Novel Approaches to Fast Filling of Hydrogen Cylinders

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- 5 Engineering, Faculty of Engineering and the Environment, University of Southampton.

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6 Declaration

- I, Pau Miquel Mir, declare that this thesis and the work presented in it are my own and has been generated by me as the result of my own original research. I confirm that:
 - 1. This work was done wholly or mainly while in candidature for a degree at this University;
 - 2. Where any part of this thesis has previously been submitted for any other qualification at this University or any other institution, this has been clearly stated;
 - 3. Where I have consulted the published work of others, this is always clearly attributed;
 - 4. Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work;
 - 5. I have acknowledged all main sources of help;
 - 6. Where the thesis is based on work done by myself jointly with others, I have made clear exactly what was done by others and what I have contributed myself;
 - 7. None of this work has been published before submission.

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25 Abstract

This is the abstract.

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70 Acronyms

- 71 **CFD** Computational Fluid Dynamics
- ODE Ordinary Differential Equation

Todo list

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1 Introduction

{sec:introduction}

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Reword

1.1 Purpose of the investigation

Hydrogen is a very promising alternative fuel for the future, mainly due to the absence of greenhouse emissions when burning it. In this regard, it is superior to current petroleum- and, more generally, carbon-based fueling systems currently used by most road vehicles. However, air pollution is a negative externality associated with carbon-based fuels, as it is a cost to a third party (in this case, society as a whole) that is not accounted for in the price of the good. By definition, the negative consequences of polluting the air are not accounted for in the price of carbon vehicles, and therefore will have little influence on a consumer's choice. Thus, if hydrogen is to succeed as an alternative to carbon fuels, it is essential that its use be as, if not more, convenient than traditional fuel.

One of the main aspects where hydrogen currently lags behind traditional fuel is the refueling experience. Given that refueling hydrogen involves its compression, there is a significant rise in temperature, which must be kept below certain standards (358 °K as per SAE J2601). This in turn leads to long refueling times, potentially lasting more than five minutes, which is cumbersome for users. Therefore, it is of prime importance to research and develop systems that enable faster refueling of hydrogen cylinders. To this end, this project builds upon a model of filling a hydrogen cylinder which has already been developed by members of the department to analyse novel methods of improving fill times.

1.2 Outline of the investigation

One of the current solutions to improve fill times involves cooling the hydrogen before filling the cylinder as to keep it below he maximum temperature. However, this is quite expensive, both in energy terms and in economic terms. Consequently, the aim of this project is to continue exploring several of the options available to reduce fill times and simultaneously reduce the energy consumption of the process, thus improving both convenience for users and energy efficiency of the fueling stations. Indeed, by building upon the existing cylinder model several options shall be considered, namely: refrigeration, flow regulation, heat sink usage, active cooling, heat pipe usage, and phase change materials. From here, several options are open to further deepen or potentially broaden the investigation. An attempt to further simplify the model can be made, perhaps even reducing it so a simple algebraic relationship. Also, the model would benefit from FEA validation to aid our understanding of the heat transfer in the structure. This would go hand in hand with analysing the temperature of the structure, and seeing how close this matches the gas temperature. Indeed, if the structure is at a much lower temperature than the gas, the case can be made that the current regulations are slightly erroneous, as they are meant to protect the materials of the structure, but instead regulate the gas temperature.

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2 Background

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2.1 Objective

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We must firstly consider what real-world relevance of this project is. As explained in Section 1, the hydrogen cylinders being considered are for road vehicles. Although still an emerging technology, the basic functioning of a hydrogen fueled vehicle is relatively well established. They store compressed hydrogen in fuel tanks at high pressures, 35 and 70 MPa being the two current standards. This hydrogen is then used in the fuel cell and converted into electricity, which can be used directly by the electric motor or stored on onboard batteries. It therefore follows that the objectives of the hydrogen storage system are several:

- High fuel capacity
- Low overall weight
 - Low fill times

These goals have certain implications. Firstly, it is clear that several tradeoffs and compromises must be made. Increasing fuel capacity can be done by either using larger tanks, which leads to higher weight, or using higher pressures, which inevitably leads to higher temperatures. These higher temperatures are problematic due to material constraints as explained below in Section 2.1.1. Indeed, they lead to longer filling times as heat has to be allowed to dissipate through the tank walls. Thus, other solutions must be developed to minimize the temperature rise when filling to high pressures.

2.1.1 Material constraints

The main reason that a problem exists, and consequently this paper (and much other work) is being undertaken, is the material limitations that exist in hydrogen cylinders. Indeed, the cylinders that are used for high pressure scenarios such as the one we are presented with, are constructed with a composite material such as carbon fibre or glass/aramid fibre. In addition, they have a liner that is made out of metal, typically aluminum, in Type III cylinders, and out of a thermoplastic material for Type IV cylinders. Of concern is the composite material, as the polymer matrix cannot withstand high temperatures, and as such the material properties of the cylinder will begin to degrade. The specific temperature at which this occurs is usually around the glass transition temperature of the epoxy, where the thermosetting polymer changes from a hard "glassy" state to a more compliant "rubbery" state.

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2.2 Previous work

We must first establish a baseline of previous work that has been conducted in this field, and subsequently analyze the shortcomings that exist in order to direct the research.

2.2.1 Experimental work

{sec:exp

Several papers describe experimental work that has been conducted regarding the fast-filling of hydrogen cylinders, in particular comparing the results to simulations. Dicken and Mérida's work indicates that the temperature inside the cylinder is rather uniform [1]. This claim is not, however supported by the work of Zheng et al [2] nor that of Woodfield et al [3], wherein large discrepancies among gas temperatures in different regions of the cylinder are found.

