

2022 CHAPTER COMPETITION SPRINT ROUND PROBLEMS 1–30

Name			
maille:			

DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO SO.

This section of the competition consists of 30 problems. You will have 40 minutes to complete all the problems. You are not allowed to use calculators, books or other aids during this round. Calculations may be done on scratch paper. All answers must be complete, legible and simplified to lowest terms. Record only final answers in the blanks in the lefthand column of the competition booklet. If you complete the problems before time is called, use the remaining time to check your answers.

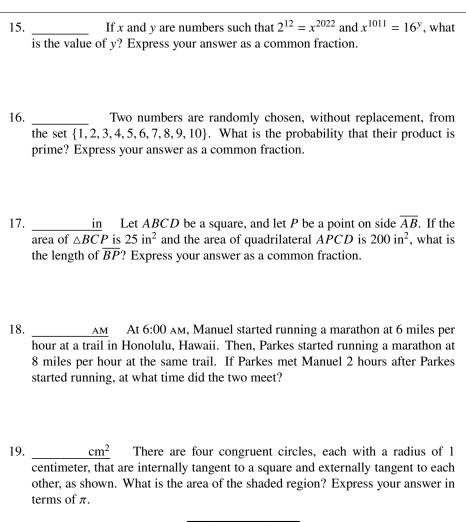
In each written round of the competition, the required unit for the answer is included in the answer blank. The plural form of the unit is always used, even if the answer appears to require the singular form of the unit. The unit provided in the answer blank is the only form of the answer that will be accepted.

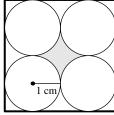
The problems and solutions for this competition were prepared by the DMC Editorial Board under the direction of:

DankBasher619, dc495, DeToasty3, firebolt360, HrishiP, john0512, nikenissan, pandabearcat, PhunsukhWangdu, pog, RedFlame2112, stayhomedomath, treemath, vsamc, & yusufsheikh2207.

1.	Solution Dwayne spent \$22.00 at the movies on soda and popcorn. If soda costs three times as much as popcorn, how much did Dwayne spend on popcorn?
2.	What is the value of 2022 · 100 + 2022?
3.	Katherine multiplies the number \diamond by 7 and then subtracts 2 from the result, while Taiki subtracts 2 from \diamond and then multiplies the resulting number by 7. What is the positive difference between Katherine and Taiki's final numbers?
4.	Vikram wrote an expression on the board, but he accidentally smudged one of the digits with his hand.
	19■ · 9
	What is the result when the minimum possible value of Vikram's expression is subtracted from the maximum possible value of Vikram's expression?
5.	There are two numbers with a square of 15. What is their product?
6.	The first five terms of an arithmetic sequence are 3, a , b , c , and 17. What is the value of $a + b + c$?
7.	units Two of the sides of an isosceles triangle have lengths 10 units and 12 units. What is the sum of the possible perimeters of the triangle?

8.	In the equations below, what is the value of <i>e</i> ?
	a+b+c+d+e=11
	a+b+c+d+f=12
	a + b + c + d + e + f = 15
9.	$\frac{\text{in}^2}{\text{with an area of 2 in}^2}$ Alice and Barbara both draw a circle. If Alice draws a circle with an area of 2 in ² , and Barbara draws twice as much as Alice, what is the area of Barbara's circle?
10.	If $\sqrt{x} + \sqrt{y} = 7$ and $\sqrt{x} - \sqrt{y} = 4$, what is the value of $x - y$?
11.	\$\frac{\\$}{\text{value of his nickels}}\$ Evan has twice the amount of nickels as he has quarters. If the value of his nickels and quarters combined is \$7.00, how much money are his nickels worth?
12.	Katie has a bag containing blue, pink, and red marbles. The ratio of blue to pink marbles is $5:7$, and the ratio of pink to red marbles is $18:11$. If the ratio of blue to red marbles is $a:b$, what is the value of $a+b$?
13.	days Every day, if Katherine remembers to water her bamboo plant, it will get 10 inches taller, but if she forgets to water it, it will get 5 inches shorter. Over a seven-day period, Katherine's bamboo plant grew from 25 inches tall to 50 inches tall. On how many days during the seven-day period did Katherine forget to water her bamboo plant?
14.	Hanami has 3 consecutive integers. If the product of two of these integers is 224, what is the product of the possible values of the third number?





$$k(\frac{1}{2} \cdot \frac{1}{3} \cdot \frac{1}{4})^{(5 \cdot 6)} = 1,$$

how many positive divisors does k have?

- 21. Bill rolls a standard six-sided die 4 times. What is the probability that he gets any number twice in a row? Express your answer as a common fraction.
- 22. _____ The grid below has been filled with positive integers in such a way that the sum of the numbers in each row is the same. However, each number in the grid has been expressed in a different base, from base-two to base-ten. What is the result when the number covered by *\psi\$ is expressed in base-ten?

*	27	30
97	86	15
201	63	442

$$\sqrt{4038 \cdot 2021 + 4040 \cdot 2020 + k} = 4046$$
.

what is the value of k?

24. $\underline{\text{values}}$ For how many integer values of n is a triangle with side lengths 7, 9, and n obtuse?

25.	The sequence a_n is defined for all integers n . If
	$(n-1)\cdot a_{n-2} = a_n - 3$
	for all odd $n \ge 1$, what is the value of a_5 ?
26.	$\frac{\text{units}^2}{\text{and } (2,5).}$ The midpoints of the sides of a triangle are $(1,0)$, $(3,0)$, and $(2,5)$. What is the area of this triangle?
27.	If p , q , and r are the roots of the polynomial
	$x^3 + 20x^2 + 21x + 22,$
	what is the value of $(p-1)(q-1)(r-1)$?
28.	If m and n are positive integers such that $\sqrt[m]{5}\sqrt[m]{25} = \sqrt[5]{5}$, what is the sum of the possible values of n ?
29.	$\frac{\text{products}}{\text{finds the product of its elements. How many distinct products can she get from this process?}}$
30.	ordered triples How many ordered triples of positive integers $\overline{(a,b,c)}$ are there such that $a\cdot b\cdot c=13500$?