$$\min_{x \in \mathbb{R}, y \in \mathbb{Z}} (a - x)^2 + 50(y - x^2)^2$$

$$|s. t. y \ge \frac{1}{2}b, x^2 \le b, x \le 0, y \ge 0$$

**Input:** 
$$a = 3.83$$
,  $b = 6.04$ 

**Solution Mapping**  $\pi_{\Theta_1}$  as Continuous Relaxation

## **Hidden State:**

$$h_x = -0.68, h_v = 9.49$$



## **Relaxed Solution:**

$$\bar{x} = -1.17, \bar{y} = 2.98$$

## **Update Continuous Var:**

$$\hat{x} = \bar{x} + h_x = -1.85$$

## **Round Integer Var:**

Sigmoid
$$(h_y) \ge 0 \to \hat{y} = [\bar{y}] = 3$$

Loss Function:  $\mathcal{L}_{Obj} + \lambda \cdot \mathcal{L}_{Penalty}$