$\{\mathtt{sec}: \mathtt{modelingWork}\}$

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2.2.2 Modeling Work

Computational Fluid Dynamics (CFD) A large amount of research has been conducted using multidimensional analysis, especially using CFD. Indeed, there are many papers describing different methods and setups, such as Dicken and Mérida's work, which uses the standard k- ε turbulence model and the Redlich-Kwong real gas equation of state for real gas properties [4]. Other investigations use more advanced property models, such as the one presented by Zhao et al., which employs REFPROP (see Section 2.5.3) in order to have more precise real gas properties [5].

Reduced order simulations Less work has been conducted regarding reduced order simulations, which employ assumptions such as axisymmetry or uniform gas temperature.

The work by Woodfield et al [3] presents a reduced order model employing a mass flow and internal energy balance for the compressed gas and one-dimensional unsteady heat conduction equation for the wall solved simultaneously. It uses the Lee-Kesler method [6] to find the compressibility and thus the density and from that the mass flow. The heat transfer coefficient between the gas and the wall is assumed to be constant: $500 \text{ W/(m}^2\text{K})$ during filling and $250 \text{ W/(m}^2\text{K})$ after full.

Similarly, the work by Monde et al [7] uses the same assumption regarding heat transfer coefficient values. They achieve a reasonable fit with experimental data, shown in Fig. 1, even though the measured heat transfer coefficients were significantly lower, shown in Table 1.

FIGURE 1: Comparison between estimated and measured temperatures by Monde et al [7]

{fig:mondeFit}

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TABLE 1: Heat transfer coefficents at various conditions by Monde et al [7]

2.2.3 Analysis

The simulation work that has been conducted can be, in broad terms, divided into complex CFD models and more simplified reduced dimensional models. It is important analyze the difference between these two systems.

CFD models have several advantages, as they take into consideration many things which reduced order models must simplify or assume. Firstly, one can represent the geometry of the cylinder more accurately using CFD. Secondly, time effects can be directly simulated without the need of timescales to be derived. However, they are extremely computationally expensive, with run times lasting from hours to weeks. It thus follows that the main advantage of reduced dimension models is that they are much less computationally expensive. This, in turn, means they can be incorporated as a part of larger analyses, in which they must be run multiple times, such as optimization routines or probabilistic whole station models.

Reduced dimension models up to date make assumptions that are difficult to support with evidence, and therefore lead to results not being very accurate. This leads to adjustments being made to the model to match the experimental data from the same experiment, which produces a better fit for the model, but leads to a less predictive model. For this reason, it is important to improve reduced order models by devising ways to calculate quantities previously assumed. This will improve the models' predictive ability, which will increase confidence in results from simulations regarding events which haven't been tried experimentally.

For instance, they assume a constant gas temperature, which, as outlined in Section 2.2.1, is supported by some experimental work, but refuted by others. For this reason, more research should be conducted to validate the uniform gas temperature approximation. Another assumption typically made is a constant heat transfer coefficient derived from time-averaged experimental results, as explained in Section 2.2.2. This report will propose a new method of deriving the heat transfer coefficient numerically to achieve better results.

209 2.3 Cylinder filling models

Several ways of modelling the cylinder can be considered when analysing their filling, with varying complexity and accuracy.

212 2.3.1 Zonal

A zonal model, also referred to as a 0-dimensional or reduced order model, refers to models that consider the gas inside the cylinder as the control volume, with homogenous properties. This allows for simpler calculations and much lower computational time.

2.3.2 Multidimensional

{sec:multidimension

Fill

More complex multidimensional models can be created, either 2D axisymmetric models or full 3D models. 2D models will not include the effects of gravity or buoyancy, but these can be considered

negligible, and the computational expense of full 3D simulations is rarely justifiable as the gains in accuracy are very small.

221 **2.4** Heat transfer models

In order to successfully analyse the behaviour of the system as a whole we must consider several local heat transfer methods that occur at different places inside of the cylinder.

224 **2.4.1** Impinging jet

The first behaviour that we will consider is that of an impinging jet of fluid onto a surface.

FIGURE 2: Impinging jet

 $\{ exttt{fig:inpinging_jet} \}$

fill

226 **2.4.2** Pipe flow

A second behaviour that we will consider is that of pipe flow. This behaviour has been the focus of much research, as it is arguably the most common mode of heat transfer that occurs in fluid systems.

{sec:turbulentJets}

2.4.3 Turbulent Jets

We must also consider turbulent jets, as the main driver of flow in the cylinder, which in turn drives convective heat transfer, is the turbulent jet that develops from the end of the nozzle throughout the length of the cylinder. Experimental results can be used to derive expressions for the axial velocity of the jet. Radial profiles of mean axial velocity can be seen in Fig. 3.

FIGURE 3: Radial profiles of mean axial velocity in a turbulent round jet with Re = 95,000. Adapted from [8] with the data from [9]

{fig:radialProfile}

By plotting the inverse of the non-dimensional speed, u_{exit}/u against x/d we get the clearly linear relationship shown in Fig. 4.

FIGURE 4: Jet speed vs distance. Adapted from [8] with the data from [9]

{fig:jetSpeed}

From this experimental result the following relationship is obtained:

where u(x) is the axial velocity at a distance x from the nozzle, x_0 is the position of the virtual origin, and c_1 is an empirical constant.

239 2.5 Methodology

Several techniques and methods will be used throughout the analysis. These are described in this section.

2.5.1 Optimization

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2.5.2 Non-dimensioning

Fill Section once work on optimization starts.

One of the fundamental principles used throughout this paper, and indeed, throughout engineering, is that of non-dimensioning. By operating using non-dimensional parameters such as the Reynolds number Re = $\frac{\rho uL}{v}$ or the Prandtl number Pr = $\frac{c_p \mu}{k}$ solving problems involving differential equations becomes simplified. Also, the analysis becomes much more general, and can be scaled.

