

# Package ‘HyperCube’

June 10, 2015

**Type** Package

**Title** Hypercube Estimator

**Version** 0.1-0

**Date** 2015-06-08

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## Description

The package ``HyperCube'' provides functions and methods for fitting linear model with hypercube estimator. This package is an implementation of the hypercube estimators introduced in [Beran, Rudolf. ``Hypercube estimators: Penalized least squares, submodel selection, and numerical stability.''' Computational Statistics & Data Analysis 71 (2014): 654-666.].

**Depends** R (>= 3.1.0)

**Imports** expm, Matrix, MASS, testthat

**LazyData** true

**License** GPL

**Suggests** knitr

**VignetteBuilder** knitr

**NeedsCompilation** no

## R topics documented:

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|-------------------|--------------------------|
| canadian.earnings | <i>Canadian earnings</i> |
|-------------------|--------------------------|

---

### Description

The canadian.earnings data frame has 205 pairs observations on Canadian workers from a 1971 Canadian Census Public Use Tape (Ullah, 1985).

### Usage

canadian.earnings

### Format

A data frame with 205 rows and 2 variables:

**age** age in years.

**log.income** logarithm of income.

### Source

Ullah, A. (1985). Specification analysis of econometric models. Journal of Quantitative Economics, 2, 187-209

---

|        |  |
|--------|--|
| dental | <i>The hardness of 120 dental fillings</i> |
|--------|--|

---

### Description

A dataset containing the response measures the hardness of dental filling obtained by 5 Dentists using 8 Gold alloys and 3 Condensation methods. The objective of the experiment was to find a dental gold filling with greater hardness.

### Usage

dental

### Format

A data frame with 120 rows and 4 variables:

**y** response measures the hardness of dental fillings

**G** the indice of 8 Gold alloys

**C** the indice of 3 Condensation methods

**D** the indice of 5 Dentists

## Details

Seheult and Tukey (2001) analyzed a three-factor layout in which the response measures the hardness of dental fillings obtained by 5 Dentists (D) using 8 Gold alloys (G) and 3 Condensation methods (C). The objective of the experiment was to find a dental gold lling with greater hardness. Condensation, properly carried out, was known to increase the hardness of a filling. The three condensation techniques used in the experiment were: (1) electromalleting, in which blows are delivered mechanically at a steady frequency; (2) hand malleting, in which a small mallet is used to deliver blows; and (3) hand condensation. The reported hardness observations are each averages of ten measurements that are not available. It was reported anecdotally that dentist 5 appeared to be physically tired before the experiment.

## Source

Seheult, A. H. and Tukey, J. W. (2001). Towards robust analysis of variance, Data Analysis from Statistical Foundations (eds. A. K. Mohammed and E. Saleh), 217-244, Nova Science Publishers, New York.

---

diffMatrix

*Difference Matrix*


---

## Description

The difference matrix described in equation (3.10) in Beran (2014).

## Usage

```
diffMatrix(p, dth)
```

## Arguments

|     |                            |
|-----|----------------------------|
| p   | number of coefficients     |
| dth | order of difference matrix |

## Examples

```
p <- 10
D <- diffMatrix(p, 5)
D
```

---

estRisk

*Estimate Risk*


---

## Description

Estimate Risk

## Usage

```
estRisk(X, y, A, estsig)
```

**Arguments**

|        |                     |
|--------|---------------------|
| X      | design matrix       |
| y      | observation         |
| A      | hypercuber operator |
| estsig | estimated variance  |

**Value**

The estimated risk

**References**

Beran, Rudolf. "Hypercube estimators: Penalized least squares, submodel selection, and numerical stability." Computational Statistics & Data Analysis 71 (2014): 654-666.

---

|          |                          |
|----------|--------------------------|
| estSigma | <i>Estimate Variance</i> |
|----------|--------------------------|

---

**Description**

Estimate Variance

**Usage**

```
estSigma(mf)
```

**Arguments**

|    |             |
|----|-------------|
| mf | model frame |
|----|-------------|

**Value**

The estimated variance

**References**

Beran, Rudolf. "Hypercube estimators: Penalized least squares, submodel selection, and numerical stability." Computational Statistics & Data Analysis 71 (2014): 654-666.

hypercube

*Hypercube Estimator Fits***Description**

The user interface for fitting linear model with Hypercube Estimator.

