

Homework-1

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1.(a) Calculate the square root of 625

We use mathematical function `sqrt()` to find the square root of a number. `sqrt(x)` computes the (principal) square root of `x`,

```
xSqrt <- sqrt(625)
```

$$\Rightarrow \sqrt{625} = 25$$

1.(b) Create a new object `y` and assign a value 100 to it

```
y <- 100
```

$$\Rightarrow y = 100$$

1.(c) Calculate the natural logarithm of `y`

```
lne <- log(y,base=exp(1))
```

$$\Rightarrow \ln_e(100) = 4.6051702$$

1.(d) Calculate the logarithm to base 10 of `y`

```
l10 <- log(y,base=10)
```

$$\Rightarrow \log_{10}(100) = 2$$

2.(a) Generate 1000 random numbers from a normal distribution with mean 0 and standard deviation 1

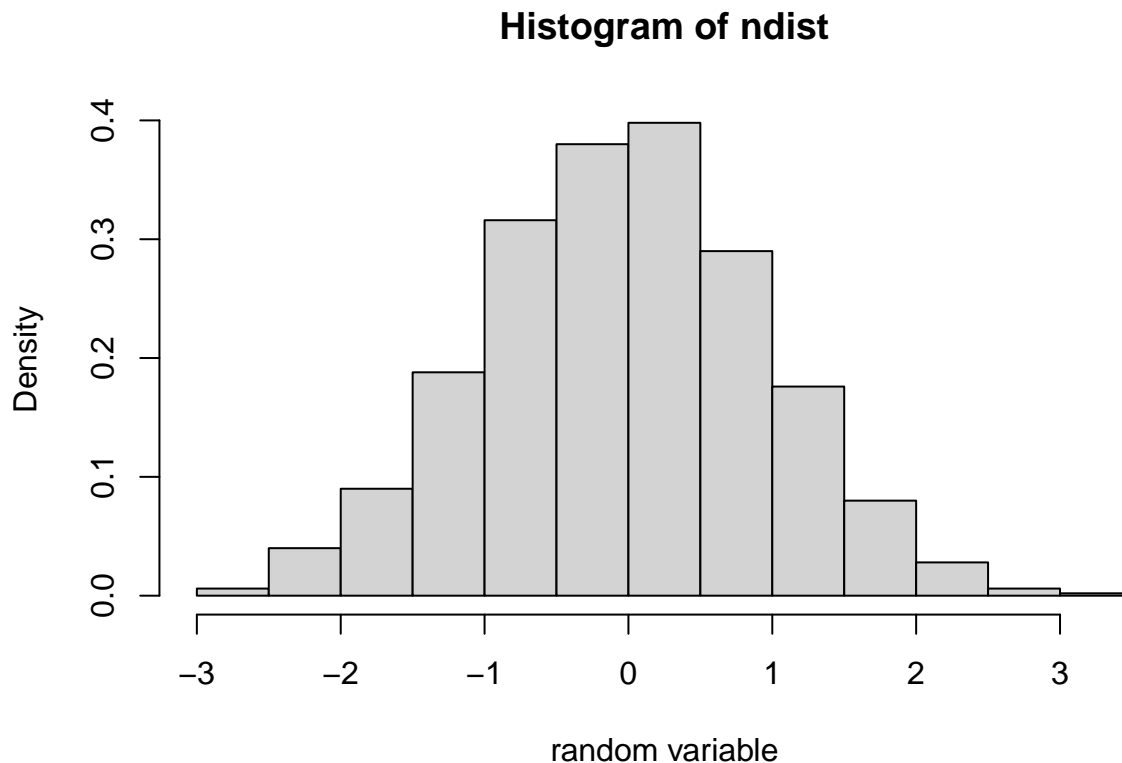
Normal distribution is a probability distribution that describes how the values of a variable are distributed. It is a symmetric distribution where most of the observations cluster around the central peak and the probabilities for values move away from the mean reduce equally in both directions. Normal distribution has two parameters, mean and standard deviation. We use 'rnorm' function to generate a normal distribution for given mean and standard deviation.

```
set.seed(4)
ndist <- rnorm(1000,mean=0,sd=1)
```

2.(b) Plot the histogram of the above normal distribution

We use generic function 'hist' to plot the distribution of a given variable.

```
hist(ndist, xlab='random variable',freq=FALSE)
```



2.(c) Calculate Mean, Standard deviation, Variance, Standard error, minimum, maximum, Median and Range of 1000 random numbers

Mean -

It is the average of the given set of numbers, that is, ratio of the sum of the numbers to the total number. We use function 'mean' to compute.

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

```
m <- mean(ndist)
```

⇒ mean = -0.034428

Variance -

It is the mean of the numbers formed by squared differences of original set from the mean. It is a numerical measure of how the data values are dispersed around the mean. We use 'var' function to compute.

```
v <- var(ndist)
```

⇒ variance = 0.9395492

Standard deviation -

The Standard Deviation is a measure of how spread out numbers are. it is the square root of the Variance. We use the function 'sd' to compute

```
stdv <- sd(ndist)
```

⇒ Standard deviation = 0.9693035

Standard error -

If a statistically independent sample of 'n' observations are taken with a standard deviation of σ , then the mean value calculated from the sample will have an associated standard error on the mean given by,

$$SE = \frac{\sigma}{\sqrt{n}}$$

```
se <- stdv/sqrt(length(ndist))
```

⇒ Standard Error = 0.0306521

Minimum -

```
mi <- min(ndist)
```

⇒ Minimum = -2.8395831

Maximum -

```
mx <- max(ndist)
```

⇒ Maximum = 3.1741867

Median -

It is the value separating the higher half from the lower half of a data sample. We use the function 'median' to compute

```
med <- median(ndist)
```

⇒ Median = -0.0397932

Range -

It is a vector containing the minimum and maximum of all the given arguments. We use the function 'range' to compute

```
rg <- range(ndist)
```

⇒ Range = -2.8395831, 3.1741867