2.5.3 Numerical methods

{sec:numerical_meth

Integrating Ordinary Differential Equations (ODEs) A central part of solving unsteady heat transfer problems involves integrating ODEs, as will be seen in Section 3. One of the simplest methods available, both conceptually and in terms of ease of implementing in code, is forward Euler time integration. It can be described as follows: given a function that can be defined by:

$$y'(t) = f(t, y(t)), \quad y(t_0) = y_0$$
 (2.2)

we can compute the approximate shape of the function given the initial point and finding the slope of the curve for small intervals. Indeed, from the initial point, we can find the tangent of the curve at that point, and take a small step along that tangent until arriving at the next point, where the procedure can be repeated. Denoting the step size as h, we can express forward Euler time integration as:

$$y_{n+1} = y_n + h f(t_n, y_n) (2.3)$$

{sec:property_model

Property models As the gases that are being treated in this report are at very high pressures, ideal gas approximations are inaccurate, and thus real gas properties must be employed. To this end, property models must be used, which can determine any gas property from two other independent properties.

The property model that will be employed throughout this analysis is REFPROP, a tool developed by the National Institute of Standards and Technology [10]. It uses values of critical and triple points together with equations for the thermodynamic and transport properties to calculate the state points of fluids.

66 3 Formulation

{sec:for

67 3.1 Governing equation

The governing equation for mass and internal energy of the gas in the tank is given by:

$$\frac{dU_{gas}}{dt} = \frac{d\left(m_{gas}u_{gas}\right)}{dt} = H_{in}\dot{m}_{in} - \dot{Q}_{out} \tag{3.1}$$

consistent time derivatives

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where U_{gas} is the total internal energy of the gas, m_{gas} is the mass of the gas, u_{gas} is the specific internal energy of the gas, $H_i n$ is the enthalpy of the inlet gas, \dot{m}_{in} the mass flow into the cylinder, and \dot{Q}_{out} is the rate of heat transfer out of the gas to the cylinder.

The change in internal energy of the gas is equal to the difference in energy entering the system in the enthalpy of gas inflow and the energy leaving the system through the walls of the cylinder. The enthalpy of the inlet can be determined from real gas models as a function of the inlet pressure and temperature. Therefore, to obtain the internal energy variation one must calculate the gas mass flow and the heat transferred to the cylinder.

278 3.2 Gas mass flow into cylinder

The nozzle and corresponding gas flow will be modeled using isentropic relations, and then a discharge coefficient relationship will be used to find the approximate real values. Indeed, the isentropic Reynold's number is first calculated as follows:

equ:reynoldsIdeal}}

$$Re_{ideal} = \frac{\rho_{exit} \ d_{inlet} \ u_{exit}}{\mu_{exit}}$$
 (3.2)

where d_{inlet} is the diameter of the inlet delivery pipe and ρ_{exit} , u_{exit} , and μ_{exit} are determined using real gas models as described in Section 2.5.3. More specifically:

$$\rho_{exit} = f(P_{exit}, S_{in}), \quad u_{exit} = \sqrt{2(H_{in} - H_{static})}, \quad \mu_{exit} = f(P_{exit}, S_{in})$$
(3.3)

where P_{exit} is the pressure at the end of the inlet tube, S_{in} is the entropy at the inlet, H_{in} the stagnation enthalpy at the inlet, H_{static} the static enthalpy at the end of the inlet tube. As the system is treated as isentropic, the inlet entropy can be used to calculate exit properties. We also have:

$$S_{in} = f(P_{in}, T_{in}), \quad H_{in} = f(P_{in}, T_{in}), \quad H_{static} = f(P_{exit}, S_{in})$$
 (3.4)

where P_{in} and T_{in} are the inlet pressure and temperature, respectively. The exit pressure P_{exit} is taken to be the pressure inside the gas tank. However, in the case that the inlet diameter is choked, these calculations would yield velocities higher than the speed of sound, which is impossible due to the nature of the inlet pipe. For this reason, if a velocity of Mach 1 or higher is achieved at any given time, an iterative process is used to find the value of P_{exit} that will yield a velocity equal to the speed of sound, and the rest of properties and ultimately the Reynolds number calculated accordingly.

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In order to find the real mass flow an empirical discharge coefficient is employed.

$$C_D = \frac{\dot{m}_{in}}{\dot{m}_{ideal}} = c_2 + c_3 \operatorname{Re}_{ideal}$$
 (3.5)

A discharge coefficient must be used to account for the formation of a boundary layer inside the inlet tube. The empirical model that was used was obtained from , and uses the following values:

Citation

$$c_2 = 0.938, \quad c_3 = -2.71$$
 (3.6)

From the real mass flow the actual Reynold's number of the inflow can be calculated and used to find

forced convection heat transfer coefficients in Section 3.3.1 and Eq. (3.11) as follows:

avoid forward references

$$Re = \frac{4\dot{m}_{in}}{\pi u d} \tag{3.7}$$

98 3.3 Heat transfer from gas to cylinder

The heat transferred from the gas to the wall of the tank is given by a simple convection relationship:

$$\dot{Q} = hA \left(T_{gas} - T_{wall} \right)$$
 (3.8) {{equ:convection}}

where A is the internal surface area of the cylinder, h is the heat transfer coefficient, and T_{gas} and T_{wall} are the temperatures of the gas and the wall, respectively. The heat transfer coefficient is a result of the combination of both forced and natural convection. This is expressed as follows, as per [11] and [12]:

$$h = \sqrt[4]{h_f^4 + h_n^4} \tag{3.9}$$

where h_f is the heat transfer coefficient due to forced convection and h_n is the heat transfer coefficient due to natural convection. Each coefficient can be non-dimensionalised using Nusselt's numbers, expressed as:

$$Nu_f = \frac{h_f D}{k}, \quad Nu_n = \frac{h_n D}{k}$$
(3.10)

where D is the characteristic length, in this case the diameter of the cylinder, and k, the thermal conductivity of the fluid. The values of the Nusselt's numbers can be determined from empirical correlations, as detailed in Sections 3.3.1 and 3.3.2.