**Usage**

```
hypercube(...)

## Default S3 method:
hypercube(X, y, V, ...)

## S3 method for class formula
hypercube(formula, data, V, ...)
```

**Arguments**

|         |   |
|---------|---|
| ...     | other optional arguments                            |
| X       | design matrix                                       |
| y       | observation   |
| V       | symmetric matrix whose eigenvalues all lie in [0,1] |
| formula | formula to get estimate                             |
| data    | data you want to analysis                           |

**Value**

A object of the class "hypercube" containing the following:

**coefficients** Estimated coefficients  $\hat{\beta}$  under hypercube estimator

**fitted.values** Fitted values ( $\hat{\eta}$ ) under hypercube estimator

**residuals** residuals,  $y - \hat{\eta}$

**estsigma2** Estimated variance of  $\epsilon$ . If the rank of the design matrix X is greater than the number of observation, the variance is estimated using least square regression. If the rank is equal to the number of observation, and if the model has more than one factor, the variance is estimated using additive submodel fit. If neither of the above cases, users need to provide their own estimated variance.

**estrisk** Estimated risk, which involved the estimated variance.

**V** Symmetric matrix with all eigenvalues lie in [0,1]. The matrix V used the hypercube estimator.

**modelframe** The modelframe constructed from the argument formula and data.

**Methods (by class)**

- **default**: Default method for hypercube
- **formula**: Formula method for hypercube

**Note**

This package is still under development. For data with degree of freedom equal to zero, it may not be handled well. It is due the fact that it is not obvious to estimate the variance of the random error. Users need to provide estimated variance of random error in such cases.

**References**

Beran, Rudolf. "Hypercube estimators: Penalized least squares, submodel selection, and numerical stability." Computational Statistics & Data Analysis 71 (2014): 654-666.

**See Also**

[hypercubeOptimization](#)

**Examples**

```
## Example 1 in Beran (2014)
## Fitting Canadian earning data with Hypercube Estimator

# The number of age, p, in Example 1 in Beran (2014).
p <- length(unique(canadian.earnings[,1]))
# D_5 as in equation (3.10) in Beran (2014)
D <- diffMatrix(p, 5)
# The parameter nu in equation (3.11) in Beran (2014)
nu <- 100
# The matrix W in equation (3.11) in Beran (2014)
W <- nu * t(D) %*% D
# Convert W to V, as described in (1.6) in Beran (2014)
V <- plsW2V(W)
# The variable age should be considered as a factor
canadian.earnings[, "age"] <- factor(canadian.earnings[, "age"])
# Hypercube Estimator Fit
hcm0d <- hypercube( log.income ~ age -1, data=canadian.earnings, V)

# Plot of data
plot(as.numeric(as.character(canadian.earnings$age)),
     canadian.earnings$log.income,
     xlab = "age", ylab = "log(income)")
# Plot of fitted line
lines(levels(canadian.earnings$age), hcm0d$coefficients)

## Example 2 in Beran (2014)
## Fitting rat litter data

# Projection matrices as decribed in equation (5.4) in Beran (2014)
litter.proj <- projectCreate( ~ mother:infant -1, data = litter)
# If only additive effect is consider,
# take V = P1 + P2 + P3 (notation in equation (5.4) in Beran (2014))
component <- cbind(c(0,0), c(1,0), c(0,1))
V <- projectWeight(litter.proj, component = component)
# Hypercube Estimator Fit
hcm0d <- hypercube( weight ~ mother:infant -1, data = litter, V)

# Estimated Risk
summary(hcm0d)
```

```
## Hypercube Estimator with optimal risk
##
hcmoopt <- hypercubeOptimization( weight ~ mother:infant -1,
                                data = litter
                                )
# The optimal projection coefficient which minimizes the risk.
hcmoopt$projcoef

# The minimum risk
hcmoopt$estrisk

# The Hypercube Estimator fit with the V of the optimal projection.
summary(hcmoopt$est)
```

---

|              |  |
|--------------|--|
| hypercubeEst | <i>Estimation on linear Mode for Hypercube</i> |
|--------------|--|

---

## Description

This function calculates the hypercube estimates. Users should use [hypercube](#) which is a better user interface.

