Improved Models

November 5, 2020

1 Improved Model

1.1 Data Preparation

1.1.1 Import Modified Feature Matrix

A modification has been made to the feature matrix extracted in "Data Preparation" module. The changes include:

- (1) Corrected a mistake in function that calculates the ignition temperature.
- (2) Baseline correction now only incorporate flattening and smoothing the curve, the minor peaks are no longer removed. This change is trying to keep the baseline correction result as close as the commercialized software.

The feature new matrix is stored in a .csv file, which contains features extracted from raw data based on physical meanings, as well as the labels indicating whether the material passes FR tests or not. A total of 41 observations and 5 features were included. Specifically, the output consists of 3 labels, where 0=fail, 1=pass, 2=hard to determine.

We start by importing the .csv file. Appropriate libraries are imported.

```
[1]: # Read in the data
import numpy as np
import pandas as pd
import pylab as plt
data = pd.read_csv("feature_matrix.csv")
data.head()
[1]: Total Heat Release Rurning Temperature Ignition Temperature
```

[1]:		Tota	l Heat F	Release	Burning	Temperature	Ignition	Temperatur	re \
	0			.818517	Ü	482.246	Ü	350.80	
	1		14879.	.480392		537.858		438.64	13
	2		16584.	. 116501		515.457		366.53	37
	3		20246	.452607		482.774		396.99	96
	4		26622.	. 142067		472.215		388.92	29
		Heat	Release	e Capaci [.]	ty Fire	Growth Capac	ity FR_la	ibels	
	0		259	955.1043	46	134.021	.649	2	
	1		155	591.9434	56	120.959	219	2	
	2		173	369.3657	38	77.548	988	1	
	3		213	344.2506	14	191.805	110	0	

1.1.2 Scale Data

Based on simple observation on the raw features, it is not suprised to see there are magnitude difference among all features. To eliminate the weight bias caused by descrepancy with units, standard scaling is applied and all analysis will be performed on top of the scaled dataset.

[2]:	Total Heat Release B	urning Temperature Ign	ition Temperature \
0	1.808411	-0.424203	-0.990329
1	-0.335103	0.879587	0.744864
2	0.036103	0.354409	-0.679551
3	0.833624	-0.411824	-0.077850
4	2.222013	-0.659374	-0.237209
	Heat Release Capacity	Fire Growth Capacity	FR_labels
0	1.778631	-0.202424	2
1	-0.365567	-0.258909	2
2	0.002192	-0.446622	1
3	0.824619	0.047441	0
4	2.209336	0.342840	0

###Baseline Model Pipeline Diagram

1.2 SVC Baseline Model

According to the pipeline diagram in our description file, a 90% train-test split will be performed to the scaled dataset. Support Vector Classifier (SVC) is selected as our baseline model. Grid-SearchCV is used for determining the optimal hyperparameters (C and γ) with a 3-fold cross-validation. At the end, the accuracy, precision and recall scores are printed as benchmark metrics with other potential models.

Our Support Vector Classifier (SVC) baseline model will not consider previously discussed issues of multicollinearity and outliers with the data but will establish the baseline performance for a classification model. Because dropping the outlier at index=2 made a significant difference, we will be dropping that data point for the baseline but further exploring its significance in the future.

```
[3]: # imports
     from sklearn.model_selection import train_test_split
     from sklearn.metrics import accuracy_score, recall_score, precision_score
     from sklearn.model_selection import GridSearchCV
     from sklearn.svm import SVC
     # final outlier
     origin_feature=scaled
     # perform a train-test split. 90% of original data will be used for training
     X svc = origin feature.drop(columns='FR labels').values
     y_svc = origin_feature['FR_labels'].values
     X_train_svc, X_test_svc, y_train_svc, y_test_svc = train_test_split(X_svc,__
     \rightarrowy_svc, test_size = 0.10)
     # define support vector model with rbf kernel
     svc = SVC(kernel = 'rbf')
     # build up parameter grid and perform GridSearchCV to find the best estimator
     alphas = np.array([1e-6, 1e-5, 1e-4, 1e-3, 1e-2, 1e-1, 1])
     Cs = 1 / alphas
     sigmas = np.array([1e-3, 1e-2, 1e-1, 1, 10, 100])
     gammas = 1. / 2 / sigmas**2
     param_grid_svc = {'C': Cs,'gamma': gammas}
     svc_search = GridSearchCV(svc, param_grid_svc, cv = 3)
     svc_search.fit(X_train_svc,y_train_svc)
     # resulting predictions
     predict_svc = svc_search.best_estimator_.predict(X_test_svc)
     full predict svc = svc search.best estimator .predict(X svc)
     # note: we have 3 labels, so we use average='macro' to find the average metric_
     \rightarrow for each
             label summed. This augments penalized performance caused by class ...
      \rightarrow imbalance.
     # print out the accuracy, precison and recall score for the prediction on
     \rightarrow validation set
     print('Accuracy for validation set: {}'.format(accuracy_score(y_test_svc,_
      →predict_svc)))
     print('Precision for validation set: {}'.format(precision_score(y_test_svc, ∪
      →predict_svc, average='macro')))
     print('Recall for validation set: {}\n'.format(recall_score(y_test_svc,_
      →predict_svc, average='macro')))
```

Accuracy for validation set: 0.4 Precision for validation set: 0.625 Recall for validation set: 0.625

Accuracy for full dataset: 0.6585365853658537 Precision for full dataset: 0.4380952380952381 Recall for full dataset: 0.4722222222222215

C:\Users\cjher\anaconda3\lib\site-

packages\sklearn\metrics_classification.py:1221: UndefinedMetricWarning:
Precision is ill-defined and being set to 0.0 in labels with no predicted
samples. Use `zero_division` parameter to control this behavior.
 _warn_prf(average, modifier, msg_start, len(result))

Baseline Model Discussion:

After running the above cell a few times, we notice that the score changes drastically based on the random set of X_train, y_train chosen. This is caused by our small data set and should be addressed in future models by generating or obtaining additional data. Additionally, due to the same problem, sometimes the model is unable to predict the borderline class (label 2) shown in the warning above, which is composed of materials that do not have a fixed flame retardant test result (sometimes pass and sometimes fail).

With regards to scores of the validation set and the full dataset, it seems that the data is not overfitting much and seems to generalize well when applied to the larger data set.

