

## A18

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For three correlation coefficients  $r_1$ ,  $r_2$ , and  $r_3$ , which were calculated from equal size samples, determine the average correlation coefficient

- in rough approximation with a simple arithmetic mean of the  $r_i$
- more accurate by means of the arithmetic mean of the z-transformed values, and subsequent inverse transformation.

For this task first use the numerical values (0.3, 0.8, 0.91) and then the values (0.91, 0.95, 0.99) for the correlation coefficients ( $r_1$ ;  $r_2$ ;  $r_3$ ).

Variant:

same specification, but now the three correlation coefficients come from different size samples with sample sizes  $n_1=8$ ,  $n_2=12$  und  $n_3=15$ . Note: weights are degrees of freedom  $df_i=n_i-2$ !

$$1.1 \quad \frac{0.3 + 0.8 + 0.91}{3} = 0.67$$

$$1.2 \quad \frac{0.91 + 0.95 + 0.99}{3} = 0.95$$

z TRANSFORM

$$z = \frac{1}{2} \cdot \ln \left( \frac{1+r}{1-r} \right)$$

$$r = \frac{e^{2z} - 1}{e^{2z} + 1}$$

weighted:  $\frac{\sum w_i \cdot z(r_i)}{\sum w_i}$

	1.1	1.2	1.3
	r	z	weighted
	0.3	0.30952	6
	0.8	1.09861	10
	0.91	1.52752	13
mean	0.67	0.97855	1.12762
endresult	0.67	0.75244	0.8102
	2.1	2.2	2.3
	r	z	
	0.91	1.52752	6
	0.95	1.83178	10
	0.99	2.64665	13
mean	0.95	2.00199	2.13412
endresult	0.95	0.96417	0.97237