

Structured Questions

Circular Motion

Radians / Time period & Frequency / Angular Velocity / Centripetal Force / Linear Speed / Centripetal Acceleration / Investigating Circular Motion

Medium (3 questions)	/27
Hard (2 questions)	/17
Total Marks	/44

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Medium Questions

- 1 (a) A particle-accelerator uses a ring of electromagnets to keep protons moving continuously in a **circle**. The speed v of the protons depends on the frequency f of rotation of the protons in the circular orbit.

Fig. 22 shows data points plotted on a v against f grid.

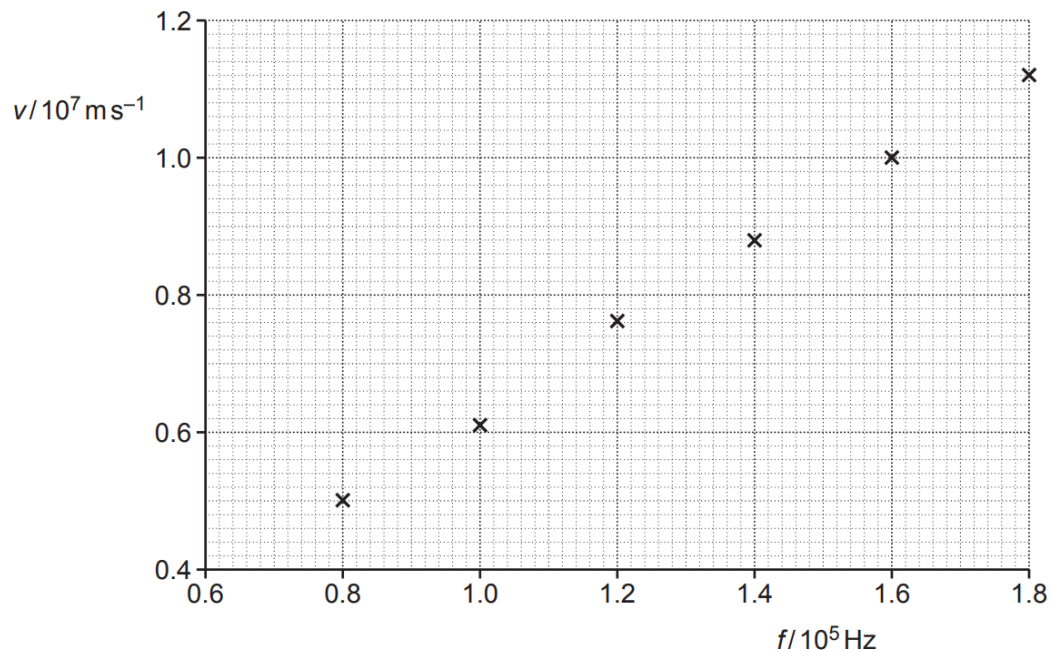


Fig. 22

- i) Show that the gradient of the graph of v against f is equal to $2\pi r$, where r is the radius of the circular path of the protons.

[2]

- ii) Show that r is about 10 m by determining the gradient of the line of best fit through the data points in Fig. 22.

[3]

- iii) The maximum speed of the protons from this accelerator is $2.0 \times 10^7 \text{ m s}^{-1}$.

Calculate the maximum centripetal force F acting on a proton at this speed.

- mass of proton = 1.7×10^{-27} kg.

$F = \dots\dots\dots$ N [3]

(8 marks)

- (b) A new particle-accelerator is now built for moving the protons in a circle of a radius 20 m.

The ring of electromagnets for this new accelerator provides the same **maximum** centripetal force as the accelerator in (a).

Calculate the maximum speed of the protons in this new accelerator.

maximum speed = $\dots\dots\dots$ m s⁻¹ [2]

(2 marks)

2 (a) At an airport, the conveyor belt for suitcases moves at a constant speed of 1.5ms^{-1} .

