

Interactions Between Knowledge Graph-Related Tasks and Analogical Reasoning

A Discussion

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Context & Motivation

Knowledge graphs (KGs) in the Web of data

- Directed and labeled multigraphs

- Nodes

Individuals

Classes

Literals

- Edges

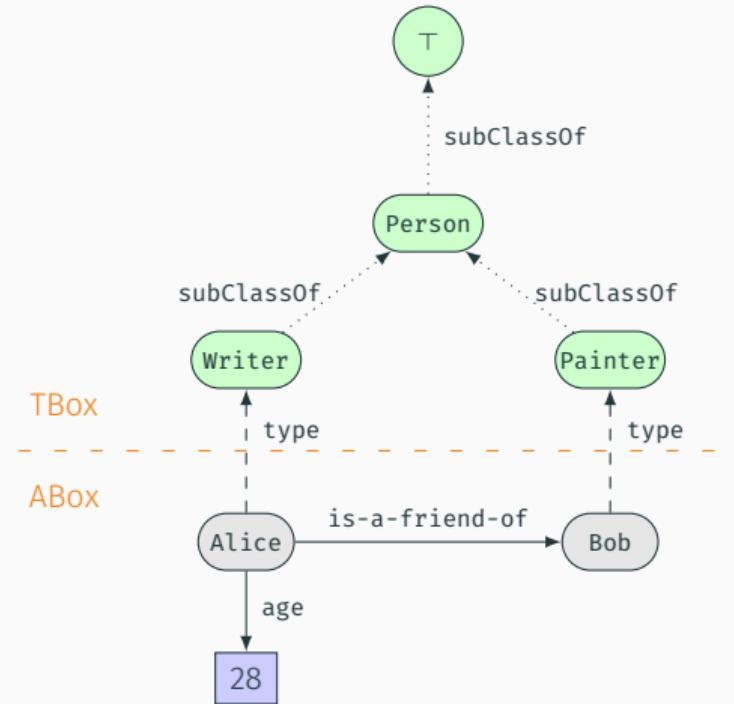
- Labeled by a predicate
- Defined by triples

(subject, predicate, object)

- Semantic Web standards

RDF, URI, RDFS, OWL, SPARQL, ...

(Berners-Lee et al. 2001)



From a general assessment about the Web of data...

- Increasing volume of available data in various formats
 - Open Data portals, internal repositories of companies
- Automatic knowledge extraction approaches to build KGs



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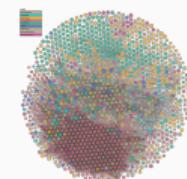
 - Increasing size and number of available KGs
 - Possible overlaps
 - Interest in their conjoint use

→ Matching similar units within and across KGs



The diagram illustrates the complex interaction between Music and the Brain. It shows that Music and Brain are interconnected, with Music influencing various cognitive domains: Memory, Language, Executive Function, and Self-Awareness. These cognitive domains are interconnected among themselves.

LOD Cloud in 2007



LOD cloud in 2020

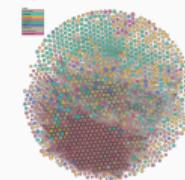
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- Increasing size and number of available KGs
 - Possible overlaps
 - Interest in their conjoint use
- Matching similar units within and across KGs
-
- KGs support various applications
e.g., search, question-answering, recommendation



LOD Cloud in 2007

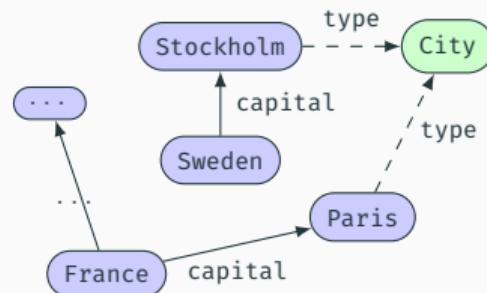


LOD cloud in 2020

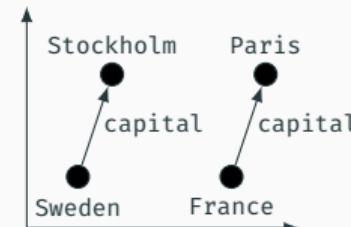
from lod-cloud.net -

From a general assessment about the Web of data...

