

上机作业2

对函数

$$f(x) = \frac{1}{1 + 25x^2}, x \in [-1, 1]$$

构造牛顿插值多项式 $p_N(x)$ ，插值节点取为：

$$1. x_i = 1 - \frac{2}{N}i, i = 0, 1, \dots, N$$

$$2. x_i = -\cos\left(\frac{2i+1}{2N+2}\pi\right), i = 0, 1, \dots, N \quad (\text{Chebyshev point})$$

并计算如下误差

$$\max_i \{|f(y_i) - p(y_i)|, y_i = \frac{i}{50} - 1, i = 0, 1, \dots, 100\}$$

对 $N = 5, 10, 20, 40$ 比较以上两组节点的结果，并在一张图中画出 $N = 20$ 时 $f(x)$ 数值计算结果。

输出形式如下：

N=5

Max Error of grid (1) : XXXXXXXXXXXXXXXXXXXX

Max Error of grid (2) : XXXXXXXXXXXXXXXXXXXX

N=10

Max Error of grid (1) : XXXXXXXXXXXXXXXXXXXX

Max Error of grid (2) : XXXXXXXXXXXXXXXXXXXX

N=20

Max Error of grid (1) : XXXXXXXXXXXXXXXXXXXX

Max Error of grid (2) : XXXXXXXXXXXXXXXXXXXX

N=40

Max Error of grid (1) : XXXXXXXXXXXXXXXXXXXX

Max Error of grid (2) : XXXXXXXXXXXXXXXXXXXX