

HW 1 pt2

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1. See DiffCrypto.py

2.

$$\begin{aligned}P_c(1) &= \left(\frac{1}{3} * \frac{1}{2}\right) + \left(\frac{1}{2} * \frac{1}{4}\right) = \frac{7}{24} \\P_c(2) &= \left(\frac{1}{6} * \frac{1}{2}\right) + \left(\frac{1}{2} * \frac{1}{2}\right) + \left(\frac{1}{3} * \frac{1}{4}\right) = \frac{5}{12} \\P_c(3) &= \left(\frac{1}{6} * \frac{1}{4}\right) + \left(\frac{1}{3} * \frac{1}{4}\right) = \frac{1}{8} \\P_c(1) &= \left(\frac{1}{6} * \frac{1}{4}\right) + \left(\frac{1}{2} * \frac{1}{4}\right) = \frac{1}{6}\end{aligned}$$

$$H(K|C) = H(K) + H(P) - H(C)$$

$$H(K) = -\left(\frac{1}{2} \log_2 \frac{1}{2} + \frac{1}{4} \log_2 \frac{1}{4} + \frac{1}{4} \log_2 \frac{1}{4}\right) = 1.5$$

$$H(P) = -\left(\frac{1}{3} \log_2 \frac{1}{3} + \frac{1}{6} \log_2 \frac{1}{6} + \frac{1}{2} \log_2 \frac{1}{2}\right) = 1.46$$

$$H(C) = -\left(\frac{7}{24} \log_2 \frac{7}{24} + \frac{5}{12} \log_2 \frac{5}{12} + \frac{1}{8} \log_2 \frac{1}{8} + \frac{1}{6} \log_2 \frac{1}{6}\right) = 1.85$$

$$H(K|C) = 1.5 + 1.46 - 1.85 = 1.11$$