

Aquarium

?? correct • solved at: ??:?? by
??

University of ??

Author: **Freek Henstra**

Overview

- We need to line some piranhas up for a group photo.
- Putting a finger in the tank causes adjacent piranhas to start swimming toward the finger.
- Find the number of seconds of finger exposure needed to put every fish in its specified place.

Aquarium - Solution

Techniques

- Intervals
- Greedy algorithms
- Amortisation

Algorithm

- Each fish needs to move by X_i places.
 - The number of finger placements to the right must be X_i more than the number to the left.
- Assume the number of placements to the left of the leftmost fish is $-X_0$.
 - Then the next number must be **0**, the next after that must be **$0+X_1$** , then **$0+X_1+X_2$** , etcetera.
 - We need all values to be non-negative. Take the minimum of value and subtract it from everything.
- Now we need to check if this number of placements is feasible
 - The answer is guaranteed to be at most $O(N \cdot K^2)$.
 - So we can just go from left to right making all valid moves.

Problem

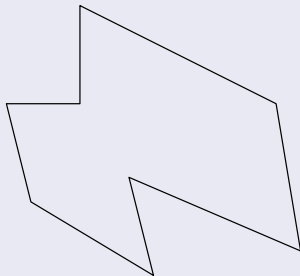
Given polygon-shaped map of a room, find region from which all parts of the room can be seen.

B — Big Brother

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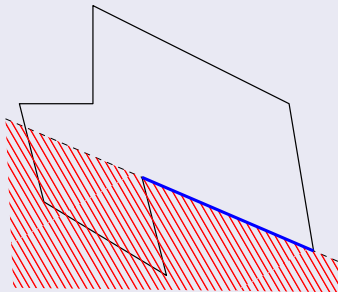
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Solution

Line segments of the polygon induce *half-planes*:
In order for points along that wall not to be obscured, we cannot be behind that wall.



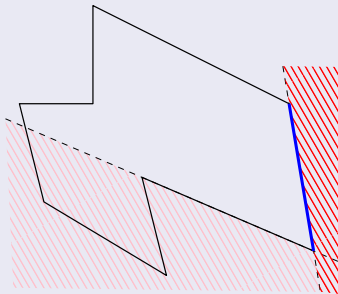
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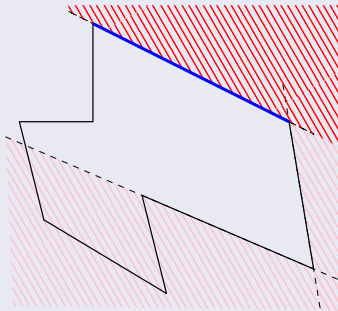
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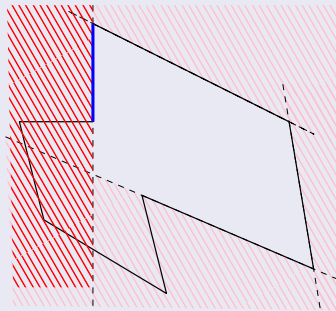
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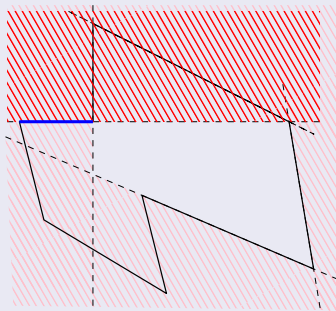
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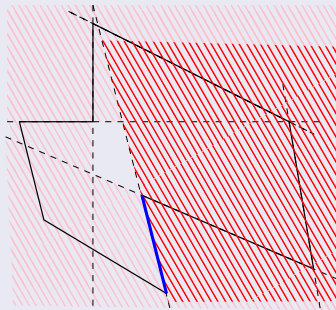
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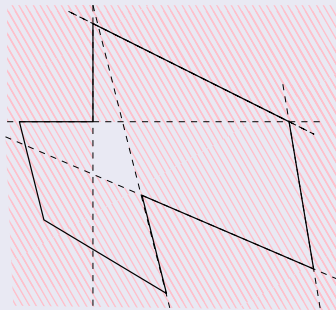
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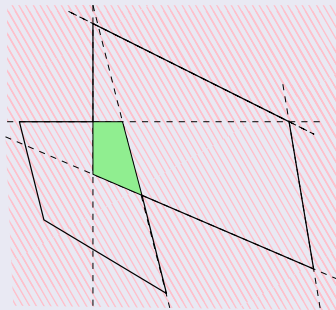
Seeing all parts of the room



Not “behind” any wall



Inside the intersection of the n half-planes.