#Improved Models

```
[4]: # Read in the data
import numpy as np
import pandas as pd
import pylab as plt
data = pd.read_csv("feature_matrix.csv")
y_label=data['FR_labels'].values
data.head()
```

```
[4]:
        Total Heat Release Burning Temperature Ignition Temperature \
     0
              24722.818517
                                         482.246
                                                               350.805
     1
              14879.480392
                                                               438.643
                                         537.858
     2
              16584.116501
                                         515.457
                                                               366.537
     3
              20246.452607
                                         482.774
                                                               396.996
```

4	26622.142067	472.215	388.929

	Heat Release Capacity	Fire Growth Capacity	FR_labels
0	25955.104346	134.021649	2
1	15591.943456	120.959219	2
2	17369.365738	77.548988	1
3	21344.250614	191.805110	0
4	28036.752193	260.118532	0

##PCA (Principal Component Analysis)

Principal Component Analysis (PCA) will be performed on the original MCC dataset, which includes raw data and curve-flattened data. 10 most important PCs will be extracted from each dataset and return a (41*10) feature matrix. This matrix, itself, will be used as the input for the prediction model. In addition, the PCA extracted matrix will be combined with the original feature matrix for prediction.

```
[5]: # run if rampy is not installed %pip install rampy
```

```
Requirement already satisfied: rampy in c:\users\cjher\anaconda3\lib\site-
packages (0.4.5)
Note: you may need to restart the kernel to use updated packages. Requirement
already satisfied: pandas in c:\users\cjher\anaconda3\lib\site-packages (from
rampy) (1.0.5)
Requirement already satisfied: scipy in c:\users\cjher\anaconda3\lib\site-
packages (from rampy) (1.5.0)
Requirement already satisfied: numpy>=1.12 in c:\users\cjher\anaconda3\lib\site-
packages (from rampy) (1.18.5)
Requirement already satisfied: scikit-learn in
c:\users\cjher\anaconda3\lib\site-packages (from rampy) (0.23.1)
Requirement already satisfied: python-dateutil>=2.6.1 in
c:\users\cjher\anaconda3\lib\site-packages (from pandas->rampy) (2.8.1)
Requirement already satisfied: pytz>=2017.2 in
c:\users\cjher\anaconda3\lib\site-packages (from pandas->rampy) (2020.1)
Requirement already satisfied: joblib>=0.11 in
c:\users\cjher\anaconda3\lib\site-packages (from scikit-learn->rampy) (0.16.0)
Requirement already satisfied: threadpoolctl>=2.0.0 in
c:\users\cjher\anaconda3\lib\site-packages (from scikit-learn->rampy) (2.1.0)
Requirement already satisfied: six>=1.5 in c:\users\cjher\anaconda3\lib\site-
packages (from python-dateutil>=2.6.1->pandas->rampy) (1.15.0)
```

```
[6]: #
    # params: x, array of temperature values; y, array of HRR values
    # returns: y_corrected_filtered, flattened and smoothed arrays;
    # https://github.com/charlesll/rampy
# https://github.com/charlesll/rampy/blob/master/examples/baseline_fit.ipynb
```

Principal Component Analysis (PCA) will be performed on the original MCC dataset, which includes raw data and curve-flattened data. 5 most important PCs will be extracted from each dataset and return a (41*10) feature matrix. This matrix, itself, will be used as the input for the prediction model. In addition, the PCA extracted matrix will combine with the feature matrix extracted based on physical meanings.

```
[7]: # Read in the raw data
df = pd.read_csv("./MCC_raw.csv")
    data_raw = df.drop([0]).astype(float)
    data_raw[data_raw.columns[::3]].head(5)
[7]: Adhesive-1-1 Adhesive-2-1 Adhesive-3-1 Adhesive-4-1 Adhesive-5-1 \
    1 73.744 74.630 74.621 74.539 74.815
```

[7]:	Adhesive-1-1	Adhesive-2-1	l Adhesive-3	-1 Adhesive-	4-1 Adhesive-5-	1 \	
1	73.744	74.630	74.6	21 74.	539 74.81	5	
2	73.711	74.653	74.6	83 74.	552 74.81	5	
3	73.749	74.659	74.7	15 74.	519 74.89	3	
4	73.741	74.688	3 74.7	24 74.	498 74.90	4	
5	73.780	74.745	5 74.7	45 74.	478 74.95	1	
	Adhesive-6-1	Adhesive-7-1	l Adhesive-8	-1 Adhesive-	9-1 Adhesive-10	-1	\
1	75.161	75.574	1 74.5	89 75.	411 75.4	04	
2	75.181	75.580	74.6	28 75.	390 75.3	52	
3	75.207	75.582	74.6	50 75.	376 75.3	45 	
4	75.236	75.617	7 74.7	04 75.	397 75.3	35 	
5	75.237	75.603	3 74.7	20 75.	365 75.3	20	
	Fiber-FR-10	Fiber-FR-11	Fiber-FR-12	Fiber-FR-13	Fiber-FR-14 \		
1	74.736	75.393	74.683	73.755	74.602		
2	74.719	75.416	74.691	73.679	74.588		
3	74.678	75.360	74.725	73.665	74.604		
4	74.652	75.418	74.756	73.647	74.628		
5	74.669	75.412	74.765	73.607	74.704		
	Fiber-FR-15	Fiber-FR-16	Fiber-17 Fi	ber-18 Fiber	-19		
1	74.629	75.068	73.866	74.566 73.	599		

74.599

73.637

73.889

2

74.670

75.021

```
3
        74.699
                      74.989
                                73.901
                                           74.622
                                                      73.658
4
        74.735
                      74.962
                                73.928
                                           74.609
                                                      73.653
5
        74.778
                      74.959
                                73.933
                                           74.644
                                                      73.733
```

[5 rows x 41 columns]

```
[8]: # Drop all non-numerical (NaN) values
def is_positive_numeric(x):
    if not np.isreal(x):
        return False
    elif not np.isfinite(x):
        return False
    elif pd.isnull(x):
        return False
    else:
        return True

numeric_map = data_raw.applymap(is_positive_numeric)
data=data_raw[numeric_map.all(axis=1).values]
data.tail(5)
```

```
[8]:
           Adhesive-1-1 Unnamed: 1 Unnamed: 2 Adhesive-2-1 Unnamed: 4 \
     1395
                737.295
                             -0.002
                                           1.016
                                                       739.624
                                                                    -5.602
     1396
                737.805
                              0.102
                                           1.022
                                                       740.144
                                                                    -5.294
     1397
                738.282
                              0.155
                                           0.987
                                                       740.684
                                                                    -5.458
                                                                    -5.387
     1398
                738.803
                              0.020
                                           0.996
                                                       741.150
     1399
                739.309
                              0.060
                                           1.028
                                                       741.652
                                                                    -5.352
           Unnamed: 5 Adhesive-3-1 Unnamed: 7 Unnamed: 8 Adhesive-4-1 ... \
     1395
                1.014
                            739.985
                                         -6.388
                                                       1.034
                                                                   735.241 ...
                1.021
     1396
                            740.486
                                         -6.147
                                                       1.003
                                                                   735.757
                                          -6.113
     1397
                1.061
                            741.009
                                                       1.025
                                                                   736.241 ...
     1398
                1.007
                            741.526
                                         -6.189
                                                       1.040
                                                                   736.738 ...
     1399
                0.969
                            742.025
                                          -6.322
                                                       1.015
                                                                   737.225 ...
           Unnamed: 113 Fiber-17 Unnamed: 115 Unnamed: 116 Fiber-18 \
     1395
                  0.998
                          737.426
                                          -0.924
                                                         1.025
                                                                 738.191
     1396
                  1.017
                          737.927
                                         -0.815
                                                         1.019
                                                                 738.698
                  1.040
                                          -0.762
                                                                 739.192
     1397
                          738.441
                                                         1.015
     1398
                  1.004
                          738.957
                                          -0.871
                                                         1.030
                                                                 739.718
                                                                 740.200
     1399
                  1.004
                          739.427
                                          -0.804
                                                         0.985
           Unnamed: 118 Unnamed: 119 Fiber-19 Unnamed: 121
                                                                Unnamed: 122
     1395
                  1.522
                                1.009
                                        737.991
                                                         3.252
                                                                       1.013
     1396
                  1.733
                                1.001
                                        738.499
                                                         3.296
                                                                       1.025
     1397
                  1.684
                                1.001
                                        739.003
                                                         3.080
                                                                       1.014
                                1.019
     1398
                  1.605
                                        739.498
                                                         3.180
                                                                       0.998
```