## Usage

```
hypercubeEst(X, y, V, ...)
```

## Arguments

|     |  |
|-----|--|
| X   | design matrix, or data-incidence matrix (as described Beran (2014))                        |
| y   | response, or observation (as described Beran (2014))                                       |
| V   | symmetric matrix whose eigenvalues all lie in [0,1] (as in equation (1.3) in Beran (2014)) |
| ... | other optional arguments   |

## Value

The function hypercubeEst returns a list containing the following:

**coefficients** Estimated coefficients  $\beta$  under hypercube estimator

**fitted.values** Fitted values ( $\eta$ ) under hypercube estimator

**residuals** residuals,  $y - \eta$

**V** Symmetric matrix with all eigenvalues lie in [0,1]. The matrix V used the hypercube estimator. (as in equation (1.3) in Beran (2014))

## References

Beran, Rudolf. "Hypercube estimators: Penalized least squares, submodel selection, and numerical stability." Computational Statistics & Data Analysis 71 (2014): 654-666.

See Also

[hypercube](#) is the user interfaces of hypercube estimators. The matrix  $V$  can be constructed using the function [projectCreate](#).

Examples

```
## The use of the function \code{hypercubeEst}.
mf <- model.frame(weight ~ mother:infant -1, data = litter)
X <- model.matrix(attr(mf, "terms"), mf)
y <- model.response(mf)
litter.proj <- projectCreate( ~ mother:infant -1, data = litter)
V <- projectWeight(litter.proj, weights = c(1,1,1,0))
hcmud <- hypercubeEst(X, y, V)
hcmud$coefficients
```

---

|             |                           |
|-------------|---------------------------|
| hypercubeOp | <i>Hypercube Operator</i> |
|-------------|---------------------------|

---

Description

Hypercube Operator

Usage

```
hypercubeOp(X, V)
```

Arguments

- X design matrix
- V symmetric matrix whose eigenvalues all lie in  $[0,1]$

References

Beran, Rudolf. "Hypercube estimators: Penalized least squares, submodel selection, and numerical stability." Computational Statistics & Data Analysis 71 (2014): 654-666.

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|                       |                               |
|-----------------------|-------------------------------|
| hypercubeOptimization | <i>Hypercube Optimization</i> |
|-----------------------|-------------------------------|

---

Description

Find the projection coefficients which minimizing the esitmated risk

Usage

```
hypercubeOptimization(formula, data, sigma = NULL)
```



**Arguments**

|         |                    |
|---------|--------------------|
| formula | formula            |
| data    | data               |
| sigma   | estimated variance |

**Value**

A list containing the following:

**est** a object of the classs "hypercube".

**projcoef** optimal coefficients for the projections.

**estrisk** the minimum estimated risk.

**References**

Beran, Rudolf. "Hypercube estimators: Penalized least squares, submodel selection, and numerical stability." Computational Statistics & Data Analysis 71 (2014): 654-666.

**See Also**

[hypercube](#)

**Examples**

```
hcmoopt <- hypercubeOptimization( weight ~ mother:infant -1, data = litter)
hcmoopt$projcoef #projction coefficients
hcmoopt$estrisk #estimated risk
```

---

litter

*Weight gain of 61 infant rat litters*


---

**Description**

A dataset containing the (average) wight gain of an infant rat litter when the infants in the litter are nursed by a rat foster-mother

**Usage**

```
litter
```

**Format**

A data frame with 61 rows and 3 variables:

**weight** the (average) weight gain of an infant rat litter

**mother** the genotype of the foster-mother nursing the infants

**infant** the genotype of the infant litter

**Details**

The rat litter data treated by Scheffe (1959) form an unbalanced two-way layout. Each response recorded is the average weight-gain of a rat litter when the infants in the litter are nursed by a rat foster-mother. Factor1 with four levels, is the genotype of the foster-mother. Factor2 with the same levels, is the genotype of the infant litter.