3.3.1 Forced convection

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{sec:forcedConvect:

As the magnitude of heat transfer is related to the flow in forced convection, the Nusselt's number can be said to be a function of the Reynolds number, taking the form:

$$Nu_{f.ss} = c_4 Re^{c_5}$$
 (3.11) {{equ:nusseltReynol}

where $Nu_{f,ss}$ is the steady state Nusselt's number and the empirical constants c_4 and c_5 are given by as:

eltReynoldsConsts}}

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$$c_4 = , \quad c_5 =$$
 (3.12)

The initial work this project builds upon uses the flow at the nozzle to determine the heat transfer at the wall of the cylinder. This assumes that the hydrogen flows instantaneously from the nozzle to the wall, when in reality there is of course a time delay. This assumption is acceptable for stable inflows, hence us referring to the steady state Nusselt's number $Nu_{f,ss}$, but for more complex filling patterns and also for improved accuracy it becomes necessary to incorporate hysteresis. Indeed, the heat transfer coefficient at the wall in fact can be said to depend on the nozzle flow seconds prior, or more generally, on the history of the nozzle flow. This can be modeled as follows:

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$$\frac{d}{dt}\left(Nu_f\right) = \frac{Nu_{f,ss} - Nu_f}{\tau} \tag{3.13}$$

where τ is the time scale, which reflects the amount of time it takes for the flow to recirculate. Two time scales are considered, as two different situations may be present. The flow in the cylinder may be driven by the inflow of mass from the nozzle, in which case we have a time scale of production τ_{prod} . However, if the inflow halts, the flow field in the cylinder will be driven by the dissipation of the existing flow and thus the time scale is denoted τ_{diss} . Therefore the overall time scale is given by the minimum of these two:

explain why it's minimum

$$\tau = \min\left(\tau_{prod}, \tau_{diss}\right) \tag{3.14}$$

The production time scale is given by the spatial integral of the axial speed of the jet, which is given in Eq. (2.1) in Section 2.4.3.

$$\tau_{prod} = \int_0^L \frac{1}{u(x)} dx = \frac{1}{c_1 u_{exit}} \int_0^L (x - x_0) dx
= \frac{\frac{L^2}{2} - x_0 L}{c_1 du_{exit}}$$
(3.15)

As we have $x_0 \ll L$ we can write:

$$\tau_{prod} = \frac{L^2}{2c_1 du_{exit}} \tag{3.16}$$

and defining $c_6 = \frac{1}{2c_1}$:

$$\tau_{prod} = c_6 \frac{L^2}{u_{exit}d} \tag{3.17}$$

The dissipation time scale can be said to be proportional to the length of the cylinder L and the recirculation velocity u_{recirc} :

$$\tau_{diss} = c_7 \frac{L}{u_{recirc}} \tag{3.18}$$

Let us assume that instantaneous Nusselt's number depends on u_{recirc} as it depends on Re^{c_5} and $c_5 \sim \mathcal{O}(1)$. From Eq. (3.11) we know that:

$$\frac{Du_{recirc}}{v} = c_8 \text{Nu}_f \tag{3.19}$$

We can therefore rewrite:

$$\tau_{diss} = \frac{c_7}{c_8} \frac{LD}{v N u_f} \tag{3.20}$$

Combining the two constants and absorbing the L/D coefficient:

$$\tau_{diss} = c_9 \frac{L^2}{v N u_f} \tag{3.21}$$

We can then make use of the fact that in steady state we know $au_{prod} = au_{diss}$, which leads to:

$$\tau_{diss} = c_9 \frac{L^2}{v_{\text{Nu}_f}} = c_6 \frac{L^2}{u_{exit}d}$$
 (3.22)

Substituting the definitions of Nusselt's and Reynolds numbers from Eqs. (3.2) and (3.11):

$$c_9 = c_6 \frac{v \text{Nu}_f}{u_{\text{orit}} d} = c_4 c_6 \tag{3.23}$$

Which leads to a final definition of au_{diss} interms of literature constants ::

$$\tau_{diss} = \frac{c_4}{2c_1} \frac{L^2}{v \operatorname{Nu}_f} \tag{3.24}$$

Therefore, in a pure dissipation scenario, where $Nu_{f,ss} \rightarrow 0$, we have:

$$\frac{d}{dt}\left(\mathrm{Nu}_f\right) = -\mathrm{Nu}_f^2 \frac{2c_1}{c_4} \frac{v}{LD} \tag{3.25}$$

Thus, when the inflow stops the heat transfer at the wall will decrease quadratically.

3.3.2 Natural convection

{sec:naturalConvect

Natural convection is caused by buoyancy driven flow, so the natural Nusselt's number can be found to be related to the Rayleigh's number (itself a product of Grashof's and Prandt's numbers) by the following relationship:

$$Nu_n = c_{10} Ra^{c_{11}} (3.26)$$

where Rayleigh's number is defined as:

$$Ra = \left| \frac{g\beta \left(T_{wall} - T_{gas} \right) D^3}{v\alpha} \right| \tag{3.27}$$

where g is the acceleration due to gravity, β is the coefficient of thermal expansion, D is the characteristic length, in this case the cylinder diameter, v is the kinematic viscosity, and α is the thermal diffusivity, as defined by:

nermalDiffusivity}}

cite

$$\alpha = \frac{k}{\rho c} \tag{3.28}$$

where k is the material's thermal conductivity, ρ is the density of the material, and c is the specific heat capacity of the material. The coefficients are given by:

$$c_{10} =, \quad c_{11} = \tag{3.29}$$

3.4 Heat transfer across cylinder

The main mode of heat transfer that occurs in the cylinder and that will be used throughout this report is heat conduction through the wall of the cylinder. This is modeled using:

$$\frac{\partial T}{\partial t} = \alpha \frac{\partial^2 T}{\partial x^2} \tag{3.30}$$

where α is the thermal diffusivity, as defined in Eq. (3.28). This differential equation will be solved using forward Euler time integration as described in Section 2.5.3. Solving this equation will yield the temperature distribution throughout the thickness of the cylinder wall, and more specifically, the internal wall temperature that is used to calculate the heat transferred out of the gas in Eq. (3.8).