In Fig. 4.1, a suitcase of mass 8.0kg has reached the line labelled **XX'**.

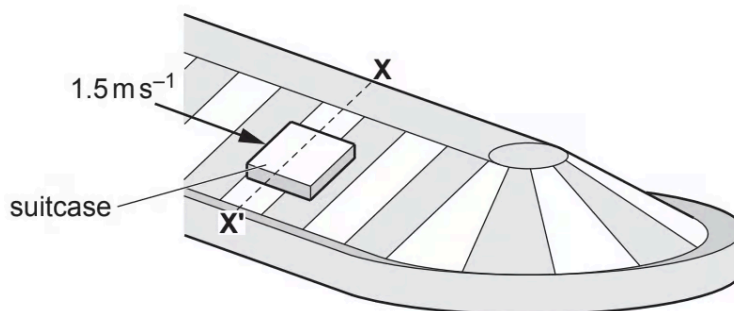


Fig. 4.1

Fig. 4.2 shows the situation in vertical cross-section. The frictional force F prevents the suitcase of weight W from sliding to the bottom of the belt. The normal contact force on the suitcase is R . The belt is inclined at an angle of 30° to the horizontal.

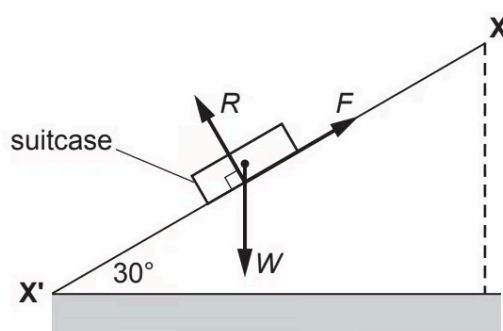


Fig. 4.2 (not to scale)

By using a vector triangle, or by resolving forces, calculate the magnitude of forces F and R .

$F = \dots\dots\dots \text{ N}$ $R = \dots\dots\dots \text{ N}$

[3]

(3 marks)

(b) Fig. 4.3 shows the suitcase and the forces acting on it at the line labelled **YY'**.

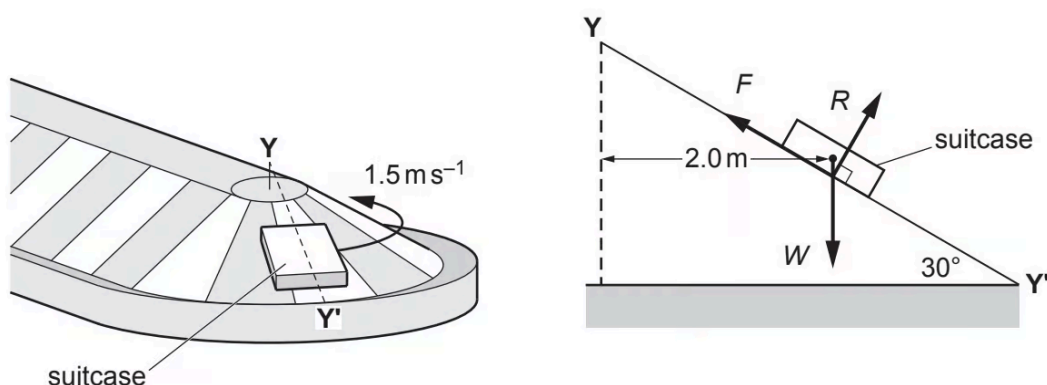


Fig. 4.3

The centre of mass of the suitcase is now moving at 1.5 ms^{-1} along a semi-circular arc of radius 2.0 m .

i) Calculate the magnitude of the centripetal force acting on the suitcase.

centripetal force = N [2]

ii) When the suitcase is at line **YY'**, the magnitude of force F is larger and the magnitude of force R is smaller than at **XX'**. Explain why this is so.

[4]

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(6 marks)

3 (a) Fig. 21 shows the drum of a washing machine.

