

## SOLUTION OF EXERCISESHEET 6

#### Exercise 6-1

(a)

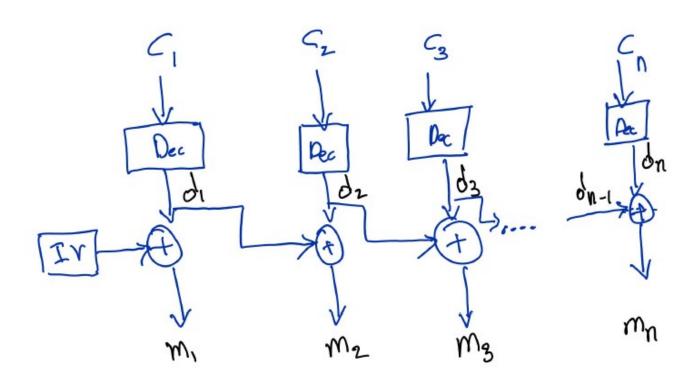


Figure 1: Decryption for CBC\* mode

(b) As shown in the above figure, let us assume

$$d_i = \mathsf{Dec} (c_i)$$

So

$$m_1 = d_1 \oplus IV$$
  
$$m_2 = d_2 \oplus d_1 \dots$$

To show that this CBC\* doesn't have indistinguishable encryptions, let us consider message in the format  $m=m_1||m_2||m_3||...||m_n$ . Also we know for CPA, adversary A is allowed of multiple encryptions.

Let us consider A choose two messages i.e., m1 and m2

$$m1 = m1_1 || m1_2 || m1_3 || ... || m1_n$$
  
 $m1 = m2_1 || m2_2 || m2_3 || ... || m2_n$ 

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And m1 is choosen in such a way that  $m1_1 == m1_2 == m1_3 == \dots == m1_n$  and m2 is choosen in such a way that  $m2_1 \neq m2_2 \neq m2_3 \neq \dots \neq m2_n$ 

With these kind of messages choosen, A can distingush m1 and m2 by checking

$$c_1 == c_3 == \dots == c_i$$
  
 $c_2 == c_4 == \dots == c_{i+1}$   
where  $i$  is an odd number  $\leq n$ 

If the above check is statisfied then the cipher c corresponds to m1. Else it corresponds to m2. With this construction A can distingush between the messages with a probability equal to 1.

#### Exercise 6-2

**Task:** Show that  $\Pi_{CBC}$  is not CCA-secure by demonstrating a successful adversary. Assume n=3

The adversary  $\mathcal{A}$  can choose the two messages  $m_0=m_0^1||m_0^2=000\ 000$  and  $m_1=m_1^1||m_1^2=111\ 111$  which he sends to the challenger. Then he gets the ciphertext  $c_b=(c_b^0||c_b^1||c_b^2)=(IV||f_k(IV\oplus m_b^1)||f_k(f_k(IV\oplus m_b^1)\oplus m_b^2))$  back.

Then  $\mathcal A$  flipps the last bit from  $c_b^2$ , so  $(c_b^2)'=c_b^2\oplus 001$  and asks the decryption oracle for the decryption of  $c_b'=c_b^0||c_b^1||(c_b^2)'$ . Because  $c_b'\neq c_b$  the decryption oracle answers with  $m'=f_k^{-1}(c_b^1)\oplus c_b^0||f_k^{-1}(c_b^2)\oplus c_b^1=f_k^{-1}(f_k(IV\oplus m_b^1))\oplus IV||f_k^{-1}((c_b^2)')\oplus f_k(IV\oplus m_b^1)=m_b^1||f_k^{-1}((c_b^2)')\oplus f_k(IV\oplus m_b^1)$  is now either  $m_0^1$  or  $m_1^1$  because the change in  $(c_b^2)'$  doesn't impact  $m_b^1$ . So the adversary can say for sure, if the recieved civertext  $c_b$  is the encoding for  $m_0$  or  $m_1$ .

 $\Rightarrow \Pi_{CBC}$  mode is not CCA-secure

#### Exercise 6-3

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a) Let F be a pseudorandom permutation. Then F and  $F^{-1}$  are pseudorandom permutations.

 $\Pi_{M} = (Gen, Mac, Vrfy)$ 

$$\begin{array}{ccc} \underline{\mathrm{Gen}(1^{\lambda})} & \underline{\mathrm{Mac_k(c)}} & \underline{\mathrm{Vrfy_k(c,t)}} \\ k \leftarrow \mathrm{Gen}(1^{\lambda}) & \underline{t} \leftarrow \mathrm{F}_k^{-1}(c) & \text{if } t = \mathrm{Mac_k}(m) \\ \mathbf{return} \ k & \mathbf{return} \ t & \mathbf{return} \ 1 \\ & \mathbf{return} \ 0 & \end{array}$$

 $\Pi_{\rm E} = ({\rm Gen, Enc, Dec})$ 

Because  $\operatorname{Enc}_k(m), \operatorname{Mac}_k(\operatorname{Enc}_k(m)) = \operatorname{F}_k(m \parallel r), \operatorname{F}_k^{-1}(\operatorname{F}_k(m \parallel r)) = \operatorname{F}_k(m \parallel r), (m \parallel r)$ 

**TODO** Beweise