360 3.4.1 Discretization

361 **3.4.2 Outer Wall**

52 3.5 Throttling

Throttling is introduced in order to more accurately represent real life conditions. When a maximum temperature is reached, the inflow of hydrogen must be stopped in order to protect the materials of the tank, as detailed in Section 2.1.1. A simple method of throttling, with the flow stopping at the designated maximum temperature, 85 °C, and the flow restarting at a chosen temperature. The optimum temperature at which flow restarts was considered in this study, and results are presentedl in ??

3.6 Optimization

General stuff:

- Check tense and person
- Check for repetition
- Check for excessive verbose

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4 Results

 $\{sec:results\}$

5 Discusion

{sec:discusion}

6 Conclusion

{sec:conclusion}

This is the conclusion.

5 Appendices

A Filling Code

{app:filling_code}

```
%Author: Vishagen Ramasamy
   %Date: -
   % Copyright University of Southampton 2017.
   \% No warranty either expressed or implied is given to the results produced
   % by this software. Neither the University, students or its employees
   %accept any responsibility for use of or reliance on results produced by
   %this software.
   %% script that computes the filling of the tank(s)
10
   %% Importing the pressure and temperature profile at the entrance of the delivery pipe from Dicken a
11
12
   % and calulating the stagnation enthalpy and entropy
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   for j = 1:maxt
        time(j+1) = (j)*dt;
                                                                                    % Time as filling proce
15
        for i = 1:tank_number
16
            \% Select inlet pressure / temperature profile based on user input
17
18
            if blnUseStandardData == 1
19
                % Constant inlet pressure profile
                P_inlet(i,j+1) = ConstPressKPa;
20
21
            else
                % Read inlet pressure profile from specified file
22
23
                P_inlet(i, j+1) = interp1(InletPressureData(:,1),InletPressureData(:,3), dt*j);
            end
24
25
            if blnUseStandardData == 1
26
                %Temp_inlet(i,j+1) = interp1(time_in, temp_in, dt*j);
27
                                                                          % Temperature profile after the
                Temp_inlet(i, j+1) = ConstTempK;
28
            else
29
                % Read inlet temperature profile from specified file
30
31
                Temp_inlet(i, j+1) = interp1(InletTempData(:,1), InletTempData(:,3), dt*j);
            end
32
33
            h_inlet(i,j+1) = refpropm('H','T',Temp_inlet(i,j+1),'P',P_inlet(i,j+1),Fluid{i}, refpropdir)
34
            entropy_inlet(i,j+1) = refpropm('S','T',Temp_inlet(i,j+1),'P',P_inlet(i,j+1),Fluid{i}, refpr
35
36
            %% Determine which pressure to use at the exit of the delivery pipe which is dependent upon
37
38
39
            if l_d(i) > 3 \&\& blnOneZone{i} == 0
                                                           % The length-to-diameter ratio of the tank(s) d
                Pressure_exit = P_gas_zone1{i}(j);
                                                      \% The pressure at the exit of the delivery pipe is
40
41
42
                Pressure_exit = P_gas(i,j);
                                                      % The pressure at the exit of the delivery pipe is
43
44
            if (P_inlet(i,j+1) > Pressure_exit) % condition for filling of tank(s)
45
                sound_exit(i,j+1) = refpropm('A','P',Pressure_exit,'S',entropy_inlet(i,j+1),Fluid{i}, re
46
                h_static_exit(i,j+1) = refpropm('H','P',Pressure_exit,'S',entropy_inlet(i,j+1),Fluid{i},
47
                visc_exit(i,j+1) = refpropm('V','P',Pressure_exit,'S',entropy_inlet(i,j+1),Fluid{i}, ref
48
                mach_{exit(i,j+1)} = sqrt(2*(h_{inlet(i,j+1)}-h_{static_{exit(i,j+1)}})/sound_{exit(i,j+1)}^2);
49
50
                %% If Mach number is greater than one, the exit pressure is greater than the pressure wi
51
                \% is incremetally increased and iterated in a while loop until mach number is equal to
52
53
54
                Inlet_entropy = entropy_inlet(i,j+1);
55
                Inlet_stagnation_enthalpy = h_inlet(i,j+1);
56
                P_guess = Pressure_exit;
57
58
                if mach_exit(i,j+1) > 1
                    Pressure_exit = find_exit_pressure(Inlet_stagnation_enthalpy,Inlet_entropy,Fluid{i},
59
                    sound_exit(i,j+1) = refpropm('A','P',Pressure_exit,'S',Inlet_entropy,Fluid{i}, refpr
60
                    h_static_exit(i,j+1) = refpropm('H','P',Pressure_exit,'S',Inlet_entropy,Fluid{i}, re
61
```

```
visc_exit(i,j+1) = refpropm('V','P',Pressure_exit,'S',Inlet_entropy,Fluid{i}, refpropdir);
   62
                                                                                                    mach_{exit(i,j+1)} = sqrt(2*(h_{inlet(i,j+1)-h_{static_exit(i,j+1)})/sound_{exit(i,j+1)^2});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        % C
   63
                                                                                 end
   64
   65
   66
                                                                                 %% Calculation of the mass flow rate into the tank(s)
   67
                                                                                 rho_exit(i,j+1) = refpropm('D','P',Pressure_exit,'S',Inlet_entropy,Fluid{i}, refpropdir);
   68
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % Calcui
                                                                                 vel_exit(i,j+1) = mach_exit(i,j+1)*sound_exit(i,j+1);
   69
                                                                                 Re_exit_isentropic(i,j+1) = rho_exit(i,j+1) *d_inlet*vel_exit(i,j+1)/visc_exit(i,j+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % Calcu
   70
   71
                                                                                 cd(i,j+1) = I + J/(Re_exit_isentropic(i,j+1)^(0.25));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % Calcui
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % Calcu
   72
                                                                                 mfr(i,j+1) = cd(i,j+1)*rho_exit(i,j+1)*vel_exit(i,j+1)*A_inlet;
                                                                                 Re_entrance_actual(i,j+1)= 4*mfr(i,j+1)/(pi*d_inlet*visc_exit(i,j+1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % Calcu
   73
   74
                                                                                 dM_inlet = mfr(i,j+1)*dt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    % Amoun
                                                             end
   75
   76
                                                             %% Heat transfer calculations & caluclations of the thermodynamic properties of the gas in the tank(s)
   77
                                                             if l_d(i) \le 3 \mid blnOneZone\{i\} == 1
   78
   79
                                                                                                                                                   a_1*Re_entrance_actual(i,j+1)^(b_1);
                                                                                 Nus(i,j+1) =
                                                                                                                                                                                                                                                                                                                                                                                                                                        % Nusselt number and Reynolds
