

## Amazon Co-purchasing Network Analysis

The project uses the Amazon Product Co-purchasing network dataset to analyze the relationship between each product and their similarity. The first thing is writing a read file function, which reads the data set that contains pairs of size values separated by whitespace and returns them as a vector of tuples. Second, I am trying to find communities, in which I use Tarjan's strongly connected components (SCC) algorithm for detecting communities in an undirected graph. I use the **petgraph** crate's `UnGraph` and **tarjan\_scc** algorithm to find strongly connected components. The algorithm uses a depth-first search with a stack to traverse the graph and identify strongly connected components. The result that I get contains vectors of node indices representing the strongly connected components in the graph. In `friend analysis.rs`, there are three different functions. The `subgraph` function takes a vector of edges and a vector of node indices representing a community. It creates an undirected graph (`UnGraph`) from the input edges, converting node indices to `NodeIndex`. The `calculate_product_similarity` Function initializes a `HashMap (product_similarity)` to store the product similarities between nodes in the community and then iterates over each pair of nodes in the community and calculates the Jaccard similarity based on common neighbors. The `analyze_friend_of_friend` function takes a vector of edges (`edges`), a vector of node indices representing a community (`community`), and a `HashMap` of product similarities and initializes a `HashMap (common_customers)` to store the count of common customers between pairs of nodes. Then the function iterates over pairs of nodes in the community and counts the common neighbors. Then, the results are stored in the `common_customers` `HashMap` and sorted in descending order based on the count of common customers.

The main function reads the `amazon.txt` file and stores the result in the `edges`. It creates a subset of edges (`edges_subset`) by cloning and taking the first `subset_size` elements from the `edges` vector. It uses the `find_communities` function to detect communities in the graph represented by `edges`. Then iterates over the detected communities, printing details for each community using the `print_community_details` function. After that, for each community, it calculates product similarity using the `calculate_product_similarity` function and analyzes friend-of-friend relationships using the `analyze_friend_of_friend` function.

Output:

Component 0: [0, 10, 1035, 355, 155, 2838, 4161, 1528, 1705, 16666, 71407, 191581, 26607, 26608, 26606, 122385, 158520, 159994, 307320, 348286, 348285, 381167, 154530, 154538, 163073, 163072, 154537, 154535, 154534, 154533, 154536, 154532, 154531, 151148, 1744, 1946, 1743, 11379, 14862, 44489, 122582, 201211, 224601, 237491, 224600, 224602, 241996, 241995, 304687, 354118, 161233, 247296, 328247]

Friend-of-Friend Analysis in Community 0:

Pair: (10, 15), Common Customers: 1, Jaccard Similarity: 0.25

Pair: (9, 10), Common Customers: 1, Jaccard Similarity: 0.25

Pair: (15, 10), Common Customers: 1, Jaccard Similarity: 0.25

Pair: (0, 10), Common Customers: 1, Jaccard Similarity: 0.25

Pair: (10, 9), Common Customers: 1, Jaccard Similarity: 0.25

Component 1: [1, 3943, 5919, 102346, 121904, 74677, 121903, 93657, 223249, 266551, 326328, 337155, 164250, 229240, 323666, 270056, 270057, 283097, 316322, 316321, 316320, 316319, 316318, 303666, 233742, 344550, 357993, 357992, 46, 112, 184, 2515, 2508, 6384, 6383, 9779, 59033, 150127, 249195, 264908, 265017, 265016, 265015, 339300, 382855, 381334, 374958, 374836, 380743, 383216, 374835, 374957, 374956, 374834, 374833, 374832, 374831, 374829, 366242, 374830, 279778, 249194, 279779, 330965, 356453, 330960, 330963, 347789, 341531, 341532, 340106, 340102, 341530, 341529, 274201, 350779, 368989, 389904, 368988, 387655, 395772, 158281, 294325, 294327, 296116, 295161, 295088, 294463, 294462, 294326, 294324, 294323, 272153, 265700, 158282, 158279, 158278, 70994, 268661, 351112, 384444, 384442, 384443, 384441, 384440, 158276, 245516, 143445, 143447, 174377, 199205, 265014, 339101, 363826, 382801, 380143, 380142, 390808]

Friend-of-Friend Analysis in Community 1:

Pair: (3, 3), Common Customers: 0, Jaccard Similarity: 0.00

Component 2: [2, 118, 189, 246, 1139, 28933, 65061, 17769, 29547, 29549, 39338, 112012, 267536, 290015, 290014, 290013, 290012, 37765, 112011, 244, 13798, 14307, 14306, 164877, 192186, 297436, 239839, 192516, 299996, 358377, 376108, 358376, 358375, 382109, 382108, 382110, 374624, 196032, 239100, 346833, 5, 53, 117, 28927, 257211, 257210, 252125, 185176, 217640, 251126, 324318, 324317, 324316, 324315, 301859, 301856, 315723, 315721, 363049, 363048, 87730, 149745, 261331, 149748, 110280, 211247, 159748, 203100, 282415]

Friend-of-Friend Analysis in Community 2:

Pair: (0, 1), Common Customers: 1, Jaccard Similarity: 0.17

Pair: (1, 0), Common Customers: 1, Jaccard Similarity: 0.17

Pair: (1, 1), Common Customers: 0, Jaccard Similarity: 0.00

Pair: (0, 0), Common Customers: 0, Jaccard Similarity: 0.00

Component 3: [3, 4955, 5543, 12774, 5542, 235, 12469, 33305, 37283, 67779, 57111, 57112, 30748, 30747, 65962, 119130, 255974, 97377, 130690, 222099, 284920, 284923, 339512, 284922, 284921, 250684, 248898, 179320, 248899, 269631, 277644, 333008, 277645, 179919, 146498, 179918, 185783, 45, 1045, 2749, 10308, 23576, 33358, 96718, 113673, 272420, 272421, 272419, 139220, 138470, 304082, 284768, 80408, 113672, 232536, 144707, 221697, 226967, 226968, 144706, 188175, 143361, 143360, 131839, 143359, 131838, 128263, 131840, 126350, 126348, 126349, 80409, 89150, 89148, 65243, 35046, 80410, 190176, 232539, 264512, 312335, 317961, 365521, 380508, 380510, 338643, 380509, 312334, 312333, 239317, 264510, 232537, 232535, 157495, 157493, 159014, 157494, 157492, 157491, 91450, 70047, 54216, 54214, 54215, 54211, 54213, 54217, 54212, 54210, 54209, 22476, 22474, 396077, 379431, 340727, 340726, 54690, 93469, 93466, 94501, 299724, 93468, 93467, 93465, 86012, 211877, 60220, 12111, 29620, 29619, 78105, 78103, 163554, 134383, 177156, 177157, 201194, 194816, 194815, 194814, 215123, 334160, 357987, 348499, 348501, 348500, 245966, 327837, 331580, 358872, 212981, 225591, 307336, 225590, 368598, 368597, 10977, 45527, 153609, 191424, 246939, 115366, 259164, 292405, 293433, 292406, 292404, 293434, 356842, 389565, 389606, 397707]

Friend-of-Friend Analysis in Community 3:

Pair: (8, 8), Common Customers: 0, Jaccard Similarity: 0.00

Pair: (2, 8), Common Customers: 0, Jaccard Similarity: 0.00

Pair: (8, 2), Common Customers: 0, Jaccard Similarity: 0.00

Pair: (2, 2), Common Customers: 0, Jaccard Similarity: 0.00

Component 4: [4, 1033, 1522, 2341, 13740, 106134, 280396, 311622, 311621, 311620, 311619, 17498, 109014, 297567, 359577, 365409, 365758, 371005, 54, 1053, 2750, 45481, 1961, 14013, 52348, 23398, 23399, 37647, 101001, 174415, 211002, 211001, 245772, 245770, 333940, 110039, 110048, 185528, 164345, 164349, 173455, 237334, 262586, 262587, 171655, 170099, 170103, 193792, 331515, 371999, 371998, 371997, 371996, 360352, 279368, 331509, 331514, 331513, 331512, 331511, 331510, 64960, 125883, 113460, 166372, 215924, 215926, 215927, 218683, 296256, 324169, 183905, 131886, 73210, 95575, 95576, 73209, 73208, 73206, 54589, 54588, 54587, 54586, 73207, 54585, 54584, 54583, 324167, 324166, 357876, 245426, 230072, 328401]

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In component 0: the list of number are node indices that belong to this community.

For each pair of nodes, the output provides information such as:

- Pair: (node1, node2): The indices of two nodes in the community.

- Common Customers: The number of common customers (neighbors) between the two nodes.
- Jaccard Similarity: The Jaccard similarity coefficient is calculated based on the common neighbors.