

## Keystream Generators

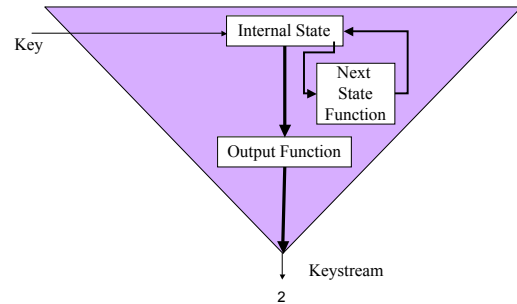
### Random Number Generators

### Block Ciphers

### Chaining

1

## Keystream Generator



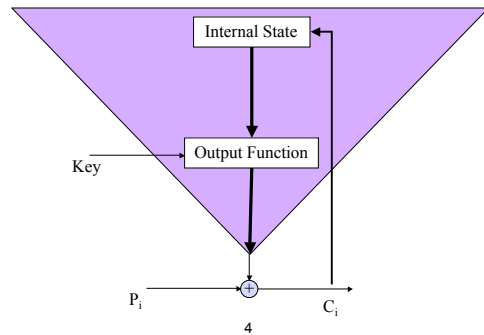
2

## Synchronous Stream Cipher

- Keystream is generated from the key  $K$
- Sender and receiver must be synchronized
- One-bit error in ciphertext produces one-bit error in plaintext
- Upon loss of synchronization both sides start afresh with a new key
- Any deletions and insertions will cause loss of synchronization
- Mallory can toggle/change bits

3

## Self-Synchronizing Stream Cipher



4

## Self-Synchronizing Stream Cipher

- Internal state is the function only of the previous  $n$  ciphertext bits and depends on the key  $K$
- Decryption keystream generator will completely synchronize with encryption generator after receiving  $n$  bits
- Advantage:
  - Recovery from loss of bits after  $n$  bits
- Drawback:
  - Error extension – one-bit error in ciphertext produces  $n$  errors in plaintext
  - Mallory can replay messages

5

## Generating Random Numbers

- We need to generate a sequence that looks random but is reproducible
- There shouldn't be any obvious regularities, otherwise Eve can learn the pattern after seeing several numbers, and guess the next ones
- We would like to cover the whole range of numbers (e.g.  $2^n$  if the number has  $n$  bits)

6

## Linear Congruential Generators

- Generators of the form

$$X_n = (aX_{n-1} + b) \bmod m$$

- A period of a generator is number of steps before it repeats the sequence
- If  $a$ ,  $b$  and  $m$  are properly chosen, this generator will be *maximal period generator* and have period of  $m$
- It has been proven that any polynomial congruential generator can be broken

7

## Linear Feedback Shift Registers

- Used for cryptography today
- A **shift register** is transformed in every step through **feedback function**
  - Contents are shifted one bit to the right, the bit that "falls out" is the output
  - New leftmost bit is XOR of some bits in the shift register, **tap sequence**
  - If we choose a proper tap sequence period will be  $2^n - 1$

8

## Linear Feedback Shift Registers

$$X^4 = X^4 \oplus X^1$$

1111		0110	1	1000	1
0111	1	0011	0	1100	0
1011	1	1001	1	1110	0
0101	1	0100	1	1111	0
1010	1	0010	0		
1101	0	0001	0		

9

## Linear Feedback Shift Registers

- Proper tap sequences are those where a polynomial from a tap sequence + 1 is a **primitive polynomial** in  $GF(2)$
- There are tables of primitive polynomials (I posted some of them on our class page)
- LFSR is fast in hardware but slow in software
- LFSR are not themselves secure but they are used as building blocks in encryption algorithms