The response measured in the experiment is the (average) weight gain of an infant rat litter when the infants in the litter are nursed by a rat foster-mother. Factor 1 is the genotype of the foster-mother nursing the infants. Factor 2 is the genotype of the infant litter.

**Source**

D.W. Bailey, The Inheritance of Maternal Influences on the Growth of the Rat (1953).

---

|        |   |
|--------|---|
| monkey | <i>Response of 5 different monkey-pairs</i> |
|--------|---|

---

**Description**

A dataset containing reports responses to a certain stimulus that were measured for 5 different monkey-pairs (the subjects) in 5 different periods under 5 different conditions

**Usage**

monkey

**Format**

A data frame with 25 rows and 4 variables:

**cond** the condition

**monkeys** the monkey pair

**period** the monkey pair

**response** responses to a certain stimulus

**Source**

Data from Query no. 113, edited by G.W. Sender, Biometrics, Vol. 11, 1955, p.112

---

|       |                              |
|-------|------------------------------|
| motor | <i>Accelations over time</i> |
|-------|------------------------------|

---

### Description

A dataset containing 133 observation of motorsycle acceleration against time in a simulated motorcycle accident. The  $p = 277$  possible observation times constitute the vector  $t = (1, 2, \dots, 277)$ . Accelerations were observed at only  $q < p$  of these equally spaced time, sometimes with replication.

### Usage

```
motor
```

### Format

A data frame with 133 rows and 2 variables:

**t** The time in milliseconds since impact  
**accel** The recorded head acceleration (in g)

### Source

Silverman, B.W. (1985) Some aspects of the spline smoothing approach to non-parametric curve fitting. *Journal of the Royal Statistical Society, B*, 47, 1-52.

---

|        |                                    |
|--------|------------------------------------|
| plsW2V | <i>Covert W matrix to V matrix</i> |
|--------|------------------------------------|

---

### Description

Convert  $W$  to  $V$ , as described in (1.6) in Beran (2014)

### Usage

```
plsW2V(W)
```

### Arguments

$W$  a matrix, penalized least square

### Value

The function `plsW2V` returns a matrix  $V$  for the Hypercube Estimator.

### Examples

```
# D_5 as in equation (3.10) in Beran (2014)
p <- 45
D <- diffMatrix(p, 5)
# The matrix W in equation (3.11) in Beran (2014)
W <- t(D) %*% D
# Convert W to V, as described in (1.6) in Beran (2014)
V <- plsW2V(W)
```

---

|                   |  |
|-------------------|--|
| predict.hypercube | <i>Predict method for Hypercube Estimator Fits</i> |
|-------------------|--|

---

**Description**

Predict method for Hypercube Estimator Fits

**Usage**

```
## S3 method for class hypercube  
predict(object, newdata = NULL, ...)
```

**Arguments**

|         |                                    |
|---------|------------------------------------|
| object  | an object of the class "hypercube" |
| newdata | new data                           |
| ...     | other arguments                    |

---

|                 |                                    |
|-----------------|------------------------------------|
| print.hypercube | <i>Print methods for hypercube</i> |
|-----------------|------------------------------------|

---

**Description**

Print methods for hypercube

**Usage**

```
## S3 method for class hypercube  
print(x, ...)
```

**Arguments**

|     |                                |
|-----|--------------------------------|
| x   | an object of class "hypercube" |
| ... | other arguments                |

---

```
print.summary.hypercube
```

*Print methods for summary.hypercube*

---

## Description

Print methods for summary.hypercube

## Usage

```
## S3 method for class summary.hypercube
print(x, ...)
```

## Arguments

|     |  |
|-----|--|
| x   | an object of class "summary.hypercube" |
| ... | other arguments                        |

---

```
projectCreate
```

*Functions for object "projection.hypercube"*

---

## Description

The standard ANOVA projections as described in equation (5.4) in Beran (2014).

