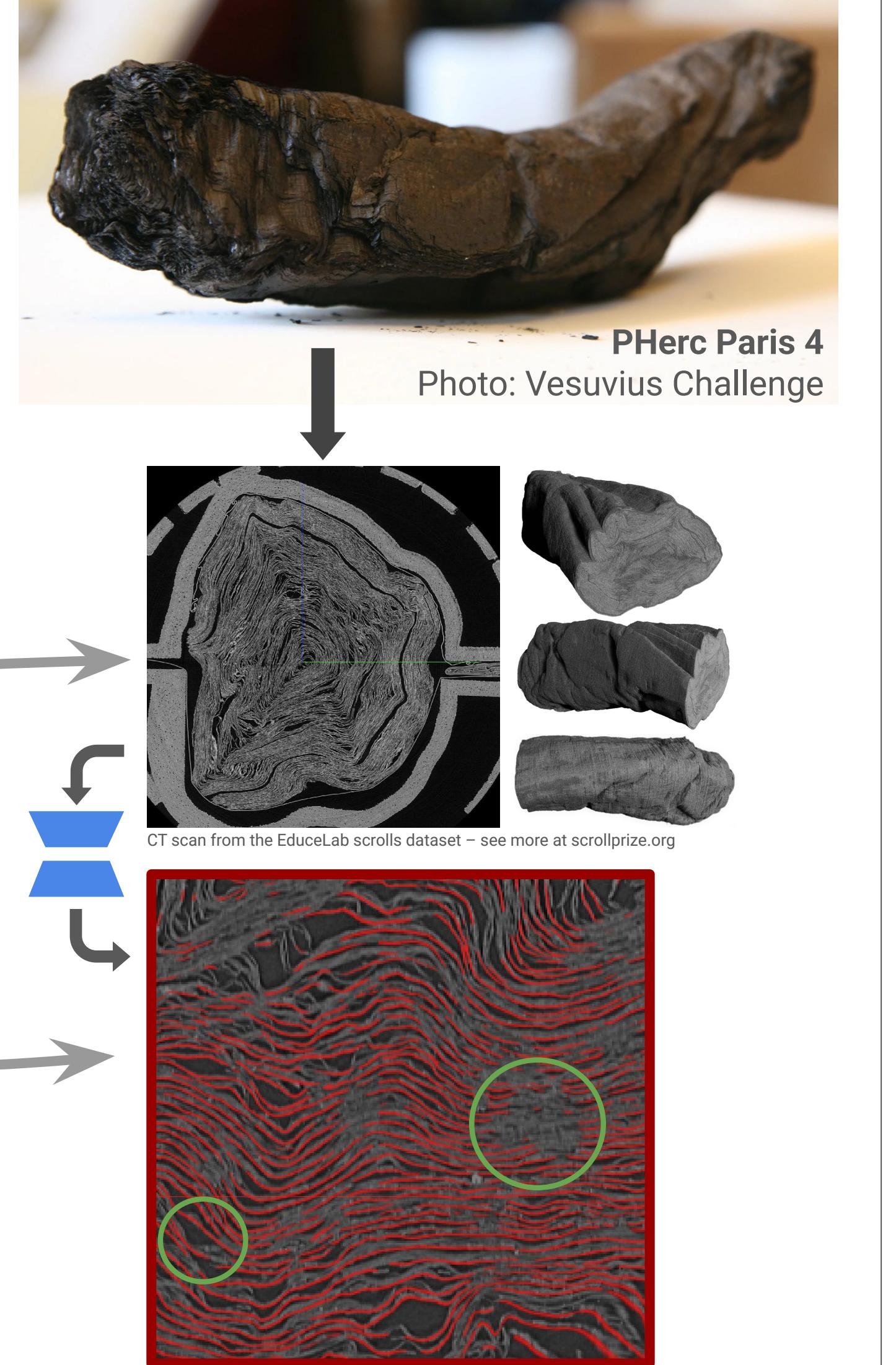


Virtually Unrolling the Herculaneum Papyri by Diffeomorphic Spiral Fitting

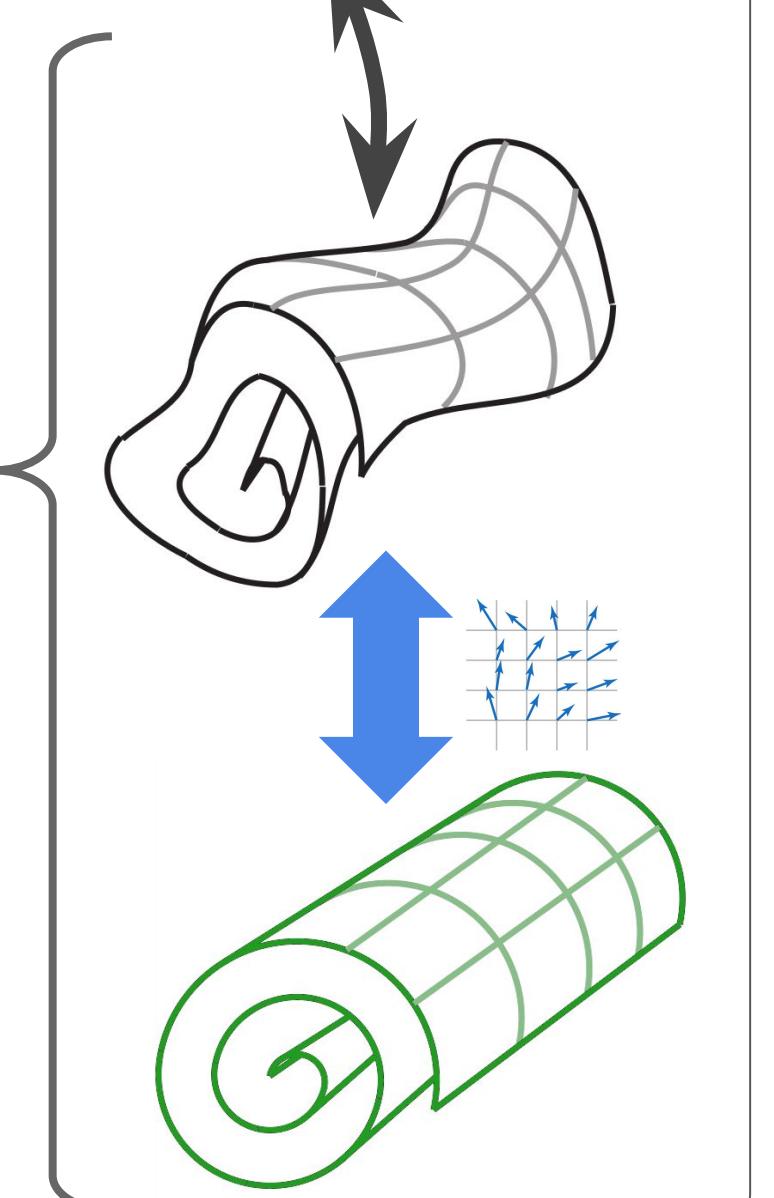
Paul Henderson

- AD79: papyrus scrolls charred & buried by Mount Vesuvius
- excavated starting c1752
- many are **impossible** to unroll physically
- solution: µCT scans + **virtual unrolling**
 - seek a 2D mesh representation of where the original papyrus surface passes in 3D
- **but:** CTs look like this 🤔
 - very dense
 - very distorted
 - some wraps broken / missing