1399 1.433 1.007 740.014 3.073 1.010

[5 rows x 123 columns]

In the following cell, two 2-D arrays storing the x values (temperature) and y values (HRR) are created.

- 1) xy_raw: x & y values for raw data
- 2) xy _flattened: x & y values for curve flattened data

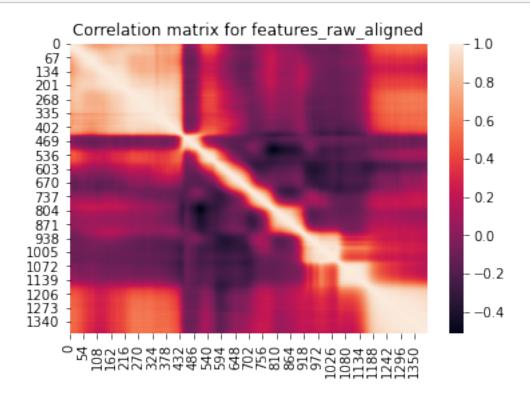
```
[9]: import warnings
     warnings.filterwarnings("ignore")
     xy_raw=[]
     xy_flattened=[]
     xy_corrected=[]
     for i in range(0, data.shape[1], 3):
         \# extract values for x and y and HR
         select = data.iloc[:,i:i+3]
         x = select.iloc[:,0].values
         xy_raw.append(x)
         xy_flattened.append(x)
         y = select.iloc[:,1].values
         xy_raw.append(y)
         y_b= baseflatten(x,y) #flatten the curve
         xy_flattened.append(y_b.flatten())
         # Uncomment the codes to check the baseline corrected curves
         #fig, ax=plt.subplots()
         \#ax.plot(x,y,label='original\ data')
         \#ax.plot(x,y_b,label='flattened data')
         #ax.legend()
     xy raw=np.array(xy raw)
     xy_flattened=np.array(xy_flattened)
```

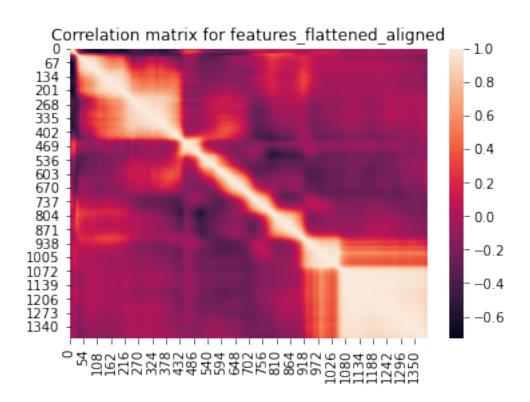
y values (HRR values) will be used for PCA, the following cells will extract two matrices with 41 rows (observations) and 1399 columns (y values as features).

```
[10]: features_raw=xy_raw[1::2,:]
    print(features_raw.shape)
    features_flattened=xy_flattened[1::2,:]
    print(features_flattened.shape)
```

(41, 1399) (41, 1399) Because the x values deviate slightly among each observation, it might lead to error if we use original y values directly. Therefore, for each observation, a linear interpolation will be performed and all y values will be re-calculated based on the same x values. Aligned feature matrices and heatmap for correlation matrices are printed below

```
[11]: from scipy import interpolate
      # define new aligned x values
      x aligned=np.linspace(max(xy raw[::2,1]),min(xy raw[::2,-1]),num=1400)
      \# function interpolating each observations, and return a new feature matrix.
       \rightarrow with aligned x values
      def align data(xy inp):
          features inp aligned=[]
          for i in range (0,41):
              x = xy_{inp}[2*i,:]
              y=xy_inp[2*i+1,:]
              # interpolate the curve
              interp = interpolate.interp1d(x, y)
              y_aligned=interp(x_aligned)
              features_inp_aligned.append(y_aligned)
              # Uncomment the codes to check the interpolation results
              #fig, ax=plt.subplots()
              \#ax.plot(x,y,label='original\ data')
              #ax.plot(x_aligned,y_aligned,label='interpolated data')
              #ax.legend()
          features_inp_aligned=np.array(features_inp_aligned)
          return features_inp_aligned
[12]: # Calculate feature matrices with aligned data
      features raw aligned=align data(xy raw)
      features_flattened_aligned=align_data(xy_flattened)
      print(features_raw_aligned.shape)
      print(features_flattened_aligned.shape)
     (41, 1400)
     (41, 1400)
[13]: import seaborn as sns
      corr raw aligned=np.corrcoef(features raw aligned.T)
      hm1=sns.heatmap(corr_raw_aligned).set_title('Correlation matrix for_
       plt.figure()
      corr_flattened_aligned=np.corrcoef(features_flattened_aligned.T)
```