## Usage

```
projectCreate(formula, data)

projectSub(proj, component)

projectWeight(proj, component = NULL, weights = NULL)

projectFun(proj, component = NULL)
```

## Arguments

|           |   |
|-----------|---|
| formula   | input formula without response variable. For example, "~ mother:infant -1".   |
| data      | input data  |
| proj      | an object of class "projection.hypercube".  |
| component | a vector or a matrix to specify with components in the proj are used. See examples for how to use.                                |
| weights   | The weights for the weighted sum of projection matrix. The order of the weights should be the same as the order of the component. |

## Details

The standard ANOVA projections as described in equation (5.4) in Beran (2014). The set of projections are symmetric, idempotent, mutually orthogonal matrix. The linear combinations of the projection matrices are used as the matrix  $V$  (equation (1.3) in Beran (2014)) of the hypercube estimators. Please provide the formula in the form, for example in the data "litter", "~ mother:infant -1". No response and No intercept. Only the interaction of factors.

## Value

The function `projectCreate` creates a object of the "projection.hypercube", which is a list containing all the projection matrices. Also, the object "projection.hypercube" contains the following attributes:

**variables** The names of the variables in the formula

**nlevels** The numbers of levels of the factor in each variable

**dims** The dimension of the projection matrices

**component** The names of the projection matrices stored in the objects

The function `projectSub` returns a object of "projection.hypercube", which contains only the projection matrices according to the argument component.

The function `projectWeight` returns a projection matrix which is the weighed sum of the projection matrices according to component and weights.

The function `projectFun` returns a function which computes and returns a weighted sum of projection matrices according to component in the argument of `projectFun`. The argument of the returned function is the weight. See example for how to use.

## Functions

- `projectSub`: Subset of object "projection.hypercube"
- `projectWeight`: Weighted sum of matrix in object "projection.hypercube"
- `projectFun`: Functions of object "projection.hypercube"

## References

Beran, Rudolf. "Hypercube estimators: Penalized least squares, submodel selection, and numerical stability." Computational Statistics & Data Analysis 71 (2014): 654-666.

## Examples

```
proj <- projectCreate( ~ mother:infant -1, data = litter)

## proj contains the projection matrices :
## proj[["mother0:infant0"]], proj[["mother1:infant0"]], ...
## To see all the names of the projection matrices:
attr(proj, "component")

## If only the additive effects are needed,
## i.e. "mother0:infant0", "mother1:infant0" and "mother0:infant1",
component <- cbind(c(0,0), c(1,0), c(0,1))
proj.sub <- projectSub(proj, component)
attr(proj.sub, "component")
```

```
## If we want
## P = 1 * proj[["mother0:infant0"]] + 0.5 * proj[["mother1:infant0"]]
component <- cbind(c(0,0), c(1,0), c(0,1))
weights <- c(1, 0.5, 0)
proj.weights <- projectWeight(proj, component, weights)

## Create a function for more weighted projection matrices.
component <- cbind(c(0,0), c(1,0), c(0,1))
proj.fun <- projectFun(proj, component)

## Same as proj.weights in above example
weights <- c(1, 0.5, 0)
proj.fun(weights)

## Use the projection matrices for hypercube estimator
V <- proj.fun(weights)
hcmud <- hypercube(weight ~ mother:infant -1, data = litter, V = V)
summary(hcmud)
```

summary.hypercube

*Summary method for Hypercube Estimator Fits***Description**

Summary method for Hypercube Estimator Fits

**Usage**

```
## S3 method for class hypercube
summary(object, ...)
```

**Arguments**

|        |                                |
|--------|--------------------------------|
| object | an object of class "hypercube" |
| ...    | other arguments                |

vineyard

*Vineyard***Description**

A dataset containing records the grape yield harvested in each row of a vinyard in three succeed years

**Usage**

```
vineyard
```

**Format**

A data frame with 52 rows and 4 variables:

**row** the vineyard row number

**year1** reporting the harvest yield in first year

**year2** reporting the harvest yield in second year

**year3** reporting the harvest yield in third year

**Source**

Simonoff, Jeffrey S. Smoothing methods in statistics. Springer Science & Business Media, 2012.



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