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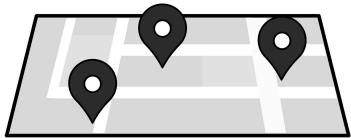
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Statistics at 4-hour mark: 36 submissions, 11 accepted, first after 00:28



Kleptocrat

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Author: **Jorke de Vlas**

Overview

- Given a connected undirected graph, find a path from A to N that minimizes XOR of the values on the edges.

Kleptocrat - Solution

Techniques

- Linear Algebra
- Cycles

Algorithm

- Observation: walking back and forth does not change the XOR-value since $x \oplus x = 0$.
- When there is a cycle starting from c with XOR-value v , we may walk from a to c , around the cycle, back to a and then to b giving a value of $w \oplus v$ where w was the value of a path from a to b .
- This is an equation over \mathbb{F}_2 and the v_i can be reduced with Gaussian Elimination giving 64 values.

Kleptocrat - Solution (cont.)

Techniques

- Linear Algebra
- Cycles

Algorithm

- See v_i as vectors in F_2^{64} by writing v_i in base 2.
- The linear combinations form a subspace of dimension at most 64: find a basis, which has at most 64 elements.
- Now, given an initial path w , for i from 63 to 0, look if w has a 1 in the i th binary digit and check if there is a basis element with i as most significant digit, in which XOR w with this value.

D — Dams in Distress

Problem

We get a rooted tree forming a system of $n \leq 200\,000$ dams. Overflowing a dam causes it to break and release all its water downstream. What is minimum amount of water we need to add at one dam in order for w units of water to reach the root?

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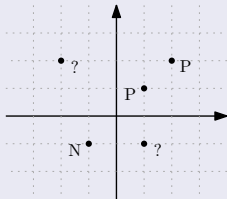
Statistics at 4-hour mark: 270 submissions, 90 accepted, first after 00:32

E — Exhaustive Experiment

Problem

We have n points which are potentially faulty. We can test points but tests only tell us if there is a faulty point within a cone above the test point. Given test results what is minimum number of faulty points?

Solution (1/2)

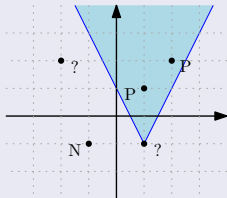


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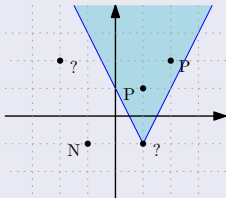
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- 1 First let us simplify the geometry: scale x -coordinate by 2 and rotate 45 degrees



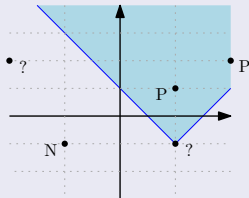
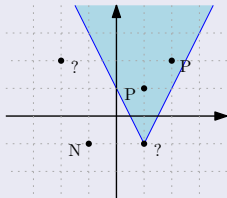
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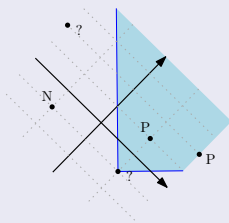
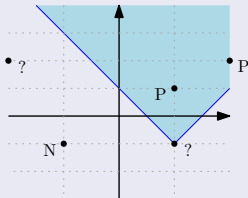
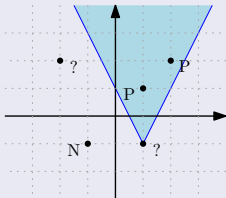
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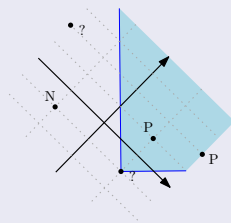
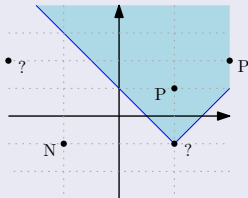
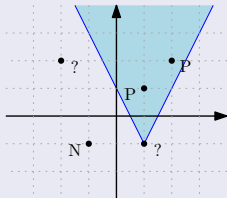
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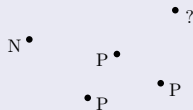
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- 2 Now cone of points affected becomes a quadrant!

