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Calculate all partial correlation coefficients for the following correlation matrix R:

$$R=\begin{pmatrix} 1 & 0{,}2495 & 0{,}3332 \\ 0{,}2495 & 1 & 0{,}5029 \\ 0{,}3332 & 0{,}5029 & 1 \end{pmatrix}$$

The above simple correlation coefficients r_{ij} come from a study of n = 142 women, in which X_1 stands for blood pressure, X_2 cholesterol concentration, and X_3 age. So $r_{13} = 0{,}3332$ is the correlation coefficient between blood pressure and age.
At the error level of $\alpha = 5\%$ test the null hypothesis H0: $\rho_{12.3} = 0$ against the alternative hypothesis H1: $\rho_{12.3} \neq 0$. Can you discard the hypothesis that blood pressure and cholesterol concentration are independent under partialization of age?

Note: the partial correlation coefficient is tested with the t-distribution (same as with r_s or r_{xy}), but with a slightly modified test statistic, namely $t_{calc} = r_{xy.z} \cdot \sqrt{\frac{n-3}{1-r_{xy.z}^2}}$ with df=n-3.

r_{12} r_{13} r_{21} r_{23} r_{31} r_{32}

$r_{12.3}$ $r_{13.2}$ $r_{21.3}$ $r_{23.1}$ $r_{31.2}$ $r_{32.1}$

$$r_{12.3} = r_{21.3} = \frac{r_{12} - r_{13} \cdot r_{23}}{\sqrt{1-r_{13}^2}\sqrt{1-r_{23}^2}} = \frac{0.2495 - 0.3332 \cdot 0.5029}{\sqrt{1-0.3332^2}\sqrt{1-0.5029^2}} = 0.1005$$

$$r_{13.2} = r_{31.2} = 0.2482$$

$$r_{23.1} = r_{32.1} = 0.7597$$

$$t_{calc} = r_{12.3} \cdot \sqrt{\frac{142-3}{1-r_{12.3}^2}} = 0.1005 \cdot \sqrt{\frac{139}{1-0.1005^2}} = 1.1909$$

$$t_{120,0.05} = 1.658 > 1.1909$$

H0 is valid