

BlackHoleImages: A Wolfram Mathematica packet for analytical black hole imaging

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Summary

Black holes are astrophysical objects for which the gravitational field is strong enough that even particles moving at the speed of light cannot escape their influence. For their proper visualization, general relativistic effects on photon trajectories must thus be implemented. These include the changed shape of the trajectories, but also the changes in frequency and intensity, which is especially of interest when we study accretion disks forming in the black hole's proximity.

Statement of need

BlackHoleImages is a Wolfram Mathematica packet for generating images of accretion disks or stellar background in the Kerr geometry, which is usable for rotating, uncharged black holes. It contains ready-to-use functions in the KerrImages package, which allow imaging of equatorial disks described by the simple “alpha disk” model proposed by Shakura and Sunyaev ([Shakura & Sunyaev, 1973](#)), and also the stellar background distorted by the Kerr geometry.

The disk model is implemented in the AlphaDiskModel package, which can be redesigned as needed in future implementations. The analytical implementation of null geodesics in the Kerr spacetime is contained within the KerrNullGeodesics package. The solutions themselves were mostly taken from Gralla and Lupsasca ([Gralla & Lupsasca, 2020](#)) with some minor changes made to suit the initial conditions at infinity.

We expect this packet to be used primarily for studying the observational characteristics of accretion disks of black holes, including dynamical processes in the disk, since the time delay of each geodesic is also computable in this packet. The packet can also be used for educational purposes, such as plotting null geodesics of the Kerr metric or illustrating the lensing effects, or for any other purpose where the computation of photon trajectories is necessary.

The packet may be complemented with the KerrGeodesics Mathematica package ([Black Hole Perturbation Toolkit, n.d.](#)) which can be used to compute timelike geodesics. Among published codes that deal in more detail with the physics of accretion disks, we might mention TLUSTY, a Fortran77 code that can be used to model stellar atmospheres and accretion disks ([Hubeny & Lanz, 2017](#)).

Black Hole Perturbation Toolkit. (n.d.). (bhptoolkit.org).

Gralla, S. E., & Lupsasca, A. (2020). Null geodesics of the kerr exterior. *Physical Review D*, 101(4).

Hubeny, I., & Lanz, T. (2017). *A brief introductory guide to TLUSTY and SYNSPEC.* <https://arxiv.org/abs/1706.01859>

- ³⁸ Shakura, N. I., & Sunyaev, R. A. (1973). Black holes in binary systems. Observational
³⁹ appearance. *24*, 337–355.

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