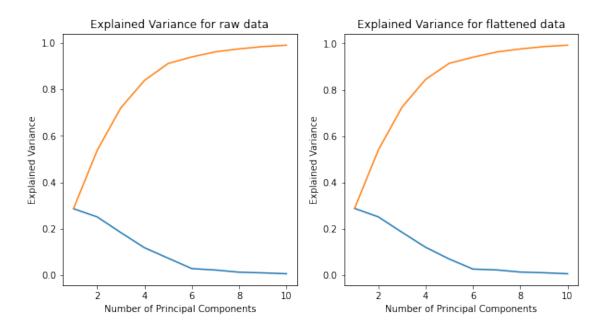




Find the first 10 PCs based on aligned features

```
[14]: from sklearn.decomposition import PCA
      pca_raw=PCA(n_components=k)
      pca_flattened=PCA(n_components=k)
      pca corrected=PCA(n components=k)
      raw_pc=pca_raw.fit_transform(features_raw_aligned)
      print(raw_pc[0,:])
      flattened_pc=pca_flattened.fit_transform(features_flattened_aligned)
      print(flattened_pc[0,:])
     [-686.42103209 311.84630269 710.71679886 -241.66235881 837.55141237
       -73.54494024 35.39005441 -50.01410212 132.44691814 -177.28925658
     [-675.35973346 297.70606542 709.67295662 -210.1040181 880.6852894
        14.376059
                      74.34795734 49.63853734 170.4150219 -148.95422749]
[15]: raw_mean=raw_pc.mean(axis=0)
      flattened_mean=flattened_pc.mean(axis=0)
      fig,axes=plt.subplots(1,2,figsize=(10,5))
      axes[0].plot(range(1,len(raw_mean)+1),pca_raw.explained_variance_ratio_)
      axes[0].plot(range(1,len(raw_mean)+1),np.cumsum(pca_raw.
      →explained_variance_ratio_))
      axes[0].set xlabel('Number of Principal Components')
      axes[0].set_ylabel('Explained Variance')
      axes[0].set_title('Explained Variance for raw data')
      axes[1].plot(range(1,len(flattened_mean)+1),pca_flattened.
      →explained_variance_ratio_)
      axes[1].plot(range(1,len(flattened_mean)+1),np.cumsum(pca_flattened.
      →explained_variance_ratio_))
      axes[1].set_xlabel('Number of Principal Components')
      axes[1].set_ylabel('Explained Variance')
      axes[1].set_title('Explained Variance for flattened data')
```

[15]: Text(0.5, 1.0, 'Explained Variance for flattened data')

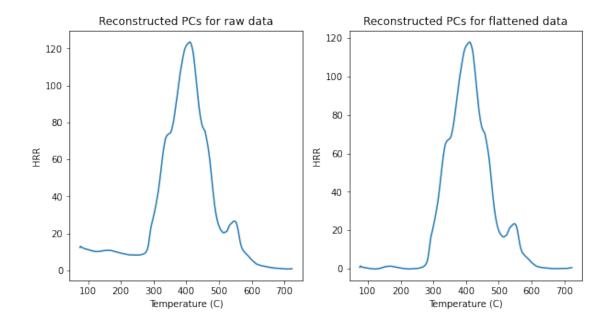


```
[16]: raw_reconstructed=pca_raw.inverse_transform(raw_mean)
    flattened_reconstructed=pca_flattened.inverse_transform(flattened_mean)

fig,axes=plt.subplots(1,2,figsize=(10,5))
    axes[0].plot(x_aligned,raw_reconstructed)
    axes[0].set_xlabel('Temperature (C)')
    axes[0].set_ylabel('HRR')
    axes[0].set_title('Reconstructed PCs for raw data')

axes[1].plot(x_aligned,flattened_reconstructed)
    axes[1].set_xlabel('Temperature (C)')
    axes[1].set_ylabel('HRR')
    axes[1].set_title('Reconstructed PCs for flattened data')
```

[16]: Text(0.5, 1.0, 'Reconstructed PCs for flattened data')



1.2.1 Forward selection to determine most predictive PCs???

```
[17]: from sklearn.model_selection import train_test_split
      from sklearn.metrics import accuracy_score, recall_score, precision_score
      from sklearn.model_selection import GridSearchCV
      from sklearn.svm import SVC
      def baseline_predict(X_svc,y_svc):
          # perform a train-test split. 90% of original data will be used for training
          X_train_svc, X_test_svc, y_train_svc, y_test_svc = train_test_split(X_svc,__
       \rightarrowy_svc, test_size = 0.10)
          # define support vector model with rbf kernel
          svc = SVC(kernel = 'rbf')
          # build up parameter grid and perform GridSearchCV to find the bestu
       \rightarrow estimator
          alphas = np.array([1e-6, 1e-5, 1e-4, 1e-3, 1e-2, 1e-1, 1])
          Cs = 1 / alphas
          sigmas = np.array([1e-3, 1e-2, 1e-1, 1, 10, 100])
          gammas = 1. / 2 / sigmas**2
          param_grid_svc = {'C': Cs,'gamma': gammas}
          svc_search = GridSearchCV(svc, param_grid_svc, cv = 3)
          svc_search.fit(X_train_svc,y_train_svc)
```

```
# resulting predictions
predict_svc = svc_search.best_estimator_.predict(X_test_svc)
full_predict_svc = svc_search.best_estimator_.predict(X_svc)

test_accuracy=accuracy_score(y_test_svc, predict_svc)
test_precision=precision_score(y_test_svc, predict_svc, average='macro')
test_recall=recall_score(y_test_svc, predict_svc, average='macro')

full_accuracy=accuracy_score(y_svc, full_predict_svc)
full_precision=precision_score(y_svc, full_predict_svc, average='macro')
full_recall=recall_score(y_svc, full_predict_svc, average='macro')
return__
otest_accuracy,test_precision,test_recall,full_accuracy,full_precision,full_recall
```