10

## Block Cipher Example

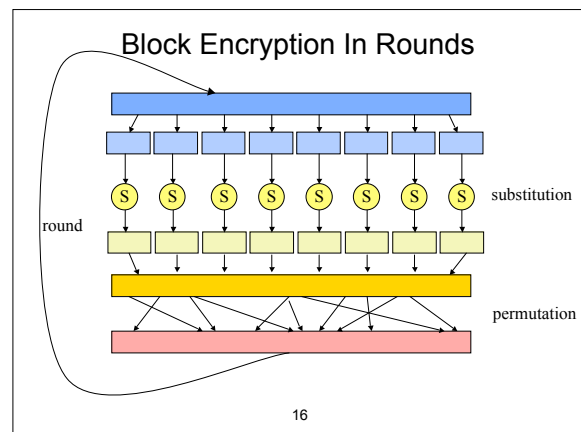
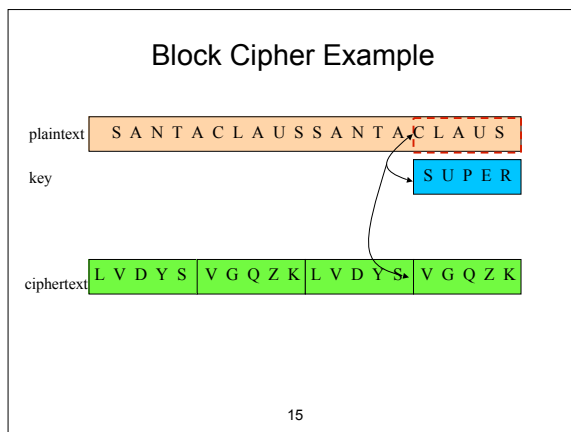
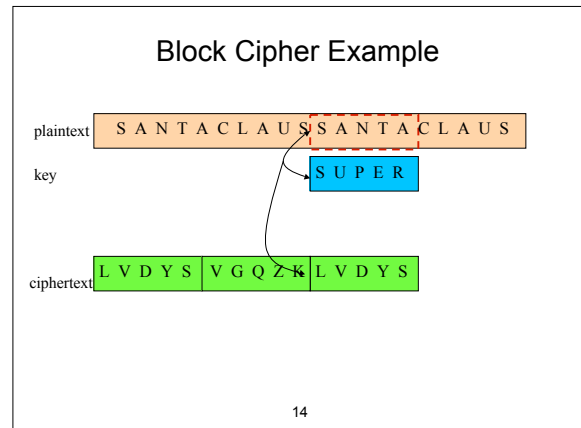
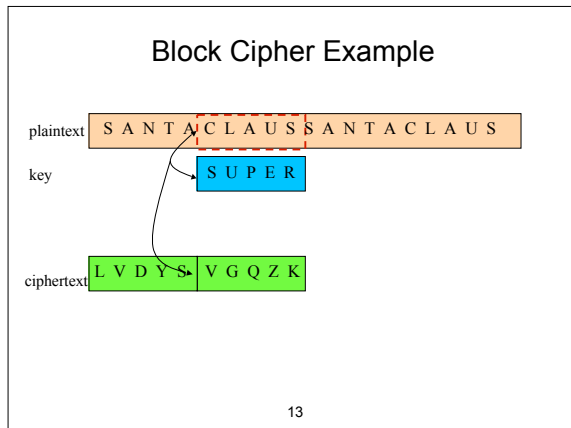
plaintext **SANTACLAUSSANTACLAUS**  
key **SUPER**

11

## Block Cipher Example

plaintext **SANTACLAUSSANTACLAUS**  
key **SUPER**  
ciphertext **LV DYS**

12



### Encrypting A Large Message

- Electronic Code Book (ECB)
- Cipher Block Chaining (CBC)
- $k$ -bit Cipher Feedback Mode (CFB)
- $k$ -bit Output Feedback Mode (OFB)
- Things to consider:
  - Can we encrypt/decrypt efficiently (as soon as bits arrive)
  - How hard it is to break encryption
  - What if a bit is flipped on the channel
  - What if we lose a bit on the channel

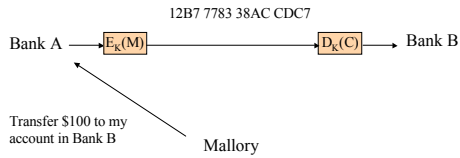
17

### Electronic Code Book (ECB)

- Precompute and store mapping for every possible block
  - Fast encryption/decryption – just a table lookup
  - Ability to process text in any order and in parallel
  - Table size could be enormous even for 64 bit blocks so we need to make the mapping depend on the key
- Eve can detect which blocks map to other blocks, by seeing several plaintext and corresponding ciphertext messages
- Due to language redundancy even partial decryption might provide enough information
- Bit error invalidates one block
- Bit loss/addition is not recoverable

18

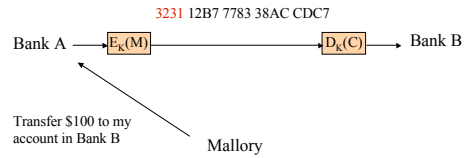
## Block Replay



- Mallory does this couple of times, looks for similar block sequences.
- She can now replay 12B7 7783 38AC CDC7 at will

19

## Block Replay



- Bank adds timestamps
- Mallory picks specific blocks of message carrying his name and account number and replaces those in other messages between Bank A and Bank B

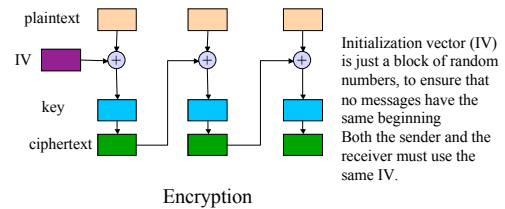
20

## Cipher Block Chaining (CBC)

- Problem with ECB is that Mallory can replace, add or drop blocks at will
- Chaining prevents this by adding feedback
  - Each ciphertext block depends on all previous blocks
- Also, with CBC, same plaintext blocks will encrypt to different ciphertext blocks thus obscuring patterns in plaintext

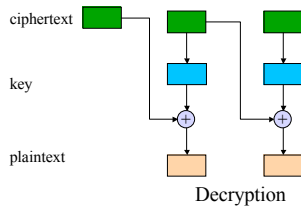
21

## Cipher Block Chaining (CBC)



22

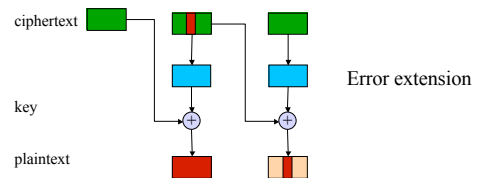
## Cipher Block Chaining (CBC)



23

## Error Recovery

- An error in plaintext affects the rest of the message but is easily spotted and removed after decryption
- An error in ciphertext affects one block and several bits of plaintext



24

### Potential Problems With CBC

- Mallory can:
  - Add blocks
  - Drop blocks
  - Introduce bit errors
- Bit loss/addition is not recoverable

25