

Structured Questions

Planetary Motion

Kepler's Three Laws of Motion / Circular Orbits in Gravitational Fields /
Geostationary Orbits

Medium (2 questions)	/24
Hard (1 question)	/10
Total Marks	/34

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Medium Questions

1 (a) The diagram below shows the Earth in space.



i) On the diagram above, draw a minimum of **four** gravitational field lines to map out the gravitational field pattern around the Earth.

[1]

ii) On the same diagram above, show **two** different points where the gravitational potential is the same. Label these points **X** and **Y**.

[1]

(2 marks)

(b) A satellite is in a circular geostationary orbit around the centre of the Earth. The satellite has both kinetic energy and gravitational potential energy.

The mass of the satellite is 2500 kg and the radius of its circular orbit is $4.22 \times 10^7 \text{ m}$.
The mass of the Earth is $5.97 \times 10^{24} \text{ kg}$.

- Describe some of the features of a geostationary orbit.
- Calculate the **total** energy of the satellite in its geostationary orbit.

[6]

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(6 marks)

2 (a) Phobos is one of the two moons orbiting Mars. Fig. 17.1 shows Phobos and Mars.

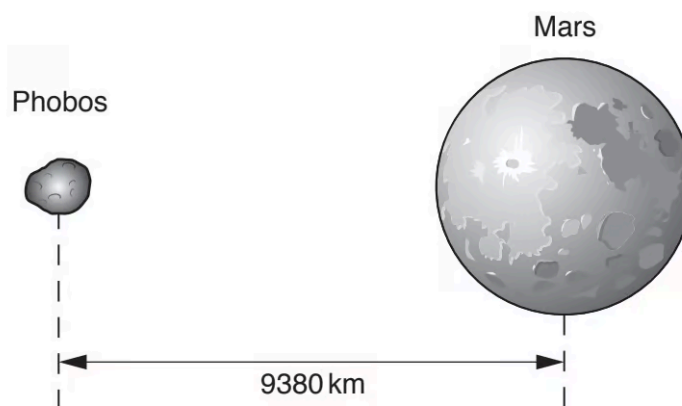


Fig. 17.1

The orbit of Phobos may be assumed to be a circle. The centre of Phobos is at a distance 9380 km from the centre of Mars and it has an orbital speed $2.14 \times 10^3 \text{ m s}^{-1}$.

i) On Fig. 17.1, draw an arrow to show the direction of the force which keeps Phobos in its orbit.

[1]

ii) Calculate the orbital period T of Phobos.

$T = \dots\dots\dots \text{ s}$ **[2]**

iii) Calculate the mass M of Mars.

$M = \dots\dots\dots \text{ kg}$ **[3]**

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(6 marks)

(b) The gravitational field strength at a distance r from the centre of Mars is g .

The table below shows some data on Mars.

$g / \text{N kg}^{-1}$	r / km	$\lg (g / \text{N kg}^{-1})$	$\lg (r / \text{km})$
1.19	6000	0.076	3.78
0.87	7000		
0.67	8000	-0.174	3.78
0.53	9000	-0.276	3.95
0.43	10000	-0.367	4.00

i) Complete the table by calculating the missing values.

[1]

ii) Fig. 17.2 shows the graph of $\lg (g / \text{N kg}^{-1})$ against $\lg (r / \text{km})$.

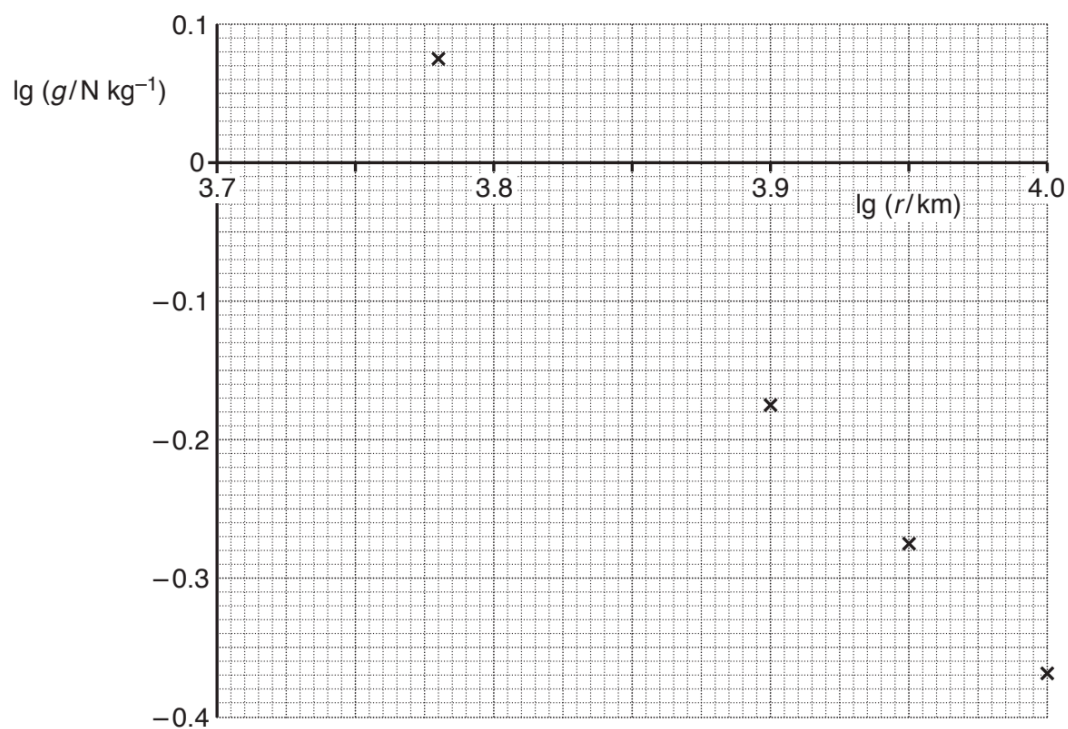


Fig. 17.2

1. Plot the missing data point on the graph and draw the straight line of best fit.

[2]

