

# Dual Supervised Learning

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# Motivations

- NLG는 auto-regressive task로, teacher forcing을 통해 학습
  - 학습과 추론 방법 사이에 괴리가 생겨, 성능이 저하될 수 있음
- MRT(RL)은 괴리가 없으나, 샘플링 기반 방식이므로 매우 비효율적임
- MLE 방식 위에서, regularization을 통해 문제를 풀 수는 없을까?

# Bayes Theorem

- From Bayes theorem:

$$P(y|x) = \frac{P(x|y)P(y)}{P(x)}$$

- Given dataset, it would be always true,

$$\mathcal{B} = \{x^n, y^n\}_{n=1}^N$$

$$P(y^n|x^n)P(x^n) = P(x^n|y^n)P(y^n)$$

$$\log P(y^n|x^n) + \log P(x^n) = \log P(x^n|y^n) + \log P(y^n)$$

# Equations

- Objectives:

$$\hat{\theta}_{x \rightarrow y} = \operatorname{argmin}_{\theta_{x \rightarrow y} \in \Theta} \sum_{i=1}^N \ell(f(x^i; \theta_{x \rightarrow y}), y^i)$$

$$\hat{\theta}_{y \rightarrow x} = \operatorname{argmin}_{\theta_{y \rightarrow x} \in \Theta} \sum_{i=1}^N \ell(f(y^i; \theta_{y \rightarrow x}), x^i)$$

$$\text{s.t. } P(y^i | x^i) P(x^i) = P(x^i | y^i) P(y^i).$$

# Equations

- New Objectives:

$$\mathcal{L}(\theta_{x \rightarrow y}) = \sum_{i=1}^N \left( \ell(f(x^i; \theta_{x \rightarrow y}), y^i) + \lambda \mathcal{L}_{\text{dual}}(x^i, y^i; \theta_{x \rightarrow y}, \theta_{y \rightarrow x}) \right)$$

$$\mathcal{L}(\theta_{y \rightarrow x}) = \sum_{i=1}^N \left( \ell(f(y^i; \theta_{y \rightarrow x}), x^i) + \lambda \mathcal{L}_{\text{dual}}(x^i, y^i; \theta_{x \rightarrow y}, \theta_{y \rightarrow x}) \right)$$

where  $\mathcal{L}_{\text{dual}}(x^i, y^i; \theta_{x \rightarrow y}, \theta_{y \rightarrow x}) = \left\| \left( \log P(y^i | x^i; \theta_{x \rightarrow y}) + \log \hat{P}(x^i) \right) - \left( \log P(x^i | y^i; \theta_{y \rightarrow x}) + \log \hat{P}(y^i) \right) \right\|_2^2$ .

# Equations

- Note that we need to get derivative of each model:

$$\mathcal{L}(\theta_{x \rightarrow y}) = \sum_{i=1}^N \left( \ell(f(x^i; \theta_{x \rightarrow y}), y^i) + \lambda \mathcal{L}_{\text{dual}}(x^i, y^i; \theta_{x \rightarrow y}, \theta_{y \rightarrow x}) \right)$$

$$\mathcal{L}(\theta_{y \rightarrow x}) = \sum_{i=1}^N \left( \ell(f(y^i; \theta_{y \rightarrow x}), x^i) + \lambda \mathcal{L}_{\text{dual}}(x^i, y^i; \theta_{x \rightarrow y}, \theta_{y \rightarrow x}) \right)$$

where  $\mathcal{L}_{\text{dual}}(x^i, y^i; \theta_{x \rightarrow y}, \theta_{y \rightarrow x}) = \left\| (\log P(y^i | x^i; \theta_{x \rightarrow y}) + \log \hat{P}(x^i)) - (\log P(x^i | y^i; \theta_{y \rightarrow x}) + \log \hat{P}(y^i)) \right\|_2^2$ .

$$\nabla_{\theta_{x \rightarrow y}} \mathcal{L}_{\text{dual}}(x^i, y^i; \theta_{x \rightarrow y}, \theta_{y \rightarrow x}) = \nabla_{\theta_{x \rightarrow y}} \left\| (\log P(y^i | x^i; \theta_{x \rightarrow y}) + \log \hat{P}(x^i)) - (\log P(x^i | y^i; \theta_{y \rightarrow x}) + \log \hat{P}(y^i)) \right\|_2^2.$$

# Evaluation

- MLE 방식이지만, 기존의 RL 방식을 뛰어넘음

Table 2. Summary of some existing En→Fr translations

Model	Brief description	BLEU
NMT[1]	<i>standard NMT</i>	33.08
MRT[2]	<i>Direct optimizing BLEU</i>	34.23
DSL	<i>Refer to Algorithm 1</i>	<b>34.84</b>
[1] (Jean et al., 2015); [2] (Shen et al., 2016)		

← MLE with Cross Entropy

← Reinforcement Learning

# Summary

- MLE 방식 위에서, teacher forcing으로 인한 괴리를 해결하려 함
  - 비효율적인 RL을 쓰지 않고도, 더 뛰어난 성능 확보 가능
- Bayes Theorem을 통해 유도된 매우 간단하고 직관적인 regularization term
- 하나의 병렬 코퍼스로부터, 두 개의 모델을 동시에 학습하며 시너지 효과
  - 언어 모델이 추가로 필요한 것은 단점으로 작용