- Various methods for KG construction, matching, refinement, and usage
- **Impressive performance of Knowledge Graph Embeddings**



Graph structures
(e.g., nodes)



d -dimensional space
preserving graph properties

(Cai et al. 2018; Chami et al. 2020; Ji et al. 2020; Nickel et al. 2016; Wang et al. 2017)

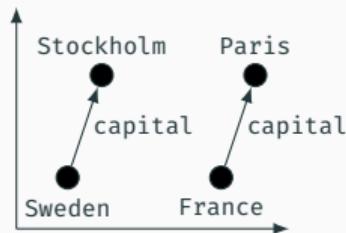
- Various types of models, e.g., translational, convolutional

... to our research questions about analogies

- Analogies have been extensively studied in NLP (Alsaidi et al. 2021)
- High performance when leveraging word / character embeddings

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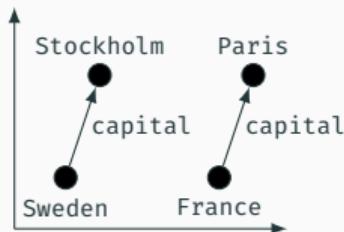


e.g., TransE (Bordes et al. 2013)

$$\overrightarrow{\text{France}} - \overrightarrow{\text{Paris}} = \overrightarrow{\text{Sweden}} - \overrightarrow{\text{Stockholm}} = \overrightarrow{\text{capitalof}}$$

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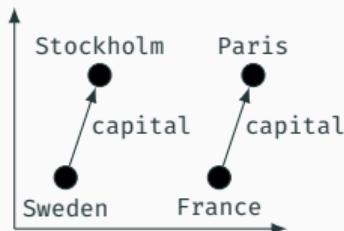
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- Analogical inference desirable for KG refinement (Liu et al. 2017)
- KG link prediction and data mining approaches for analogy solving (Portisch et al. 2022)

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Towards further interactions between analogical reasoning and
KG-related tasks?

... to our research questions about analogies

Towards further interactions between analogical reasoning and
KG-related tasks?

The examples of

- Semantic Table Interpretation
- Knowledge Matching
- KG-based Recommendation

Semantic Table Interpretation

Semantic Table Interpretation: definition & tasks

Understanding the semantic content of tables by annotating with KG elements

| Country | Capital | Official language(s) | GDP (US\$ million) |
|-------------|-----------------|----------------------------------|--------------------|
| Finland | (empty) | Finnish, Swedish | 297,617 |
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Semantic Table Interpretation: definition & tasks

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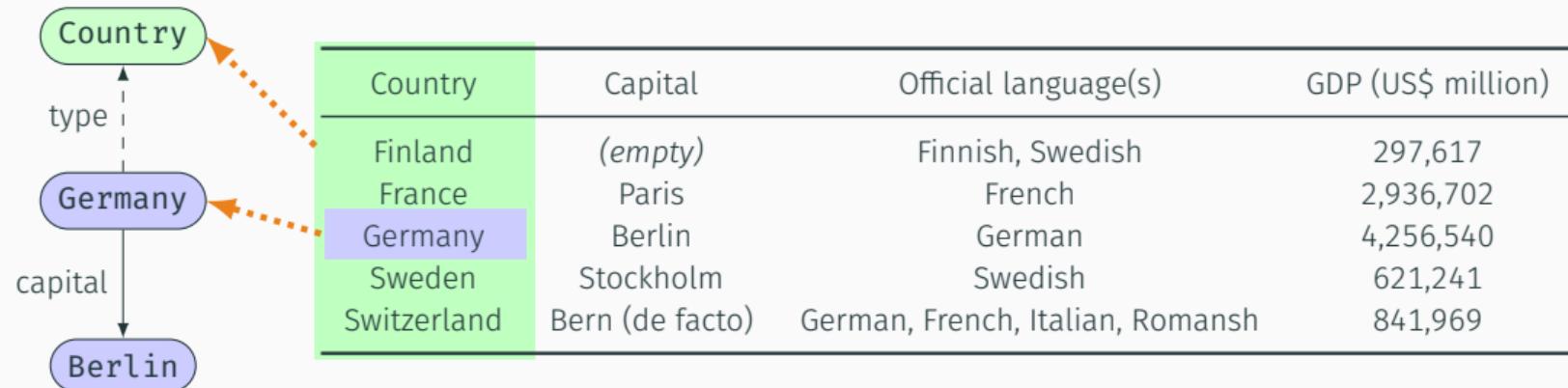
The diagram illustrates the semantic interpretation of a table row for Germany. On the left, a green rounded rectangle labeled "Country" has a dashed arrow labeled "type" pointing up to it. Below it, a purple rounded rectangle labeled "Germany" has a solid arrow labeled "capital" pointing down to a blue rounded rectangle labeled "Berlin". A dotted orange arrow points from the "Germany" entity to the "Germany" cell in the table row. The table itself has four columns: Country, Capital, Official language(s), and GDP (US\$ million). The data rows are:

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Cell-Entity Annotation (CEA) associates cells with entities;

