

INF102 Inlevering 1 hausten 2013

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Oppgave 1

a)

What is the running time for these code fragments? Answer with a Θ -relation.

Given $n \leq p \leq m$ there are three separate loops that must be taken into account giving us the relation $\Theta(n * p * m)$.

b)

Given $p \leq q = n$ and both p and q are affected by the if/else statement depending on the value of m – this is a binary search. So $\Theta(\log n)$.

c)

Given $n * \sum_{k=0}^{\log(n)} \frac{1}{2^k}$ this geometric set converges on 2 giving us $\Theta(n)$.

Oppgave 2

a)

$$20n^4 + 123n^2 + 1000\log(n) \\ \sim (20n^4)$$

b)

$$120n^3 + 5n^2\log(n) \\ \sim (120n^3)$$

c)

$$100n^4 + 2^n \\ \sim (2^n)$$

d)

$$n + n^l\log(n) + \log(n) \\ \sim (n)$$

e)

$$2^{10} + n \\ \sim (n)$$

f)

$$2^{10}n \\ \sim (2^{10}n)$$

Oppgave 3

a)

To implement `sorterFrekvence(Comparable[] a)`, I started by creating a class called `Tuples` to create a key, value pair to maintain the values in the `Comparable` array.

```
//Tuples.java
import org.omg.CORBA.OMGVMCID;

public class Tuple implements Comparable {

    private int key;

    private Comparable value;

    public Tuple(int key, Comparable value) {
        this.key = key;
        this.value = value;
    }

    public int getKey() {
        return key;
    }

    public Comparable getValue() {
        return value;
    }

    @Override
    public int compareTo(Object o) {
        Tuple tuple = (Tuple) o;
        if (key > tuple.getKey() {
            return 1;
        } else if (key < tuple.getKey() {
            return -1;
        } else {
            return 0;
        }
    }

    public String toString() {

        return "Key, Value: " + key + "\t" + value;
    }
}
```

```

}
\\

//Oppgave3a.java
import java.util.ArrayList;

public class Oppgave3a {

    @SuppressWarnings("unchecked")
    static Comparable[] sorterFrekvens(Comparable[] input) {
        Merge.sort(input);
        int counter = 0;

        ArrayList<Tuple> myData = new ArrayList<Tuple>();

        while (counter < input.length) {

            int howmany = 0;
            while ((counter + howmany + 1 < input.length)
                && (input[counter + howmany].compareTo(input[counter
                + howmany + 1])) &= 0) {
                howmany++;
            }

            myData.add(new Tuple(howmany + 1, input[counter + howmany]));
            counter += howmany + 1;
        }

        Tuple[] returnable = new Tuple[myData.size()]<+>;

        for (int i = 0; i < myData.size(); i++) {
            returnable[i] = myData.get(i);
        }

        for (int i = 0; i < returnable.length; i++) {
            System.out.printf("Value, Key: %d\t %d\n",
                returnable[i].getValue(), returnable[i].getKey());
        }
        int countThis = 0;
        for (int i = input.length - 1, j = 0; (i >= 0) &&
            j < returnable.length; j++) {
            while (++countThis < returnable[j].getKey() {
                input[i--] = returnable[j].getValue();
            }
            countThis = 0;
        }
        return input;
    }

    public static void main(String[] args) {
        Integer[] stuff = {3,4,1,8,5,3,5,5};

        Comparable[] somethingsomethingdarkside =
            sorterFrekvens(stuff);
    }
}

```

```

        for (int i = 0; i < somethingsomethingdarkside.length; i++)
        {
            System.out.printf('%s \n',
                               somethingsomethingdarkside[i].toString());
        }
    }
}

```

b)

The Θ relation for my `sorterFrekvens(Comparable[] a)` method is $\Theta(n^2)$ because of the for loop that goes through the input array twice.

c)

i) copy elements in b to a and after merge sort a

This uses a for loop to transfer all the elements from b to a and then to merge sort which takes $N \log(N)$. So $N^2 \log(N)$ gets the $\sim (N^2)$. ii) sort each row in b, and after merge together the rows over in a

This uses a merge sort for each row, so we have $\frac{N \log(N)}{N} * N \log(N)$. Then we get the $\sim (N \log N)$ both rows and columns in b er $n = 2^k$, when k is a whole number. Proposition F says that top-down mergesort uses between $1/2 N \log(N)$ and $N \log(N)$ compares to sort any array of length N.

d)

e)

The frequency sorting algorithm that we created in the section a can be used to write this implementation. All that we have to do is not take in the set of numbers, but instead take in a set of strings and compare the frequency of the given strings. This is fine because we have used Comparable.

Oppgave 4

a)

selection sort, shell sort, merge sort java files attached.

b)

shell sort and merge sort further

c)

give an estimation of how large a table each of these algorithms can sort in a minute given the machine that you are using.