2. Use Fig. 17.2 to show that the gradient of the straight line of best fit is -2 .

[1]

3. Explain why the gradient of the straight line of best fit is -2 .

[2]

(6 marks)

- (c) In July 2018, the closest distance between the centre of Mars and the centre of Earth was 5.8×10^{10} m.

Fig. 17.3 shows the variation of the **resultant** gravitational field strength g between the two planets with distance r from the centre of the **Earth**.

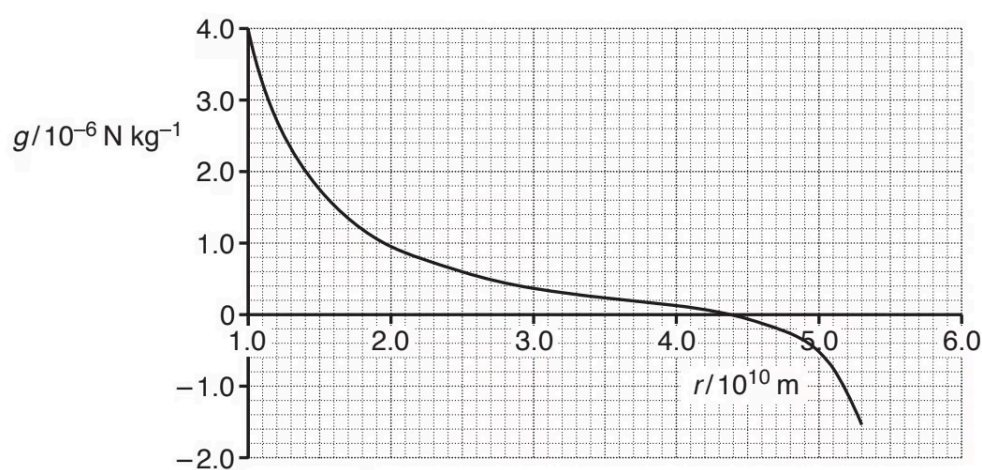


Fig. 17.3

- i) Explain briefly the overall shape of the graph in Fig. 17.3.

[2]

- ii) Use the value of r when $g = 0$ from Fig. 17.3 to determine the ratio

$$\frac{\text{mass of Earth}}{\text{mass of Mars}}$$

$$\frac{\text{mass of Earth}}{\text{mass of Mars}} = \dots\dots\dots [2]$$

(4 marks)

Hard Questions

- 1 (a)** A binary star is a pair of stars which move in circular orbits around their common centre of mass.

In this question consider the stars to be point masses situated at their centres.

Fig. 3.1 shows a binary star where the mass of each star is m . The stars move in the same circular orbit.

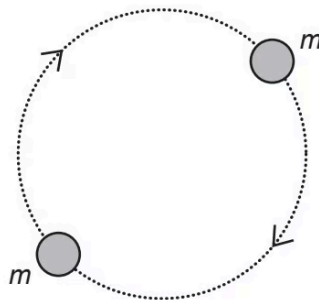


Fig. 3.1

- i) Explain why the stars of equal mass must always be diametrically opposite as they travel in the circular orbit.

[2]

- ii) The centres of the two stars are separated by a distance of $2R$ equal to $3.6 \times 10^{10} \text{ m}$, where R is the radius of the orbit. The stars have an orbital period T of 20.5 days. The mass of each star is given by the equation

$$m = \frac{16 \pi^2 R^3}{GT^2}$$

where G is the gravitational constant.

Calculate the mass m of each star in terms of the mass M_\odot of the Sun.

$$1 \text{ day} = 86400 \text{ s} \quad M_\odot = 2.0 \times 10^{30} \text{ kg}$$

$$m = \dots\dots\dots M_\odot \quad \mathbf{[3]}$$

iii) The stars are viewed from Earth in the plane of rotation.

The stars are observed using light that has wavelength of 656 nm in the laboratory. The observed light from the stars is Doppler shifted.

Calculate the maximum change in the observed wavelength $\Delta\lambda$ of this light from the orbiting stars. Give your answer in nm.

$\Delta\lambda = \dots\dots\dots$ nm [2]

(7 marks)

(b) Fig. 3.2 shows a binary star where the masses of the stars are $4m$ and m .

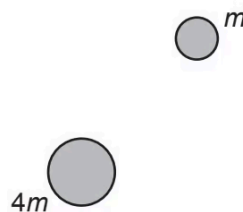


Fig. 3.2

i) The centre of mass of the binary star lies at the surface of the star of mass $4m$. Draw on Fig. 3.2 two circles to represent the orbits of **both** stars.

[1]

ii) Explain why the smaller mass star travels faster in its orbit than the larger mass star.

[2]

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(3 marks)