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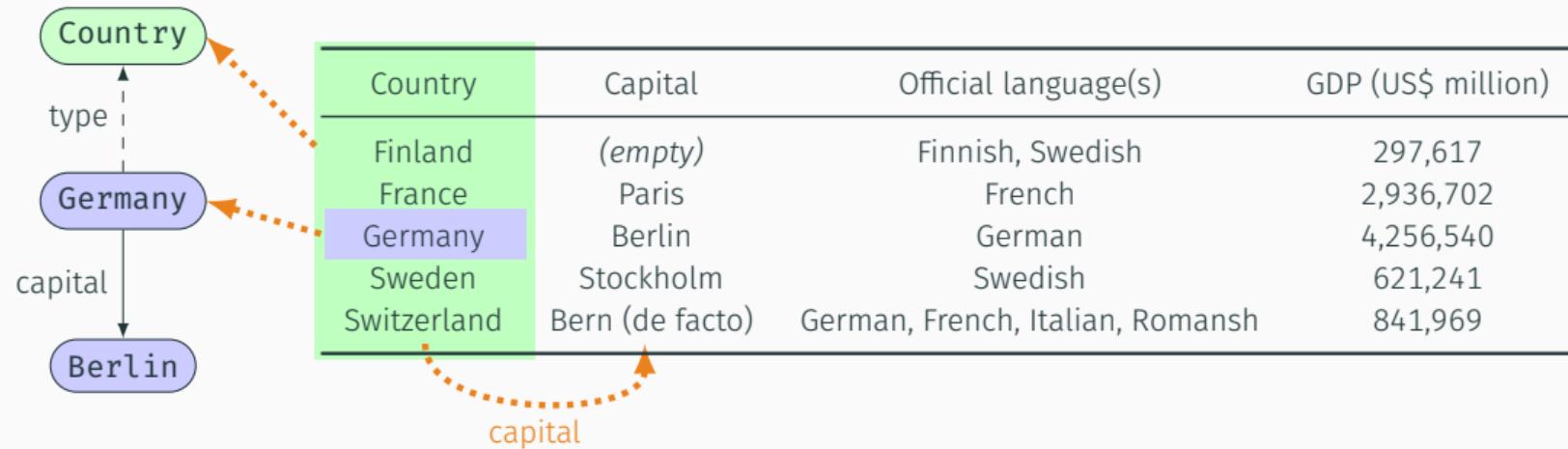
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Semantic Table Interpretation: definition & tasks

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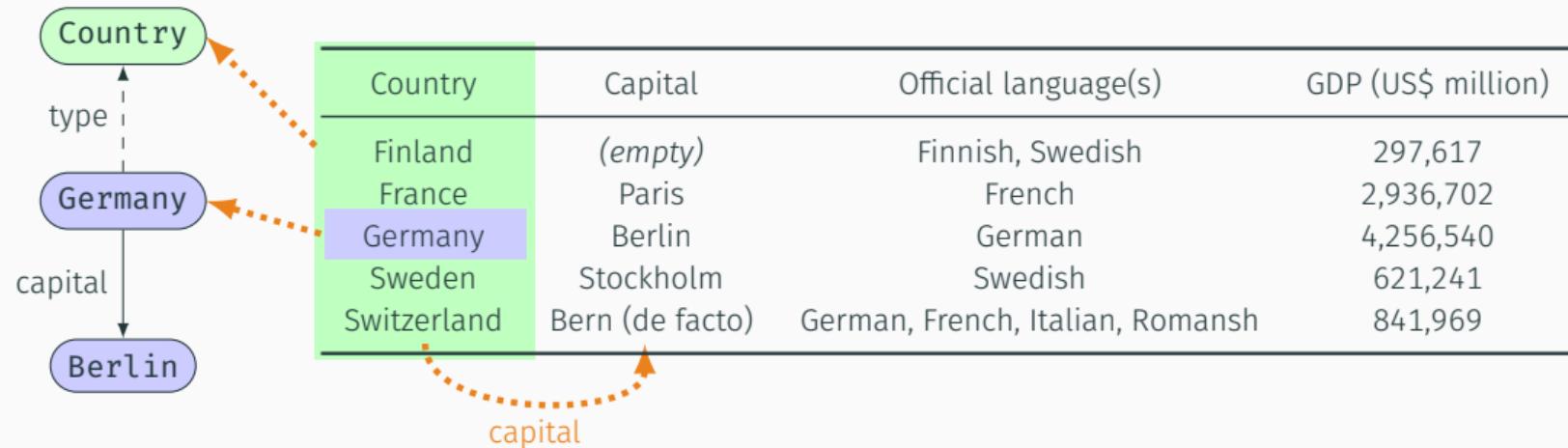
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Column-Type Annotation (CTA) associates columns with types;

Columns-Property Annotation (CPA) associates pairs of columns with properties.