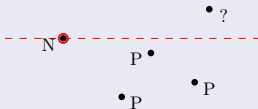
Solution (2/2)



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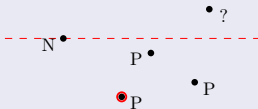
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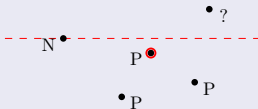
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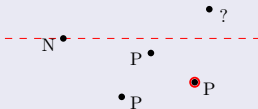
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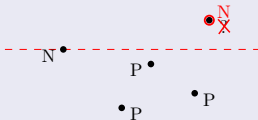
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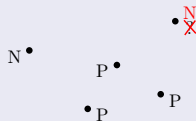
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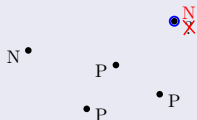
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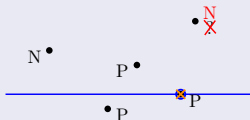
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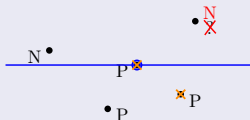
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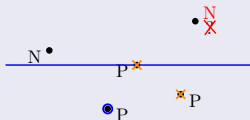
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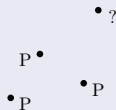
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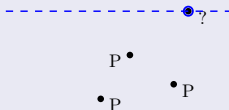
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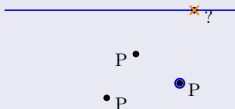
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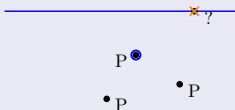
E — Exhaustive Experiment

Solution (2/2)



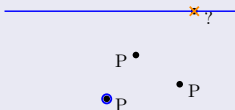
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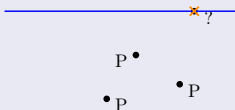
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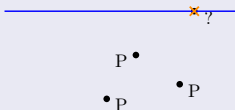
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Statistics at 4-hour mark: 18 submissions, 3 accepted, first after 01:14

Problem

We have one movie and n critics with opinions x_1, \dots, x_n on how good it is.

If current review average of the movie exceeds a reviewers opinion they will score it 0, otherwise they will score it m .

Order the critics so that the film ends up getting review average exactly k/n .

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- 3 So k must be divisible by m (otherwise impossible), and we need exactly $p = k/m$ positive reviews.

Solution

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Statistics at 4-hour mark: 62 submissions, 21 accepted, first after 00:43

Problem

Given sequence of $n \leq 10^6$ digits 1/2/3, count how many subsequences have the form “12+3”
(“2+” means 1 or more twos)

G — Gig Combinatorics

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Statistics at 4-hour mark: 437 submissions, 78 accepted, first after 00:04

H — Hiring and Firing

Problem

A company hires and fires workers over up to 100 000 days. Assign an HR employee to each day so that for each worker a different HR employee is assigned the day they are hired and the day they are fired. Minimize number of HR employees used.

Solution (1/3)

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H — Hiring and Firing

Solution (2/3)

- 1 Mark the days on a timeline and draw an arc for each worker:



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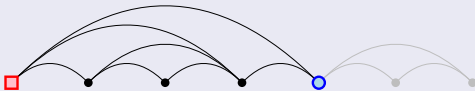


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So if we have three colors, will always be a choice available for the middle vertex.

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In other words, 3 colors is always enough!