   80
                                                                                 k_gas(i,j+1) = refpropm('L','T',Temp_gas(i,j),'P',P_gas(i,j),Fluid{i}, refpropdir); % Thermal condu
   81
   82
                                                                                 heat\_coef\_forced(i,j+1) = Nus(i,j+1)*k\_gas(i,j+1)/d\_tank(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                        % Calculation of the heat tran
   83
                                                                                 if Inner_wall_boundary(i) == 1
   84
                                                                                                    Qsurf(i,j+1) = -dt*surf_area(i)*heat_coef_forced(i,j+1)*(Temp_gas(i,j)-Inner_temp_wall_isothermatical entry and interpretation of the content of the content
   85
   86
                                                                                 else
                                                                                                    87
                                                                                                    Temp_wall\{i\}(1,j+1) = Temp_wall\{i\}(1,j) + CFL_liner(i)*(Temp_wall\{i\}(2,j) - Temp_wall\{i\}(1,j) - Q_i 
   88
   89
   90
                                                                                                    if Outer_wall_boundary(i)==1
                                                                                                                       Temp_wall{i}(number_of_gridpoints(i),j+1) = Outer_temp_wall_isothermal(i);
   91
   92
                                                                                                                         Temp_wall{i}(number_of_gridpoints(i),j+1) = Temp_wall{i}(number_of_gridpoints(i),j)+2*CFL_1
   93
   94
                                                                                                    \mbox{\ensuremath{\mbox{\%}}} Computation of the temperature of the struture of the tank(s)
   95
   96
                                                                                                    for k=2:number_of_gridpoints(i)-1
                                                                                                                        if (k>=2)&&(k<=int_pt_liner_laminate(i)-1)</pre>
   97
                                                                                                                                            \label{temp_wall_i} Temp\_wall\{i\}(k,j+1) = Temp\_wall\{i\}(k,j) + CFL\_liner(i) * (Temp\_wall\{i\}(k+1,j) - 2*Temp\_wall\{i\}(k+1,j) + (Temp\_wall(k+1,j) - 2*Temp\_wall(k+1,j) + (Temp\_wall(k+1,j) + (Temp\_wall(k+1,j) + (Temp\_wall(k+1,j) + (Temp\_wall(k+1,j) + (Temp\_wall(k+1,j) + (Temp\_wall(k+1,j) 
   98
                                                                                                                         elseif (k>=int_pt_liner_laminate(i)+1)&&(k<=number_of_gridpoints(i)-1)
   99
                                                                                                                                           Temp_wall\{i\}(k,j+1) = Temp_wall\{i\}(k,j) + CFL_laminate(i) * (Temp_wall\{i\}(k+1,j) - 2 * Temp_wall\{i\}(k,j+1) = Temp_wall\{i\}(k,j) + CFL_laminate(i) * (Temp_wall\{i\}(k+1,j) - 2 * Temp_wall\{i\}(k,j+1) = Temp_wall\{i\}(k,j) + CFL_laminate(i) * (Temp_wall\{i\}(k+1,j) - 2 * Temp_wall\{i\}(k+1,j) - 2 * Temp_wall(i) - 2 * Temp_wall
100
101
                                                                                                                         else
                                                                                                                                            Temp_wall{i}(k,j+1) = (cond_laminate(i)*(Temp_wall{i}(k+1,j)+CFL_laminate(i)*(Temp_wall-
102
103
                                                                                                                         end
                                                                                                    end
104
105
                                                                                 end
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         % Mass of gas in
                                                                                 m_{gas}(i,j+1) = m_{gas}(i,j) + dM_{inlet};
106
                                                                                 \label{eq:loss_surf} Ugas(\texttt{i},\texttt{j}+\texttt{1}) = Ugas(\texttt{i},\texttt{j}) + Qsurf(\texttt{i},\texttt{j}+\texttt{1}) + h_inlet(\texttt{i},\texttt{j}+\texttt{1}) * dM_inlet;
107
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         % Internal energy
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         % Specific energy
                                                                                 u_{gas}(i,j+1) = U_{gas}(i,j+1)/m_{gas}(i,j+1);
108
109
                                                                                 rho_gas(i,j+1)=m_gas(i,j+1)/vol_tank(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         % Density of the
                                                                                P_gas(i,j+1) = refpropm('P','D',rho_gas(i,j+1),'U',u_gas(i,j+1),Fluid{i}, refpropdir);
Temp_gas(i,j+1) = refpropm('T','D',rho_gas(i,j+1),'U',u_gas(i,j+1),Fluid{i}, refpropdir);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  %
110
111
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 %
112
                                                             else
113
                                                                               Re_compression(i,j+1) = Re_entrance_actual(i,j+1)*(d_inlet/d_tank(i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         % Reynolds number
114
115
                                                                                 Nus_zone1{i}(j+1) = a_1*Re_entrance_actual(i,j+1)^(b_1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         % Nusselt number
116
                                                                                 Nus_{zone2\{i\}(j+1)} = c_1*Re_{compression(i,j+1)^(d_1)};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         % Nusselt number
117
118
                                                                                 k_gas_zone1{i}(j+1) = refpropm('L','T',Temp_gas_zone1{i}(j),'P',P_gas_zone1{i}(j),Fluid{i}, refprop
119
                                                                                 k\_gas\_zone2\{i\}(j+1) = refpropm('L','T',Temp\_gas\_zone2\{i\}(j),'P',P\_gas\_zone2\{i\}(j),Fluid\{i\}, refpropm('L','T',Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Temp\_gas\_zone2\{i\}(j),Te
120
121
                                                                                \label{eq:heat_coef_forced_zone1_i} $$ heat_coef_forced_zone1_{i}(j+1) = Nus_zone1_{i}(j+1)*k_gas_zone1_{i}(j+1)/d_tank(i); $$ heat_coef_forced_zone1_{i}(j+1)/d_tank(i); $$ h
122
                                                                                \label{eq:heat_coef_forced_zone2} \begin{aligned} \text{heat\_coef\_forced\_zone2}\{i\}(j+1) &= \text{Nus\_zone2}\{i\}(j+1) * \text{k\_gas\_zone2}\{i\}(j+1)/1 \text{\_zone2\_total}(i); \end{aligned}
123
124
125
                                                                                 \% Step 1. Equating the respecting values of zone 1 and zone 2 to
                                                                                 \mbox{\ensuremath{\mbox{\%}}} matrices with 'similar' names
126
```