Semantic Table Interpretation: (some) applications

Understanding the semantic content of tables by annotating with KG elements



- KG completion with table content
- Table completion with KG content
- Data set search services

Semantic Table Interpretation: issues

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- Different encoding charsets
- Misaligned cells, **missing values**
- Little context to **disambiguate candidate entities**, e.g., from Wikidata
 - Q142 (**Germany**, the European country)
 - Q13505654 (**Germany**, the constituency of the European Parliament)

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- **Useful property: semantic coherence of columns**

Analogies to support Semantic Table Interpretation

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- Useful property: semantic coherence of columns
- Allows to see a table through the lens of analogies
 - e.g., from pairs of columns, France : Paris :: Germany : Berlin
- Filling missing values → analogy solving
 - Retrieval (entity in KG) or generation (entity not in KG)
- Disambiguation → choose the entity that maximizes analogy detection

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- **Scalability issue:** from “Country” and “Capital” → 12 analogies
- Are all analogies necessary? Restricting to the most *useful*?

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- **Alternative view** (Prade et al. 2010; Hug et al. 2016)

- Rows r_i vectors $\vec{r}_i = (r_{i1}, r_{i2}, \dots, r_{in})$
- Analogies holding b/w some components $J \subset [1, n]$
- Analogies should hold b/w remaining components

$$\frac{\forall j \in J, r_{1j} : r_{2j} :: r_{3j} : r_{4j}}{\forall k \in [1, n] \setminus J, r_{1k} : r_{2k} :: r_{3k} : r_{4k}}$$

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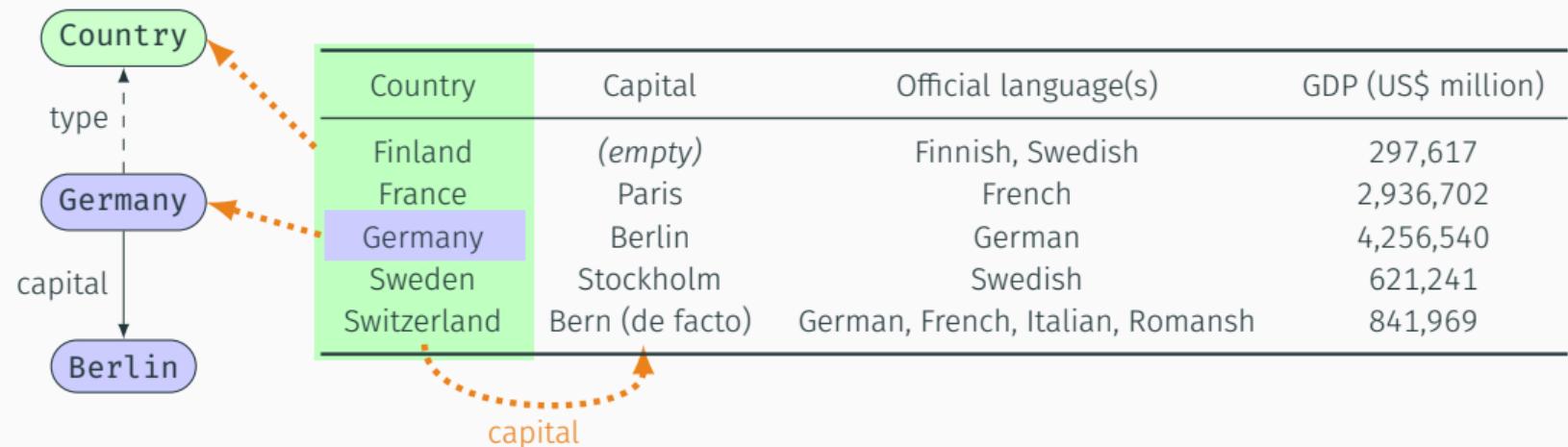
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- **Scalability?**

- **(Dis)advantages of each view?**

Analogies to support Semantic Table Interpretation: opportunities & challenges

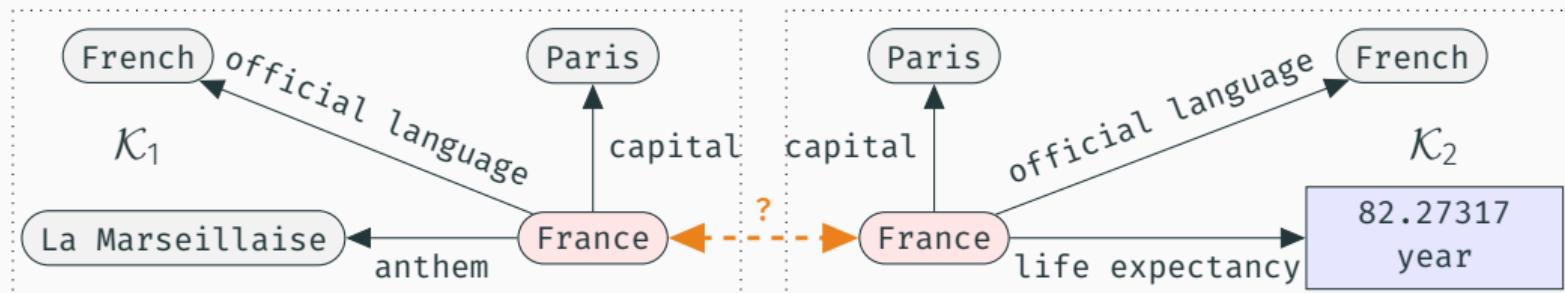


- **Interactions between analogies and STI**
 - Analogy tasks could rely on graph or table embeddings
- **Challenges**
 - Cells with multiple entities, mix of entities and literals, other forms of tables, ...