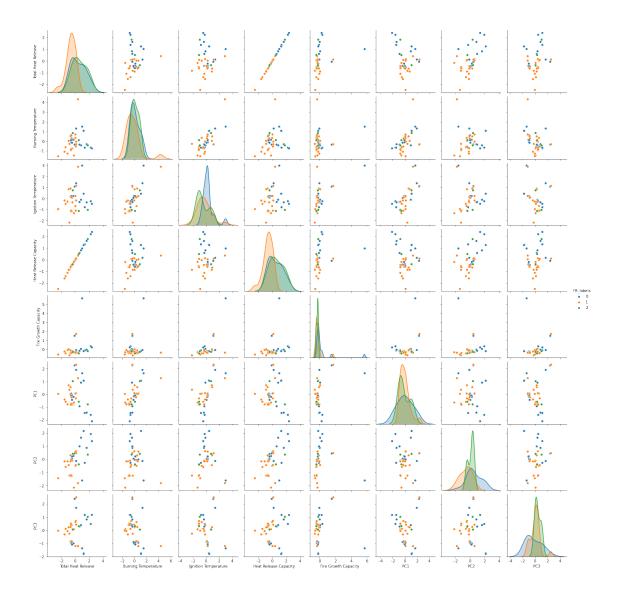
1.3 Generative Model

Due to the small size of our dataset, it is n

```
[18]: feature matrix = pd.read csv("feature matrix.csv")
      feature matrix['PC1'] = flattened pc[:,0]
      feature_matrix['PC2'] = flattened_pc[:,1]
      feature_matrix['PC3'] = flattened_pc[:,2]
      feature_matrix.head(10)
[18]:
         Total Heat Release Burning Temperature Ignition Temperature \
      0
               24722.818517
                                          482.246
                                                                 350.805
               14879.480392
                                          537.858
                                                                 438.643
      1
      2
                                                                 366.537
               16584.116501
                                          515.457
      3
               20246.452607
                                          482.774
                                                                 396.996
      4
               26622.142067
                                          472.215
                                                                 388.929
      5
               12581.675639
                                          488.529
                                                                 292.177
      6
               27364.231613
                                          468.963
                                                                 377.870
      7
               14539.335519
                                          469.506
                                                                 384.928
      8
               15665.463662
                                          437.267
                                                                 334.539
               13535.355054
      9
                                                                 343.769
                                          461.318
         Heat Release Capacity Fire Growth Capacity FR_labels
                                                                           PC1 \
                  25955.104346
                                                                2 -675.359733
      0
                                           134.021649
      1
                  15591.943456
                                           120.959219
                                                                    909.690756
      2
                  17369.365738
                                           77.548988
                                                                     63.184583
      3
                  21344.250614
                                                                  785.952883
                                           191.805110
      4
                  28036.752193
                                           260.118532
                                                                0 -1375.196882
      5
                  13257.707466
                                            36.933912
                                                                    312.467042
      6
                  28900.669510
                                           238.762552
                                                                0 -1823.270549
      7
                  15291.533325
                                           139.195486
                                                                1 -673.781301
                  16466.951534
                                                                1 -534.780041
      8
                                           114.496239
```

```
9
                 14282.096095
                                          84.124726
                                                          1 -613.962631
                PC2
                            PC3
         297.706065 709.672957
        342.229152 38.531590
      1
      2 -388.364571 435.757401
      3 1344.401661 280.523465
      4 1562.118158 335.994645
      5 -994.660995 -171.510404
      6 1123.422047 811.066965
        -70.424838 63.789101
      8 -1735.166316 67.101112
      9 -1013.199055 282.618485
[19]: data = feature matrix
      # import standard scaler
      from sklearn.preprocessing import StandardScaler
      # scale the data (excluding labels)
      scaler = StandardScaler()
      scaled = scaler.fit_transform(data.drop(columns='FR_labels'))
      scaled = pd.DataFrame(scaled)
      scaled.columns = data.drop(columns='FR_labels').columns
      scaled['FR_labels'] = data.loc[:,'FR_labels']
                                                      # add FR labels to new_
      \rightarrow dataframe
      scaled.head()
      origin_feature_matrix=scaled
      origin_feature_matrix.shape
[19]: (41, 9)
[20]: # plot
      import seaborn as sns
      sns.pairplot(scaled,hue='FR_labels')
```

[20]: <seaborn.axisgrid.PairGrid at 0x1da30125670>



###Gaussian Mixture

```
[21]: y = scaled['FR_labels']
from sklearn.mixture import GaussianMixture

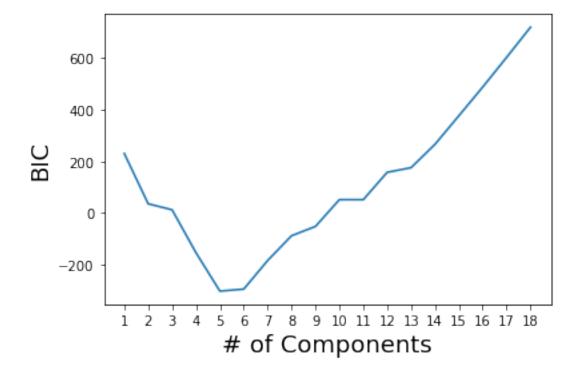
X = scaled.drop(columns='FR_labels')[y == 0].values
n_components = np.arange(1, 19)

BICs = []
models = []
for n in n_components:
    gmm_n = GaussianMixture(n, covariance_type = 'full').fit(X)
    bic = gmm_n.bic(X)
    BICs.append(bic)
```

```
models.append(gmm_n)

fig, ax = plt.subplots()
ax.plot(n_components, BICs)
ax.set_xlabel('# of Components', size = 18);
ax.set_ylabel('BIC', size = 18)
ax.set_xticks(n_components);
best_n=[]
best_n.append(n_components[BICs == min(BICs)][0])
print(best_n)
```

[5]



```
[22]: y = scaled['FR_labels']
from sklearn.mixture import GaussianMixture

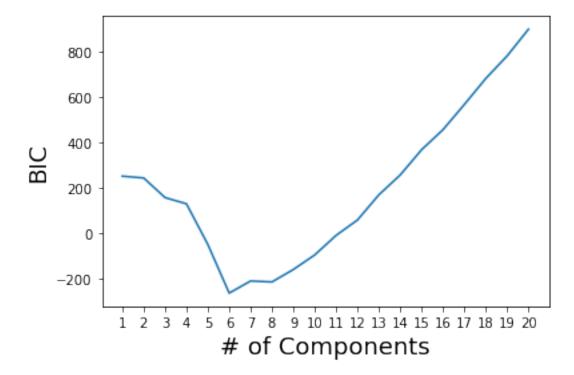
X = scaled.drop(columns='FR_labels')[y == 1].values
n_components = np.arange(1, 21)

BICs = []
models = []
for n in n_components:
    gmm_n = GaussianMixture(n, covariance_type = 'full').fit(X)
```

```
bic = gmm_n.bic(X)
BICs.append(bic)
models.append(gmm_n)

fig, ax = plt.subplots()
ax.plot(n_components, BICs)
ax.set_xlabel('# of Components', size = 18);
ax.set_ylabel('BIC', size = 18)
ax.set_xticks(n_components);
best_n.append(n_components[BICs == min(BICs)][0])
print(best_n)
```

[5, 6]



```
[23]: vals = []
for i in range(0,2):
    X = scaled.drop(columns='FR_labels')[y == i].values
    gmm = GaussianMixture(n_components = 5, covariance_type = 'full')
    gmm.fit(X)
    new = gmm.sample(100)
    vals.append(new[0])
```