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Statistics at 4-hour mark: 22 submissions, 0 accepted, first after N/A

I — Infection Estimation

Problem

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Solution

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$100, 100 \cdot 1.01, 100 \cdot 1.01^2, \dots, 100 \cdot 1.01^i, \dots, 5 \cdot 10^6$
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$$\Pr[\text{infected} = t \mid \text{yes}] = \frac{\Pr[\text{yes} \mid \text{infected} = t] \cdot \Pr[\text{infected} = t]}{\Pr[\text{yes}]}$$

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Statistics at 4-hour mark: 46 submissions, 6 accepted, first after 01:03



Lost Map

?? correct • solved at: ??:?? by
??
??

Author: **Robin Lee**

Overview

- Two map fragments (strings) are badly damaged and some items are replaced by "?"s
- Find how many ways you can overlay the two fragments so that no non-"?" values conflict.

Lost Map - Solution

Techniques

- FFT
- Convolution

Algorithm

- We can treat the “?” and non-“?” values completely separately.
 - We make two separate binary strings
 - One encoding “?” as 0 values and everything else as 1 values
 - One encoding “?” as several -1s and everything else as its binary representation (takes $\log K$ bits where K is the number of directions)
 - If we reverse one array, then the **convolution** of both versions of the binary strings from each map can be used to find the number of bits matching each time
 - We need the number of bits across both convolutions to exactly equal the length of the string.
- Pitfalls: FFT needs to be **fast**.

K — Keep Calm and Carry Off

Problem

Given two 1 000 000-digit integers A and B , find the smallest non-negative integer X such that $A + X$ and $B - X$ (or $A - X$ and $B + X$) can be added without carry.

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Solution

Simplifying assumptions:

- 1 A and B have the same number of digits (or zero-pad)
- 2 it is always the first integer we add to (try both options; take the best one)

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- 1 If digits in i th position have $a_i + b_i \geq 10$ there is a carry in i th position.
- 2 We must increment a_i and decrement $b_i \pmod{10}$ until there is no longer carry.

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- 2 We must increment a_i and decrement $b_i \pmod{10}$ until there is no longer carry.
- 3 This happens when a_i turns to 0 (i.e. we add $9 - a_i$).

K — Keep Calm and Carry Off

Problem

Given two 1 000 000-digit integers A and B , find the smallest non-negative integer X such that $A + X$ and $B - X$ (or $A - X$ and $B + X$) can be added without carry.

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- 5 Lets us compute $A + X$ easily, subtract A to get X .

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Example:

$$A = 811765432113$$

$$B = 111234567897$$

$$\text{Target } A + X = 812000000000$$

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Statistics at 4-hour mark: 115 submissions, 11 accepted, first after 00:44

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Solution (1/2)

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for every cell (i, j) there is a neighboring cell (i', j') belonging to a different region.

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- 2 If we manage to find this, problem becomes easy:
 - Use the partition as a starting point.
 - For every cell (i, j) where two or more regions should overlap, extend the region from (i', j') into (i, j) .

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Find three connected regions in a grid. For each cell prescribed whether it should contain a single region or at least two different regions.

Solution (2/2)

- 1 How to find the starting point partition?

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Find three connected regions in a grid. For each cell prescribed whether it should contain a single region or at least two different regions.

Solution (2/2)

① How to find the starting point partition?

② If dimensions not too small, one possible pattern —————>

```
ACCCCCCC
ACBBBBBB
ACBCCCCB
ACBCCBCB
ACBBBBBC
ACCCCCCB
```


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Solution (2/2)

- ① How to find the starting point partition?
- ② If dimensions not too small, one possible pattern —————→
- ③ Case when dimensions are small is left as exercise...
 - when at least two rows and columns the above works
 - case with only one row or one column easy to solve directly

A C C C C C C C C

A C B B B B B B B

A C B C C C C C B

A C B C C C B C B

A C B B B B B C B

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```
ACCCCCCC
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ACBCCCCB
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ACBBBBBC
ACCCCCCB
```

Statistics at 4-hour mark: 5 submissions, 0 accepted, first after N/A