- neural networks can *kinda* localise the sheet – but many gaps & false joins
- cannot easily 'read off' a 2D surface mesh



Idea

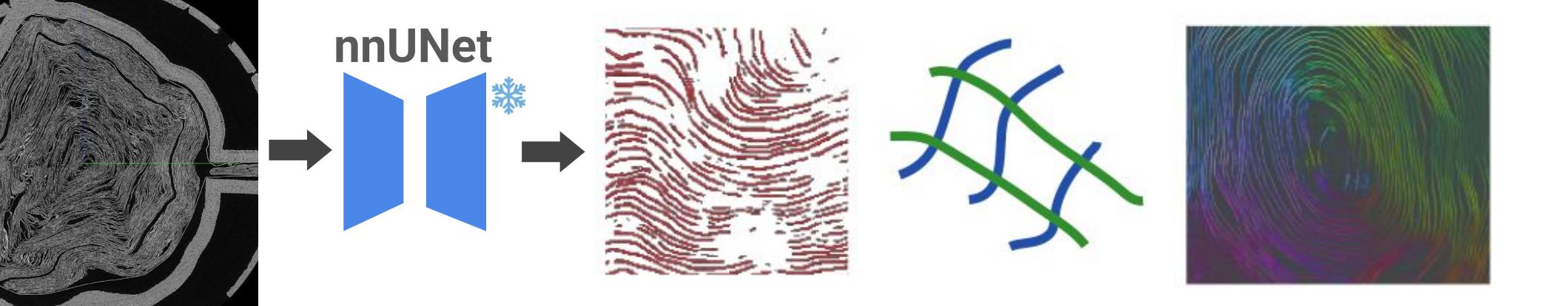
- the physical scroll is a rectangular sheet, rolled up, then badly distorted following the eruption
- our aim: invert this process, i.e. **find a 'good' rolled sheet + deformation that explains the observed scan data**
- the deformation is a **diffeomorphism** that distorts an **ideal scroll** into the shape in the scans
- very different to existing bottom-up methods!