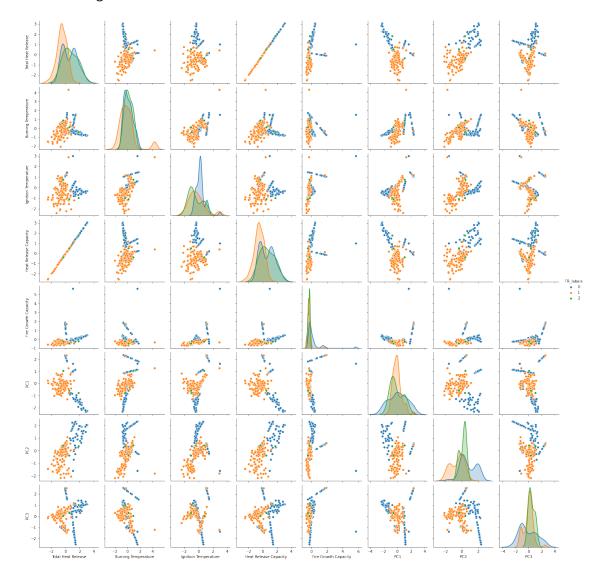
```
[24]: new0 = pd.DataFrame(vals[0])
      new0['FR_labels'] = np.zeros(100).astype(int)
      new0.columns = scaled.columns
      new1 = pd.DataFrame(vals[1])
      new1['FR_labels'] = np.ones(100).astype(int)
      new1.columns = scaled.columns
      final = scaled.append(new0)
      final = final.append(new1)
      final
[24]:
          Total Heat Release Burning Temperature Ignition Temperature
                    1.808411
                                        -0.424203
                                                              -0.990329
      0
      1
                   -0.335103
                                         0.879587
                                                               0.744864
      2
                    0.036103
                                                              -0.679551
                                         0.354409
      3
                    0.833624
                                        -0.411824
                                                              -0.077850
      4
                    2.222013
                                        -0.659374
                                                              -0.237209
      95
                   -1.081838
                                         0.224518
                                                               1.123469
      96
                   -0.510300
                                         0.109623
                                                               0.655658
      97
                   -0.077270
                                         0.667905
                                                               0.413082
                   -0.682197
      98
                                         0.255999
                                                               0.562615
      99
                   -0.509503
                                         0.540363
                                                               0.933226
          Heat Release Capacity Fire Growth Capacity
                                                            PC1
                                                                      PC2
                                                                                PC3 \
      0
                       1.778631
                                            -0.202424 -0.780066 0.367749 1.022207
      1
                      -0.365567
                                            -0.258909 1.050728
                                                                 0.422747
                                                                           0.055501
      2
                       0.002192
                                            -0.446622 0.072981 -0.479737
                                                                           0.627661
      3
                       0.824619
                                             0.047441 0.907806
                                                                1.660705
                                                                           0.404063
      4
                       2.209336
                                             0.342840 -1.588405
                                                                1.929644
                                                                           0.483964
      95
                      -1.085874
                                            -0.012660 0.706580 -0.133468
                                                                          0.858272
                      -0.490908
      96
                                            -0.065789 0.236920 0.120113 0.023390
      97
                      -0.069270
                                            98
                      -0.656169
                                            -0.160562   0.267802   -0.090997   -0.167082
      99
                      -0.504532
                                            -0.067655 0.765922 0.313542 0.012615
          FR labels
      0
                  2
                  2
      1
      2
                  1
      3
                  0
      4
                  0
      . .
      95
                  1
      96
                  1
      97
                  1
      98
```

99 1

[241 rows x 9 columns]

[25]: sns.pairplot(final,hue='FR_labels')

[25]: <seaborn.axisgrid.PairGrid at 0x1da2a6b3fd0>



This actually doesn't look too bad. It seems to preserve the distribution of the original data, even with the addition of 100 points. I did not add points for $FR_label=2$ class because it is sparse to begin with.

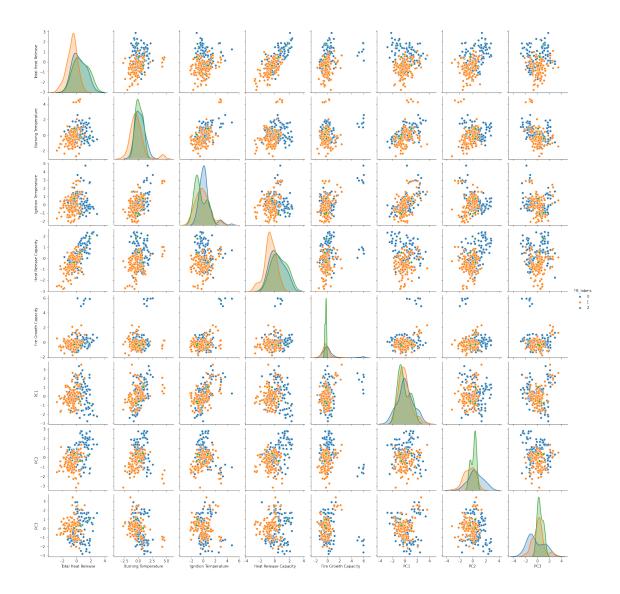
###Kernel Density Estimation

```
[26]: from sklearn.neighbors import KernelDensity
     from sklearn.model_selection import GridSearchCV
[27]: vals = []
     for i in range (0,2):
       X = scaled.drop(columns='FR_labels')[y == i].values
       # use grid search cross-validation to optimize the bandwidth
       params = {'bandwidth': np.logspace(-1, 1, 20)}
       grid = GridSearchCV(KernelDensity(kernel='gaussian'), params)
       grid.fit(X)
       print("best bandwidth: {0}".format(grid.best_estimator_.bandwidth))
       print(grid.best_estimator_.score(X))
       # use the best estimator to compute the kernel density estimate
       kde = KernelDensity(bandwidth = .54, kernel = 'gaussian')
       kde.fit(X)
       print(np.logspace(-1, 1, 20))
       print(kde.score(X))
       new = kde.sample(100)
       vals.append(new)
     best bandwidth: 0.6951927961775606
     -117.70908947368294
     Γ0.1
                 0.1274275
                            0.16237767 0.20691381 0.26366509 0.33598183
       0.42813324 0.54555948 0.6951928
                                         0.88586679 1.12883789 1.43844989
       1.83298071 2.33572147 2.97635144 3.79269019 4.83293024 6.15848211
       7.8475997 10.
                            ]
     -83.34054583333229
     best bandwidth: 0.6951927961775606
     -136.85204064684024
     Γ0.1
                 0.42813324 0.54555948 0.6951928
                                         0.88586679 1.12883789 1.43844989
       1.83298071 2.33572147 2.97635144 3.79269019 4.83293024 6.15848211
       7.8475997 10.
                            1
     -100.98346153566186
[28]: new0 = pd.DataFrame(vals[0])
     new0['FR labels'] = np.zeros(100).astype(int)
     new0.columns = scaled.columns
     new1 = pd.DataFrame(vals[1])
     new1['FR_labels'] = np.ones(100).astype(int)
     new1.columns = scaled.columns
     final = scaled.append(new0)
     final = final.append(new1)
     final
```

```
[28]:
          Total Heat Release
                             Burning Temperature Ignition Temperature
                     1.808411
                                          -0.424203
                                                                 -0.990329
      0
      1
                    -0.335103
                                           0.879587
                                                                  0.744864
      2
                    0.036103
                                           0.354409
                                                                 -0.679551
      3
                    0.833624
                                         -0.411824
                                                                 -0.077850
      4
                    2.222013
                                          -0.659374
                                                                 -0.237209
      95
                    -0.662276
                                           0.455443
                                                                  0.575375
      96
                    -1.212980
                                          -0.655079
                                                                 -1.953262
      97
                   -1.405636
                                          -0.472365
                                                                  0.574471
                    -0.583222
                                          -1.688204
      98
                                                                 -0.885139
      99
                   -0.438033
                                           0.439771
                                                                  1.278297
                                                                                    PC3 \
          Heat Release Capacity Fire Growth Capacity
                                                               PC1
                                                                         PC2
      0
                        1.778631
                                              -0.202424 -0.780066
                                                                    0.367749
                                                                              1.022207
                       -0.365567
      1
                                              -0.258909 1.050728
                                                                    0.422747
                                                                              0.055501
      2
                        0.002192
                                              -0.446622 0.072981 -0.479737
                                                                              0.627661
      3
                        0.824619
                                               0.047441 0.907806
                                                                              0.404063
                                                                    1.660705
      4
                        2.209336
                                               0.342840 -1.588405
                                                                    1.929644
                                                                              0.483964
      95
                       -1.039101
                                              -0.368334 1.675698 -0.934325
                                                                              1.177548
                       -1.265756
      96
                                              -0.464628   0.370434   -1.385647
                                                                              0.177019
      97
                       -1.904052
                                              -0.719317 0.514430 0.012650
                                                                              0.604339
                       -0.377791
      98
                                              -1.735399 0.139514 -1.019283
                                                                              0.736869
      99
                        0.251828
                                              0.217014 -1.312832 0.217401 -0.103642
          FR_labels
                  2
      0
                  2
      1
      2
                   1
                   0
      3
      4
                   0
      95
                   1
                   1
      96
                   1
      97
                   1
      98
      99
      [241 rows x 9 columns]
```