127

193

```
Vgas(1)=volume_zone1(i);
128
                                                                               Vgas(2)=volume_zone2(i);
129
                                                                               Mgas(1)=m_gas_zone1{i}(j);
130
131
                                                                               Mgas(2)=m_gas_zone2{i}(j);
132
                                                                               Ugas_twozone(1)=u_gas_zone1{i}(j)*Mgas(1);
                                                                               Ugas_twozone(2)=u_gas_zone2{i}(j)*Mgas(2);
133
134
                                                                               Asurf(1)=surface_area_zone1(i);
                                                                               Asurf(2)=surface_area_zone2(i);
135
                                                                               Tgas(1)=Temp_gas_zone1{i}(j);
136
                                                                               Tgas(2)=Temp_gas_zone2{i}(j);
137
138
                                                                               if Inner_wall_boundary(i) == 1
                                                                                                   Twall(1,1)=Inner_temp_wall_isothermal(i);
139
140
                                                                                                   Twall(2,1)=Inner_temp_wall_isothermal(i);
                                                                               else
141
142
                                                                                                   Twall(1,1)=Temp_wall_zone1{i}(1,j);
                                                                                                   Twall(2,1)=Temp_wall_zone2{i}(1,j);
143
                                                                               end
144
                                                                               % Step 2: apply the change of internal energy due to heat transfer and mass
145
                                                                               % input through nozzle:
146
147
148
                                                                               dM_inlet = mfr(i,j+1)*dt;
149
                                                                               Qsurf(1)=- dt*Asurf(1)*(heat_coef_forced_zone1{i}(j+1))*(Tgas(1)-Twall(1,1));
150
                                                                               Qsurf(2)=- dt*Asurf(2)*(heat_coef_forced_zone2{i}(j+1))*(Tgas(2)-Twall(2,1));
151
152
                                                                               Ugas_twozone(1)=Ugas_twozone(1)+Qsurf(1)+h_inlet(i,j+1)*dM_inlet;
153
                                                                               Ugas_twozone(2)=Ugas_twozone(2)+Qsurf(2);
154
155
156
                                                                               Mgas(1)=Mgas(1)+dM_inlet;
                                                                               Mgas(2)=Mgas(2);
157
                                                                               for m=1:2
159
                                                                                                  hgas(m)=refpropm('H','D',Mgas(m)/Vgas(m),'U',Ugas_twozone(m)/Mgas(m),Fluid{i}, refpr
160
                                                                               end
161
162
163
                                                                               \% Step 2: Find the amount of mass that needs to be transferred from zone 1
164
                                                                               % to zone 2 to equalise their pressure
165
                                                                               % (we assume forward Euler integration, therefore we use the specific
166
167
                                                                               \% enthalpies h from the start of the timestep. We provide enthalpies for
                                                                               % both zones in case the flow gets reversed).
168
169
                                                                               dM_guess = dM_inlet*(volume_zone2(i)/(volume_zone1(i)+volume_zone2(i))) ;
170
171
                                                                               dM_12 = find_dM_12(hgas,Vgas,Mgas,Ugas_twozone,Fluid{i},dM_guess, refpropdir);
172
173
                                                                               \% Step 3: Apply this change to the mass and update all properties:
174
175
                                                                               m_{gas\_zone1{i}(j+1)=Mgas(1)-dM_12;
                                                                               m_{gas\_zone2{i}(j+1)=Mgas(2)+dM_12;
176
177
                                                                               u_{gas}=0 u_{g
178
                                                                               u_{gas_{zone}(1)}(j+1)=(U_{gas_{two_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(1)+min(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2))/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{gas_{zone}(2)+max(0,dM_{12})*hgas(2)/m_{g
179
180
                                                                               rho_gas_zone1{i}(j+1)=m_gas_zone1{i}(j+1)/volume_zone1(i);
181
                                                                               182
183
                                                                               \label{temp_gas_zone1} Temp\_gas\_zone1\{i\}(j+1) = refpropm('T', 'D', rho\_gas\_zone1\{i\}(j+1), 'U', u\_gas\_zone1\{i\}(j+1), Farabox{ and } farabox{ also } farabox{ 
184
                                                                               Temp\_gas\_zone2\{i\}(j+1) = refpropm('T','D', rho\_gas\_zone2\{i\}(j+1),'U', u\_gas\_zone2\{i\}(j+1), Full formula for the context of t
185
186
                                                                               P_{gas\_zone1\{i\}(j+1)=refpropm('P','D',rho\_gas\_zone1\{i\}(j+1),'U', u\_gas\_zone1\{i\}(j+1),Flui}
187
                                                                               P_gas_zone2{i}(j+1)=refpropm('P','D',rho_gas_zone2{i}(j+1),'U', u_gas_zone2{i}(j+1),Flui
188
189
                                                                               m_{gas}(i,j+1) = m_{gas}zone1\{i\}(j+1) + m_{gas}zone2\{i\}(j+1);
190
191
                                                                               rho_gas(i,j+1) = m_gas(i,j+1)/vol_tank(i);
                                                                                u_{gas}(i,j+1) = (u_{gas\_zone1}\{i\}(j+1)*m_{gas\_zone1}\{i\}(j+1) + u_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)*m_{gas\_zone2}\{i\}(j+1)
192
```