Knowledge Matching

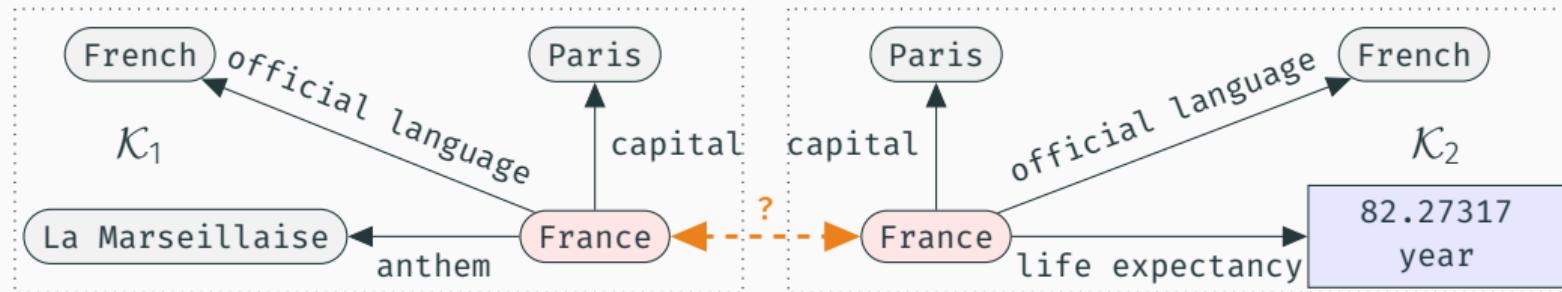
Knowledge Matching: definition

- KGs are concurrently published and edited → possible overlaps
→ **Key task in matching their content** (Euzenat et al. 2013)



Identifying, within aggregated KGs or across KGs,
equivalent, more specific, weakly related, or contradictory elements
(e.g., nodes, predicates)

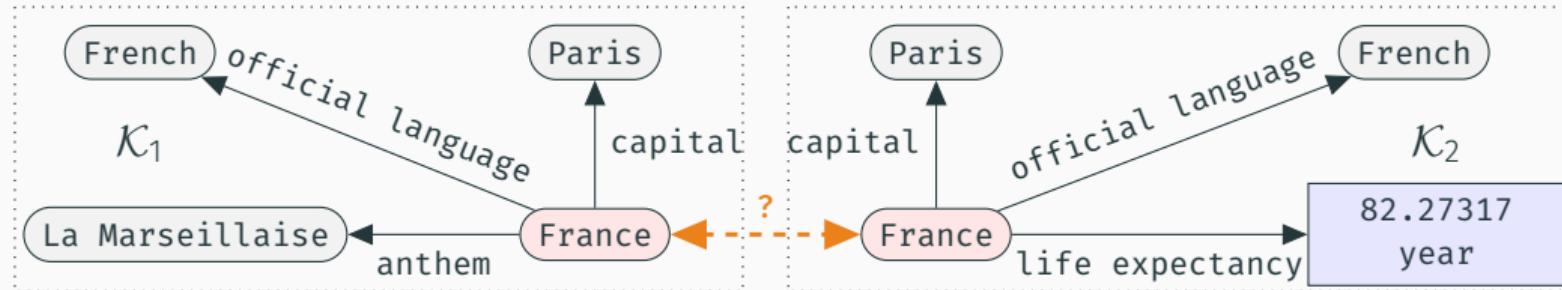
Analogies to support Knowledge Matching



Analogy-based node matching

- Nodes can be seen in analogies with their neighbors
e.g., based on the **capital** predicate, $\text{France}_{\mathcal{K}_1} : \text{Paris}_{\mathcal{K}_1} :: \text{France}_{\mathcal{K}_2} : \text{Paris}_{\mathcal{K}_2}$

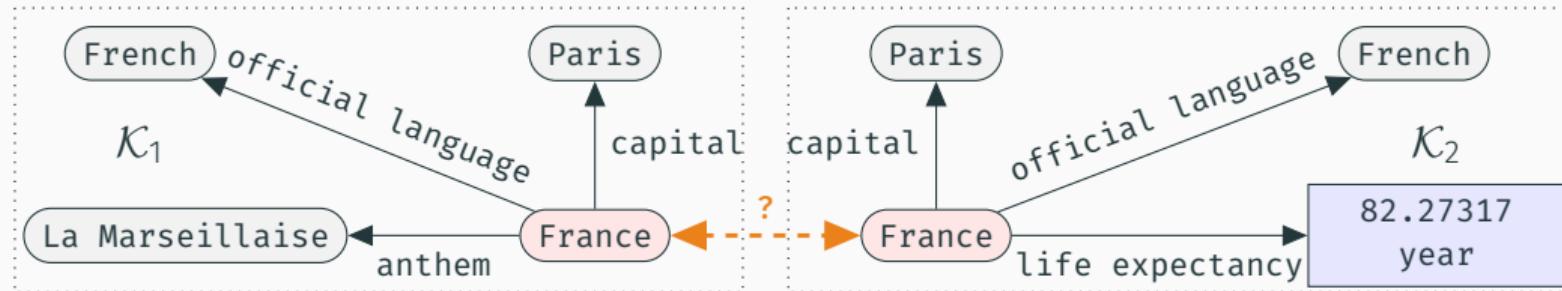
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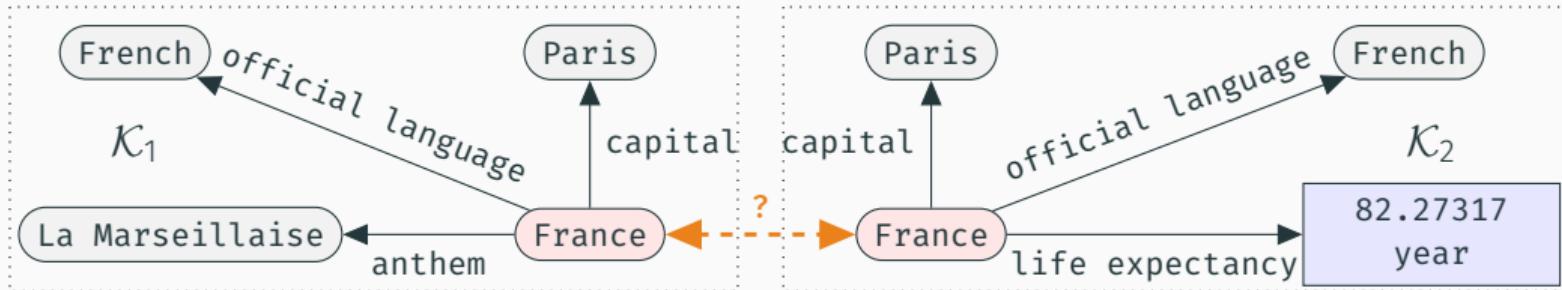
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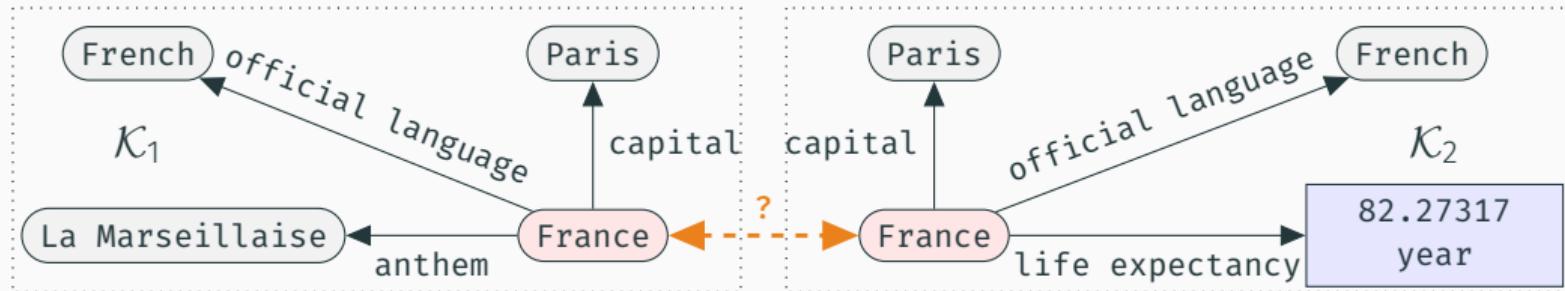
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- Scalability? Sufficient overlaps?**

Analogies to support Knowledge Matching



Analogy-based node matching (alternate view – analogy solving)

- Based on alignments: predicting x such that

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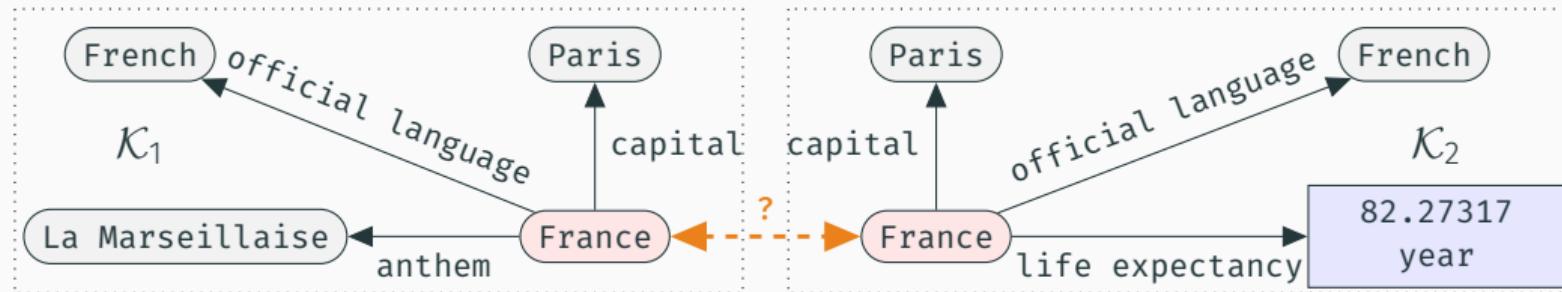
Choose the mostly output x

- Based on existing edges: predicting x such that

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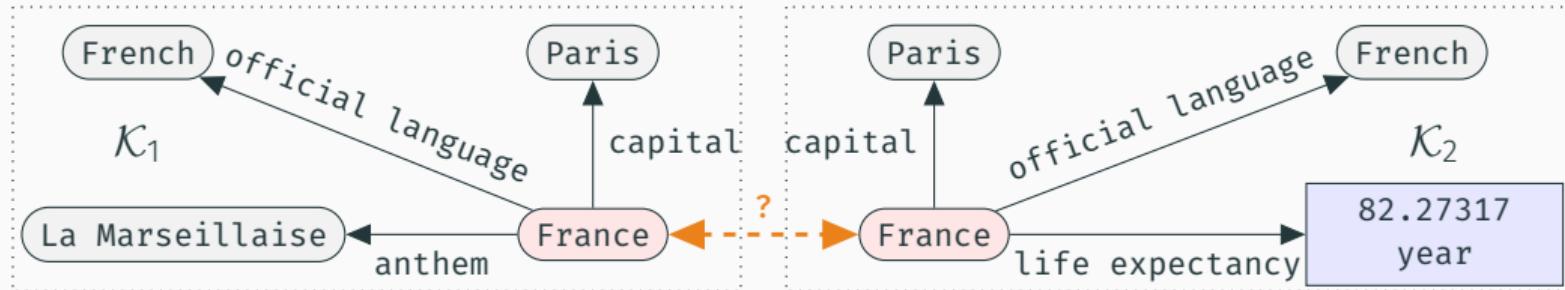
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Scalability? Completeness?

Analogies to support Knowledge Matching



Analogy-based predicate matching (**analogy detection**)

Analogical proportions hold between linked entities → identical predicates

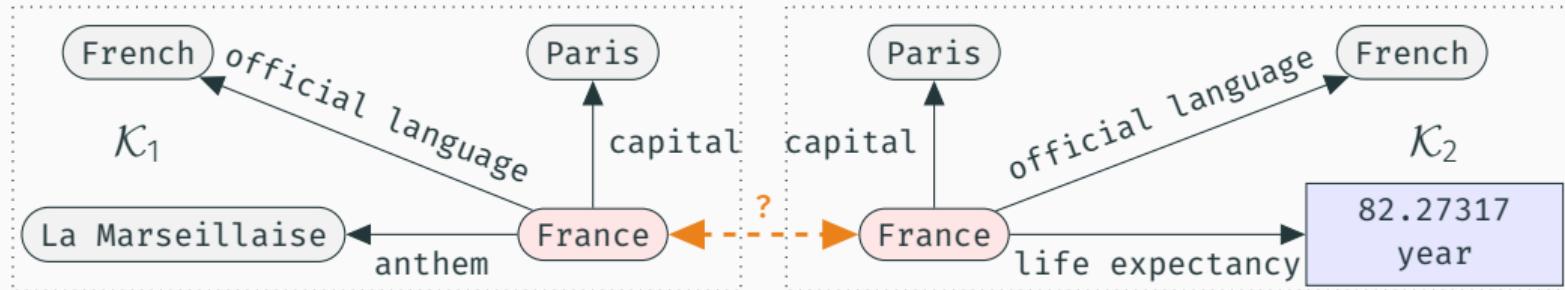
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$$\rightarrow \text{capital}_{\mathcal{K}_1} = \text{capital}_{\mathcal{K}_2}$$

Analogies to support Knowledge Matching



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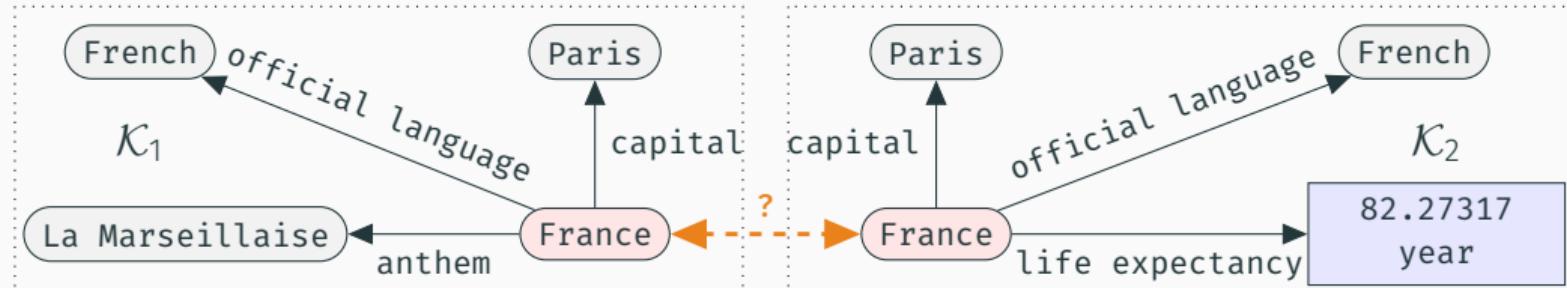
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Scalability?

Analogies to support Knowledge Matching: opportunities & challenges



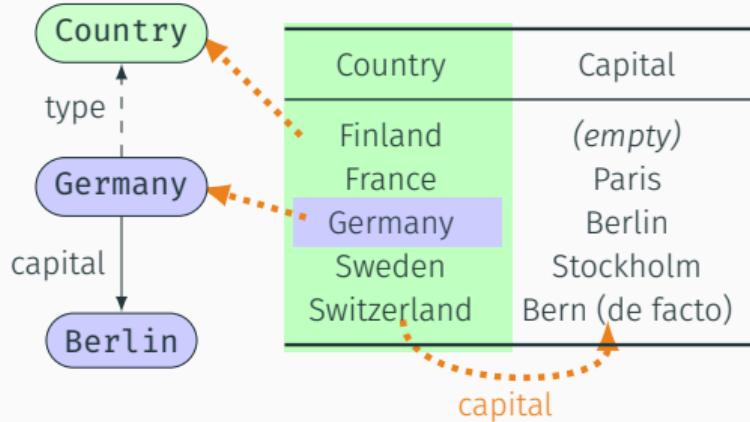
- Integrate analogical inference in knowledge matching matching
→ Analogical inference in symbolic or graph embedding-based approaches
- Challenges
→ Mix of entities and literals, completeness / sufficient overlaps, ...

Conclusion & Perspectives

Conclusion & Perspectives

- Analogies naturally appear in KG-related tasks
 - Semantic Table Interpretation
 - Knowledge Matching
- Similarly to NLP, one could leverage Knowledge Graph Embedding
- Open questions
 - Actual improvement in performance?
 - Analogical setting to choose?
 - Scalability?
- Other interactions to study?
e.g., analogies and KGs to support eXplainable AI (Hüllermeier 2020; Tiddi et al. 2022)

Thank you for your attention!

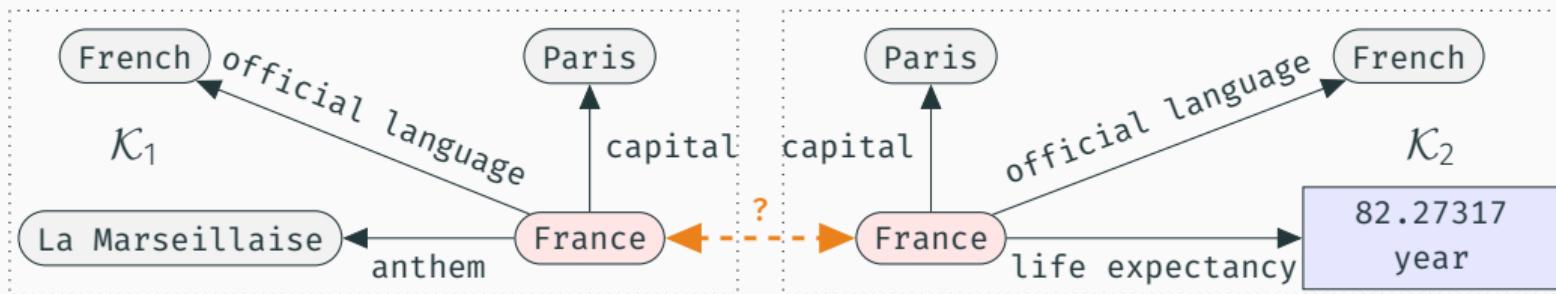


Analogy for STI

France : Paris :: Finland : ?

Analogy for Knowledge Matching

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Bibliography i

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