[29]: <seaborn.axisgrid.PairGrid at 0x1da449d2cd0>

[29]: sns.pairplot(final,hue='FR_labels')



##Classifiers

```
[30]: X_ori=origin_feature_matrix.drop(columns='FR_labels').values
y_ori=origin_feature_matrix['FR_labels'].values
X_ori.shape
```

[30]: (41, 8)

SVC (Baseline model)

```
[31]: # perform a train-test split. 90% of original data will be used for training
X_svc = final.drop(columns='FR_labels').values
y_svc = final['FR_labels'].values
```

```
X_train_svc, X_test_svc, y_train_svc, y_test_svc = train_test_split(X_svc,__
\rightarrowy_svc, test_size = 0.25)
# define support vector model with rbf kernel
svc = SVC(kernel = 'rbf')
# build up parameter grid and perform GridSearchCV to find the best estimator
alphas = np.array([1e-6, 1e-5, 1e-4, 1e-3, 1e-2, 1e-1, 1])
Cs = 1 / alphas
sigmas = np.array([1e-3, 1e-2, 1e-1, 1, 10, 100])
gammas = 1. / 2 / sigmas**2
param_grid_svc = {'C': Cs,'gamma': gammas}
svc_search = GridSearchCV(svc, param_grid_svc, cv = 5)
svc_search.fit(X_train_svc,y_train_svc)
# resulting predictions
predict_svc = svc_search.best_estimator_.predict(X_test_svc)
full_predict_svc = svc_search.best_estimator_.predict(X_svc)
origin predict svc = svc search.best estimator .predict(X ori)
# note: we have 3 labels, so we use average='macro' to find the average metric_
\rightarrow for each
        label summed. This augments penalized performance caused by class ...
\rightarrow imbalance.
# print out the accuracy, precison and recall score for the prediction on
\rightarrow validation set
print('Accuracy for validation set: {}'.format(accuracy_score(y_test_svc,_
→predict_svc)))
print('Precision for validation set: {}'.format(precision_score(y_test_svc,__

→predict_svc, average='macro')))
print('Recall for validation set: {}\n'.format(recall_score(y_test_svc,_u
→predict_svc, average='macro')))
# print out the accuracy, precison and recall score for the prediction on full_{\sqcup}
print('Accuracy for full dataset: {}'.format(accuracy_score(y_svc,__
→full_predict_svc)))
print('Precision for full dataset: {}'.format(precision_score(y_svc,__
print('Recall for full dataset: {}'.format(recall_score(y_svc,__

→full_predict_svc, average='macro')))
# print out the accuracy, precison and recall score for the prediction on u
→original dataset (before data generation)
```

```
print('Accuracy for original dataset: {}'.format(accuracy_score(y_ori,u
       →origin_predict_svc)))
      print('Precision for original dataset: {}'.format(precision_score(y_ori,u
      →origin_predict_svc, average='macro')))
      print('Recall for original dataset: {}'.format(recall_score(y_ori,_
       →origin_predict_svc, average='macro')))
     Accuracy for validation set: 0.7868852459016393
     Precision for validation set: 0.7981283422459893
     Recall for validation set: 0.7511261261261262
     Accuracy for full dataset: 0.9377593360995851
     Precision for full dataset: 0.959494927998865
     Recall for full dataset: 0.9581920903954803
     Accuracy for original dataset: 0.9024390243902439
     Precision for original dataset: 0.9393939393939394
     Recall for original dataset: 0.93333333333333333
     ####Decision Tree
[32]: from sklearn.tree import DecisionTreeClassifier
      X_DT = final.drop(columns='FR_labels').values
      y_DT = final['FR_labels'].values
      X_train_DT, X_test_DT, y_train_DT, y_test_DT = train_test_split(X_DT, y_DT,__
      \rightarrowtest_size = 0.25)
      # Create dtree instance
      dtree = DecisionTreeClassifier()
      # Create parameter grid - currently just max depth
      \max_{\text{depths}} = [2,3,5,10,15,20,100]
      criterions = ['gini', 'entropy']
      param_grid_dtree = {'max_depth': max_depths, 'criterion': criterions}
      print(X_DT.shape)
      print(y_DT.shape)
     (241, 8)
     (241,)
[33]: # GridSearch Hyperparameter Tuning
      DT_search = GridSearchCV(dtree, param_grid_dtree, cv=5)
      DT_search.fit(X_train_DT, y_train_DT)
      # Predict both the testing set and the full data set
      dtree_prediction = DT_search.best_estimator_.predict(X_test_DT)
      dtree_full_prediction = DT_search.best_estimator_.predict(X_DT)
      dtree_origin_prediction = DT_search.best_estimator_.predict(X_ori)
```

```
# note: we have 3 labels, so we use average='macro' to find the average metric_
         label summed. This augments penalized performance caused by classu
 \rightarrow imbalance.
# print out the accuracy, precison and recall score for the prediction on \square
 \rightarrow validation set
print('Accuracy for validation set: {}'.format(accuracy_score(y_test_DT,__
 →dtree prediction)))
print('Precision for validation set: {}'.format(precision_score(y_test_DT,__

→dtree_prediction, average='macro')))
print('Recall for validation set: {}\n'.format(recall_score(y_test_DT,_
 →dtree_prediction, average='macro')))
# print out the accuracy, precison and recall score for the prediction on full_{\mathsf{L}}
 \rightarrow dataset
print('Accuracy for full dataset: {}'.format(accuracy_score(y_DT,_
 →dtree full prediction)))
print('Precision for full dataset: {}'.format(precision_score(y_DT,_
 →dtree_full_prediction, average='macro')))
print('Recall for full dataset: {}\n'.format(recall_score(y_DT,__
 →dtree_full_prediction, average='macro')))
# print out the accuracy, precison and recall score for the prediction on \square
 →original dataset (before data generation)
print('Accuracy for original dataset: {}'.format(accuracy_score(y_ori,u
 →dtree_origin_prediction)))
print('Precision for original dataset: {}'.format(precision_score(y_ori,u

→dtree_origin_prediction, average='macro')))
print('Recall for original dataset: {}'.format(recall_score(y_ori,_

dtree_origin_prediction, average='macro')))
Accuracy for validation set: 0.7704918032786885
Precision for validation set: 0.5241301907968574
Recall for validation set: 0.5132616487455196
Accuracy for full dataset: 0.8464730290456431
Precision for full dataset: 0.7945893719806763
Recall for full dataset: 0.7885122410546139
```