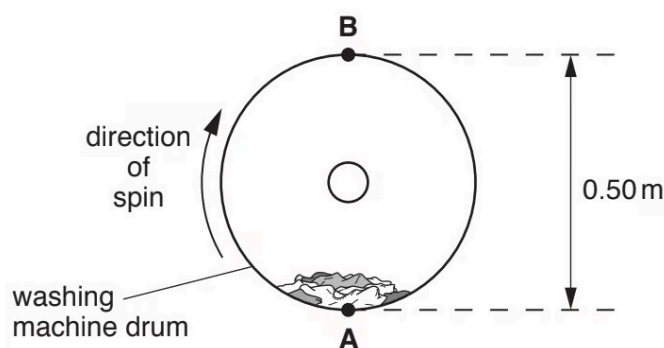


Fig. 21

The clothes inside the drum are spun in a **vertical** circular motion in a clockwise direction.

When the drum is at rest, the weight of the clothes is equal to the normal contact force on the clothes at point **A**. Explain why these two forces are **not** an example of Newton's Third Law of motion.

[2]

(2 marks)

- (b) The drum has diameter 0.50 m. The manufacturer of the washing machine claims that the drum spins at 1600 ± 100 revolutions per minute.

Calculate the speed of rotation of the drum and the absolute uncertainty in this value.

speed = \pm m s^{-1} [3]

(3 marks)

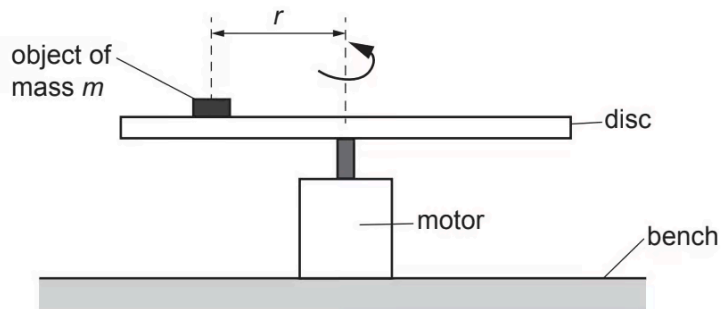
- (c) The washing machine is switched off and the speed of the drum slowly decreases. The clothes at the top of the drum at point **B** start to drop off at a certain speed v . At this speed v , the normal contact force on the clothes is zero. Calculate the speed v .

$v = \dots\dots\dots \text{ m s}^{-1}$ [3]

(3 marks)

Hard Questions

- 1 (a) A small object of mass m is placed on a rotating horizontal metal disc at a distance r from the centre of the disc.



The frequency of rotation is adjusted using a motor attached to the disc.

The frequency of rotation of the disc is slowly increased from zero, until the object slips off. At this point, the friction F acting on the object is equal to the centripetal force.

The friction F is given by the expression $F = kmg$, where k is a constant and g is the acceleration of free fall. The constant k has no units.

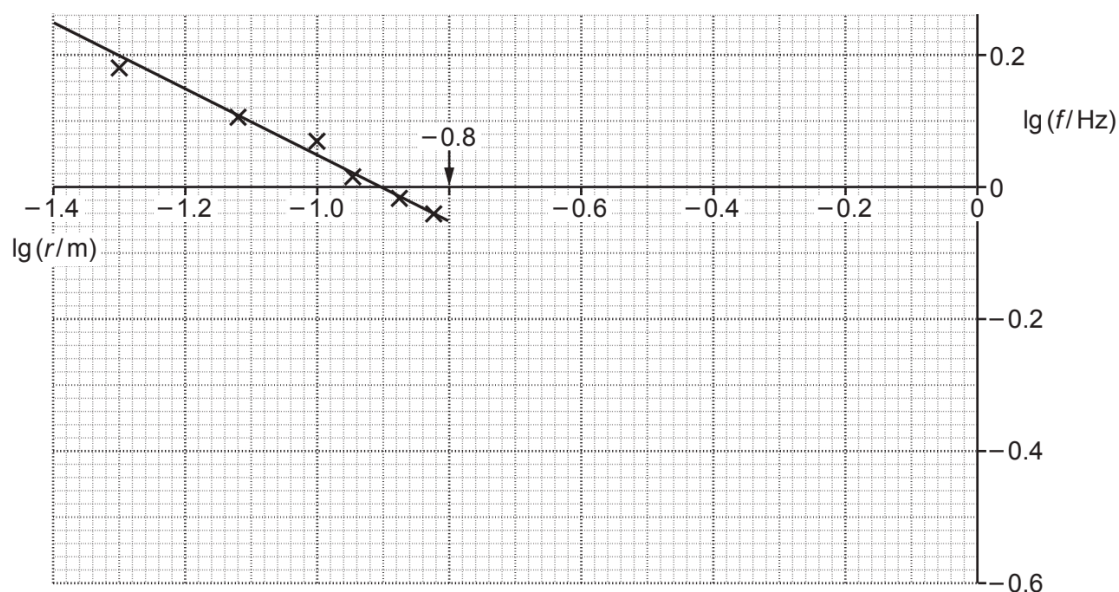
Show that the frequency f at which the object slips off is given by the equation

$$f^2 = \left(\frac{gk}{4\pi^2} \right) \times \frac{1}{r}.$$

[3]

(3 marks)

(b) A student plots a graph of $\lg(f/\text{Hz})$ against $\lg(r/\text{m})$.



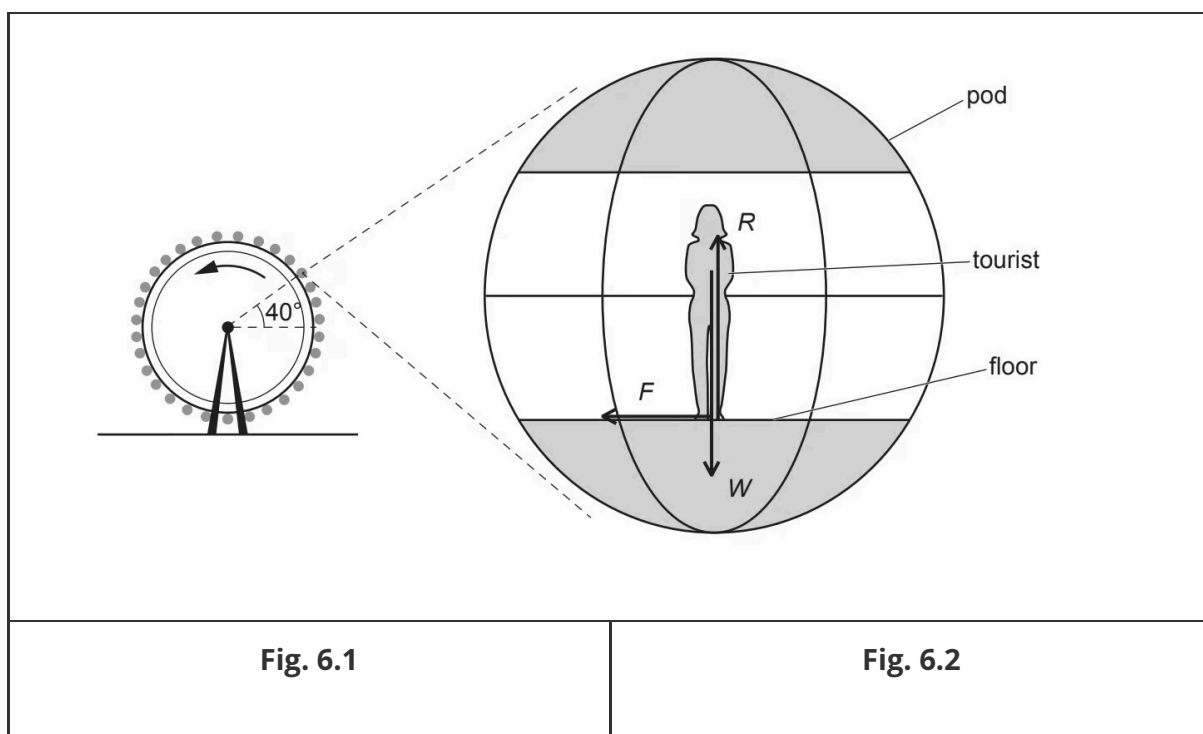
For this graph: $y\text{-intercept} = \frac{1}{2} \times \lg\left(\frac{gk}{4\pi^2}\right)$

Use the graph to determine the constant k . Write your answer to 2 significant figures.

$k = \dots\dots\dots$ [4]

(4 marks)

- 2 (a)** The London Eye, shown rotating anticlockwise in **Fig. 6.1**, is a giant wheel which rotates slowly at a constant speed.



Tourists stand in pods around the circumference of the wheel.

The floor remains horizontal at all times.

At time $t = 0$, a tourist who has a weight W of 650 N enters a pod at the bottom of the wheel.

Fig. 6.2 shows the forces acting on the tourist at a later time, when the angle between the pod's position and the centre of the wheel is 40° above the horizontal. R is the normal contact force and F is friction.

The resultant upward force ($R - W$) on the tourist changes during the 30 minutes of the rotation of the London Eye as shown in **Fig. 6.3**.

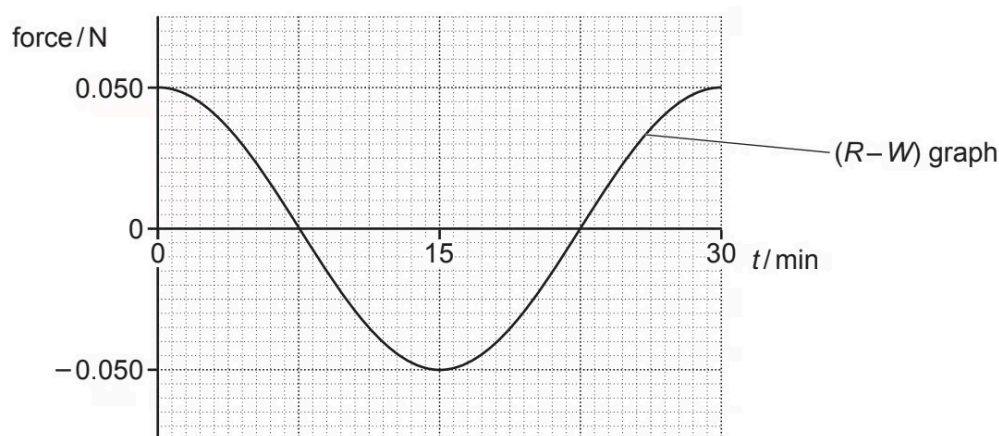


Fig. 6.3

Explain how the graph in **Fig. 6.3** shows that the magnitude of the centripetal force on the tourist during the rotation is 0.050 N.

[1]

(1 mark)

(b) i) Explain why the horizontal force F between the floor and the tourist is necessary.

[2]

ii) Draw on **Fig. 6.3** the variation of the horizontal force F during the 30 minutes of the anticlockwise rotation of the London Eye. Take forces to the right to be positive.

[2]

iii) Calculate the magnitude of force F when the pod is at the position shown in **Fig. 6.2**, at 40° above the horizontal.

$F = \dots\dots\dots$ N [2]

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(6 marks)

- (c)** Calculate the distance d of the centre of mass of the tourist from the centre of rotation of the London Eye.

$d = \dots\dots\dots$ m **[3]**

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(3 marks)