

## 2022 CHAPTER COMPETITION SPRINT ROUND PROBLEMS 1–30

Name		
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## DO NOT BEGIN UNTIL YOU ARE INSTRUCTED TO SO.

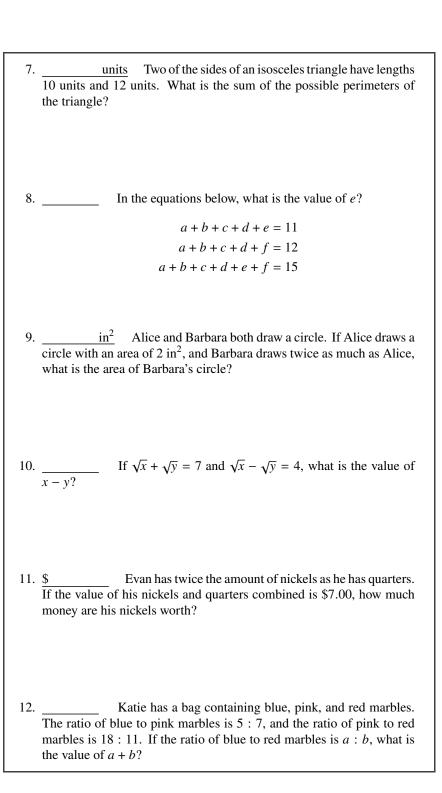
This section of the competition consists of 30 problems. You will have 40 minutes to complete all the problems. You are not allowed to use calculators, books or other aids during this round. Calculations may be done on scratch paper. All answers must be complete, legible and simplified to lowest terms. Record only final answers in the blanks in the lefthand column of the competition booklet. If you complete the problems before time is called, use the remaining time to check your answers.

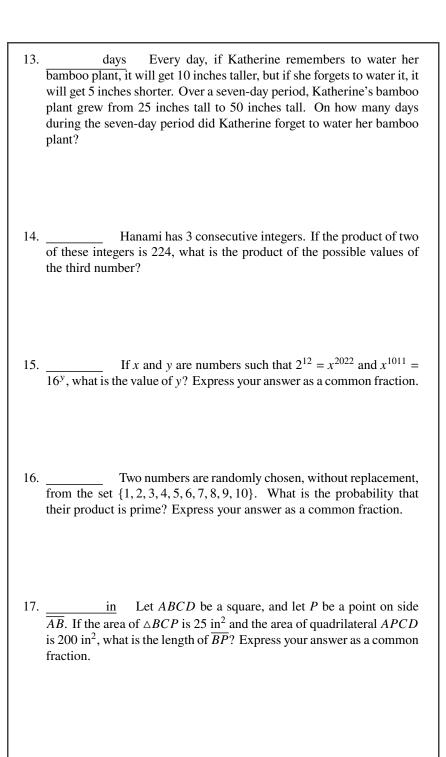
In each written round of the competition, the required unit for the answer is included in the answer blank. The plural form of the unit is always used, even if the answer appears to require the singular form of the unit. The unit provided in the answer blank is the only form of the answer that will be accepted.

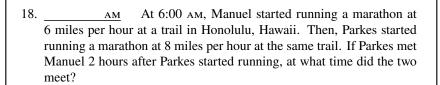
The problems and solutions for this competition were prepared by the DMC Editorial Board under the direction of:

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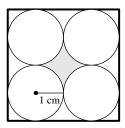
1. \$\frac{\\$}{\corn.}\$ Dwayne spent \$22.00 at the movies on soda and pop- corn. If soda costs three times as much as popcorn, how much did Dwayne spend on popcorn?
2 What is the value of 2022 · 100 + 2022?
3 Katherine multiplies the number ◊ by 7 and then subtracts 2 from the result, while Taiki subtracts 2 from ◊ and then multiplies the resulting number by 7. What is the positive difference between Katherine and Taiki's final numbers?
4 Vikram wrote an expression on the board, but he accidentally smudged one of the digits with his hand.  19■ · 9  What is the result when the minimum possible value of Vikram's expression is subtracted from the maximum possible value of Vikram's expression?
5 There are two numbers with a square of 15. What is their product?
6. The first five terms of an arithmetic sequence are 3, $a$ , $b$ , $c$ , and 17. What is the value of $a + b + c$ ?







19.  $\frac{\text{cm}^2}{\text{of 1 centimeter}}$  There are four congruent circles, each with a radius of 1 centimeter, that are internally tangent to a square and externally tangent to each other, as shown. What is the area of the shaded region? Express your answer in terms of  $\pi$ .



20. positive divisors If k is a real number such that

$$k(\frac{1}{2} \cdot \frac{1}{3} \cdot \frac{1}{4})^{(5 \cdot 6)} = 1,$$

how many positive divisors does k have?

21. \_\_\_\_\_ Bill rolls a standard six-sided die 4 times. What is the probability that he gets any number twice in a row? Express your answer as a common fraction.

22. The grid below has been filled with positive integers in such a way that the sum of the numbers in each row is the same. However, each number in the grid has been expressed in a different base, from base-two to base-ten. What is the result when the number covered by  $\bigstar$  is expressed in base-ten?

*	27	30
97	86	15
201	63	442

$$\sqrt{4038 \cdot 2021 + 4040 \cdot 2020 + k} = 4046.$$

what is the value of k?

- 24.  $\frac{\text{values}}{\text{side lengths 7, 9, and } n}$  For how many integer values of n is a triangle with
- 25. \_\_\_\_\_ The sequence  $a_n$  is defined for all integers n. If

$$(n-1)\cdot a_{n-2} = a_n - 3$$

for all odd  $n \ge 1$ , what is the value of  $a_5$ ?

26.  $\frac{\text{units}^2}{(3,0), \text{ and } (2,5)}$ . The midpoints of the sides of a triangle are (1,0), what is the area of this triangle?

$$x^3 + 20x^2 + 21x + 22$$
,

what is the value of (p-1)(q-1)(r-1)?

28. If m and n are positive integers such that 
$$\sqrt[m]{5}\sqrt[n]{25} = \sqrt[5]{5}$$
, what is the sum of the possible values of n?

29.  $\frac{\text{products}}{\{1, 2, 3, 4, 5, 6\} \text{ and finds the product of its elements. How many distinct products can she get from this process?}$ 

30. ordered triples How many ordered triples of positive integers (a, b, c) are there such that  $a \cdot b \cdot c = 13500$ ?