26

Accuracy for original dataset: 0.8292682926829268 Precision for original dataset: 0.89444444444445 Recall for original dataset: 0.78888888888888888

###Random Forest

```
[34]: from sklearn.ensemble import RandomForestClassifier
      X_RF = final.drop(columns='FR_labels').values
      y_RF = final['FR_labels'].values
      X_train_RF, X_test_RF, y_train_RF, y_test_RF = train_test_split(X_RF, y_RF,__
       \rightarrowtest size = 0.25)
      # Instantiate random forest model
      ranfor = RandomForestClassifier()
      # Create parameter grid
      # We are searching over two hyperparameters for our Random Forest model
      n_estimators = [3, 5, 7, 10, 15, 20, 25, 50, 100]
      maximum feats = ['auto', 'log2']
      \max_{depths} = [2,3,5,10,15,20,100]
      criterions = ['gini', 'entropy']
      param_grid_ranfor = {'n_estimators': n_estimators, 'criterion': criterions, __
       →'max_features': maximum_feats, 'max_depth': max_depths}
[35]: # GridSearch Hyperparameter Tuning
      RF_search = GridSearchCV(ranfor, param_grid_ranfor, cv=5)
      RF_search.fit(X_train_RF, y_train_RF)
      # Predict both the testing set and the full data set
      ranfor_prediction = RF_search.best_estimator_.predict(X_test_RF)
      ranfor_full_prediction = RF_search.best_estimator_.predict(X_RF)
      ranfor_origin_prediction = RF_search.best_estimator_.predict(X_ori)
      # note: we have 3 labels, so we use average='macro' to find the average metric_
       \rightarrow for each
              label summed. This augments penalized performance caused by class ...
       \rightarrow imbalance.
      # print out the accuracy, precison and recall score for the prediction on \square
       \rightarrow validation set
      print('Accuracy for validation set: {}'.format(accuracy_score(y_test_RF,_
       →ranfor_prediction)))
      print('Precision for validation set: {}'.format(precision_score(y_test_RF,_
       →ranfor_prediction, average='macro')))
      print('Recall for validation set: {}\n'.format(recall_score(y_test_RF,_u
       →ranfor_prediction, average='macro')))
      # print out the accuracy, precison and recall score for the prediction on full_{\mathsf{U}}
       \rightarrow dataset
```

```
print('Accuracy for full dataset: {}'.format(accuracy_score(y_RF,__
       →ranfor_full_prediction)))
      print('Precision for full dataset: {}'.format(precision_score(y_RF,_
      →ranfor_full_prediction, average='macro')))
      print('Recall for full dataset: {}\n'.format(recall_score(y_RF,__
       →ranfor_full_prediction, average='macro')))
      # print out the accuracy, precison and recall score for the prediction on \square
      →original dataset (before data generation)
      print('Accuracy for original dataset: {}'.format(accuracy_score(y_ori,u
       →ranfor_origin_prediction)))
      print('Precision for original dataset: {}'.format(precision_score(y_ori,_
      →ranfor_origin_prediction, average='macro')))
      print('Recall for original dataset: {}'.format(recall_score(y_ori,_
       →ranfor_origin_prediction, average='macro')))
     Accuracy for validation set: 0.6721311475409836
     Precision for validation set: 0.6726190476190477
     Recall for validation set: 0.671505376344086
     Accuracy for full dataset: 0.9128630705394191
     Precision for full dataset: 0.9414553267012283
     Recall for full dataset: 0.8328154425612052
     Accuracy for original dataset: 0.9024390243902439
     Precision for original dataset: 0.9324561403508772
     Recall for original dataset: 0.837037037037037
     ###KNN
[36]: from sklearn.neighbors import KNeighborsClassifier
      X_KNN = final.drop(columns='FR_labels').values
      y_KNN = final['FR_labels'].values
      X_train_KNN, X_test_KNN, y_train_KNN, y_test_KNN = train_test_split(X_KNN, __
      \rightarrowy_KNN, test_size = 0.25)
      KNN = KNeighborsClassifier()
      \# neighbors = np.array([2,4,6,8,10,12,15,18,20,15])
      neighbors = np.array([2,3])
      KNN_param_grid = {'n_neighbors': neighbors}
[37]: # Hyperparameter tunning
      KNN_search = GridSearchCV(KNN, KNN_param_grid, cv=5)
      KNN_search.fit(X_train_KNN, y_train_KNN)
      # resulting predictions
```

```
predict_KNN = KNN_search.best_estimator_.predict(X_test_KNN)
full_predict_KNN = KNN_search.best_estimator_.predict(X KNN)
origin_predict_KNN = KNN_search.best_estimator_.predict(X_ori)
# note: we have 3 labels, so we use average='macro' to find the average metric_
\rightarrow for each
        label summed. This augments penalized performance caused by classi
\rightarrow imbalance.
# print out the accuracy, precison and recall score for the prediction on \Box
\rightarrow validation set
print('Accuracy for validation set: {}'.format(accuracy_score(y_test_KNN,__
→predict_KNN)))
print('Precision for validation set: {}'.format(precision_score(y_test_KNN,_u
→predict_KNN, average='macro')))
print('Recall for validation set: {}\n'.format(recall_score(y_test_KNN,__
→predict_KNN, average='macro')))
# print out the accuracy, precison and recall score for the prediction on full_{\mathsf{L}}
\rightarrow dataset
print('Accuracy for full dataset: {}'.format(accuracy_score(y_KNN,__
→full_predict_KNN)))
print('Precision for full dataset: {}'.format(precision_score(y_KNN,__

→full_predict_KNN, average='macro')))
print('Recall for full dataset: {}\n'.format(recall_score(y_KNN,__
→full_predict_KNN, average='macro')))
# print out the accuracy, precison and recall score for the prediction on \square
→ original dataset (before data generation)
print('Accuracy for original dataset: {}'.format(accuracy_score(y_ori,_
→origin predict KNN)))
print('Precision for original dataset: {}'.format(precision_score(y_ori,u

→origin_predict_KNN, average='macro')))
print('Recall for original dataset: {}'.format(recall_score(y_ori,_
 →origin_predict_KNN, average='macro')))
```

Accuracy for validation set: 0.7704918032786885 Precision for validation set: 0.5132902298850575 Recall for validation set: 0.5306513409961685

Accuracy for full dataset: 0.8755186721991701 Precision for full dataset: 0.5839307048984468 Recall for full dataset: 0.5911487758945386

Accuracy for original dataset: 0.8292682926829268 Precision for original dataset: 0.5531746031746031 Recall for original dataset: 0.5981481481481481 []: