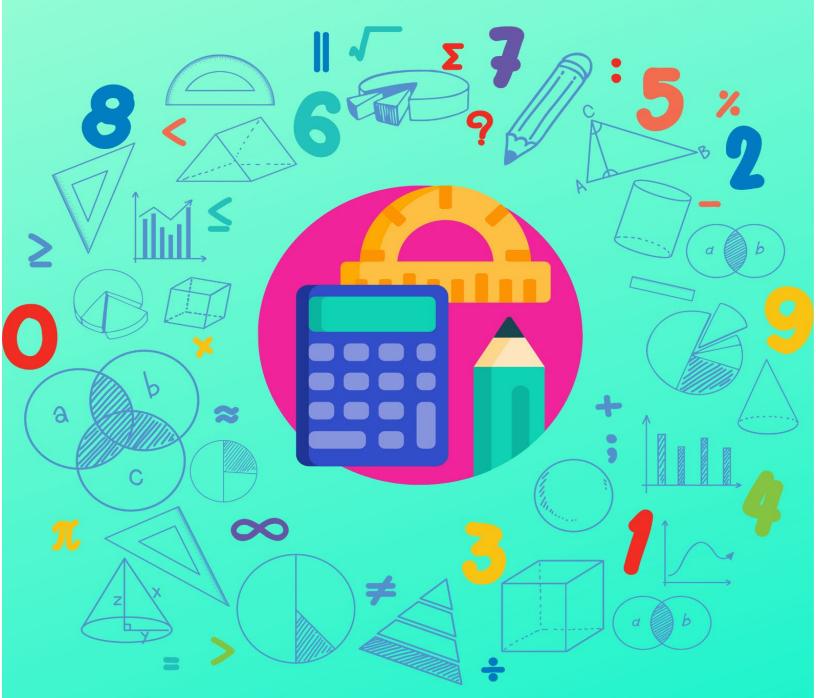


# A-Level Maths Revision Guide

Suitable for AQA, Edexcel and OCR





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#### **PURE MATHEMATICS**

A video with the whole of pure maths can be found here: <a href="https://youtu.be/s0E8Slo3Pqw">https://youtu.be/s0E8Slo3Pqw</a>

Proc	f:			
		Self-assessment		ent
	Knowledge Checklist	First	Second	Final
	These are the bits the exam board wants you to know, make sure you can do all of these	review 4-7 months before exam	review 1-2 months before exam	review Week before exam
	I can use proof by deduction. I can use proof by exhaustion.	0 0 0 0 0	©	© ⊕ 8 © ⊕ 8
	I can use disproof by counter example.	9 9 8 9 9 8	© (2) (3) (3) (4) (4) (4) (4) (4) (4) (4) (4) (4) (4	©
	I can use proof by contradiction.			

# Algebra & Functions:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can use the laws of indices for all rational exponents.	© © 8	© © 8	© © 8
I understand the equivalence between indices and surds. https://youtu.be/Q7WkzIYFI58	◎ ⊕ ⊗	◎ ⊕ ⊗	◎
I can manipulate surds, including rationalising the denominator. <a href="https://youtu.be/bBvwOnNow_U">https://youtu.be/bBvwOnNow_U</a>	© © 8	© © 8	© © 8
I can solve simultaneous equations by elimination. I can solve simultaneous equations by	© © 8	© © 8	© © 8
substitution. <a href="https://youtu.be/">https://youtu.be/</a> bWGbAoxklq	◎ ≌ 8	◎ ≌ 8	◎ ≌ ⊗
I can find the discriminant of a quadratic function.	© © 8	© © 8	◎ ◎ ⊗



