

A19

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For a sample with $n = 25$ elements a correlation coefficient r_{xy} according to Bravais-Pearson was calculated with a value of $r = 0,86$. Find a 95%- and a 99%-confidence interval for the unknown value of the population parameter ρ according to formula $z_{1,2} = \hat{z} \pm z_{Tab} \cdot \frac{1}{\sqrt{n-3}}$, with subsequent back transformation of both z-values (where \hat{z} is Fishers z-transform of the correlation coefficient and z_{Tab} is the 2-tailed quantile from a table of the normal distribution).

$$\hat{z} = \frac{1}{2} \cdot \ln\left(\frac{1+r}{1-r}\right) = 1.2933$$

$$z_{TAB}(0.95) = 1.960$$

$$z_{TAB}(0.99) = 2.576$$

$$CI_{0.95} = 1.2933 \pm 1.96 \cdot \frac{1}{\sqrt{22}}$$

$$CI_{0.99} = 1.2933 \pm 2.576 \cdot \frac{1}{\sqrt{22}}$$

| | r | Ztab | Zfrom | Zto | from | to |
|-------|--------|-------|---------|---------|---------|---------|
| CI 95 | 1.2933 | 1.96 | 0.87543 | 1.71117 | 0.70412 | 0.93679 |
| CI 99 | 1.2933 | 2.576 | 0.74409 | 1.84251 | 0.63161 | 0.95104 |