 $Ugas(i,j+1) = u_gas(i,j+1)*m_gas(i,j+1);$

```
Temp_gas(i,j+1) = refpropm('T','D',rho_gas(i,j+1),'U',u_gas(i,j+1),Fluid{i}, refpropdir);
 194
                                                                                                                                                           P_gas(i,j+1) = refpropm('P','D',rho_gas(i,j+1),'U',u_gas(i,j+1),Fluid{i}, refpropdir);
 195
 196
 197
                                                                                                                                                           if Inner_wall_boundary(i) == 1
                                                                                                                                                                                                 198
                                                                                                                                                                                                 Qsurf_zone2{i}(j+1) = -dt*surface_area_zone2(i)* heat_coef_forced_zone2{i}(j+1)*(Temp_gas_zone2
 199
 200
                                                                                                                                                           else
                                                                                                                                                                                                 Qsurf_zone1{i}(j+1) = -dt*surface_area_zone1(i)* heat_coef_forced_zone1{i}(j+1)*(Temp_gas_zone1
 201
                                                                                                                                                                                               Qsurf\_zone2\{i\}(j+1) = -dt * surface\_area\_zone2(i) * heat\_coef\_forced\_zone2\{i\}(j+1) * (Temp\_gas\_zone2(i) * forced\_zone2(i) * forced\_zone2
 202
 203
                                                                                                                                                                                               Temp\_wall\_zone1\{i\}(1,j+1) = Temp\_wall\_zone1\{i\}(1,j) + CFL\_liner(i)*(Temp\_wall\_zone1\{i\}(2,j) - Temp\_wall\_zone1\{i\}(2,j) + CFL\_liner(i)*(Temp\_wall\_zone1\{i\}(2,j) - Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Temp\_wall\_zone1*(i)*(Tem
 204
                                                                                                                                                                                                 Temp\_wall\_zone2\{i\}(1,j+1) = Temp\_wall\_zone2\{i\}(1,j) + CFL\_liner(i)*(Temp\_wall\_zone2\{i\}(2,j) - Temp\_wall\_zone2\{i\}(2,j) + 
 205
 206
                                                                                                                                                                                                 if Outer_wall_boundary(i)==1
 207
                                                                                                                                                                                                                                      Temp_wall_zone1{i}(number_of_gridpoints(i),j+1) = Outer_temp_wall_isothermal(i);
 208
                                                                                                                                                                                                                                        Temp_wall_zone2{i}(number_of_gridpoints(i),j+1) = Outer_temp_wall_isothermal(i);
 209
                                                                                                                                                                                                 else
 210
                                                                                                                                                                                                                                        Temp_wall_zone1{i}(number_of_gridpoints(i),j+1) = Temp_wall_zone1{i}(number_of_gridpoints(i)
211
                                                                                                                                                                                                                                        Temp_wall_zone2{i}(number_of_gridpoints(i),j+1) = Temp_wall_zone2{i}(number_of_gridpoints(i)
212
                                                                                                                                                                                                 end
213
 214
                                                                                                                                                                                                 % Computation of the temperature of the struture of the tank(s)
                                                                                                                                                                                                 for k=2:number_of_gridpoints(i)-1
215
                                                                                                                                                                                                                                        if (k>=2)&&(k<=int_pt_liner_laminate(i)-1)</pre>
                                                                                                                                                                                                                                                                             Temp_wall_zone1{i}(k,j+1) = Temp_wall_zone1{i}(k,j)+CFL_liner(i)*(Temp_wall_zone1{i}(k+
217
                                                                                                                                                                                                                                                                            \label{temp_wall_zone2} Temp_wall_zone2\{i\}(k,j) + CFL_liner(i)*(Temp_wall_zone2\{i\}(k+1)) + CFL_liner(i)*(Temp_wall_zo
 218
                                                                                                                                                                                                                                        elseif (k>=int_pt_liner_laminate(i)+1)&&(k<=number_of_gridpoints(i)-1)
219
                                                                                                                                                                                                                                                                            \label{temp_wall_zone1} Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_wall_zone1*(Temp_w
 220
                                                                                                                                                                                                                                                                            \label{temp_wall_zone2} Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k,j)+CFL_laminate(i)*(Temp_wall_z
221
 222
                                                                                                                                                                                                                                                                            Temp\_wall\_zone1\{i\}(k,j+1) = (cond\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1\{i\}(k+1,j)+CFL\_laminate(i)*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_wall\_zone1*(Temp\_w
223
                                                                                                                                                                                                                                                                            Temp_wall_zone2\{i\}(k,j+1) = (cond_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(k+1,j)+CFL_laminate(i)*(Temp_wall_zone2\{i\}(
 224
                                                                                                                                                                                                                                        end
225
 226
                                                                                                                                                                                                 end
                                                                                                                                                           end
 227
 228
 229
                                                                                                                      end
 230
                                                                                  end
231
                                         end
232
```

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