I can solve a quadratic equation by factorisation, completing the square and the quadratic formula.	© © 8	© © 8	©
I can solve quadratic equations in a function of the unknown.  https://youtu.be/p_qnFs9Sc8	© ⊜ ⊗	© © 8	◎ ⊜ ⊗
I can represent and solve linear and quadratic inequalities graphically. <a href="https://youtu.be/Ltx8FrmGDOc">https://youtu.be/Ltx8FrmGDOc</a>	© © 8	© © 8	©
I can manipulate polynomials, including expanding and factorising cubic expressions. <a href="https://youtu.be/1M4cg3Gif74">https://youtu.be/1M4cg3Gif74</a>	© <del>(</del>	© <del>©</del> 8	◎ ⊜ ⊗
I can simplify rational expressions, including by algebraic division. <a href="https://youtu.be/J7NxXZNbMwc">https://youtu.be/J7NxXZNbMwc</a>	© ⊕ ⊗	© © 8	◎
I can sketch the graphs of functions, including	◎ ≌ ⊗	◎ ≌ ⊗	◎ ⊜ ⊗
those with asymptotes. I can use graphs to solve equations. <a href="https://youtu.be/4tCNS6A2d20">https://youtu.be/4tCNS6A2d20</a>	© © 8	© © 8	© <del>(</del> (8)
I can sketch transformations on the graphs of			
functions, including the modulus and	◎	◎ ≌ ⊗	◎ ≌ ⊗
combinations of these.			
https://youtu.be/NRAtJdjWOXo https://youtu.be/C6ccPVEhxHU			
I understand inverse functions, composite			
functions and decomposition of rational	◎ ≌ ⊗	◎ ⊜ ⊗	◎ ⊜ ⊗
functions into partial fractions.			
I can use functions in modelling, including limitations of and refinements to models.	© © ®	© <del>©</del> 8	© <del>©</del> 8

Coordinate Geometry:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	<b>Final review</b> Week before exam
I can understand and use the equation of a straight line, in different forms and with parallel or perpendicular gradients. <a href="https://youtu.be/5pr5iAmmQqw">https://youtu.be/5pr5iAmmQqw</a>	◎ ⊜ ⊗	◎ ⊜ ⊗	© <del>(</del> 8
I can understand and use the equation of a circle, including tangents.	© © 8	© © 8	© © 8



https://youtu.be/tzpmuYkM93M			
I can understand and use the parametric equations of curves, including converting to and from Cartesian form.  https://youtu.be/Lh2NAMFM55U	© © 8	© © 8	© © 8

Sequences & Series:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can understand and use binomial expansion, including the use of Pascal's triangle. <a href="https://youtu.be/IKN7EsaWRcE">https://youtu.be/IKN7EsaWRcE</a>	© © 8	© © 8	© © 8
I can work with arithmetic progressions, including the formula for the nth term and sum to n terms.  https://youtu.be/huYbiAgfbtI	◎ ⊜ ⊗	◎ ⊜ ⊗	◎ ⊜ ⊗
I can work with geometric progressions, including the formula for the nth term, sum of a finite series and sum to infinity of a convergent series.  https://youtu.be/rKawwzsP2Ho	◎ ⊜ ⊗	◎ ⊜ ⊗	◎
I understand the definitions of sequences and series and can use them in modelling, including increasing, decreasing and periodic sequences.	© © 8	© © 8	© © 8



Trigonometry:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I understand and can use the definitions of sine, cosine and tangent.	© © 8	© © 8	© <del>(</del> (8)
I can use the sine rule, cosine rule and the formula for the area of a triangle.	© © 8	© © 8	◎ ⊕ ⊗
I can find small angle approximations of sine, cosine and tangent.	◎ ⊜ ⊗	◎ ⊜ ⊗	◎
I can work with radians, including for arc length and sector area.  https://youtu.be/ltQGsMEJ_ys	© © 8	© © 8	©
I can understand and use the sine, cosine and tangent graphs, including exact values and their multiples.	© <del>(</del> 8	© © 8	◎ ⊜ ⊗
I can solve trigonometric equations in a given interval. <a href="https://youtu.be/rHXL2yAgbwq">https://youtu.be/rHXL2yAgbwq</a>	© <del>©</del> 8	© <del>©</del> 8	◎ ⊜ ⊗
I can understand and use the definitions of secant, cosecant, cotangent and of arcsin, arccos and arctan.	© © 8	© © 8	©
I can use <b>the double angle formulae and</b> trigonometric identities to solve equations. <a href="https://youtu.be/Dhd_XvirQTU">https://youtu.be/Dhd_XvirQTU</a>	© <del>©</del> 8	© <del>©</del> 8	© © 8