Model

- ideal scroll: extruded archimedean spiral $s(\theta, z; \omega) = \left(-\frac{\omega}{\theta} \cos \theta, -\frac{\omega}{\theta} \sin \theta, z \right)$
 - free parameter: winding rate ω
- deformation: three **diffeomorphic** stages
 - z-dependent global xy-scale
 - integrated constant velocity field
 - local scaling of winding gaps
$$\begin{cases} \frac{d}{dt} \phi^{(t)}(\mathbf{x}) = \mathbf{u}(\phi^{(t)}(\mathbf{x})) \\ T_{\text{flow}}(\mathbf{x}) = \phi^{(1)}(\mathbf{x}) \\ \phi^{(0)}(\mathbf{x}) = \mathbf{x} \end{cases}$$

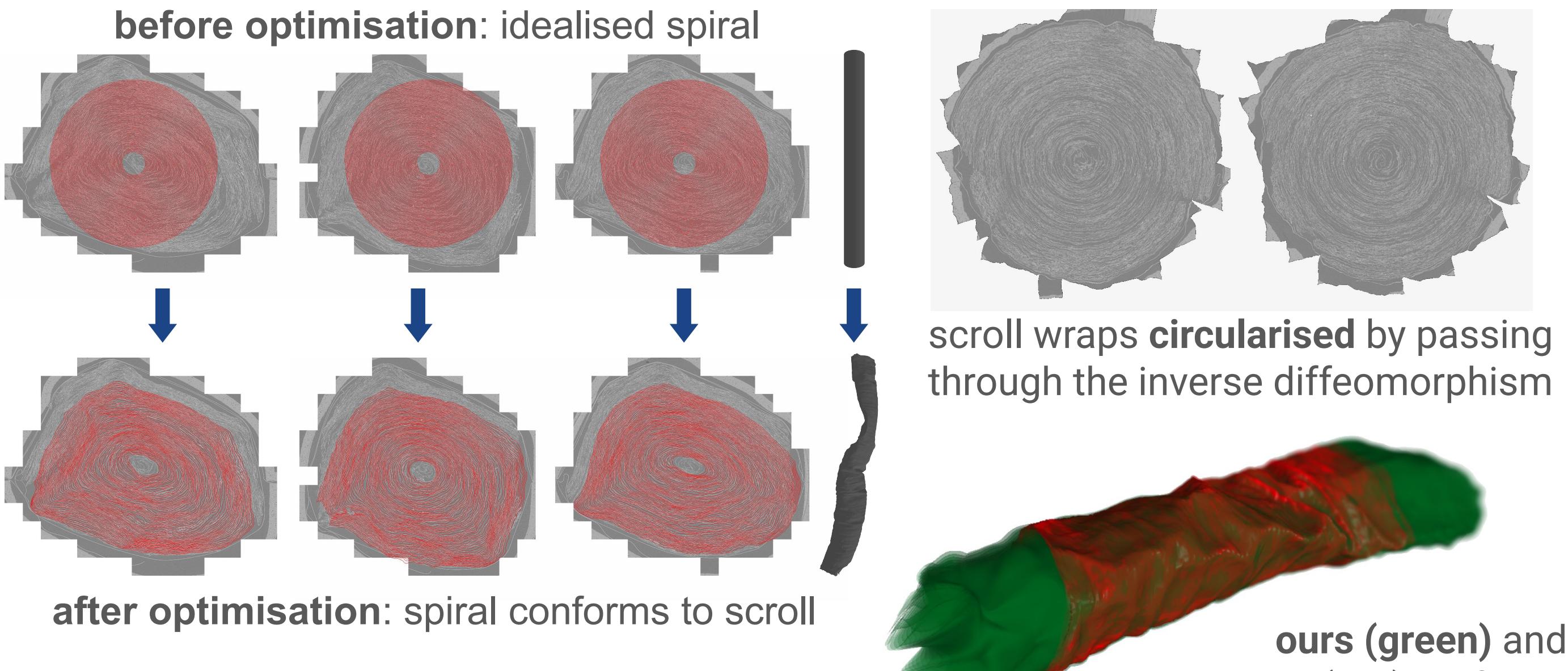
Fitting

- **targets:** use pre-trained nnUNet to extract (**imperfect**) **surfaces**, **papyrus fibers**, and **normals**
- optimise **winding density & diffeomorphism** jointly to match these
- **losses:**
 - (deformed) spiral normals match predictions
 - points on the same predicted surface (connected component) lie on the same deformed spiral winding
 - average spacing of deformed spiral windings matches that of predicted surfaces
 - each predicted surface/fiber is near one spiral winding



Results

- validated on two Herculaneum papyri
- quantitative results better *ThaumatoAnakalyptor*, the only other fully-automated approach that can tackle large portions of these scrolls



Ink visible in our unrolled version of PHerc 0172

Ink detected in our unrolled version of PHerc Paris 4