



$$T(x,0) = T_i = T_{w0} = 4ab \text{ [K]}$$

$$-k \left. \frac{\partial T}{\partial x} \right|_{x=0} = h [T_{\infty} - T(0,t)]$$

$$\eta = x / (4\alpha t)^{1/2}$$

$$\alpha = \frac{k}{\rho c} = \frac{3b}{70ab \times 6ab}$$

Case 3 for semi-infinite solids:

$$\frac{T(x,t) - T_i}{T_{\infty} - T_i} = \text{erfc}\left(\frac{x}{2\sqrt{\alpha t}}\right) - \left[\exp\left(\frac{hx}{k} + \frac{h^2 \alpha t}{k^2}\right) \right] \left[\text{erfc}\left(\frac{x}{2\sqrt{\alpha t}} + \frac{h\sqrt{\alpha t}}{k}\right) \right]$$

where, $\text{erfc } w = 1 - \text{erf } w$

$T(0.1b [m], 3b \times 60 \text{ sec.}) \rightarrow$ we need to find

Using the formula,

$$\frac{T - 4ab}{3ab - 4ab} = \operatorname{erfc}\left(\frac{0.1b}{2\sqrt{\frac{3b \times 3b \times 60}{70ab \times 6ab}}}\right)$$

$$- \exp\left(\frac{1ab \times 0.1b}{3b} + \frac{(1ab)^2 \times (3b)^2 \times 60}{70ab \times 6ab \times (3b)^2}\right)$$

$$\times \operatorname{erfc}\left(\frac{0.1b}{2\sqrt{\frac{(3b)^2 \times 60}{70ab \times 6ab}}} + \frac{1ab \sqrt{\frac{3b^2 \times 60}{70ab \times 6ab}}}{3b}\right)$$

Let $a = 7$ $b = 1$

$$\frac{T - 471}{371 - 471} = \operatorname{erfc}\left(\frac{0.11}{0.2204}\right) - \exp\left(\frac{171 \times 0.11}{31} + \frac{(171)^2 \times 60}{7071 \times 671}\right)$$

$$\times \operatorname{erfc}\left(\frac{0.11}{0.2204} + \frac{171 \times 0.1102}{31}\right)$$

$$\frac{T - 471}{371 - 471} = \operatorname{erfc}(0.499) - \exp(0.975) \times \operatorname{erfc}(1.107)$$

$$\frac{T - 471}{371 - 471} = [1 - \operatorname{erf}(0.499)] - \exp(0.975) \times [1 - \operatorname{erf}(1.107)]$$

Using Appendix B:

$$w = 0.499 \rightarrow \text{erf}(0.499) \approx 0.5203$$

$$w = 1.107 \rightarrow \text{erf}(1.107) \approx 0.88$$

Then,

$$\frac{T - 471}{-100} = (1 - 0.5203) - 2.6511 \times (1 - 0.88)$$

$$\frac{T - 471}{-100} = 0.161$$

T @ 0.11m after $31 \times 60 \text{ sec}$:

$$T = 471 - 16.1 = 454.9 \text{ [K]}$$