#### Exponentials & Logarithms:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I know and can use the functions a <sup>x</sup> , e <sup>x</sup> and their graphs.	◎ ⊜ ⊗	◎ ≌ ⊗	◎
I know and can use the functions $log_a x$ , $ln x$ and their graphs.	© © 8	© © Ø	◎
I can solve equations in the form $a^x = b$	◎ ≌ ⊗	◎ ⊜ ⊗	◎ ⊜ ⊗
I can understand and use the laws of logarithms.	© <del>(</del> 8	© <del>©</del> 8	◎ ⊜ ⊗
I can use logarithmic graphs to estimate parameters in relationships or in modelling.	© <del>(</del> 8	© <del>©</del> 8	◎ ⊜ ⊗

#### Differentiation:

2 videos covering the differentiation topic found here:

Part 1: <a href="https://youtu.be/KlbNTcIlct4">https://youtu.be/KlbNTcIlct4</a>

Part 2 (special examples): <a href="https://youtu.be/i4SPcgFjhv8">https://youtu.be/i4SPcgFjhv8</a>

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I understand and can use the first derivative of as the gradient of the tangent. I understand and can use the second derivative	◎ ⊜ ⊗	◎ ⊜ ⊗	◎ ◎ ⊗
as the rate of change of gradient I can apply differentiation to find:	◎	© <del>©</del> 8	◎
gradients, tangents and normals minima and maxima	◎ ≌ ⊗	◎ ≌ ⊗	◎
if a function is increasing/decreasing  points of inflection. <a href="https://youtu.be/T1vVCpbCGvw">https://youtu.be/T1vVCpbCGvw</a> <a href="https://youtu.be/47nSzfk-Tik">https://youtu.be/47nSzfk-Tik</a>	© @ 8 © @ 8	© @ 8 © @ 8	© © 8 © © 8



I can show differentiation from first principles for small positive integer values of x, sin x and cos x.	© © 8	© © 8	© © 8
I can differentiate standard functions including:			
$x^n$ $e^{kx}$ and $a^{kx}$ $\sin kx$ , $\cos kx$ and $\tan kx$ $\ln x$	© (2) (3) (3) (2) (3) (3) (2) (3) (4) (4) (4) (5) (4) (4) (6) (7)	© (2) (3) (3) (2) (3) (3) (2) (3) (4) (4) (4) (5) (4) (4) (6) (7)	© (2) (3) (3) (2) (3) (3) (2) (3) (4) (4) (4) (5) (4) (4) (6) (7)
I can differentiate using:			
Product rule <a href="https://youtu.be/izFXH_gLO8E">https://youtu.be/izFXH_gLO8E</a>	◎ ⊜ ⊗	◎ ⊜ ⊗	◎ ⊜ ⊗
Quotient rule https://youtu.be/3TTMaosfw5U	◎ ≌ 8	© <del>©</del> 8	© <del>©</del> 8
Chain rule https://youtu.be/P8q6B9VZ9aI	◎ ⊜ ⊗	◎ ⊜ ⊗	◎ ≌ 8
I can construct differential equations in pure mathematics or in context.	© <del>©</del> 8	© <del>©</del> 8	◎ ⊜ ⊗
I can interpret the solution of a differential equation in the context of solving a problem, including limitations of the solution.	© © 8	© © 8	◎ ⊜ ⊗



#### Integration:

A video for first principles of integration can be found here:

https://youtu.be/K0KlOh SEqQ

More difficult examples can be found in a video here: <a href="https://youtu.be/xqY\_hp-3-Wc">https://youtu.be/xqY\_hp-3-Wc</a>

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I know that integration is the opposite of differentiation and that indefinite integrals require a constant.	© © 8	©	© © 8
I can integrate standard functions including:  x <sup>n</sup> e <sup>kx</sup> and <sup>1</sup> / <sub>x</sub> sin kx and cos kx	© © 8 © © 8 © © 8	© @ 8 © @ 8 © @ 8	© © 8 © © 8 © © 8
I can evaluate definite integrals and use definite integrals to find the area under a curve <b>or the area between two curves</b> . <a href="https://youtu.be/I4">https://youtu.be/I4</a> -5Ei3zUI	© © 8	© © 8	© © 8
I can use: Integration by substitution <a href="https://youtu.be/iXUYUvui7UQ">https://youtu.be/iXUYUvui7UQ</a>	© © 8	© © 8	
Integration by parts <a href="https://youtu.be/HC524mZKT60">https://youtu.be/HC524mZKT60</a> Integration using partial fractions	© © 8 © © 8	©	© © 8 © © 8
I can understand and use integration as the limit of a sum.	© © 8	© © 8	© © 8



## Numerical Methods:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can locate roots by considering changes in sign, understanding how these methods can fail.	© © 8	© © 8	© @
I can solve equations using iterative methods, including using staircase and cobweb diagrams.	© © 8	© © 8	© @
I can solve equations using the Newton-Raphson method and other recurrence relations, understanding how these methods can fail.	© © 8	© © 8	© © 8
I can understand and use numerical integration of functions, including the use of the trapezium rule and estimating the approximate area under a curve and limits that it must lie between.	© © 8	© © 8	© © ®

#### Vectors:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can use vectors in two <b>and three</b> dimensions.	◎ ⊜ ⊗	◎ ⊜ ⊗	◎ ⊜ ⊗
I can calculate the magnitude and direction of a vector and convert between magnitude/direction forms.	© © 8 © © 8	© © 8 © © 8	© © 8 © © 8



I can add vectors diagrammatically and perform the algebraic operations of vector addition and multiplication by scalars.	© © 8 © © 8	© © 8 © © 8	© 9 8 © 9 8
I can understand and use position vectors.	◎	© <del>(</del> 8	◎ ⊜ ⊗
I can calculate the distance between two points represented by position vectors.	© © 8	© © 8	◎

## **Mechanics**

Quantities and units in mechanics:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can understand and use units in the S.I. system: length, time, mass.	◎ ⊕ ⊗	© <del>©</del> 8	© <del>-</del> 8
I can understand and use derived units: velocity, acceleration, force, weight, <b>moment</b> .	© <del>©</del> 8	◎	◎ ⊜ ⊗



#### Kinematics:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	<b>Final review</b> Week before exam
I can understand and use the language of kinematics, including position, displacement, distance travelled, velocity, speed and acceleration.	◎ ≌ 8	◎ ≌ 8	© © 8
I can interpret and use graphs in kinematics for motion in a straight line, displacement against time and interpretation of gradient, velocity against time and interpretation of gradient and area under the graph.	◎	◎	© © 8
I can derive and use the formulae for constant acceleration for motion in a straight line, including SUVAT formulae.	© © 8	© © 8	© © 8
I can use calculus in kinematics for motion in a straight line.	© © 8	© © 8	© © 8
I can derive and use the formulae to model motion under gravity in a vertical plane using vectors, such as for projectile motion.	© <del>©</del> 8	© <del>©</del> 8	© © 8



Forces & Newton's Laws:

Video for this topic is here: <a href="https://youtu.be/31j8J5EZtIM">https://youtu.be/31j8J5EZtIM</a>

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can understand the concept of a force, including normal reaction, tension, thrust, compression and resistance.	☺ ⊜ ⊗	© © 8	© © 8
I can understand and use Newton's first law.	© © 8	©	©
I can understand and use Newton's second law for motion in a straight line <b>and situations</b> where forces need to be resolved.	© <del>©</del> 8	© <del>©</del> 8	© <del>©</del> 8
I can understand and use Newton's third law, including:	© <del>©</del> 8	© <del>©</del> 8	© <del>©</del> 8
Equilibrium of forces on a particle and motion in a straight line. Application to problems involving smooth pulleys and connected particles.	© © Ø	© © Ø	© © Ø
Resolving forces in two dimensions. Equilibrium of a particle under coplanar forces.	© 9 8 © 9 8	© © 8 © © 8	© 9 8 © 9 8
I can understand and use weight and motion in a straight line under gravity.	© <del>©</del> 8	© <del>©</del> 8	© <del>©</del> 8
I can understand and use: Addition of forces. Resultant forces. Dynamics for motion in a plane.	© = 8 © = 8 © = 8	© = 8 © = 8 © = 8	© = 8 © = 8 © = 8
I can understand the concept of a frictional force in vector or component form, when the magnitude and direction of the force are given or using the $F \le \mu R$ model for friction.	© © 8	© <del>©</del> 8	© <del>©</del> 8



#### Moments:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can understand and use moments in simple static contexts.	© © 8	© © 8	©

## **Statistics**

# Statistical Sampling:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can select, use and critique sampling techniques, including: Simple random sampling. Stratified sampling. Systematic sampling. Quota sampling. Opportunity sampling.	8 8 8 8 9 9 9 9 9 9 9 9	© 8 © 9 © 9 © 9 © 9 © 9	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8



Data Presentation & Interpretation:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can interpret and use: Frequency polygons. Histograms. Cumulative frequency diagrams. Box and whisker plots.	© (2) (3) (3) (4) (4) (3) (4) (4) (4) (5) (4) (5) (6) (7)	© © 8 © © 8 © © 8 © © 8	© @ @ © @ @ © @ @
I can interpret scatter diagrams and regression lines.	© © 8	◎ ≌ ⊗	◎ ≌ ⊗
I can interpret and calculate measures of central tendency, including mean, mode and median.	© © 8	© © 8	© © 8
I can interpret and calculate measures of variation, including variance, standard deviation, range and interpercentile ranges.	© <del>©</del> 8	© © 8	© © 8
I can recognise and interpret possible outliers in data sets and statistical diagrams.	© <del>(</del> 8	© © 8	© © 8
I can select or critique data presentation techniques in the context of a statistical problem.	© © 8	© © 8	© © 8
I can clean data, including dealing with missing data, errors and outliers.	© <del>(</del> 8	© <del>(</del> 8	© <del>(</del> 8



Probability:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can use tree diagrams with independent and conditional probability. <a href="https://youtu.be/394smmY9oJU">https://youtu.be/394smmY9oJU</a>	© © 8	© © 8	©
I can use Venn diagrams with independent and conditional probability. <a href="https://youtu.be/yUqGuebVQGk">https://youtu.be/yUqGuebVQGk</a>	© © 8	© © 8	©
I can use set notation with independent and conditional probability.	© © 8	© © 8	◎ ⊜ ⊗

#### Statistical Distributions:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can understand and use discrete probability distributions, including the binomial distribution.	◎ ≌ ⊗	© © 8	© © Ø
I can understand and use the Normal distribution, including to find probabilities.	© © 8	© © 8	© © 8



Statistical Hypothesis Testing:

	Self-assessment		
Knowledge Checklist  These are the bits the exam board wants you to know, make sure you can do all of these	First review 4-7 months before exam	Second review 1-2 months before exam	Final review Week before exam
I can understand and apply the language of statistical hypothesis testing and be able to interpret a given correlation coefficient using a given p-value or critical value.	© © 8	© © 8	© ©
I can conduct a statistical hypothesis test for the proportion in the binomial distribution and interpret the results.	© © 8	© © 8	© © 8
I can conduct a statistical hypothesis test for the mean of a Normal distribution with known, given or assumed variance and interpret the results.	© © 8	© © 8	© © 8